

# CHCRUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

Colloquium: Unconventional fully gapped superconductivity in the heavy-fermion metal math xmlns="http://www.w3.org/1998/Math/MathML" display="inline">mrow>mrow>msub>Mrow>mi>CeCu/mi >/mrow>mrow>mn>2/mn>/mrow>/msub>/mrow>mrow> msub>mrow>mi>Si/mi>/mrow>mrow>mn>2/mn>/mrow >/msub>/mrow>/math>

Michael Smidman, Oliver Stockert, Emilian M. Nica, Yang Liu, Huiqiu Yuan, Qimiao Si, and Frank Steglich

> Rev. Mod. Phys. **95**, 031002 — Published 15 September 2023 DOI: 10.1103/RevModPhys.95.031002

## Unconventional fully-gapped superconductivity in the heavy-fermion metal $\mbox{CeCu}_2\mbox{Si}_2$

Michael Smidman,<sup>1, \*</sup> Oliver Stockert,<sup>2, †</sup> Emilian M. Nica,<sup>3</sup> Yang Liu,<sup>1</sup> Huiqiu Yuan,<sup>1, 4, ‡</sup> Qimiao Si,<sup>5, §</sup> and Frank Steglich<sup>1, 2, ¶</sup> <sup>1</sup>Center for Correlated Matter and School of Physics, Zhejiang University, Hangzhou 310058, China <sup>2</sup>Max Planck Institute for Chemical Physics of Solids, 01187 Dresden, Germany <sup>3</sup>Department of Physics, Arizona State University, Tempe, AZ 85281, USA <sup>4</sup>State Key Laboratory of Silicon Materials, Zhejiang University, Hangzhou 310058, China <sup>5</sup>Department of Physics and Astronomy, Rice Center for Quantum Materials, Rice University, Houston, TX 77005, USA

(Dated: March 7, 2023)

The heavy-fermion metal CeCu<sub>2</sub>Si<sub>2</sub> was the first discovered unconventional, nonphonon-mediated superconductor, and for a long time was believed to exhibit single-band *d*-wave superconductivity, as inferred from various measurements hinting at a nodal gap structure. More recently however, measurements using a range of techniques at very low temperatures ( $T \leq 0.1$  K) provided evidence for a fully-gapped superconducting order parameter. In this Colloquium, after a brief historical overview we survey the apparently conflicting results of numerous experimental studies on this compound. We then address the different theoretical scenarios which have been applied to understand the particular gap structure, including both isotropic (sign-preserving) and anisotropic twoband *s*-wave superconductivity, as well as an effective two-band *d*-wave model, where the latter can explain the currently available experimental data on CeCu<sub>2</sub>Si<sub>2</sub>. The lessons from CeCu<sub>2</sub>Si<sub>2</sub> are expected to help uncover the Cooper-pair states in other unconventional, fully-gapped superconductors with strongly correlated carriers, and in particular highlight the rich variety of such states enabled by orbital degrees of freedom.

#### CONTENTS

I.	Introduction	1
II.	The history of heavy-fermion superconductivity	3
III.	Evidence for <i>d</i> -wave superconductivity in CeCu <sub>2</sub> Si <sub>2</sub> above	
	0.1 K	6
	A. Phase diagram	6
	B. Origin of the A-phase in CeCu <sub>2</sub> Si <sub>2</sub>	8
	C. Quantum criticality	9
	D. Spin dynamics in superconducting CeCu <sub>2</sub> Si <sub>2</sub>	10
	E. Effects of potential scattering	11
	F. Evidence for <i>d</i> -wave pairing	12

*	msmi	dman@z	ju.edu.cn

<sup>†</sup> oliver.stockert@cpfs.mpg.de

- <sup>‡</sup> hqyuan@zju.edu.cn
- § qmsi@rice.edu
- $\P \ {\it Frank.Steglich@cpfs.mpg.de}$

IV.	Fully gapped unconventional superconductivity in	
	$CeCu_2Si_2$	13
	A. Evidence for a nodeless gap structure	13
	B. Fermi surface and quasiparticle dispersion	14
	C. $d + d$ matrix-pairing state	15
	D. Analysis of experimental results with the $d+d \mbox{ model}$	18
V.	Perspectives	19
VI.	Summary	19
	Acknowledgements	22
	References	22

#### I. INTRODUCTION

Strongly correlated electron systems are central to contemporary studies of quantum materials. In these materials, electron-electron interactions have a strength that reaches or even exceeds the width of the underlying noninteracting electron bands. This property is to be contrasted with conventional metals such as aluminum or ordinary semiconductors like silicon, where electronic properties can be successfully described in terms of noninteracting electrons with a materials-specific bandstructure. Instead, for strongly correlated electron systems, the interactions lead to rich emergent phenomena and novel electronic phases of matter. Examples of strongly correlated electron systems include cuprate perovskites (Lee *et al.*, 2006; Proust and Taillefer, 2019), iron-based pnictides and chalcogenides (Si *et al.*, 2016; Stewart, 2011), organic charge-transfer salts (Kanoda, 2008; Lang and Müller, 2003; Maple *et al.*, 2004), and the moiré structures of graphene and transition-metal dichalcogenides (Andrei and MacDonald, 2020; Cao *et al.*, 2018).

Among the strongly correlated electron systems, heavy fermion compounds such as CeCu<sub>2</sub>Si<sub>2</sub> take a special place. The reason is simple. These materials contain partially-filled *f*-orbitals. For these *f*-electrons, the interactions are larger than their bandwidth to such an extent that the *f*-electrons act as localized magnetic moments. Indeed, at the heart of the physics of heavy fermion materials is the Kondo effect, whereby localized magnetic moments situated in a sea of conduction electrons become screened, and below a characteristic temperature scale (the Kondo temperature  $T_K$ ), the local moments are entirely quenched leaving behind a remanent nonmagnetic Kondo singlet (Hewson, 1997). Such screened moments act as strong elastic scatterers, accounting for the peculiar logarithmic increase of the resistivity upon cooling when small concentrations of certain magnetic impurities are introduced into nonmagnetic metals (Kondo, 1964). As was detected by Triplett and Phillips, 1971 for the dilute magnetic alloys CuCr and CuFe, the impurity-derived "incremental" low-temperature specific heat is proportional to temperature,  $\Delta C(T) = \gamma T$ , with a huge coefficient  $\gamma$ , that exceeds the Sommerfeld coefficient of the host metal Cu by more than a factor of 1000. This indicates the formation of a narrow local Kondo resonance at the Fermi level  $E_F$  and could be well described in the framework of a local Fermi liquid theory (Noziéres, 1974).

Heavy fermion metals comprise of two broad classes, lanthanides and actinides. The lanthanide-based variants are commonly considered to be ideal examples of Kondo lattice systems. These materials rather than having a dilute random distribution of local moments instead host a dense, periodic lattice of Kondo ions (Aliev *et al.*, 1983a; Brandt and Moshchalkov, 1984; Fulde *et al.*, 1988; Kuramoto and Kitaoka, 2012; Ott, 1987; Stewart, 1984). The first observation of heavy-fermion phenomena, i.e., the properties of a heavy Fermi liquid, was reported for the hexagonal paramagnetic compound CeAl<sub>3</sub> (Andres *et al.*, 1975). Here, the low-temperature specific heat, which is practically identical to the 4*f*-electron contribution, was found to be proportional to temperature with a  $\gamma$  coefficient of the same gigantic size as the aforementioned value for  $\mathbf{Cu}$ Fe. In addition, the lowtemperature resistivity of CeAl<sub>3</sub> was observed to follow a  $\Delta \rho(T) = AT^2$  dependence with a huge prefactor A. These early findings were ascribed to a 4f virtual bound state at  $E_F$ . A very similar large  $\gamma$  coefficient of the low-T specific heat to that of CeAl<sub>3</sub> could be estimated for the putative paramagnetic phase of the cubic antiferromagnet CeAl<sub>2</sub> (with a similar  $T_K$ ) by treating the Ce ions as isolated Kondo centers (Schotte and Schotte, 1975). This was taken as striking evidence for the heavy fermion phenomena in these Ce compounds indeed being due to the many-body Kondo effect rather than one-particle physics (Bredl *et al.*, 1978).

The participation of the f-electrons in the electronic structure at sufficiently low temperatures causes the renormalized electronic bands to take on significant 'f-electron' character and the effective mass of the charge carriers exceeds that of ordinary conduction electrons by a factor up to about a thousand (Zwicknagl, 1992). This leads to the aforementioned unusual behaviors of canonical heavy-fermion compounds such as  $CeCu_2Si_2$ , namely the  $\gamma$  coefficient is of the order of  $J/K^2$ mol (Fig. 1(a)), and there is a correspondingly enhanced temperature-independent Pauli spin susceptibility (Grewe and Steglich, 1991; Sales and Viswanathan, 1976) (Fig. 2). As displayed in Fig. 1(b), the electrical resistivity first exhibits an increase upon cooling from high temperatures, reflecting increasing incoherent scattering similar to that which occurs from dilute magnetic impurities. At lower temperatures however, Kondo lattice effects set in whereby coherent scattering of conduction electrons from the Kondo singlets below a characteristic temperature ( $T_K \approx 15$  K for CeCu<sub>2</sub>Si<sub>2</sub> (Stockert *et al.*, 2011)) leads to a pronounced decrease of the resistivity (Coleman, 2007). In several heavy-fermion metals, this decline of the resistivity follows a Fermi-liquid-type  $AT^2$ dependence with a huge A coefficient, whereas  $CeCu_2Si_2$ exhibits non-Fermi-liquid behavior, as discussed in the following sections.

Another stark difference between Kondo lattices and the dilute impurity case is that in the former the Kondo effect competes with the indirect Ruderman, Kittel, Kasuya and Yoshida (RKKY) magnetic exchange interaction (Kasuya, 1956; Ruderman and Kittel, 1954; Yosida, 1957) which tends to stabilize the f-electron moments. While predominant Kondo screening results in a paramagnetic heavy-fermion ground state, a dominant RKKY interaction causes magnetic, most frequently antiferromagnetic order. For quite a substantial number of these heavy-fermion metals the Kondo screening turns out to almost exactly cancel the RKKY interaction in the zerotemperature limit, which may give rise to a continuous zero-temperature quantum phase transition or quantum critical point (QCP), that can be easily accessed by adjusting a suitable non-thermal control parameter, e.g., pressure, doping or magnetic fields (Gegenwart et al., 2008; Sachdev, 2011; Si and Steglich, 2010; Stewart, 2001). To get rid of the large residual entropy accumulated at the QCP, symmetry-broken novel phases are often observed, notably 'unconventional' superconductivity which cannot be accounted for by the electron-phonon mediated pairing mechanism of Bardeen, Cooper, Schrieffer theory (Norman, 2013, 2011; Stewart, 2017).

The heavy fermion metal  $CeCu_2Si_2$  was also the first unconventional superconductor to be discovered (Steglich *et al.*, 1979) (Table I), and it has recently attracted much research interest again. While it was considered a (singleband) *d*-wave superconductor for many years (Fujiwara *et al.*, 2008; Ishida *et al.*, 1999), the observation of a fully developed energy gap at very low temperatures (Kittaka *et al.*, 2014; Pang *et al.*, 2018; Takenaka *et al.*, 2017; Yamashita *et al.*, 2017) has led to proposals of CeCu<sub>2</sub>Si<sub>2</sub> being a two-band *s*-wave superconductor both with (Ikeda *et al.*, 2015; Li *et al.*, 2018), and without (Takenaka *et al.*, 2017; Tazai and Kontani, 2018, 2019; Yamashita *et al.*, 2017) a sign-change of the order parameter.

In this Colloquium article, after a brief historical overview we discuss the seemingly conflicting results of a large number of experimental studies on this material and address the different theoretical models applied to understand the particular gap structure. These models are divided into two categories. One class builds on a normal state in the presence of Kondo-driven renormalization, and utilizes the multiplicity of orbitals to realize a new kind of pairing state. In the band basis, this takes the form of a band-mixing d + d-pairing state (Nica and Si, 2021), in parallel with the proposed pairing state for the iron chalcogenides that are among the highest- $T_{\rm c}$  Fe-based superconductors (Nica *et al.*, 2017) based on strongly orbital-selective electron correlations. The other class directly works in the band basis, treats the Coulomb repulsive interaction perturbatively, and constructs a pairing state using the standard procedure of finding irreducible representations of the crystalline lattice's point group. This is exemplified by the  $s_{+-}$  scenario (Ikeda et al., 2015; Li et al., 2018), by analogy to a similar construction applied to the Fe-based superconductors (Mazin *et al.*, 2008) in which a repulsive interband interaction leads to different signs of the order parameter between hole and electron pockets. We summarize the details of these considerations throughout the body of the article. In addition, we suggest that the insights gained from the analysis of the pairing state in CeCu<sub>2</sub>Si<sub>2</sub> will have broad implications on strongly correlated superconductivity in multi-orbital systems, and discuss future efforts that may shed further light on this canonical problem in the field of strongly correlated electron systems.

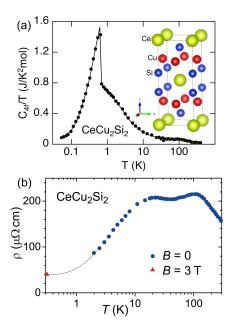


FIG. 1 (a) Contribution of the 4*f*-electrons to the specific heat in CeCu<sub>2</sub>Si<sub>2</sub>, plotted as  $C_{4f}/T$  vs. *T* on a logarithmic scale. Replotted from (Steglich, 1990). The solid line is a guide to the eyes. The inset shows the crystal structure of CeCu<sub>2</sub>Si<sub>2</sub> (ThCr<sub>2</sub>Si<sub>2</sub>-type structure, space group *I*4/*mmm*), where green, red, and blue spheres correspond to Ce, Cu and Si atoms (see labels), respectively. (b) Temperature dependence of the resistivity of CeCu<sub>2</sub>Si<sub>2</sub> on a logarithmic temperature scale, reproduced from Shan *et al.*, 2022.

## II. THE HISTORY OF HEAVY-FERMION SUPERCONDUCTIVITY

Given the strong pair-breaking effect of diluted localized spins in conventional superconductors (Abrikosov and Gor'kov, 1960; Matthias et al., 1958), the discovery of bulk superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> (Steglich *et al.*, 1979) came as a big surprise. In a BCS superconductor, a tiny amount of randomly distributed magnetic impurities fully suppresses the superconducting state (Maple, 1968; Maple et al., 1972; Riblet and Winzer, 1971; Steglich and Armbrüster, 1974), but the superconductivity is robust against doping with nonmagnetic impurities (Anderson, 1959; Balatsky et al., 2006). On the other hand, superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> relies on a periodic array of 100 at% magnetic Ce<sup>3+</sup> ions, each containing a localized 4f-shell occupied by one electron in a J = 5/2 Hund's rule ground state. Figure 2 displays the first reported evidence for the superconducting transition in CeCu<sub>2</sub>Si<sub>2</sub> at  $T_{\rm c} \approx 0.5$  K on annealed polycrystalline samples. Upon cooling through  $T_{\rm c}$ , the electrical resistivity falls to zero from a normal state with a non-saturated, nearly linear temperature dependence, while the ac susceptibility undergoes a rapid change from a strongly enhanced Pauli paramagnetic susceptibility to a large diamagnetic value [Fig. 2(a)].

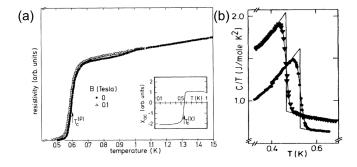


FIG. 2 (a) Resistivity  $\rho(T)$ , ac-susceptibility  $\chi_{ac}(T)$  and (b) specific heat as C/T vs T for polycrystalline CeCu<sub>2</sub>Si<sub>2</sub> indicating bulk superconductivity at  $T_c \approx 0.5$  K, after (Steglich *et al.*, 1979). The Pauli susceptibility  $(T > T_c)$  shown in the inset amounts to  $\chi_P = 82 \times 10^{-9} \text{m}^3/\text{mol}$  (Aarts, 1984). Note that the normal-state values of both  $\rho(T)$  and C(T)/T point to non-Fermi-liquid behavior. In (b) results from two different samples, with the same nominal composition and prepared in the same way, are shown. Reproduced with permission from Steglich *et al.*, 1979.

Two early observations have led to the conclusion that CeCu<sub>2</sub>Si<sub>2</sub> must be an unconventional bulk superconductor: (i) the nonmagnetic reference compound LaCu<sub>2</sub>Si<sub>2</sub> is not a superconductor, at least down to 20 mK (Steglich et al., 1979), and (ii) a tiny amount of nonmagnetic (as well as magnetic) substitution at the level of 1 at %may lead to a complete suppression of superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> (Spille *et al.*, 1983), see Sec. III.E. Further evidence for this conclusion could be drawn from the specific-heat results shown in Fig. 2(b). Here the normal-state values of C(T)/T are of the order of several hundreds of mJ/mol K<sup>2</sup>; they substantially increase upon lowering the temperature and extrapolate to about  $1 \text{ J/mol } \text{K}^2$  in the zero-temperature limit. This exceeds the Sommerfeld coefficient of the electronic specific heat of Cu by more than a factor of 1000 and this proves that similar to CeAl<sub>3</sub>, the measured specific heat in this lowtemperature range is practically identical with the electronic contribution ( $\approx C_{4f}$ ). The corresponding renormalized kinetic energy,  $k_{\rm B}T_{\rm F}^*$ , corresponds to the Kondo screening energy,  $k_{\rm B}T_{\rm K}$ ,  $T_{\rm K} \approx 15$  K (Stockert *et al.*, 2011). Therefore, the ratio  $T_{\rm c}/T_{\rm F}^*$  is of the order of 0.04, compared to  $T_c/T_F \approx 10^{-3} - 10^{-4}$  for an ordinary BCS superconductor, highlighting CeCu<sub>2</sub>Si<sub>2</sub> as a 'high- $T_{\rm c}$  superconductor' in a normalized sense (Steglich et al., 1979). On the other hand, the ratio  $T_{\rm F}^*/\theta_{\rm D}$ , where  $\theta_{\rm D}$  is the Debye temperature, also amounts to about 0.05, while in a main group metal or transition metal,  $T_{\rm F}/\theta_{\rm D}$  is of order 100. The latter warrants the electronphonon coupling in conventional BCS superconductors to be retarded, such that the Coulomb repulsion between conduction electrons is minimized and isotropic s-wave Cooper pairs may be formed.

For heavy-fermion metals, such phonon-mediated on-

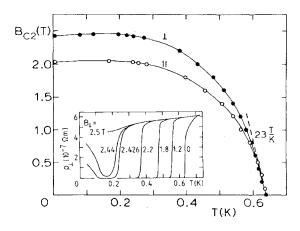


FIG. 3 Upper critical magnetic field  $B_{c2}$  vs T of a CeCu<sub>2</sub>Si<sub>2</sub> single crystal for fields applied within (||) and perpendicular to  $(\perp)$  the Ce planes as obtained from  $\rho(T)$ , measured parallel to the respective field. Only a moderate anisotropy, but a giant initial slope at  $T_c$  is found for  $B_{c2}(T)$ . Note the shallow maximum of  $B_{c2}(T)$  near T = 0.15 K as reflected in the inset by the reentrant  $\rho(T)$  behavior for  $B \geq 2.4$  T. Reproduced with permission from Assmus *et al.*, 1984.

site pairing is clearly prohibited because of their low renormalized Fermi velocity which is, at best, of the order of the velocity of sound. Nevertheless, an early proposal was put forward to explain heavy-fermion superconductivity in  $CeCu_2Si_2$  by a coupling of the heavy charge carriers to the breathing mode (Razafimandimby et al., 1984), while recently such a phonon-mediated superconductivity for this compound was expected to be realized near a magnetic instability, thanks to the vertex corrections due to multipole charge fluctuations (Tazai and Kontani, 2018). On the other hand, a broad consensus evolved shortly after the discovery of heavy-fermion superconductivity that here an electronic pairing mechanism must be operating (Machida, 1983; Tachiki and Maekawa, 1984). Therefore, CeCu<sub>2</sub>Si<sub>2</sub> was soon regarded generally as an unconventional, i.e., non-phonon-driven, superconductor. Because of the phenomenological similarity of heavy-fermion superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> with the superfluidity in <sup>3</sup>He (Osheroff *et al.*, 1972a,b), a magnetic coupling mechanism appeared to be most natural (Anderson, 1984).

The jump height at the superconducting transition,  $\Delta C/T_c$ , is comparable to the Sommerfeld coefficient, extrapolated to T = 0,  $\gamma_0 = C(T \to 0)/T \approx 1$  J/mol K<sup>2</sup> (Fig. 2(b)). This not only proved bulk superconductivity, but also led to the conclusion that the Cooper pairs are formed by heavy-mass quasiparticles (Steglich *et al.*, 1979) and to the term 'heavy-fermion superconductivity' (Rauchschwalbe *et al.*, 1982). In fact, if the superconductivity were solely carried by the coexisting light conduction electrons, the jump in the electronic specificheat coefficient at  $T_c$  would have been so tiny that within the scatter of the data it would not be resolvable in Fig. 2(b). It should be noted that recent theoretical considerations have shown that in order to form Cooper pairs in CeCu<sub>2</sub>Si<sub>2</sub>, a very large kinetic energy cost, exceeding the binding energy by a factor as high as 20, is necessary to overcompensate the similarly large exchange energy between the paired heavy quasiparticles (Stockert *et al.*, 2011). The large kinetic-energy cost has been interpreted in terms of a transfer of single-electron spectral weight to energies above a Kondo-destruction energy scale at the QCP,  $T^*$ , that is nonzero but small compared to the bare Kondo scale (Stockert *et al.*, 2011), see Sec. III.C.

The two polycrystalline samples exploited in Fig. 2(b)were prepared and annealed in the same way. Nevertheless, their specific-heat values were found to be significantly different. These variations of physical properties from one sample to the other added to the severe skepticism (Hull et al., 1981; Schneider et al., 1983) which existed throughout the first few years after the report of bulk superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> (Steglich *et al.*, 1979), subsequently confirmed by other groups (Aliev et al., 1983b, 1984; Ishikawa et al., 1983; Ōnuki et al., 1984). The cause for these 'sample dependences', see also (Aliev et al., 1983b; Stewart et al., 1983), was resolved only many years later by a thorough study of the chemical phase diagram (Müller-Reisener, 1995; Steglich et al., 2001), and the observation of a quantum critical point (QCP) that is located inside the narrow homogeneity range (Lengyel et al., 2011; Steglich et al., 2001), see Sec. III.C. The above-mentioned skepticism could be overcome after a few years, when high-quality single crystals of CeCu<sub>2</sub>Si<sub>2</sub> were prepared (Assmus et al., 1984; Onuki et al., 1984) and found to show even more pronounced superconducting phase transition anomalies compared to polycrystals. The upper critical field curve  $B_{c2}(T)$  of such a single crystal is displayed in Fig. 3. It reveals:

(i) Only a small anisotropy for the field being applied either parallel or perpendicular to the basal tetragonal plane [inset of Fig. 1], contrasting a pronounced anisotropy in the electrical resistivity (Schneider *et al.*, 1983).

(ii) A shallow maximum around T = 0.15 K (inset) which seems to correspond to a low-temperature hump in C(T)/T (Bredl *et al.*, 1984), also observed for CeAl<sub>3</sub> (Bredl *et al.*, 1984; Flouquet *et al.*, 1982; Steglich *et al.*, 1985b), which was ascribed to the opening of a partial coherence gap in the 4f-quasiparticle density of states at the Fermi level, see Table I. Later this hump was ascribed as being related to antiferromagnetic correlations (Steglich *et al.*, 1996; Stockert *et al.*, 2004). For UBe<sub>13</sub> too, a broad peak in C(T)/T at  $T_{\rm L} \approx 0.6$  K had been detected (Rauchschwalbe *et al.*, 1987a,b) and subsequently identified (Kromer *et al.*, 1998, 2000) as the precursor of an anomaly indicating a continuous phase transition at  $T_{\rm c2}$  below the superconducting  $T_{\rm c1}$  discovered for  $(U_{1-x}Th_x)Be_{13}$  in the critical concentration range 0.019  $\leq x \leq 0.045$  (Ott *et al.*, 1985). The nature of this lower-lying phase transition has yet to be resolved (Steglich and Wirth, 2016). While ultrasoundattenuation results (Batlogg *et al.*, 1985) hint at a SDW transition, pressure studies (Lambert *et al.*, 1986) and results of the lower critical field (Rauchschwalbe *et al.*, 1987a) highlight a superconducting nature of the transition at  $T_{c2}$ .

(iii) A giant initial slope at  $T_{\rm c}$  which supports the massive nature of the Cooper pairs as inferred from the giant jump anomaly  $\Delta C/T_{\rm c}$ .

(iv) Quite a strong Pauli limiting effect in the lowtemperature regime for both field configurations. This discards odd-parity (spin-triplet) pairing as observed in superfluid <sup>3</sup>He (Leggett, 1975) and originally assumed for heavy-fermion superconductors (Anderson, 1984). A spatially modulated superconducting state in CeCu<sub>2</sub>Si<sub>2</sub> at very low temperature close to the upper critical field was recently proposed based on Cu-NMR results (Kitagawa *et al.*, 2018).

A dc Josephson effect with a critical pair current of ordinary size was observed on a weak link between polycrystalline CeCu<sub>2</sub>Si<sub>2</sub> and Al (Steglich *et al.*, 1985b). This as well as Knight shift results from <sup>29</sup>Si NMR (Ueda *et al.*, 1987) lent further support to even-parity (spin-singlet) pairing in CeCu<sub>2</sub>Si<sub>2</sub>.

At around the same time, theorists proposed *d*-wave superconductivity mediated by antiferromagnetic spin fluctuations (Miyake *et al.*, 1986; Scalapino *et al.*, 1986). These theoretical studies extend the theory of ferromagnetic paramagnons developed in the <sup>3</sup>He context to the antiferromagnetic case, but the Kondo effect responsible for the heavy mass was not addressed. In more recent years, the Kondo effect has been incorporated into the study of heavy-fermion quantum criticality (Gegenwart *et al.*, 2008), with an emphasis on the notion of Kondo destruction (Coleman *et al.*, 2001; Si *et al.*, 2001). A corresponding theory for quantum-criticality-driven superconductivity in Kondo-lattice models has been advanced (Hu *et al.*, 2021a).

The discovery of heavy-fermion superconductivity in the cubic compound UBe<sub>13</sub> (Ott *et al.*, 1983) proved this phenomenon to be general and not restricted to a single material. Thereafter, UPt<sub>3</sub> (Stewart *et al.*, 1984), URu<sub>2</sub>Si<sub>2</sub> (Maple *et al.*, 1986; Palstra *et al.*, 1985; Schlabitz *et al.*, 1984, 1986), U<sub>2</sub>PtC<sub>2</sub> (Meisner *et al.*, 1984), UNi<sub>2</sub>Al<sub>3</sub> (Geibel *et al.*, 1991b), and UPd<sub>2</sub>Al<sub>3</sub> (Geibel *et al.*, 1991a) were found to be heavyfermion superconductors, too. They were followed by the pressure-induced Ce-based heavy-fermion superconductors CeCu<sub>2</sub>Ge<sub>2</sub> (Jaccard *et al.*, 1992), CeRh<sub>2</sub>Si<sub>2</sub> (Movshovich *et al.*, 1996), CeIn<sub>3</sub> and CePd<sub>2</sub>Si<sub>2</sub> (Mathur *et al.*, 1998). In the years after 2000, many of the Cebased tetragonal, so-called 115 materials, which are obtained by increasing the c/a ratio of cubic CeIn<sub>3</sub> by inserting an additional layer of  $T \ln_2$  (T: Co, Rh or Ir), as well as the related 218 and 127 compounds were shown to be heavy-fermion superconductors (Sarrao and Thompson, 2007; Thompson and Fisk, 2012). One of the Pubased isostructural compounds, PuCoGa<sub>5</sub>, exhibits the record  $T_{\rm c} = 18.5$  K for this class of superconductors (Sarrao et al., 2002). Its Rh homologue PuRhGa<sub>5</sub> (Wastin et al., 2003) as well as NpPd<sub>5</sub>Al<sub>2</sub> (Aoki et al., 2009) also show enhanced  $T_{\rm c}$  values of 8.7 K and 4.9 K, respectively. The discovery of heavy-fermion superconductivity in the noncentrosymmetric compound CePt<sub>3</sub>Si (Bauer et al., 2004) stimulated the search for noncentrosymmetric heavy-fermion as well as weakly-correlated superconductors (Bauer et al., 2012; Smidman et al., 2017), and resulted in several Ce-based counterparts. Such a lack of inversion symmetry allows for a mixing between even- and odd-parity pairing states (Gor'kov and Rashba, 2001). In the case of  $CeRh_2As_2$  which has a locally noncentrosymmetric crystal structure, two-phase superconductivity has been reported very recently, along with a proposal for a field-induced transition between an even parity phase at low fields, and an odd parity phase at elevated fields (Khim et al., 2021). Two different superconducting phases in the presence of weak antiferromagnetic order have already been established earlier for  $UPt_3$  (Joynt and Taillefer, 2002), and multifaceted behavior has been reported for thoriated  $UBe_{13}$  (Heffner et al., 1990; Oeschler et al., 2003; Ott et al., 1985) as well as URu<sub>2</sub>Si<sub>2</sub>, exhibiting a hidden-order phase (Mydosh et al., 2020). All of the three latter materials show a superconducting state with broken time-reversal symmetry (Heffner et al., 1990; Luke et al., 1993; Schemm et al., 2015, 2014).

There are only two Yb-based heavy-fermion superconductors known so far.  $\beta$ -YbAlB<sub>4</sub> with  $T_c = 80 \text{ mK}$ (Nakatsuji et al., 2008) is an intermediate-valence compound showing quantum criticality without tuning (Matsumoto et al., 2011). YbRh<sub>2</sub>Si<sub>2</sub> (Nguyen et al., 2021; Schuberth et al., 2016, 2022; Shan et al., 2022) exhibits an antiferromagnetic QCP at  $B \approx 0$  which is induced by nuclear spin order (below  $T_{\rm A} = 2.3 \text{ mK}$ ). The latter strongly competes with the primary 4*f*-electronic order ( $T_{\rm N} = 70$ mK) and causes the emergence of heavy-fermion superconductivity at ultra-low temperatures,  $T_{\rm c} = 2$  mK. As shown by (Schuberth et al., 2022), measurements of the Meissner effect point to the existence of bulk superconductivity up to magnetic fields of the order of B = 40 mT (about two-thirds of  $B_N$ , the critical field designating the Kondo-destruction QCP). Furthermore recent resistivity investigations suggest that at such elevated fields superconductivity may be of the spin-triplet variety (Nguyen et al., 2021), which is theoretically supported based on unconventional superconductivity driven by Kondo destruction at magnetic-field-induced quantum criticality in the presence of an effective Ising spin anisotropy (Hu et al., 2021b). Correlated Pr-based superconductors were also found.  $PrOs_4Sb_{12}$  shows a heavy-fermion normal-state and superconducting properties due to dominant quadrupolar rather than dipolar fluctuations (Maple *et al.*, 2002; Rotundu *et al.*, 2004), while  $PrTi_2Al_{20}$ ,  $PrV_2Al_{20}$  and  $PrIr_2Zn_{20}$  are quadrupolar Kondo-lattice systems exhibiting superconductivity and quadrupolar order (Onimaru *et al.*, 2011; Sakai *et al.*, 2012; Tsujimoto *et al.*, 2014).

A few heavy fermion superconductors are prime candidates for odd-parity pairing, i.e., the ferromagnetic compounds UGe<sub>2</sub> (Saxena *et al.*, 2000), UCoGe (Lévy *et al.*, 2005) and URhGe (Huy *et al.*, 2007) as well as UPt<sub>3</sub> (Tou *et al.*, 1998) and UNi<sub>2</sub>Al<sub>3</sub> (Ishida *et al.*, 2002). Also being discussed is UTe<sub>2</sub> (Aoki *et al.*, 2019; Ran *et al.*, 2019), which has been suggested to be a chiral topological superconductor (Jiao *et al.*, 2020), for which the role of Kondo and RKKY interactions in the magnetic correlations and superconductivity has been discussed (Chen *et al.*, 2021; Duan *et al.*, 2021, 2020; Knafo *et al.*, 2021; Thomas *et al.*, 2020).

In concluding this survey, we can state that currently about fifty heavy-fermion superconductors are known. Most of these materials are discussed in (Pfleiderer, 2009). They are complemented by the already mentioned compounds  $\beta$ -YbAlB<sub>4</sub>, Pr(Ti,V)<sub>2</sub>Al<sub>20</sub>, PrIr<sub>2</sub>Zn<sub>20</sub> YbRh<sub>2</sub>Si<sub>2</sub>, UTe<sub>2</sub>, and CeRh<sub>2</sub>As<sub>2</sub>. The majority of heavyfermion superconductors are believed to have anisotropic even-parity Cooper pairing. In the following section, we present the early evidence for single-band *d*-wave superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> down to about T = 0.1 K, see also (Stockert *et al.*, 2012).

## III. EVIDENCE FOR *d*-WAVE SUPERCONDUCTIVITY IN $CeCu_2Si_2$ ABOVE 0.1 K

#### A. Phase diagram

One of the major distinguishing features which sets CeCu<sub>2</sub>Si<sub>2</sub> apart from previously-known BCS superconductors is the close proximity between magnetism and superconductivity in the phase diagram, where both are due to the same localized 4f-electrons. This is reflected in the observation that slight tuning of the Cu:Si ratio within the homogeneity range can lead to crystals with ground states which are entirely antiferromagnetic (A-type), superconducting (S-type) or exhibit both superconductivity and magnetism (A/S-type) (Seiro *et al.*, 2010; Steglich et al., 1996). While within the context of BCS theory, magnetism and superconductivity are generally considered antagonistic, superconductivity on the border of magnetism is a common feature of broad classes of unconventional superconductors (Norman, 2013, 2011; Stewart, 2017) including heavy-fermion superconductors (Pfleiderer, 2009; Steglich and Wirth, 2016), cuprates (Lee et al., 2006; Proust and Taillefer,

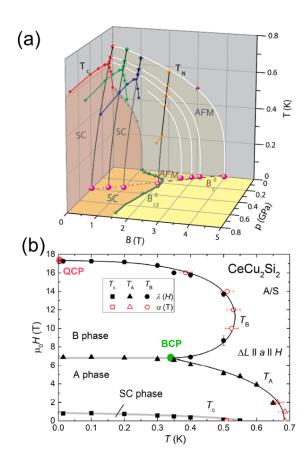


FIG. 4 (a) Temperature-pressure-magnetic field phase diagram of a single crystal of A/S-type CeCu<sub>2</sub>Si<sub>2</sub>. Reproduced with permission from Lengyel *et al.*, 2011. (b) Magnetic field - temperature diagram of single crystalline CeCu<sub>2</sub>Si<sub>2</sub>, where positions of the field-induced bicritical point (BCP) and QCP are also displayed. Reproduced with permission from Weickert *et al.*, 2018.

2019), iron-based pnictides and chalcogenides (Si *et al.*, 2016; Stewart, 2011), organic superconductors (Kanoda, 2008; Lang and Müller, 2003; Maple *et al.*, 2004) and twisted graphene superlattices (Andrei and MacDonald, 2020; Cao *et al.*, 2018), and may be related to the occurrence of Cooper pairs with a magnetically driven pairing interaction (Scalapino, 2012), rather than the conventional electron-phonon pairing mechanism.

The temperature-pressure-magnetic field diagram of an A/S-type single crystal is displayed in Fig. 4(a) (Lengyel *et al.*, 2011). At ambient pressure, two zero-field phase transitions can be detected in specific heat measurements corresponding to an antiferromagnetic transition at  $T_{\rm N} = 0.69$  K and a subsequent superconducting transition at  $T_{\rm c} = 0.46$  K. The application of moderate pressure rapidly suppresses  $T_{\rm N}$ , while  $T_{\rm c}$  shows a slight increase, and once  $T_{\rm N}$  is suppressed below  $T_{\rm c}$ , no antiferromagnetic transition is observed. When a magnetic field is applied, both  $T_{\rm N}$  and  $T_{\rm c}$  are suppressed, but the more rapid decrease of  $T_{\rm c}$  with field allows for  $T_{\rm N}$  (extrapolated

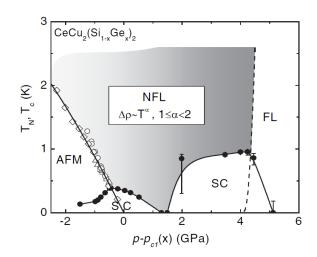


FIG. 5 Temperature - pressure phase diagram of  $\text{CeCu}_2(\text{Si}_{1-x}\text{Ge}_2)_2$ , which exhibits two superconducting domes, one centered around a lower pressure  $p_{c1}$  associated with an antiferromagnetic QCP, while the dome at higher pressures is near a possible valence transition. The diamonds, circles, triangles and squares correspond to compositions with x = 0.25, 0.1, 0.05, and 0.01, respectively. The dashed line displays the anticipated line of first-order valence transitions, ending in a critical point somewhere between 10 and 20 K. Solid lines are guides to the eye. Reproduced with permission from Yuan *et al.*, 2006.

to B = 0) to be tracked as a function of pressure to lower temperatures. From extrapolating the positions of  $B_c^0$ (where  $T_N$  vanishes) for fixed values of pressure, a line of QCPs is inferred to lie in the zero-temperature pressurefield phase diagram shown in Fig. 4(a).  $B_c^0(p) = 0$  at  $p_c = 0.39$  GPa, which is almost twice as large as the pressure where  $B_{c2}^0$  vs p exhibits a local maximum (see Sec. V).  $p_c$  can be forced to vanish, if the composition of the (homogeneous) sample becomes slightly more enriched by Cu (i.e., by reducing the average unit-cell volume). Although the ambient-pressure, zero-field QCP is masked by superconductivity, its nature can be well explored by studying the low-temperature normal state of such an S-type sample induced by applying a small external magnetic field, see Sec. III.C.

Detailed measurements of the elastic constants, thermal expansion, and magnetostriction revealed the presence of a field-induced 'B' phase, in addition to the magnetic 'A' phase found at low fields (Bruls *et al.*, 1994; Weickert *et al.*, 2018). The field-temperature phase diagram is displayed in Fig. 4(b), where there are second-order lines between the paramagnetic state and both the 'A' and 'B' phases, while going from the 'A' to 'B' phase corresponds to a first-order transition, leading to a bicritical point in the phase diagram between these phases (Weickert *et al.*, 2018). Measurements to very low temperatures and high fields show the suppression of the 'B' phase to zero temperature in applied fields of around 17 T, giving rise to a field-induced QCP. The nature of the transition from 'A' to 'B' phase is still to be determined, where the small change in magnetization between the two phases suggests that 'B' (like 'A', see below) also corresponds to a spin-density-wave (SDW) phase (Tayama *et al.*, 2003; Weickert *et al.*, 2018).

The shape of the superconducting region in the temperature-pressure phase diagram of S-type CeCu<sub>2</sub>Si<sub>2</sub> is guite unusual compared to other heavy-fermion superconductors (Knebel et al., 2006; Mathur et al., 1998), namely at low and moderate pressures  $T_{\rm c}$  does not change rapidly with pressure, while at higher pressures it reaches a maximum at around 4 GPa, well away from the point where magnetism is suppressed (Bellarbi *et al.*, 1984; Thomas et al., 1993; Yuan et al., 2003, 2006). Remarkably, upon substituting 10 at% of Si by Ge, which substantially reduces  $T_{\rm c}$ , it is found that this actually results in two superconducting domes in the phase diagram, as shown in Fig. 5, where one is centered around the antiferromagnetic QCP, and another with a higher maximum  $T_{\rm c}$  occuring at higher pressures (Yuan *et al.*, 2003, 2006). It has been suggested that these two domes correspond to superconductivity with different unconventional pairing mechanisms, with the low pressure dome corresponding to magnetically driven superconductivity and the high pressure dome driven by charge (valence) fluctuations (Holmes et al., 2004; Yuan et al., 2003). A similar phase diagram with two superconducting domes was reported for the (Pu,Co)-based 115 systems by (Bauer et al., 2012). Here, the higher  $T_c$  of PuCoGa<sub>5</sub> (18.5 K) compared to  $PuCoIn_5$  (2.5 K) was ascribed to the superconductivity of the former arising from a valence instability, while that of the latter was associated with a magnetic quantum critical point.

#### B. Origin of the A-phase in $CeCu_2Si_2$

Although the relative increase of the electrical resistivity below the ordering temperature  $T_{\rm N}$  suggested the opening of an excitation gap in CeCu<sub>2</sub>Si<sub>2</sub> due to a SDWtype of magnetic order (Gegenwart et al., 1998), direct evidence for such a scenario was lacking for a long time. The first indications for antiferromagnetic order as the characteristic of the A-phase came from NMR (Nakamura et al., 1988) and  $\mu$ SR measurements (Uemura et al., 1988, 1989) in the late 1980s, both detecting a static magnetic field (at the muon site or the nuclear site, respectively) in the ordered state. In these measurements even an incommensurate type of magnetic order in CeCu<sub>2</sub>Si<sub>2</sub> was proposed because of the distribution of local magnetic fields detected. Interestingly, while pronounced phase transition anomalies at  $T_N$  were found in both elastic-constant and thermal-expansion measurements (Bruls *et al.*, 1994), no corresponding feature was seen in the magnetic susceptibility for a long time, until a cusp-like anomaly could eventually be resolved in the susceptibility when monitored with the aid of a highresolution Faraday magnetometer (Tayama *et al.*, 2003).

In 1997, antiferromagnetic order was observed in the reference compound CeCu<sub>2</sub>Ge<sub>2</sub> using single crystal neutron diffraction (Krimmel et al., 1997) which later could be related to the nesting properties of the Fermi surface (Zwicknagl, 2007). In order to unravel the nature of the A-phase in pure  $CeCu_2Si_2$ , an approach to study the magnetic order in the Ge-substituted system  $CeCu_2(Si_{1-x}Ge_x)_2$  was chosen. Starting from pure CeCu<sub>2</sub>Ge<sub>2</sub> the antiferromagnetic order was followed in  $CeCu_2(Si_{1-x}Ge_x)_2$  with decreasing Ge content. Initially the incommensurate order in  $\text{CeCu}_2(\text{Si}_{1-x}\text{Ge}_x)_2$  was detected only for  $x \ge 0.6$  in neutron powder diffraction (Knebel et al., 1996; Krimmel and Loidl, 1997). However, measurements in powder samples with lower Ge concentrations were unsuccessful since the ordering temperature as well as the magnetically ordered moment are largely reduced for samples with low Ge content. Until the early 2000s only very small single crystals were available just enabling thermodynamic and transport measurements. Then, with substantially improved crystal growth techniques (Cao et al., 2011; Seiro et al., 2010), quite large single crystals of  $CeCu_2Si_2$  and  $CeCu_2(Si_{1-x}Ge_x)_2$  (up to  $\sim \mathrm{cm}^3$  size) could be synthesized. Now performing single crystal neutron diffraction on  $\text{CeCu}_2(\text{Si}_{1-x}\text{Ge}_x)_2$  the antiferromagnetic order could be followed to much lower Ge concentrations (Stockert et al., 2005, 2003). Finally, incommensurate antiferromagnetic order was even detected in pure A-type CeCu<sub>2</sub>Si<sub>2</sub> with a small ordered magnetic moment  $\approx 0.1 \,\mu_{\rm B}/{\rm Ce}$  (Stockert *et al.*, 2004) as shown in Fig. 6(a). The propagation wave vector  $\mathbf{k} = \mathbf{Q}_{AF} =$  $(0.215 \ 0.215 \ 0.53)$  at  $T = 50 \,\mathrm{mK}$  agrees well with theoretical calculations of the Fermi surface using a renormalized band method (Stockert et al., 2004; Zwicknagl, 1992; Zwicknagl and Pulst, 1993). They indicate nesting properties in the corrugated part of the cylindrical Fermi surface of the heavy quasiparticles at the X point of the bulk Brillouin zone [see Fig. 6(b) and Sec. IV.B, below]. Hence, the magnetic order in  $CeCu_2Si_2$  is an incommensurate SDW. This is further supported by the temperature dependence of the propagation wave vector below the ordering temperature. It is worth noting that the propagation vectors in  $\text{CeCu}_2(\text{Si}_{1-x}\text{Ge}_x)_2$  are quite similar with the largest difference being the a\*, b\* component changing from 0.215 in pure CeCu<sub>2</sub>Si<sub>2</sub> to 0.282in  $CeCu_2Ge_2$  and almost no change in the c\* component remaining close to 0.5 (Stockert *et al.*, 2005).

The interplay between antiferromagnetism and superconductivity has been studied on small A/S-type CeCu<sub>2</sub>Si<sub>2</sub> single crystals, where  $\mu$ SR measurements indicated a competition of both phenomena with a full repulsion of antiferromagnetism in the superconducting state (Feyerherm *et al.*, 1997; Luke *et al.*, 1994; Stockert *et al.*, 2006), in contrast to earlier reports on polycrystalline

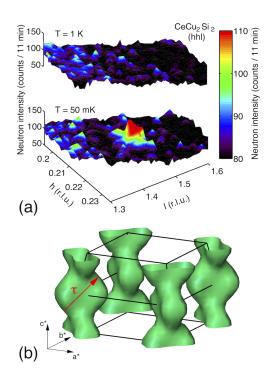


FIG. 6 (a) Neutron-diffraction intensity map of the reciprocal  $(h \ h \ l)$  plane around  $\mathbf{Q} = (0.21 \ 0.21 \ 1.45)$  in A-phase CeCu<sub>2</sub>Si<sub>2</sub> at T = 50 mK and 1 K. (b) Main heavy Fermi surface sheet in CeCu<sub>2</sub>Si<sub>2</sub> indicating the columnar nesting with wave vector  $\boldsymbol{\tau}$ . Reproduced with permission from Stockert *et al.*, 2004.

samples (Uemura *et al.*, 1988). Neutron diffraction on quite large A/S-type CeCu<sub>2</sub>Si<sub>2</sub> single crystals also revealed that magnetic order and superconductivity do not coexist in CeCu<sub>2</sub>Si<sub>2</sub> on a microscopic scale (Arndt *et al.*, 2010; Thalmeier *et al.*, 2005).

#### C. Quantum criticality

Common to many magnetically ordered Ce-based heavy-fermion systems, the application of pressure tunes the relative strengths of the magnetic exchange interactions (Ruderman-Kittel-Kasuya-Yosida interaction) and Kondo coupling, and for sufficiently large pressures the Kondo interaction dominates, suppressing magnetic order. In several cases this allows for the tuning of a secondorder antiferromagnetic transition continuously to zero temperature at a QCP, leading to the breakdown of Fermi liquid behavior at finite temperatures (Löhneysen *et al.*, 2007; Sachdev, 2011; Stewart, 2001, 2006). The RKKY interaction leads to antiferromagnetic correlations between the local moments, which reduce the amplitude of the Kondo singlet in the ground state.

Two classes of QCPs have been advanced in recent years, depending on whether this static Kondo-singlet amplitude is destroyed (Coleman *et al.*, 2001; Senthil

et al., 2004; Si et al., 2001) or remains nonzero at the antiferromagnetic QCP (Coleman and Schofield, 2005; Si and Steglich, 2010). Prototype examples of the former case of Kondo-destruction quantum criticality include Au-doped CeCu<sub>6</sub> (Schröder et al., 2000), YbRh<sub>2</sub>Si<sub>2</sub> (Friedemann et al., 2010; Gegenwart et al., 2007; Paschen et al., 2004) and CeRhIn<sub>5</sub> (Park et al., 2006; Shishido et al., 2005). In the latter case, the quantum critical behavior at energies below a certain crossover scale  $E^* = k_B T^*$  is of the SDW-type, however the critical fluctuations of the Kondo effect, i.e. partial Mott physics, sets in above the crossover energy scale. CeCu<sub>2</sub>Si<sub>2</sub> shows evidence for a line of QCPs as a function of magnetic field under pressure, in the vicinity of the disappearance of magnetic order, see Fig. 4(a). For an S-type polycrystalline sample in the low temperature normal state, the signatures of a 3D SDW-type QCP are found from a  $T^{\frac{3}{2}}$  dependence of the resistivity, as well as a  $-T^{\frac{1}{2}}$  dependence of the specific heat coefficient (Gegenwart et al., 1998). In addition, the spin-excitation spectrum at the nesting wave vector  $\boldsymbol{\tau} \approx \mathbf{Q}_{AF}$  in the normal state of superconducting (S-type) CeCu<sub>2</sub>Si<sub>2</sub> displays an almost critical slowing down when superconductivity is suppressed by a magnetic field (Arndt et al., 2011), as expected for a compound located very close to a QCP. Moreover, an  $E/T^{3/2}$  scaling of the normal state magnetic response [Fig. 7(b)] and a  $T^{3/2}$  dependence of the inverse lifetime of the spin fluctuations [Fig. 7(d)] indicate that in  $CeCu_2Si_2$  a 3D SDW-type QCP seems to be realized, in line with the aforementioned thermodynamic and transport measurements (Arndt et al., 2011; Stockert et al., 2011). Measurement of the damping rate from inelastic neutron scattering (INS) has provided evidence that the Kondo-destruction temperature scale,  $T^*$ , is nonzero but small (Smidman et al., 2018) compared to the bare Kondo scale of 15 K. Changes in C(T)/T from a squareroot to logarithmic dependence and in the quasielastic neutron-scattering damping rate from  $T^{3/2}$  to T-linear behavior are observed between 1 and 2 K, suggesting that  $T^*$  is of a similar size.

It is to be noted that  $\mathbf{Q}_{AF}$  is not a singular point in  $(\mathbf{Q}, \omega)$  space, but paramagnons are emerging out of  $\mathbf{Q}_{AF}$  with an initial linear dispersion (Arndt *et al.*, 2011; Stockert et al., 2011). Comparing the magnetic response in the normal state of superconducting (Stype)  $CeCu_2Si_2$  and the antiferromagnetic state in Atype  $CeCu_2Si_2$ , the dispersion of the (para)magnons in both states was found to be very similar, with just higher intensity for the A-type sample (Huesges et al., 2018). Upon entering the superconducting state, the dispersion of the paramagnons remains (almost) unchanged with deviations only occurring at low energy transfers below 0.5 meV due to the formation of a spin gap (Stockert et al., 2011), see Sec. III.D. Very recently, INS on S-type CeCu<sub>2</sub>Si<sub>2</sub> have been extended to higher energy transfers up to several meV (Song *et al.*, 2021). These mea-

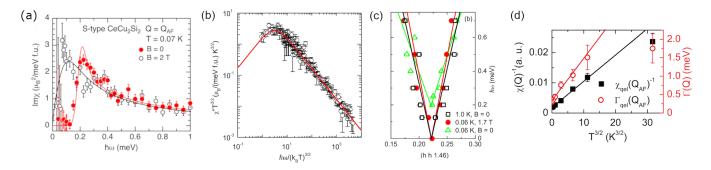


FIG. 7 Spin dynamics in CeCu<sub>2</sub>Si<sub>2</sub>. (a) Low-energy spin excitations in *S*-type CeCu<sub>2</sub>Si<sub>2</sub> at  $\mathbf{Q}_{AF}$  and T = 0.07 K in the superconducting (B = 0) and the normal state (B = 2 T). Reproduced from Stockert *et al.*, 2011. (b) Scaling of the normal-state quasielastic response in *S*-type CeCu<sub>2</sub>Si<sub>2</sub> at  $\mathbf{Q}_{AF}$  and at  $B = B_{c2} = 1.7 \text{ T}$  indicating universal scaling of the dynamical susceptibility  $\chi''T^{3/2}$  vs.  $\omega/T^{3/2}$ . (c) Dispersion of the spin excitations in the normal-state magnetic response at  $\mathbf{Q} = \mathbf{Q}_{AF}$  in *S*-type CeCu<sub>2</sub>Si<sub>2</sub> versus  $T^{3/2}$ . (b)-(d) are reproduced with permission from Arndt *et al.*, 2011.

surements fully confirm the previous experiments at low energies, i.e., the spin gap in the superconducting state (Stockert *et al.*, 2011) and the dispersive paramagnons (Arndt *et al.*, 2011; Huesges *et al.*, 2018; Stockert *et al.*, 2011). However, in addition, the dispersive spin excitations are now found to change to a dispersionless column in energy above  $\approx 1.5 \text{ meV}$  (Song *et al.*, 2021). The transition from dispersive to dispersionless magnetic excitations occurs around  $k_{\rm B}T_{\rm K}$ , i.e., the characteristic local energy scale in CeCu<sub>2</sub>Si<sub>2</sub>. Currently it is an open question, if and how these high-energy spin excitations are related to the unconventional heavy-fermion superconductivity in CeCu<sub>2</sub>Si<sub>2</sub>.

Another issue that has to be clarified by future work concerns the difference in the quantum critical exponent  $\alpha$  of the temperature dependence in the low-T resistivity of undoped CeCu<sub>2</sub>Si<sub>2</sub>,  $\Delta \rho(T) = A'T^{\alpha}$ . As already mentioned, this was found to be  $\alpha = \frac{3}{2}$  in (Gegenwart *et al.*, 1998), whereas  $\alpha = 1$  was reported in (Yuan *et al.*, 2003, 2006). In both cases, the samples had been prepared with some Cu excess pointing to S-type samples. As shown by neutron diffraction (Stockert *et al.*, 2004) as well as earlier  $\mu$ SR results (Feyerherm *et al.*, 1997; Luke *et al.*, 1994), these samples contain a minority phase of A-type that is microscopically separated from the S-type majority phase. It may be possible that, depending on the content and spatial distribution of this minority phase, the volume-integrated response in resistivity experiments is eventually responsible for the differing T-dependences observed.

#### D. Spin dynamics in superconducting $CeCu_2Si_2$

Due to the small magnetic moment and the low transition temperatures, INS experiments were performed on superconducting CeCu<sub>2</sub>Si<sub>2</sub> using cold-neutron tripleaxis spectroscopy. While the INS spectra in the normal state yield a quasielastic magnetic response at  $\mathbf{Q}_{AF}$ with slowing down and scaling behavior as already mentioned, the spin dynamics in the superconducting state well below  $T_c = 0.6 \,\mathrm{K}$  show a clear spin excitation gap at  $\mathbf{Q}_{AF}($ Stockert *et al.*, 2011, 2008) followed by a well defined maximum, often called 'spin resonance' [Figs.7(a) and (b)]. It should be noted that this maximum clearly exceeds the magnetic response in the normal state, in contrast to a simple s-wave superconductor where no obvious enhancement of the superconducting response over the normal state response is expected at energies above the spin gap. Its intensity depends on the Fermi surface topology and the paramagnon dispersion (Eremin et al., 2008) and might therefore be less pronounced than in other unconventional superconductors. With a spin-gap size of about 0.2 meV, the maximum is located at  $4k_{\rm B}T_c$  and its position is therefore smaller than  $2\Delta = 5k_{\rm B}T_c$  of the (large) charge gap (Fujiwara *et al.*, 2008). We note that this necessary condition for a 'spin resonance' to be located inside  $2\Delta$  was also fulfilled by the acoustic magnon peak in UPd<sub>2</sub>Al<sub>3</sub> (in which the  $U^{3+}$  ion has two localized and one more hybridized 5f-electron), where heavy-fermion superconductivity coexists with local-moment antiferromagnetic order (Sato et al., 2001). Like in the latter case as well as in  $CeCoIn_5$ (Song et al., 2016, 2020), the peak in  $CeCu_2Si_2$  develops in the one-particle channel, i.e. out of the aforementioned quasielastic line that persists to way above  $T_c$  for the two Ce-based compounds, and to well above  $T_N$  (>  $T_c$ ) for  $UPd_2Al_3$ . This is different from the cuprates where it manifests a singlet-triplet excitation of the d-wave condensate (Sidis et al., 2004).

Though this distinct maximum in the INS data at the edge of the spin-excitation gap should not be called a 'spin resonance' for the reasons given above, it nevertheless highlights a sign-changing superconducting order parameter. Namely, if one considers coupling between a magnetic mode (e.g. magnon/magnetic exciton) and the itinerant quasiparticles/Cooper pairs (Bernhoeft et al., 2006, 1998), the observation in  $CeCu_2Si_2$  of a significant low energy enhancement of the INS intensity along the propagation vector  $\mathbf{Q}_{\mathrm{AF}}$  in the superconducting state over that of the normal state (Stockert *et al.*, 2011), implies a large coherence factor, which necessarily requires a sign change of the superconducting order parameter along this wave vector. Alternatively, for  $CeCoIn_5$  and Fe-based superconductors it has been proposed that the low energy INS peak arises from reduced quasiparticle damping in the superconducting state, allowing for the observation of an otherwise overdamped magnon mode (Chubukov and Gor'kov, 2008; Onari et al., 2010). For two reasons, we do not consider this scenario to be viable. First, the ratio of the energy of the INS maximum to  $2\Delta$  is comparable to the universal value observed in a variety of correlated superconductors (Duan *et al.*, 2021; Yu et al., 2009). Second (and related to the first), for this scenario to occur, the universality of the INS peak in the superconducting state which occurs in a variety of systems requires some degree of commonality in the behavior of the low-energy spin excitations in their normal states. This expectation is to be contrasted with disparate behavior of the low-energy spin excitations that have been observed in the normal state of these systems. In particular, in the case of CeCu<sub>2</sub>Si<sub>2</sub>, even in the normal state the paramagnons do not appear to be overdamped as suggested by their well visible dispersion at low energies [cf. Fig. 7(c)], even up to  $k_B T_K \approx 1.5$  meV (Song et al., 2021).

The experimentally determined propagation vector  $\mathbf{Q}_{\mathrm{AF}}$  agrees very well with the theoretically obtained nesting wave vector  $\boldsymbol{\tau}$  shown in Fig. 6(b) (Stockert *et al.*, 2004; Zwicknagl, 1992; Zwicknagl and Pulst, 1993), which connects nested parts of the heavy quasiparticle band, highlighting *intraband* nesting. Importantly,  $\mathbf{Q}_{\mathrm{AF}}$  does not connect extended regions of different bands (interband nesting) of e.g. electron and hole bands (Sec. IV.B) as required by the  $s_{+-}$  pairing model that has been considered for some Fe-based superconductors (Mazin *et al.*, 2008).

#### E. Effects of potential scattering

Historically, the effect of nonmagnetic impurities has been an important test for unconventional superconductivity. This is because, while the  $T_c$  of a conventional BCS superconductor is very sensitive to magnetic impurities, the non-magnetic case has little effect (Anderson, 1959). On the other hand, for superconductors with unconventional sign-changing states, the effect of nonmagnetic impurities may become similar to magnetic impurities in a conventional material (Balatsky *et al.*, 2006). Indeed the high sensitivity of CeCu<sub>2</sub>Si<sub>2</sub> to a very small

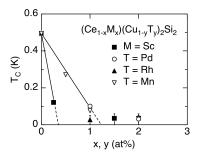


FIG. 8 Dependence of the superconducting transition temperature of CeCu<sub>2</sub>Si<sub>2</sub> polycrystals on substitutions for Ce and Cu. Replotted from (Spille *et al.*, 1983).

amount of atomic substitution of nonmagnetic impurities was one of the key pieces of early evidence allowing for the identification of an unconventional superconducting state. This is particularly the case for substitutions on the Cu site, where as shown in Fig. 8, doping around 1% of Rh, Pd or Mn completely suppresses  $T_{\rm c}$ , while similarly only 0.5% of smaller  $Sc^{3+}$  on the Ce site is needed (Spille et al., 1983). A striking difference for the Ce site is the size dependence of the dopant, where  $T_{\rm c}$ becomes increasingly insensitive for larger substituents, i.e., with critical concentrations of 6% for  $Y^{3+}$ , 10% for  $La^{3+}$  (Spille *et al.*, 1983), culminating in 20% for Th<sup>4+</sup> (Ahlheim et al., 1990). This trend with chemical pressure is analoguous to that found when applying hydrostatic pressure to  $CeCu_2Si_2$  doped with 10 at% of Ge, where  $T_{\rm c}$  is suppressed on the high pressure side of the low-pressure dome centered around the antiferromagnetic QCP [Fig. 5]. While this size effect appears to be in line with the strength of the Kondo interaction in the dependence of the volume available to the  $Ce^{3+}$  ions, the reason for the distinct site dependence in the atomic substitution experiments is yet to be unraveled.

Such small critical substitutions on the transitionmetal side being needed to suppress  $T_{\rm c}$  proves that this cannot be simply due to a significant tuning of the Kondo state. Indeed, while Ge doping expands the lattice acting as a negative pressure effect and causes a slight decrease of  $T_K$ , it is found that tuning a Ge-doped sample using pressure, which causes an increase of  $T_K$ , still yields a greatly suppressed  $T_c$  (Yuan *et al.*, 2003, 2006). Such a reduction of  $T_{\rm c}$  upon 10% Ge-doping allowed for the revelation that there are two separate superconducting domes in the temperature-pressure phase diagram, one sitting near a magnetic QCP, while the higher pressure dome potentially lies near a valence transition (Fig. 5) (Holmes et al., 2004; Yuan et al., 2003). Meanwhile for a more disordered sample with 25% Ge-doping no superconductivity is recovered even after the suppression of magnetism by pressure (Yuan *et al.*, 2004).

On the basis of recent studies of electron irradiated

samples, it was proposed that the order parameter of CeCu<sub>2</sub>Si<sub>2</sub> does not change sign across the Fermi surface, much like a conventional BCS superconductor. Namely it is reported that the suppression of  $T_{\rm c}$  upon the introduction of disorder by electron irradiation is not as rapid as expected for sign-changing pairing states such as those in the cuprates or iron pnictides, but instead is similar to some materials believed to have a conventional pairing mechanism (Yamashita et al., 2017). Moreover the lack of change in the low-temperature penetration depth of electron irradiated samples is taken as evidence for a lack of low-energy impurity-induced bound states, as also expected for sign-preserving order parameters (Takenaka et al., 2017). Since the effect of electron irradiation is likely to correspond to the displacement of Ce atoms from the lattice to interstitial sites, the resulting disorder may be compared to that manifested by the strong (factor of four) variation in the residual resistivity  $\rho_0$  going from a nearly stoichiometric A/S-type to an S-type single crystal with a small amount of Cu excess, where no depression of  $T_c$  is observed (Pang *et al.*, 2018). Similar results are well known from the cuprate high- $T_{\rm c}$  superconductors where substantial variations in  $\rho_0$  are not reflected by any significant changes in  $T_{\rm c}$ , cf. results on YBCO polycrystals (Cava et al., 1987) and single crystals (Liang et al., 1992). As discussed in Sec. IV.C, there are a number of theoretical works underlining the robustness of unconventional superconductivity against certain kinds of ordinary potential scattering (Anderson, 1997; Si et al., 2016). However, from the cuprates it is also known that atomic substitution can be quite hostile for high- $T_{\rm c}$ superconductivity (Alloul et al., 2009). For example, partial substitution of Cu on the  $CuO_2$  planes by Zn causes a strong depression of  $T_{\rm c}$  (Xiao *et al.*, 1988). Obviously, this is quite similar to the results of the aforementioned substitution experiments on CeCu<sub>2</sub>Si<sub>2</sub> (Ahlheim et al., 1988; Spille et al., 1983; Yuan et al., 2003), which are at odds with a non-sign changing superconducting state.

In summary, the aforementioned studies on  $\text{CeCu}_2\text{Si}_2$ reveal that "impurity doping", i.e., substitutional disorder, is strongly pairbreaking, while certain kinds of lattice rearrangements, induced, e.g., by electron irradiation or small changes in the Cu/Si occupation, are harmless to superconductivity. This dichotomy of harmful and harmless disorder in unconventional heavy fermion and cuprate high- $T_c$  conductors still needs to be uncovered.

#### F. Evidence for *d*-wave pairing

For a long time, the pairing state of  $CeCu_2Si_2$  was generally believed to correspond to *d*-wave superconductivity, in line with other Ce-based heavy-fermion superconductors (Thompson and Fisk, 2012), cuprate materials (Lee *et al.*, 2006; Scalapino, 1995), and organic superconductors (Kanoda, 2008; Lang and Müller, 2003). A

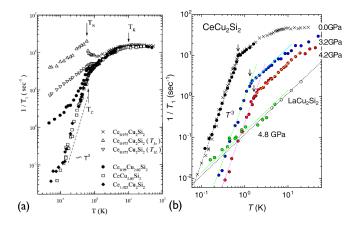


FIG. 9 Temperature dependence of the spin lattice relaxation rate  $1/T_1(T)$  of CeCu<sub>2</sub>Si<sub>2</sub>, obtained from Cu-NQR measurements (left) for various superconducting and nonsuperconducting polycrystals, and (right) single crystals of superconducting CeCu<sub>2</sub>Si<sub>2</sub> under hydrostatic pressure, as well as LaCu<sub>2</sub>Si<sub>2</sub>. No Hebel-Slichter peak at  $T_c$  and a  $T^3$  dependence is found in the superconducting samples down to around 0.1 K. The left panel is reproduced with permission from Ishida *et al.*, 1999. The right panel is reproduced from Fujiwara *et al.*, 2008, copyright 2008 The Physical Society of Japan.

decrease of the Knight shift below  $T_{\rm c}$ , the ordinary size of the dc Josephson effect between polycrystalline CeCu<sub>2</sub>Si<sub>2</sub> and Al as well as evidence for Pauli limiting of the upper critical field (Fig. 3), confirmed quite early that the Cooper pairs correspond to a singlet pairing state (Assmus et al., 1984; Ueda et al., 1987). Meanwhile the clearest evidence for the superconducting gap structure came from Cu-NQR measurements, where the spin lattice relaxation rate  $(1/T_1(T))$  displayed in Fig. 9 shows a  $T^3$ dependence down to around 0.1 K, which is characteristic of line nodes in the superconducting gap (Fujiwara *et al.*, 2008; Ishida et al., 1999), although it should be noted that the  $1/T_1(T)$  data of Ishida *et al.* (Ishida *et al.*, 1999) also show some deviation from  $T^3$  behavior at the lowest temperatures, as clearly demonstrated in recent NQR experiments extended to somewhat lower temperature (Kitagawa et al., 2017), see below. Evidence for nodal superconductivity was also inferred from measurements of other thermodynamic quantities, including a  $T^2$  dependence of the magnetic penetration depth (Gross et al., 1988), which is consistent with *d*-wave superconductivity in the presence of strong impurity scattering (Hirschfeld and Goldenfeld, 1993). The requirement that the order parameter is (i) spin singlet, (ii) with gap nodes, and (iii) changes sign on the regions of the renormalized Fermi surface connected by the nesting wave vector  $\boldsymbol{\tau} \approx \mathbf{Q}_{AF}$ , is most readily satisfied by a  $d_{x^2-y^2}$  pairing state, similar to that generally believed to apply to the cuprate high- $T_{\rm c}$ superconductors (Scalapino, 1995). On the other hand, in isothermal magnetoresistance measurements the angu-

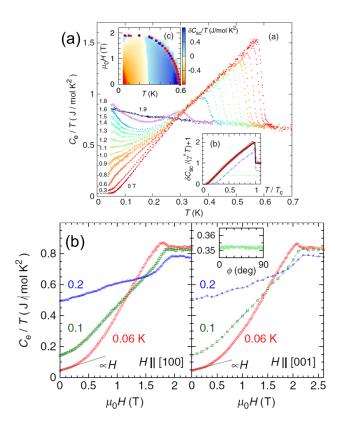


FIG. 10 (a) Temperature dependence of the electronic contribution to the specific heat as  $C_e/T$  of CeCu<sub>2</sub>Si<sub>2</sub> down to temperatures of 0.04 K. The lower inset displays the analysis of the data using a nodeless two-gap model, while the upper panel shows the data as a contour plot. (b) The field dependence of the electronic specific heat coefficient at various temperatures for fields along the [100] (left) and [001] directions. At 0.06 K, linear behavior is observed at low fields for both field orientations. The inset in the right panel shows  $C_e/T$  as a function of the in-plane azimuthal field-angle  $\phi$ , which remains constant. Reproduced with permission from Kittaka *et al.*, 2014.

lar dependence of the upper critical field in the *ab*-plane at 40 mK was found to be most compatible with a  $d_{xy}$ state, although the small amplitude of this modulation made it difficult for firm conclusions to be drawn (Vieyra *et al.*, 2011). Nevertheless, a *d*-wave pairing state of some form with line nodes was long considered to be the most likely candidate pairing state.

## IV. FULLY GAPPED UNCONVENTIONAL SUPERCONDUCTIVITY IN $CeCu_2Si_2$

#### A. Evidence for a nodeless gap structure

The understanding of the superconducting state of  $CeCu_2Si_2$  underwent a radical overhaul following the results from low-temperature specific measurements of Kittaka *et al.* (Kittaka *et al.*, 2014, 2016), which revealed

that the superconducting gap is fully open over the whole Fermi surface. Here the temperature dependence of the electronic contribution to the specific heat  $C_{\rm e} \ (\approx C_{4f})$  of S-type single crystals measured down to 0.04 K begins to flatten upon approaching the lowest measured temperature, and was best described by an exponentially activated temperature dependence, rather than following the  $C_{\rm e} \sim T^2$  behavior of a superconductor with line nodes, as shown in Fig. 10(a). This analysis suggested nodeless superconductivity with a gap  $\Delta_0 = 0.39 k_{\rm B} T_{\rm c}$ . Since this is considerably less than the value of  $1.76k_{\rm B}T_{\rm c}$  derived from weak-coupling BCS theory, in order to demonstrate the presence of a fully open gap in thermodynamic quantities such as the specific heat and penetration depth, measurements across a wide temperature range down to at least 0.05 K are required. A further advantage of this study is the very small residual  $\gamma_0 = 0.028 \text{ J mol}^{-1} \text{ K}^{-2}$ , which again allows for the inference of a lack of low-energy excitations. After subtracting an estimate of the phonon contribution, the data up to  $T_{\rm c}$  could not be described by a model with a single gap, but were instead accounted for by a model with two nodeless isotropic gaps.

These conclusions were supported by specific heat measurements in applied magnetic fields, displayed in Fig. 10(b). Here the isothermal  $C_{\rm e}/T$  at the lowest temperature of 0.06 K exhibits a linear field dependence, as opposed to the  $H^{0.5}$  behavior of a *d*-wave superconductor. The range of this low-field linear region is relatively narrow, and at higher fields there is a pronounced increase of  $C_{\rm e}/T$ . Just below  $B_{\rm c2}$ ,  $C_{\rm e}/T$  even overshoots the normal state value, and the origin of this strong enhancement needs still to be clarified by future work. Upon rotating the field within the *ab*-plane, no modulation of the specific heat is observed, whereas in the single band *d*-wave scenario a four-fold oscillation is predicted theoretically (Boyd et al., 2009; Vorontsov and Vekhter, 2007), and observed experimentally in the  $CeTIn_5$  series of heavyfermion superconductors (An et al., 2010; Aoki et al., 2004; Lu et al., 2012). Furthermore, measurements as a function of the polar angle  $\theta$  reveal simply the two-fold oscillations arising naturally from the tetragonal symmetry (Kittaka et al., 2016).

It should be noted that early evidence for a potentially exponential temperature dependence of the lowtemperature specific heat was provided by measurements of CeCu<sub>2</sub>Si<sub>2</sub> polycrystals, which revealed power-law behaviour with an exponent of two near  $T_c$ , but close to three at T = 0.05 K (Steglich *et al.*, 1985a). Further early evidence for fully gapped superconductivity was reported from a point contact study of CeCu<sub>2</sub>Si<sub>2</sub> measured at 0.03 K (De Wilde *et al.*, 1994). They found that the differential resistance curves are flat around zero bias, which is characteristic of a fully open gap, in stark contrast to that observed in UPt<sub>3</sub> where the curves have a triangular shape around zero voltage suggesting the presence of gap nodes.

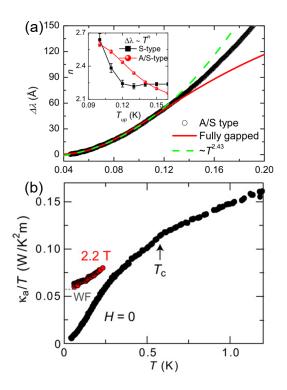


FIG. 11 (a) Temperature dependence of the magnetic penetration depth shift of an A/S-type CeCu<sub>2</sub>Si<sub>2</sub> single crystal, measured using the tunnel-diode-oscillator-based method. The solid line shows the fit to the low temperature data with a model for a fully gapped superconductor, where the lack of nodes in the gap is corroborated by an exponent n that is consistently larger than two (inset). Reproduced from Pang *et al.*, 2018 (b) Temperature dependence of the in-plane thermal conductivity as  $\kappa_a/T$  of CeCu<sub>2</sub>Si<sub>2</sub>, which in the superconducting state (H = 0) extrapolates to zero at T = 0, clearly demonstrating fully gapped superconductivity. Also shown are the data in the normal state, which demonstrates the validity of the Wiedemann-Franz law. Reproduced from Yamashita *et al.*, 2017, available under a Creative Commons NonCommercial 4.0 International Public License.

Penetration depth measurements performed down to  $T \approx 0.05$  K also demonstrate a fully open gap (Pang et al., 2018; Takenaka et al., 2017; Yamashita et al., 2017). As shown in Fig. 11(a), the low temperature penetration depth shift  $\Delta\lambda(T)$  is well described by the expression for a fully gapped material, with gap values well below that of BCS theory (in the range of  $0.5 - 1k_{\rm B}T_c$ ). Moreover, when analyzed using a power law dependence  $\Delta\lambda(T) \sim T^n$  in temperature intervals with decreasing upper limits, the low temperature exponents are consistently found to increase with n > 2, exceeding the bounds expected for a line nodal superconductor of n = 1 and n = 2 in the clean and dirty limits, respectively.

Fully gapped superconductivity was also deduced from recent thermal conductivity measurements, where the coefficient of the in-plane thermal conductivity  $\kappa_a/T$ extrapolates to zero at zero temperature [Fig. 11(b)], again showing evidence for the lack of low-energy excitations expected for nodeless superconductivity (Yamashita et al., 2017). This is further supported by measurements of the magnetic-field dependence of  $\kappa_a/T$ . where there is little change with applied field in the low field region. It is noted that more ambiguous results were found from earlier thermal conductivity studies of  $CeCu_2Si_2$  (Vieyra, 2012), while the recent measurements reported by (Yamashita et al., 2017) benefited from samples with lower non-superconducting fractions, as well as better contacts between the heater and the sample. Whereas earlier NQR measurements were found to exhibit a  $T^3$  dependence of  $1/T_1(T)$  down to around 0.1 K (Fujiwara et al., 2008; Ishida et al., 1999), more recent results show a deviation from this behavior at very low temperatures which can be accounted for by a small but nodeless gap (Kitagawa *et al.*, 2017).

While most recent low-temperature measurements have indicated that the superconducting gap is fully open, including also small-angle neutron scattering measurements (Campillo et al., 2021), results from a lowtemperature scanning spectroscopy study were less conclusive, which may be related to the fact that no good cleaves have been achieved in CeCu<sub>2</sub>Si<sub>2</sub> until very recently (see Sec. IV.B). The tunneling spectra measured at low temperatures show two clear features at different voltage bias, providing clear evidence for multiple gaps or an anisotropic gap structure (Enavat *et al.*, 2016). However, the data were best accounted for by a model where the large gap is fully open, but the small gap is nodal. The reason for this discrepancy is not clear, but it should be noted that the density of states of the d+d band mixing pairing state (Sec. IV.C) is linear for energies just above the small gap parameter, much like a line nodal superconductor, and therefore this could reconcile these results with other recent findings of nodeless superconductivity.

#### B. Fermi surface and quasiparticle dispersion

In order to unravel the electronic correlations and superconductivity in CeCu<sub>2</sub>Si<sub>2</sub>, the Fermi surface and quasiparticle dispersions close to  $E_F$  are crucial. While the Fermi surface of CeCu<sub>2</sub>Si<sub>2</sub> has been predicted by a number of theoretical studies (Ikeda *et al.*, 2015; Li *et al.*, 2018; Luo *et al.*, 2020; Pourovskii *et al.*, 2014; Zwicknagl, 2016; Zwicknagl and Pulst, 1993), direct momentumresolved measurements from angle-resolved photoemission spectroscopy (ARPES) are challenging due to the difficulty of sample cleavage (Reinert *et al.*, 2001). Recently, such experimental obstacles have been overcome due to an improved sample preparation method and a newly developed ARPES technique with a small beam spot (Wu *et al.*, 2021b). Figure 12 summarizes the ARPES results from a typical S-type single crystal. The

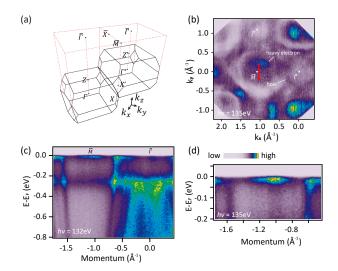


FIG. 12 The Fermi surface and quasiparticle dispersion of S-type CeCu<sub>2</sub>Si<sub>2</sub> from ARPES measurements. (a) Threedimensional bulk Brillouin zone (black solid lines) and the projected surface Brillouin zone (red dashed lines) of CeCu<sub>2</sub>Si<sub>2</sub>. (b) The experimental  $k_x$ - $k_y$  map at 10 K taken with 135 eV photons. The red arrow indicates the in-plane component of the SDW ordering wave vector  $\mathbf{Q}_{AF}$  observed by neutron diffraction (Sec. III.B). (c) Band dispersion along  $\overline{\Gamma}$ - $\overline{M}$  at 10 K. (d) Zoom-in view of the heavy electron band near  $E_F$ . Reproduced with permission from Wu *et al.*, 2021b.

experimental Fermi surface of CeCu<sub>2</sub>Si<sub>2</sub> consists of threedimensional hole bands centered at the bulk Z point [projecting onto the  $\bar{\Gamma}$  point of the surface Brillouin zone] and a quasi-2D electron band at the X-point ( $\bar{M}$  point at the surface Brillouin zone corner), see Figs. 12(a) and (b). Measurements of the energy-momentum dispersion show that the quasi-2D electron band is of predominant 4fcharacter and possesses a large effective mass [Figs. 12(c) and (d)], while the hole bands near the  $\bar{\Gamma}$  point are mainly derived from the lighter conduction bands.

The heavy electron band observed near the  $\overline{M}$  point makes an important contribution to the Fermi surface and is crucial for the heavy-fermion superconductivity (Zwicknagl and Pulst, 1993). Photon-energy dependent scans and detailed analysis reveal that this heavy electron band is cylindrical in momentum space and has an effective mass of  $\approx 120m_e$ . Here the effective mass is estimated by first dividing the experimental ARPES spectra by the (resolution-convoluted) Fermi-Dirac distribution function and then fitting the extracted quasiparticle dispersion with a parabola. Due to the limited energy resolution in ARPES, the effective mass estimation can have relatively large uncertainty. Note that the (zero temperature) effective mass used in the renormalized band calculation is  $\approx 500m_e$  (Zwicknagl, 2016; Zwicknagl and Pulst, 1993). Given that the ARPES was performed down to 10 K, at which temperature  $C_{4f}/T \approx 0.125 \,\mathrm{J \cdot mol^{-1} \cdot K^{-2}}$ [Fig. 1]) is approximately seven times smaller than in the

low temperature limit (Steglich, 1990), the estimated effective masses indicate a very good correspondence between ARPES and the specific heat. As illustrated in Fig. 6(a), renormalized band calculations (Stockert *et al.*, 2004; Zwicknagl and Pulst, 1993) reveal that this heavy electron band has a warped part with flat parallel sides connected by a nesting vector  $\boldsymbol{\tau}$ , in excellent agreement with the SDW ordering wave vector  $\mathbf{Q}_{\mathrm{AF}}$  observed in neutron diffraction [Figs. 6(a) and (b)] (Stockert *et al.*, 2004). The experimental contour of this heavy band shown in Fig. 12(b) is in fairly good agreement with these calculations. Another interesting observation is that the outer hole band near the  $\overline{\Gamma}$  point contains appreciable 4f weight and bends slightly near  $E_F$ , which is the hallmark of hybridization between conduction and 4f electrons (Chen et al., 2017; Im et al., 2008; Jang et al., 2020; Wu et al., 2021a). Its enclosed area is close to the values obtained from quantum oscillation measurements (Hunt et al., 1990; Tayama et al., 2003), which however, could not detect the heavy electron band at the  $\overline{M}$  point. Note that the detection of heavy bands can be particularly challenging in quantum oscillation experiments, due to the rapid decay of the quantum oscillation amplitudes with temperature for heavy orbits (Shoenberg, 2009).

#### C. d + d matrix-pairing state

As discussed in Sec. III.F, the majority of the experiments in superconducting CeCu<sub>2</sub>Si<sub>2</sub> have been interpreted in terms of a single-band, *d*-wave Cooper pairing. The new results presented in Sec. IV.A point toward the emergence of a full gap. Although a single-band *d*-wave pairing state is at odds with the more recent results, the underlying sign-changing nature of the pairing state under a  $C_{4z}$  rotation continues to play an important role. This is best illustrated by the large peak in the INS intensity in the superconducting state [Fig. 7(a)] associated with a pairing state which changes sign *within* the heavy, cylindrical bands near the edge of the Brillouin zone, as illustrated in Fig. 13.

The robustness of the sign-changing nature of the pairing states suggests that new pairing candidates have to reconcile this feature with the emergence of a full gap. An important requirement is that the sign-changing but also gapped pairing state must belong to a single irreducible representation of the point group. Indeed, unlike systems such as UPt<sub>3</sub> (Fisher *et al.*, 1989; Schemm *et al.*, 2014), there have been no reports of multiple superconducting transitions in CeCu<sub>2</sub>Si<sub>2</sub> which further break symmetry with decreasing temperature. Similarly, the lack of evidence for time-reversal symmetry breaking in the superconducting state makes d + id or s + id pairing states unlikely, since these are gapped and sign-changing but only at the price of breaking both point-group and

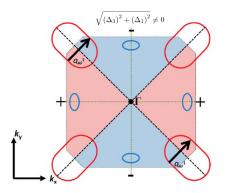


FIG. 13 Projection of the renormalized heavy Fermi surface and ordering wave vector  $\mathbf{Q}_{AF} = (0.215, 0.215, 0.53)$ onto the  $k_z = 0$  plane of the 3D Brillouin zone at zerotemperature. The dashed lines indicate the nodes of the individual components of d + d pairing. The diagonal black and vertical/horizontal green dashed lines denote the nodes of  $\Delta_3(\mathbf{k}) \propto d_{x^2-y^2}$  and  $\Delta_1(\mathbf{k}) \propto d_{xy}$ , respectively (see Eq. 1). The effective gap is determined by the addition in quadrature of the two components. Since the nodes of the  $\Delta_3$  and  $\Delta_1$ components do not overlap except at isolated points of the Brillouin zone, d + d pairing is always gapped on the Fermi surface. The wave vector for the peak of the observed antiferromagnetic fluctuations projected onto the  $(k_x, k_y)$  plane,  $\mathbf{Q}_{AF}^{||},$  connects parts of the cylindrical Fermi surface near the edges (red pill-shapes) where  $\Delta_3 \propto d_{x^2-y^2}$  has opposite signs, leading to the emergence of a pronounced peak inside the superconducting gap in INS experiments. Reproduced from Pang et al., 2018.

time-reversal symmetries. We instead consider a pairing state that can reconcile the features of superconducting CeCu<sub>2</sub>Si<sub>2</sub> while preserving the symmetries already mentioned. This is a multi-band d + d pairing of concurrent intra-band  $d_{x^2-y^2}$  and inter-band  $d_{xy}$ -waves (Nica and Si, 2021; Nica *et al.*, 2017). In it's most general form, d + d pairing is

$$\Delta_{d+d} = \begin{pmatrix} \Delta_3(\mathbf{k}) & \Delta_1(\mathbf{k}) \\ \Delta_1(\mathbf{k}) & -\Delta_3(\mathbf{k}) \end{pmatrix}, \tag{1}$$

where the intra- and inter-band components  $\Delta_3$  and  $\Delta_1$ transform as  $d_{x^2-y^2}$  and  $d_{xy}$ , respectively. This matrixpairing state, which is intrinsically multi-band, has additional structure due to the band space on which it is defined. The intra-band  $d_{x^2-y^2}$  component naturally satisfies the required sign-change, much like a single-band dwave pairing. In contrast to the latter, the matrix structure of d + d pairing, due to the anti-commuting Pauli matrices, also ensures that the gap is determined by the addition in quadrature of the two distinct d-wave components. Consequently, the Bogoliubov-de Gennes (BdG) quasiparticle spectrum shows a full gap everywhere on the Fermi surface. As recently discussed in (Nica and Si, 2021), d + d pairing is a natural d-wave analogue to the spin-triplet pairing states of <sup>3</sup>He-B, with the bands playing a role similar to the spin as far as the matrix structure is concerned in the former and latter cases, respectively. The d + d pairing yields good fits to penetration depth, specific heat, and NQR data well below and closer to  $T_c$ alike (Pang *et al.*, 2018; Smidman *et al.*, 2018), as discussed in the following subsection.

While d + d pairing defined in the band basis provides a direct interpretation of the experimental results, its stability is more naturally addressed using microscopic matrix-pairing candidates defined in the orbital/spin space of the paired electrons. Matrix-pairing states which transform according to the irreducible representations of the point group can be constructed from the decomposition of the products of two-orbital, or more generally, spin-orbit coupled multiplets of definite symmetry. This approach was illustrated in the alkaline Feselenides, which are also strongly-correlated multi-band superconductors. [The properties of other Fe-selenide superconductors with a similar or higher  $T_c$  as the alkaline Fe-selenides, including the Li-intercalated iron selenides (Lu et al., 2015) and even the single-layer FeSe, the  $T_c$ record holder of the iron-based superconductors (Wang et al., 2012a), are similar (Si et al., 2016).] In spite of the difference in the nature of their basic constituents, these Fe-based superconductors remarkably share some of the experimental signatures that are similar to those in CeCu<sub>2</sub>Si<sub>2</sub>, namely, fully-gapped superconductivity, as indicated by ARPES experiments (Mou et al., 2011; Wang et al., 2011, 2012b; Xu et al., 2012), which supports a spin resonance in the INS spectrum (Friemel *et al.*, 2012; Park et al., 2011). The wave vector of the resonance at  $\mathbf{Q}_{\text{Alkaline FeSe}} = (0.5, 0.25, 0.5)$  (Friemel *et al.*, 2012; Park et al., 2011) is distinct from what one could expect from the sign-changing s-wave pairing which, in any case, is unlikely given the absence of hole pockets at the center of the Brillouin zone. Nica et al., 2017 introduced an  $s\tau_3$ matrix-pairing state, which consists of an s-wave form factor multiplied by a  $\tau_3$  Pauli matrix in the space of the Fe  $d_{xz/yz}$  orbitals. Because the  $s\tau_3$  matrix does not commute with the symmetry-dictated kinetic part, the multi-orbital  $s\tau_3$  pairing is equivalent to d+d pairing in the band basis (Nica and Si, 2021; Nica et al., 2017). On the other hand,  $s\tau_3$  transforms as a single  $B_{1g}$  irreducible representation of the  $D_{4h}$  point group. This implies that d + d pairing also belongs to the same representation and that it preserves both point-group and time-reversal symmetries. When the normal-state band splitting near the Fermi level is small, the BdG quasiparticle spectrum shows a full gap everywhere in the Brillouin zone. Generically, the BdG spectrum is always nodeless everywhere on the Fermi surface. Away from the Fermi surface, nodes can occur in the BdG spectrum when the band splitting exceeds a certain threshold. However, in strongly correlated systems only nodal excitations on the Fermi surface are long lived and, correspondingly, sharply defined; any

putative nodal excitations away from the Fermi surface involve a large correlation-induced damping in the normal state, and the distinction between nodal and gapped excitations is obviated (Nica and Si, 2021; Nica *et al.*, 2017). Finally, we note that the  $s\tau_3$  and the equivalent d + d pairings are energetically favored: they are stabilized in a multi-orbital  $t - J_1 - J_2$  model (Nica *et al.*, 2017) in the regime where  $A_{1g}$  and  $B_{1g}$  pairing channels are quasi-degenerate.

Following the important precedent of the alkaline Feselenides, (Nica and Si, 2021) constructed a microscopic candidate for even-parity, spin-singlet d + d pairing which incorporates the nature of the electronic states in  $CeCu_2Si_2$ . Matrix-pairing candidates can be constructed within the quasi-localized f electron sector, corresponding to f - f pairing, but also in the f - c and c - c sectors, where c stands for a conduction electron. As indicated by several experiments (Amorese et al., 2020; Goremychkin and Osborn, 1993; Rueff et al., 2015) and by LDA+DMFT studies (Pourovskii *et al.*, 2014), the  ${}^{2}F_{5/2}$ electron states split under the influence of the crystallineelectric-field into a ground-state  $\Gamma_7$  Kramers doublet and excited  $\Gamma_6$  and  $\Gamma_7$  doublets. Within the f - f pairing sector, the product of two ground-state  $\Gamma_7$  doublets decomposes into  $\Gamma_1, \Gamma_2$  and  $\Gamma_5$  irreducible representations. As previously discussed, CeCu<sub>2</sub>Si<sub>2</sub> does not show signs of multiple superconducting transitions, implying that twocomponent pairing states belonging to  $\Gamma_5$  are unlikely to occur. From the remaining two representations, the matrix associated with  $\Gamma_2$  is symmetric and thus incompatible with the even-parity, spin-singlet nature of the pairing candidate. The only possible pairing candidate within the f - f sector is a matrix belonging to the identity  $\Gamma_1$  representation. Because this matrix transforms trivially under the point group, the symmetry of f - fpairing states are determined entirely by the form factor. This implies that f - f pairing is not likely to support d+d pairing. Nica and Si, 2021 considered an alternative in the f - c pairing sector.

Conduction electron states which belong to the  $\Gamma_6$  irreducible representation can be constructed by first taking linear combinations of the Cu  $d_{x^2-y^2}$  orbitals which transform as  $(p_x, p_y)$  within each unit cell:

$$p_x = d_{x^2 - y^2}^{(4)} - d_{x^2 - y^2}^{(2)} \tag{2}$$

$$p_y = d_{x^2 - y^2}^{(1)} - d_{x^2 - y^2}^{(3)}, \tag{3}$$

as illustrated in Fig. 14. The spin-orbit coupling can be incorporated to obtain the  $\Gamma_6$  states

$$\Psi_{\Gamma_6;1/2} = \frac{i}{2} \left[ p_x + i p_y \right] \phi_{-1/2} \tag{4}$$

$$\Psi_{\Gamma_6;-1/2} = \frac{i}{2} \left[ p_x - i p_y \right] \phi_{1/2},\tag{5}$$

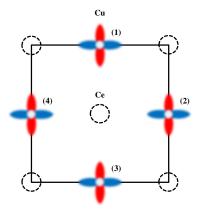


FIG. 14 Single Cu plane in the unit cell of CeCu<sub>2</sub>Si<sub>2</sub>. The four sites labeled (1) - (4) correspond to Cu  $d_{x^2-y^2}$  orbitals in the plane. The dashed-line circles represent the Ce sites projected onto the Cu-plane. Reproduced from Nica and Si, 2021, under a Creative Commons Attribution 4.0 International License.

where the  $\phi$ 's denote spin-1/2 states. Note that the four d orbitals are localized on distinct sites in the unit cell. The  $\Psi$  states are examples of a Zhang-Rice construction (Zhang and Rice, 1988). The decomposition of the products of f-electron  $\Gamma_7$  doublets, belonging to the ground-state multiplet, and  $\Gamma_6$  conduction electron doublets includes a sign-changing  $\Gamma_3$  irreducible representation. When multiplied by a featureless s-wave form factor, the matrix associated with  $\Gamma_3 f - c$  pairing is the analogue of the  $s\tau_3$  pairing introduced in the context of the alkaline Fe-selenides.  $s\Gamma_3$  thus provides a microscopic candidate for d + d pairing in CeCu<sub>2</sub>Si<sub>2</sub>. Evidence supporting this type of pairing was provided by x-ray absorption spectroscopy experiments (Amorese et al., 2020) which indicated a finite admixture of the f-electron  $\Gamma_6$  in the ground-state of CeCu<sub>2</sub>Si<sub>2</sub>. It is important to recall that the microscopic candidate for d + d pairing introduced in (Nica and Si, 2021) was constructed using only the point-group symmetry and a minimal input provided by the nature of the lowest-energy 4f Kramers doublet. In spite of its simplicity, this construction (i) demonstrates how d + d pairing can emerge in principle, and (ii) provides a well-defined microscopic candidate for any future detailed theoretical studies of the pairing symmetry in  $CeCu_2Si_2$  that also incorporate the complex bandstructure of the normal state.

Sign-changing  $s_{+-}$  pairing states were also advanced to explain the gapped, sign-changing superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> (Ikeda *et al.*, 2015; Li *et al.*, 2018). We briefly summarize two of the most important differences between d+d and  $s_{+-}$  pairing states. Firstly, although both candidates are sign-changing and therefore conducive to a large peak in the INS intensity inside the superconducting gap, they also imply very different ways of involving the states on the Fermi surface. Li et al., 2018 (see also Ikeda et al., 2015) carried out DFT+U calculations, which capture neither the Kondo effect nor the associated renormalization towards heavy single-electron excitations. Physically, the proposed  $s_{+-}$  picture invokes a wave vector that spans the distance between the heavy cylindrical Fermi surface (red pockets in Fig. 13) and the hole pocket near the Z-point (bulk Brillouin zone) projected from light bands (not shown), which does not generate enough spin spectral weight for either the observed antiferromagnetic order or the observed INS spectrum in the superconducting state. A lack of such extended nesting between these different surfaces can also be inferred experimentally from the ARPES results (Sec. IV.B) due to the electron and hole pockets being observed to have very different shapes and effective masses. In contrast, the d + d pairing implies a wave vector spanning within the same cylindrical heavy Fermi surface (red pockets in Fig. 13). The latter picture is naturally associated with a realistic heavy-fermion SDW instability, due to the enhanced density-of-states on these pockets. Secondly, d+dand  $s_{+-}$  pairing states have distinct nodal structures. As already discussed, the d + d pairing state has no nodes on the Fermi surface (see Fig. 13). By contrast, the  $s_{+-}$ pairing state has gap zeroes that would generally be expected to intersect the extended hole Fermi surface of  $CeCu_2Si_2$ , leading to nodal excitations. This is different from the case of Fe-based superconductors, which typically have disconnected hole and electron pockets at the zone center and edges. These points imply that the  $s_{+-}$ picture is not viable.

We conclude this section by briefly revisiting the effects of disorder on the paired states in  $CeCu_2Si_2$ . As mentioned in Sec. III.E, the weak suppression of  $T_c$ in electron-irradiated samples was argued to point towards a more conventional order-parameter that does not change sign (Takenaka et al., 2017; Yamashita et al., 2017), an interpretation which usually relies on the perturbative Abrikosov-Gor'kov theory. However, d-wave pairing in strongly correlated settings is expected to be much less sensitive to disorder introduced via nonmagnetic potential scattering (Anderson, 1997). Studies in models with strong, short-range exchange interactions are consistent with this expectation (Chakraborty et al., 2017; Garg et al., 2008). This implies that d + d pairing states are also robust against this type of disorder in a broader class of materials with similar strong exchange interactions. These include for instance the alkaline Fe-selenides, where the d + d state in the form of  $s\tau_3$  pairing was stabilized in a multi-orbital  $t - J_1 - J_2$ model (Nica and Si, 2021). We expect that strong correlations also protect the d+d pairing state in CeCu<sub>2</sub>Si<sub>2</sub>. In contrast, as already mentioned above,  $T_c$  can be sharply suppressed in  $CeCu_2Si_2$  via atomic substitution, as is the case for instance in high- $T_c$  superconductors with Zn substituted for Cu on the  $CuO_2$  planes (Loram *et al.*, 1990).

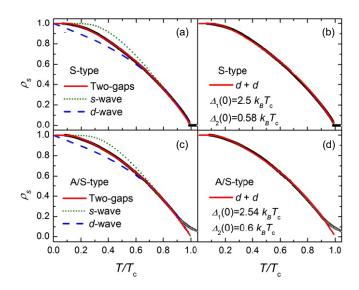


FIG. 15 Temperature dependence of the superfluid density derived from penetration depth measurements using the tunnel-diode-oscillator-based method from. Panels (a) and (b) display fits to the superfluid density of an S-type sample with an isotropic two gap model and d + d band-mixing pairing model, respectively, while (c) and (d) show the corresponding results for the A/S-type sample. Reproduced from Pang *et al.*, 2018.

#### D. Analysis of experimental results with the d + d model

Upon converting the penetration depth data measured using the tunnel-diode-oscillator-based method to the superfluid density, Pang et al. found that the temperature dependence could be described both by an isotropic two-gap model, as well as one for the d + d band mixing pairing state (Pang et al., 2018; Smidman et al., 2018), which is displayed in Fig. 15. For the latter case, a simple model of the gap function is given by  $\Delta(T,\phi) = [(\Delta_1(T)\cos 2\phi)^2 + (\Delta_2(T)\sin 2\phi)^2]^{\frac{1}{2}},$  which has a four-fold oscillatory component where one of the gap parameters corresponds to the gap minimum and the other to the maximum. The basis for applying this model is explained in the previous subsection, and it is found that this describes the data across the whole temperature range well. The fitted values of the gap parameters for measurements of the S-type sample were  $2.5k_{\rm B}T_{\rm c}$ and  $0.58k_{\rm B}T_{\rm c}$ , where the small but finite gap minimum ensures a nodeless gap across the Fermi surface, and is close to the magnitude obtained from the low temperature analysis of  $\Delta\lambda(T)$  (Sec. IV.A). This model can also fit the temperature dependence of the specific heat (Pang et al., 2018; Smidman et al., 2018), including the data previously reported by Kittaka et al. (Kittaka et al., 2014).

In the case of the recent NQR measurements, this d+dband mixing pairing model can well account for  $1/T_1(T)$ across the whole temperature range, including the deviation from  $T^3$  behavior resolved at the lowest temperatures from recent measurements (Kitagawa et al., 2017; Smidman et al., 2018). Although the simple twoband BCS model can also describe the low temperature  $1/T_1(T)$  results, it is less accurate at elevated temperatures, where it deviates from the data, culminating in the prediction of a pronounced Hebel-Slichter coherence peak below  $T_{\rm c}$ . Such an enhancement, which is a hallmark of conventional BCS superconductivity, is absent from the data (Fig. 9), which is in-line with a sign-changing order parameter. In the  $s_{+-}$  scenario this peak is somewhat suppressed, but still present in the model. In analogy with the Fe-based superconductors, effects such as quasiparticle damping and impurity-induced bound states (in the case of  $s_{+-}$  pairing) could potentially account for the deviations from these two models (Bang and Stewart, 2017). On the other hand, for a d + d band mixing pairing state the coherence peak is naturally avoided due to the sign change of the intraband pairing component (Kitagawa et al., 2017; Smidman et al., 2018).

#### V. PERSPECTIVES

Despite the progress made on this prototypical heavyfermion superconductor, a number of points are worthy of further investigations.

Although the band-mixing d + d-pairing state can account for all the experimental results, more direct experimental evidence for such a scenario is still lacking. To unambiguously discriminate between different fully gapped models likely requires high-resolution momentum resolved experimental probes of the superconducting gap at very low temperatures, which is very challenging. In addition, while recent proposals have given a microscopic basis to the d + d-pairing state (Nica and Si, 2021), a fully developed microscopic theory for CeCu<sub>2</sub>Si<sub>2</sub> is still necessary. Indeed, developing fully microscopic theories for strongly correlated superconductors remains a grand challenge of condensed matter physics.

The effect of nonmagnetic potential scattering on CeCu<sub>2</sub>Si<sub>2</sub> still lacks a complete theoretical and experimental understanding. This is especially so concerning the variable sensitivity of the superconductivity to substitutional disorder, which appears to be site-dependent, as well as to various types of lattice rearrangement, such as that induced by electron irradiation. There is a pronounced size dependence for substitutions on the Cesite, where the magnitude of the  $T_c$ -depression is found to be *anticorrelated* to the volume of the so obtained "Kondo hole", while Ge atoms exchanged for Si are less strong pairbreakers. The origin of this nonuniversal impact of substitutional disorder on the superconductivity of CeCu<sub>2</sub>Si<sub>2</sub>, as well as the dichotomy between "harmful" and "harmless" (e.g., electron-irradiation-induced) disorder are interesting open questions to be unraveled

by future work.

We also note that CeCu<sub>2</sub>Si<sub>2</sub> has often been regarded as a prototypical example of both heavy-fermion superconductivity, as well as SDW-type quantum criticality, but the extent to which the findings extend to other heavyfermion systems is currently unclear. In particular, the nodeless superconducting gap structure of CeCu<sub>2</sub>Si<sub>2</sub> is distinct from the clearly evidenced nodal  $d_{x^2-y^2}$  superconductivity in Ce(Co,Ir)In<sub>5</sub> (Allan *et al.*, 2013; An *et al.*, 2010; Izawa *et al.*, 2001; Kasahara *et al.*, 2008; Lu *et al.*, 2012; Park *et al.*, 2008; Zhou *et al.*, 2013).

The spin-excitation spectrum of CeCu<sub>2</sub>Si<sub>2</sub> consists of both long-wavelength SDW-type fluctuations (paramagnons), as well as high-frequency Mott-like fluctuations of 4f electron spins. It is of special interest to understand the role played by these different types of spin fluctuations in either promoting or breaking apart the Cooper pairs. In this context, it is interesting that the  $B_{c2}(p)$ curve in the T = 0 plane of Fig. 4(a) exhibits its maximum at a pressure which is only about half the value of the critical pressure  $p_c$  at B = 0. When increasing the pressure far away from this QCP, in the absence of quantum-critical SDW fluctuations,  $B_{c2}(p)$  is found to increase which apparently means that superconductivity becomes strengthened. However, when further approaching the QCP (at  $p_c/2 ), under increas$ ingly dominant SDW-type quantum critical fluctuations,  $B_{c2}(p)$  turns out to decrease and superconductivity deteriorates. A similar conclusion can be drawn from the evolution of  $T_{\rm c}(p)$  for the low-pressure dome displayed in Fig. 5 and may also apply to other correlated metals showing a superconducting dome centered at an SDWor putative SDW- type QCP, such as  $Ba(Fe_{1-x}Co_x)_2As_2$ (Chu et al., 2009) or  $CePd_2Si_2$  (Mathur et al., 1998). This non-monotonic evolution suggests that the Motttype critical excitations are pair-promoting, while the ultra-low-temperature (below  $T^* = 1$  K) SDW-type critical excitations in CeCu<sub>2</sub>Si<sub>2</sub> are pair-breaking. Interestingly, the theoretical work of Hu et al., 2021a, for an SDW-type quantum criticality of Kondo-lattice systems, reached a similar conclusion that the Mott-type quantum critical fluctuations at energies above  $T^*$  are primarily instrumental for the Cooper-pair formation. Together, these considerations suggest that the heavy-fermion superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> should be compared with those of systems with local (Kondo-destroying) rather than itinerant (SDW-type) QCPs (Nguyen et al., 2021; Park et al., 2006; Schuberth et al., 2016, 2022; Shan et al., 2022: Shishido et al., 2005).

#### VI. SUMMARY

 $CeCu_2Si_2$  was originally considered a prototypical intermediate-valence metal (Sales and Viswanathan, 1976). The discovery of heavy-fermion behavior (Steglich et al., 1979) in this compound led to the notion that it belongs to the family of Ce-based Kondo-lattice systems (Bredl et al., 1984, 1978) and, most importantly,  $CeCu_2Si_2$  is the first discovered unconventional superconductor (Steglich et al., 1979). Over 40 years of intense research on this system have posed several severe challenges and surprising solutions most of which are covered in this article. In the following, we briefly summarize our current knowledge on  $CeCu_2Si_2$ .

Its Kondo-lattice ground state, implying a local J =5/2 spin-orbit split Hund's rule multiplet of trivalent Ce, which is further split by the tetragonal crystalline-electric field into two  $\Gamma_7$  and a  $\Gamma_6$  Kramers doublets (Amorese et al., 2020), could be recently verified by ARPES experiments performed at 10 K (Wu et al., 2021b), well below the lattice Kondo temperature of 15 K. These investigations revealed a 'large (renormalized) Fermi surface' to which the Ce-4f electrons substantially contribute, i.e., a heavy electron band near the X-point of the bulk Brillouin zone. For this heavy band the effective charge-carrier mass  $m^*$  estimated from ARPES of  $m^* \approx 120 m_{\rm e}$  is in very good agreement with that obtained from specific-heat results at the same temperature (Fig. 1) (Steglich, 1990). In addition, ARPES revealed a hole band with small, but significant 4fcontribution near the bulk Z-point which corresponds to the distinct Fermi surface pocket with moderately enhanced  $m^* \approx 5 m_{\rm e}$  that had been detected by magnetic quantum oscillation measurements (Hunt et al., 1990; Tayama et al., 2003). In contrast to the aforementioned ground-state and thermodynamic properties which probe the large Fermi surface of the Kondo-lattice state of CeCu<sub>2</sub>Si<sub>2</sub> at finite temperatures, transport measurements (Shan et al., 2022; Sun and Steglich, 2013) appear to be dominated down to very low temperatures by the fundamental local scattering process underlying the Kondo screening, i.e., scattering of ordinary conduction electrons from the Ce-derived localized 4f-spins, see also (Coleman *et al.*, 1985). Upon volume compression, Cebased Kondo-lattice systems commonly show a strengthening of the Kondo interaction and eventually a transition into an intermediate-valence state. This has been observed for  $CeCu_2Si_2$  as well (Holmes *et al.*, 2004; Yuan et al., 2003, 2006).

One of the characteristics of these types of materials is their closeness to magnetism. Many of them exhibit a magnetically ordered low-temperature phase in the vicinity of a QCP. While the discovery of superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> with a finite magnetic moment in each unit cell came as a big surprise for most researchers in the field of superconductivity, this might indeed have been expected for researchers working on superfluid <sup>3</sup>He (Vollhardt and Wölfle, 1990). With the discovery of a heavy-fermion low-temperature phase in CeAl<sub>3</sub> (Andres *et al.*, 1975), which resembles the renormalized normal phase of (charge-neutral) liquid <sup>3</sup>He at

sufficiently low temperatures, the question might have arisen: Is there a superconducting analogue in a heavyfermion metal like CeAl<sub>3</sub> to the superfluid phases in <sup>3</sup>He? Not surprisingly, magnetically-driven superconductivity in heavy-fermion metals was proposed quite early by theorists (Anderson, 1984; Miyake *et al.*, 1986; Scalapino *et al.*, 1986) and was then gradually verified experimentally (Aeppli *et al.*, 1989; Sato *et al.*, 2001). In the case of CeCu<sub>2</sub>Si<sub>2</sub>, it became clear from the outset that a BCStype phonon-mediated Cooper-pairing mechanism is incapable of explaining why the non-magnetic analogue compound LaCu<sub>2</sub>Si<sub>2</sub> is not a superconductor (Steglich *et al.*, 1979) as well as the drastic pair-breaking effect of certain non-magnetic impurities, notably when substituted for Cu in CeCu<sub>2</sub>Si<sub>2</sub> (Spille *et al.*, 1983).

In more recent years,  $CeCu_2Si_2$ , along with  $CeCu_{6-x}Au_x$ , YbRh<sub>2</sub>Si<sub>2</sub> and CeRhIn<sub>5</sub>, have played a prominent role in the understanding of heavy-fermion quantum criticality (Gegenwart et al., 2008). Theoretical studies of Kondo-lattice models have led to the notion of Kondo destruction (Coleman et al., 2001; Si et al., 2001), which characterizes Mott-type quantum criticality for an electron localization-delocalization transition. More recently, it has been argued that partial Mott quantum criticality also forms the basis for the ferromagnetic instabilities in the heavy-fermion metals YbNi<sub>4</sub>( $P_{1-x}As_x$ )<sub>2</sub> (Steppke et al., 2013) and  $CeRh_6Ge_4$  (Shen et al., 2020). In  $CeCu_2Si_2$ , it has been suggested that SDW-type critical excitations operate below an energy scale of  $T^*$  that is nonzero but much smaller than the Kondo temperature, while the Mott-type critical excitations describe the quantum criticality above this energy scale (Gegenwart et al., 2008; Smidman et al., 2018). Theoretical studies that incorporate the Kondo destruction physics in quantum-criticality-driven superconductivity have recently been developed (Hu et al., 2021a).

In the low-temperature normal state of S-type  $CeCu_2Si_2$ , the critical exponent of the power-law Tdependence of the resistivity turned out to be ambiguous, i.e. 1.5 (Gegenwart et al., 1998) or 1 (Yuan et al., 2003, 2006), presumably due to the spatial distribution of a magnetically ordered minority phase (Stockert *et al.*, 2011) that may modify the volume-integrated response in resistivity experiments. From the temperature dependences of both C(T)/T and the damping rate measured in the INS spectrum (Arndt et al., 2011; Gegenwart et al., 2008; Smidman et al., 2018),  $T^* \sim 1 - 2$  K can be inferred, which is on the same order of magnitude as the spin excitation gap in the magnetic response in the superconducting state. Nevertheless, the linear paramagnon dispersion relation observed above the spin-gap energy  $\hbar\omega_{\rm gap}$  extends to about 1.5 meV (Song *et al.*, 2021). Except for these paramagnon excitations, the magnetic INS response comprises of Mott-type fluctuations of local Ce-moments with frequencies in the range  $k_B T^*/\hbar$  to  $k_B T_K/\hbar$ . The existence of a nonzero Kondo-destruction

energy scale  $k_B T^*$  that is small compared to the Kondo temperature has also been inferred from the large kinetic energy loss as  $CeCu_2Si_2$  goes from the normal to the superconducting state; this kinetic energy loss overcompensates the majority of the exchange energy saving in the same process (Stockert *et al.*, 2011). This overcompensation results in a pair-formation energy that is smaller than the exchange energy by a factor of about twenty - characteristic of magnetically-driven Cooper pairing of slowly propagating Kondo singlets (Stockert *et al.*, 2011). As far as the magnetism in  $CeCu_2Si_2$  is concerned, the nature of the high-field B-phase (Bruls et al., 1994), and of its QCP at about 17 T (Weickert et al., 2018) as well as the first-order phase transition between this B-phase and the adjacent low-field SDW A-phase (Tayama et al., 2003) need further detailed exploration. Meanwhile the field dependence of the specific heat in the superconducting state exhibits an unusual upturn at intermediate fields culminating in a strongly enhanced value just below  $B_{c2}$  (Kittaka *et al.*, 2014, 2016). The origin of this behavior still needs to be determined, especially whether it is related to a spatially modulated superconductivity (Kitagawa *et al.*, 2018) or other inferred effects of strong Pauli-paramagnetic limiting (Campillo *et al.*, 2021).

Another striking phenomenon is the occurrence of a second superconducting dome in CeCu<sub>2</sub>Si<sub>2</sub> at pressures well above the critical pressure at which SDW order disappears. There, the  $T_c$  is around three times larger than in low pressure conditions (Yuan *et al.*, 2003, 2006). Although such a scenario was hinted at by the unusual shape of the  $T_c$  vs p plateau, the existence of a distinct second high pressure dome was only apparent upon doping with Ge to weaken the superconductivity (Fig. 5), and suggests a different unconventional pairing mechanism at higher pressures, namely one related to valence fluctuations (Holmes *et al.*, 2004; Yuan *et al.*, 2003).

For a long time,  $CeCu_2Si_2$  was believed to be a singleband d-wave superconductor with line nodes in the energy gap. The strongest evidence for this conclusion came from NQR measurements down to 0.1 K, which revealed the absence of a Hebel-Slichter peak at  $T_c$  and a  $T^3$  dependence of  $1/T_1(T)$  (Fujiwara *et al.*, 2008; Ishida et al., 1999). A  $d_{x^2-y^2}$  state was concluded from INS (Eremin et al., 2008; Stockert et al., 2011), while  $d_{xy}$ was deduced from the anisotropy of the upper critical field determined from the resistivity (Vieyra *et al.*, 2011). This understanding was overturned by the results of lowtemperature specific-heat (Kittaka et al., 2014, 2016), penetration depth (Pang et al., 2018; Takenaka et al., 2017; Yamashita et al., 2017), thermal conductivity (Yamashita et al., 2017), and more recent NQR measurements on CeCu<sub>2</sub>Si<sub>2</sub> single crystals (Kitagawa et al., 2017) which reveal a small, but finite fully open superconducting gap. Theoretical proposals to account for these findings include both isotropic (non-sign-changing) (Takenaka et al., 2017; Yamashita et al., 2017) and anisotropic

(sign-changing) s-wave pairings (Ikeda et al., 2015; Li et al., 2018), as well as a d + d matrix pairing state (Nica and Si, 2021; Nica et al., 2017; Pang et al., 2018)(see Table II).

The aforementioned *s*-wave pairings are disfavored for the following reasons:

(i) As discussed in Sec. III.D, a pronounced maximum is observed in the INS intensity inside the superconducting gap, exactly at the SDW ordering wave vector  $\mathbf{Q}_{AF}$ . The latter equals the nesting vector  $\boldsymbol{\tau}$  inside the warped part of the cylindrical heavy-electron band at the Xpoint of the bulk Brillouin zone (Smidman et al., 2018; Wu et al., 2021b). This maximum demonstrates a signchange of the superconducting order parameter along  $\tau$ , which means intraband pairing as already discussed. No such sign change is possible for isotropic BCS-type pairing. In addition, such onsite pairing is unfavorable in a heavy-fermion superconductor as the heavy charge carriers forming the Cooper pairs only have a tiny kinetic energy of order  $k_{\rm B}T_{\rm K}$ , which is of the same order as their renormalized Coulomb repulsion. For an onsite pairing to operate in a BCS superconductor, the kinetic energy is much larger than the effective Coulomb repulsion. In an innovative approach, (Tazai and Kontani, 2018, 2019) succeeded in showing that both phonon-mediated and electronically-driven s-wave heavy fermion superconductivity can arise from higher multipole charge fluctuations. However, the *magnetically-driven* nature of the superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> (Stockert *et al.*, 2011) necessitates sign-changing superconductivity (Scalapino, 2012). More generally, such an s-wave pairing without a sign change is difficult to be reconciled with the exclusion of onsite pairing associated with the strong Coulomb repulsion of the 4f electrons.

(ii) Anisotropic s-wave pairing also cannot explain the superconductivity of CeCu<sub>2</sub>Si<sub>2</sub>. In order to account for the pronounced peak observed in INS at  $\mathbf{Q}_{AF}$  inside the superconducting gap, there would need to be *inter*band nesting connected by the SDW ordering wave vector, whereas ARPES measurements (Wu et al., 2021b) and calculations of the renormalized electronic structure (Zwicknagl, 1992; Zwicknagl and Pulst, 1993) demonstrate that this ordering wave vector must connect regions within the heavy electron pocket, as indeed revealed by neutron diffraction (Stockert *et al.*, 2004), see Fig.6(b). This confirms that there is a sign change of the order parameter within this band, in contrast to the  $s_{+-}$ scenario where the sign changes between the hole and electron pockets (Li et al., 2018) (see also Ikeda et al., 2015).

A d + d pairing state with intra and interband components provides a natural resolution to all currently available experimental results, and is in line with the importance of the non-perturbative effect of the strong Coulomb repulsion of the 4f-electrons in the form of a Kondo effect. The intraband *d*-wave component accounts for the sign change on the heavy warped cylindrical bands. The two distinct components added in quadrature also ensure a fully gapped Fermi surface. This pairing state belongs to a single irreducible representation of the point group, which coincides with that of a singleband *d*-wave, and therefore implies a single transition to the superconducting phase, as observed in  $CeCu_2Si_2$ . On the microscopic level, d + d pairing is equivalent to a matrix-pairing state between f-electrons in  $\Gamma_7$  doublets and conduction electrons belonging to  $\Gamma_6$  doublets. The non-trivial matrix structure ensures the presence of the two d-wave components in the band basis. Similar d + dcandidates were proposed in the context of the alkaline Fe-selenides (Nica and Si, 2021; Nica et al., 2017), suggesting a common theme in unconventional superconductivity. Nevertheless, in line with other classes of unconventional superconductors, the unambiguous determination of the pairing state and mechanisms of CeCu<sub>2</sub>Si<sub>2</sub> still requires a fully developed microscopic theory together with additional experimental results able to discriminate between different scenarios.

Taking all these together, CeCu<sub>2</sub>Si<sub>2</sub>, the very first unconventional superconductor ever discovered, continues to grow in its role as a model system for strong correlation physics. The historical intuition about CeCu<sub>2</sub>Si<sub>2</sub> as a solid-state generalization of the superfluidity observed in liquid <sup>3</sup>He inspired the early considerations regarding the interplay between antiferromagnetic correlations and *d*-wave superconductivity. The observation that the Cooper pairs in  $CeCu_2Si_2$  are formed by the extremely heavy charge carriers existing in the lowtemperature phase of the Kondo lattice proved the superconducting pairing mechanism to be incompatible with the conventional one of BCS theory. In modern times,  $CeCu_2Si_2$ , like  $CeCu_{6-x}Au_x$  (Löhneysen *et al.*, 1994; Schröder et al., 2000), CePd<sub>2</sub>Si<sub>2</sub> (Mathur et al., 1998), CeCoIn<sub>5</sub> (Paglione *et al.*, 2003), and CeRhIn<sub>5</sub> (Park et al., 2006; Shishido et al., 2005), has served as a model system for heavy fermion antiferromagnetic quantum criticality. Intriguingly, here, the Landau-type SDW quantum criticality interplays with the beyond-Landau Mott-type quantum criticality in different energy ranges below the Kondo temperature. Moving further to just over the past few years, CeCu<sub>2</sub>Si<sub>2</sub> has emerged as a model system for multiband superconductivity with strongly correlated carriers. We certainly won't be surprised if the future will bring out yet more surprises about the superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> and related heavy-fermion systems.

#### Acknowledgements

We would like to thank Wolf Aßmus, Ang Cai, Lei Chen, Piers Coleman, Pengcheng Dai, Onur Erten, Zach Fisk, Philipp Gegenwart, Christoph Geibel, Norbert Grewe, Malte Grosche, Haoyu Hu, Kenji Ishida, Kevin Ingersent, Lin Jiao, Hirale S. Jeevan, Stefan Kirchner, Michael Lang, Michael Loewenhaupt, Alois Loidl, Bruno Lüthi, Brian Maple, Kazumasa Miyake, Guiming Pang, Silke Paschen, Jed H. Pixley, Noriaki Sato, Doug Scalapino, Erwin Schuberth, Andrea Severing, Yu Song, Günter Sparn, Greg R. Stewart, Joe D. Thompson, Hao Tjeng, Roxanne Tutchton, Hilbert von Löhneysen, Franziska Weickert, Steffen Wirth, Rong Yu, Jinglei Zhang, Jian-Xin Zhu, and Gertrud Zwicknagl for useful discussions. Part of these discussions took place at the 2019 Zhejiang Workshop on Correlated Matter, which provided the initial motivation for this work. This work was supported by the National Key R&D Program of China (2022YFA1402203), the Key R&D Program of Zhejiang Province, China (2021C01002), the National Natural Science Foundation of China (12222410, 12034017, 11974306 and 12174331), the Zhejiang Provincial Natural Science Foundation of China (LR22A040002), at Arizona State University by the NSF Grant No. DMR-2220603 and an ASU startup grant; at Rice University by the NSF Grant No. DMR-2220603 and the Robert A. Welch Foundation Grant No. C-1411. Q.S. acknowledges the hospitality of the Aspen Center for Physics, which is supported by NSF Grant No. PHY-1607611.

#### REFERENCES

- Aarts, J (1984), Ph.D. thesis (University of Amsterdam), (Unpublished).
- Abrikosov, A A, and L. P. Gor'kov (1960), Zh. Experim. i Teor. Fiz. **39**, 1781–1796, [JETP **12**, 1243 (1961)].
- Aeppli, G, D. Bishop, C. Broholm, E. Bucher, K. Siemensmeyer, M. Steiner, and N. Stüsser (1989), "Magnetic order in the different superconducting states of UPt<sub>3</sub>," Phys. Rev. Lett. **63** (6), 676–679.
- Ahlheim, U, M. Winkelmann, P. van Aken, C.D. Bredl, F. Steglich, and G.R. Stewart (1988), "Pair breaking in the heavy-fermion superconductors  $\text{Ce}_{1-x}M_x\text{Cu}_{2.2}\text{Si}_2$  and  $U_{1-x}M_x\text{Be}_{13}$  (*M*: Th, La, Y and Gd)," J. Magn. Magn. Mater. **76-77**, 520 – 522.
- Ahlheim, U, M. Winkelmann, C. Schank, C. Geibel, F. Steglich, and A.L. Giorgi (1990), "Influence of Th substitution in the heavy fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub>," Physica B: Condensed Matter **163** (1), 391 – 394.
- Aliev, F G, N. B. Brandt, V. V. Moshchalkov, and S. M. Chudinov (1983a), "The appearance of the many-body resonance at the Fermi level in Kondo-lattices," Solid State Commun. 47 (9), 693–697.
- Aliev, F G, N. B. Brandt, V. V. Moshchalkov, and S. M. Chudinov (1983b), "Superconductivity in CeCu<sub>2</sub>Si<sub>2</sub>," Solid State Commun. 45 (3), 215–218.
- Aliev, F G, N. B. Brandt, V. V. Moshchalkov, and S. M. Chudinov (1984), "Electric and magnetic properties of the Kondo-lattice compound CeCu<sub>2</sub>Si<sub>2</sub>," J. Low Temp. Phys. 57 (1), 61–93.
- Allan, M P, F. Massee, D. K. Morr, J. Van Dyke, A. W. Rost, A. P. Mackenzie, C. Petrovic, and J. C. Davis (2013),

"Imaging Cooper pairing of heavy fermions in  $CeCoIn_5$ ," Nature Physics **9** (8), 468–473.

- Alloul, H, J. Bobroff, M. Gabay, and P. J. Hirschfeld (2009), "Defects in correlated metals and superconductors," Rev. Mod. Phys. 81, 45–108.
- Amorese, Andrea, Andrea Marino, Martin Sundermann, Kai Chen, Zhiwei Hu, Thomas Willers, Fadi Choueikani, Philippe Ohresser, Javier Herrero-Martin, Stefano Agrestini, Chien-Te Chen, Hong-Ji Lin, Maurits W. Haverkort, Silvia Seiro, Christoph Geibel, Frank Steglich, Liu Hao Tjeng, Gertrud Zwicknagl, and Andrea Severing (2020), "Possible multiorbital ground state in CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B 102, 245146.
- An, K, T. Sakakibara, R. Settai, Y. Onuki, M. Hiragi, M. Ichioka, and K. Machida (2010), "Sign reversal of fieldangle resolved heat capacity oscillations in a heavy fermion superconductor CeCoIn<sub>5</sub> and  $d_{x^2-y^2}$  pairing symmetry," Phys. Rev. Lett. **104**, 037002.
- Anderson, P W (1959), "Theory of dirty superconductors," J. Phys. Chem. Solids 11 (1), 26–30.
- Anderson, P W (1984), "Heavy-electron superconductors, spin fluctuations, and triplet pairing," Phys. Rev. B 30, 1549–1550.
- Anderson, P W (1997), The Theory of Superconductivity in the High- $T_c$  Cuprate Superconductors (Princeton University Press, Princeton).
- Andrei, Eva Y, and Allan H. MacDonald (2020), "Graphene bilayers with a twist," Nature Materials 19 (12), 1265– 1275.
- Andres, K, J. E. Graebner, and H. R. Ott (1975), "4f-Virtual-bound-state formation in CeAl<sub>3</sub> at low temperatures," Phys. Rev. Lett. 35, 1779–1782.
- Aoki, D, Y. Haga, T. D. Matsuda, S. Ikeda, Y. Homma, H. Sakai, Y. Shiokawa, E. Yamamoto, A. Nakamura, R. Settai, and Y. Ōnuki (2009), "Unconventional superconductivity of NpPd<sub>5</sub>Al<sub>2</sub>," J. Phys.: Condens. Matter **21** (16), 164203.
- Aoki, Dai, Ai Nakamura, Fuminori Honda, DeXin Li, Yoshiya Homma, Yusei Shimizu, Yoshiki J. Sato, Georg Knebel, Jean-Pascal Brison, Alexandre Pourret, Daniel Braithwaite, Gerard Lapertot, Qun Niu, Michal Vališka, Hisatomo Harima, and Jacques Flouquet (2019), "Unconventional superconductivity in heavy fermion UTe<sub>2</sub>," J. Phys. Soc. Jpn. 88 (4), 043702.
- Aoki, H, T. Sakakibara, H. Shishido, R. Settai, Y. Onuki, P. Miranović, and K. Machida (2004), "Field-angle dependence of the zero-energy density of states in the unconventional heavy-fermion superconductor CeCoIn<sub>5</sub>," J. Phys.: Condens. Matter 16 (3), L13.
- Arndt, J, O. Stockert, E. Faulhaber, P. Fouquet, H. S. Jeevan, C. Geibel, M. Loewenhaupt, and F. Steglich (2010), "Characteristics of the magnetic order in CeCu<sub>2</sub>Si<sub>2</sub> revealed by neutron spin-echo measurements," J. Phys.: Conf. Ser. 200 (1), 012009.
- Arndt, J, O. Stockert, K. Schmalzl, E. Faulhaber, H. S. Jeevan, C. Geibel, W. Schmidt, M. Loewenhaupt, and F. Steglich (2011), "Spin fluctuations in normal state CeCu<sub>2</sub>Si<sub>2</sub> on approaching the quantum critical point," Phys. Rev. Lett. **106**, 246401.
- Assmus, W, M. Herrmann, U. Rauchschwalbe, S. Riegel, W. Lieke, H. Spille, S. Horn, G. Weber, F. Steglich, and G. Cordier (1984), "Superconductivity in CeCu<sub>2</sub>Si<sub>2</sub> single crystals," Phys. Rev. Lett. **52**, 469–472.

- Balatsky, A V, I. Vekhter, and Jian-Xin Zhu (2006), "Impurity-induced states in conventional and unconventional superconductors," Rev. Mod. Phys. 78, 373–433.
- Bang, Y, and G. R. Stewart (2017), "Superconducting properties of the s+/- -wave state: Fe-based superconductors,"
  J. Phys.: Condens. Matter 29 (12), 123003.
- Batlogg, B, D. Bishop, B. Golding, C. M. Varma, Z. Fisk, J. L. Smith, and H. R. Ott (1985), "λ-shaped ultrasoundattenuation peak in superconducting (U,Th)Be<sub>13</sub>," Phys. Rev. Lett. 55, 1319–1322.
- Bauer, E, G. Hilscher, H. Michor, Ch. Paul, E. W. Scheidt, A. Gribanov, Yu. Seropegin, H. Noël, M. Sigrist, and P. Rogl (2004), "Heavy fermion superconductivity and magnetic order in noncentrosymmetric CePt<sub>3</sub>Si," Phys. Rev. Lett. **92**, 027003.
- Bauer, E D, M. M. Altarawneh, P. H. Tobash, K. Gofryk, O. E. Ayala-Valenzuela, J. N. Mitchell, R. D. McDonald, C. H. Mielke, F. Ronning, J.-C. Griveau, E. Colineau, R. Eloirdi, R. Caciuffo, B. L. Scott, O. Janka, S. M. Kauzlarich, and J. D. Thompson (2012), "Localized 5f electrons in superconducting PuCoIn<sub>5</sub>: consequences for superconductivity in PuCoGa<sub>5</sub>," J. Phys.: Condens. Matter 24 (5), 052206.
- Bellarbi, B, A. Benoit, D. Jaccard, J. M. Mignot, and H. F. Braun (1984), "High-pressure valence instability and T<sub>c</sub> maximum in superconducting CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B **30**, 1182–1187.
- Bernhoeft, N, A Hiess, N Metoki, G H Lander, and B Roessli (2006), "Magnetization dynamics in the normal and superconducting phases of UPd<sub>2</sub>Al<sub>3</sub>: II. Inferences on the nodal gap symmetry," J. Phys.: Condens. Matter 18 (26), 5961– 5972.
- Bernhoeft, N, N. Sato, B. Roessli, N. Aso, A. Hiess, G. H. Lander, Y. Endoh, and T. Komatsubara (1998), "Enhancement of magnetic fluctuations on passing below T<sub>c</sub> in the heavy fermion superconductor UPd<sub>2</sub>Al<sub>3</sub>," Phys. Rev. Lett. 81, 4244–4247.
- Boyd, G R, P. J. Hirschfeld, I. Vekhter, and A. B. Vorontsov (2009), "Inversion of specific heat oscillations with in-plane magnetic field angle in two-dimensional *d*-wave superconductors," Phys. Rev. B **79**, 064525.
- Brandt, N B, and V. V. Moshchalkov (1984), "Concentrated Kondo systems," Adv. Phys. 33 (5), 373–467.
- Bredl, C D, S. Horn, F. Steglich, B. Lüthi, and Richard M. Martin (1984), "Low-temperature specific heat of CeCu<sub>2</sub>Si<sub>2</sub> and CeAl<sub>3</sub>: Coherence effects in Kondo lattice systems," Phys. Rev. Lett. **52**, 1982–1985.
- Bredl, C D, F. Steglich, and K. D. Schotte (1978), "Specific heat of concentrated Kondo systems:(La, Ce)Al<sub>2</sub> and CeAl<sub>2</sub>," Z. Phys. B **29** (4), 327–340.
- Bruls, G, B. Wolf, D. Finsterbusch, P. Thalmeier, I. Kouroudis, W. Sun, W. Assmus, B. Lüthi, M. Lang, K. Gloos, F. Steglich, and R. Modler (1994), "Unusual *B - T* phase diagram of the heavy-fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. **72**, 1754–1757.
- Bucher, E, J. P. Maita, G. W. Hull, R. C. Fulton, and A. S. Cooper (1975), "Electronic properties of beryllides of the rare earth and some actinides," Phys. Rev. B 11, 440–449.
- Campillo, E, R. Riyat, S. Pollard, P. Jefferies, A. T. Holmes, R. Cubitt, J. S. White, J. Gavilano, Z. Huesges, O. Stockert, E. M. Forgan, and E. Blackburn (2021), "Observations of the effect of strong Pauli paramagnetism on the vortex lattice in superconducting CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B 104, 184508.

- Cao, Chongde, Micha Deppe, Günter Behr, Wolfgang Löser, Nadja Wizent, Olga Kataeva, and Bernd Büchner (2011), "Single crystal growth of the CeCu<sub>2</sub>Si<sub>2</sub> intermetallic compound by a vertical floating zone method," Crystal Growth & Design 11 (2), 431–435.
- Cao, Yuan, Valla Fatemi, Shiang Fang, Kenji Watanabe, Takashi Taniguchi, Efthimios Kaxiras, and Pablo Jarillo-Herrero (2018), "Unconventional superconductivity in magic-angle graphene superlattices," Nature 556 (7699), 43–50.
- Cava, R J, B. Batlogg, R. B. van Dover, D. W. Murphy, S. Sunshine, T. Siegrist, J. P. Remeika, E. A. Rietman, S. Zahurak, and G. P. Espinosa (1987), "Bulk superconductivity at 91 K in single-phase oxygen-deficient perovskite Ba<sub>2</sub>YCu<sub>3</sub>O<sub>9-δ</sub>," Phys. Rev. Lett. **58**, 1676–1679.
- Chakraborty, Debmalya, Nitin Kaushal, and Amit Ghosal (2017), "Pairing theory for strongly correlated *d*-wave superconductors," Phys. Rev. B **96**, 134518.
- Chen, Lei, Haoyu Hu, Christopher Lane, Emilian M Nica, Jian-Xin Zhu, and Qimiao Si (2021), "Multiorbital spintriplet pairing and spin resonance in the heavy-fermion superconductor UTe<sub>2</sub>," arXiv preprint arXiv:2112.14750.
- Chen, Q Y, D. F. Xu, X. H. Niu, J. Jiang, R. Peng, H. C. Xu, C. H. P. Wen, Z. F. Ding, K. Huang, L. Shu, Y. J. Zhang, H. Lee, V. N. Strocov, M. Shi, F. Bisti, T. Schmitt, Y. B. Huang, P. Dudin, X. C. Lai, S. Kirchner, H. Q. Yuan, and D. L. Feng (2017), "Direct observation of how the heavy-fermion state develops in CeCoIn<sub>5</sub>," Phys. Rev. B 96, 045107.
- Chu, Jiun-Haw, James G. Analytis, Chris Kucharczyk, and Ian R. Fisher (2009), "Determination of the phase diagram of the electron-doped superconductor  $Ba(Fe_{1-x}Co_x)_2As_2$ ," Phys. Rev. B **79**, 014506.
- Chubukov, A V, and L. P. Gor'kov (2008), "Spin resonance in three-dimensional superconductors: The case of CeCoIn<sub>5</sub>," Phys. Rev. Lett. **101**, 147004.
- Coleman, P, P. W. Anderson, and T. V. Ramakrishnan (1985), "Theory for the anomalous Hall constant of mixedvalence systems," Phys. Rev. Lett. 55, 414–417.
- Coleman, P, C. Pépin, Q. Si, and R. Ramazashvili (2001), "How do Fermi liquids get heavy and die?" J. Phys.: Condens. Matter 13, R723.
- Coleman, P, and A. J. Schofield (2005), "Quantum criticality," Nature 433, 226–229.
- Coleman, Piers (2007), "Heavy fermions: Electrons at the edge of magnetism," in *Handbook of Magnetism and Advanced Magnetic Materials* (John Wiley & Sons, Ltd).
- De Wilde, Y, J. Heil, A. G. M. Jansen, P. Wyder, R. Deltour, W. Assmus, A. Menovsky, W. Sun, and L. Taillefer (1994), "Andreev reflections on heavy-fermion superconductors," Phys. Rev. Lett. **72**, 2278–2281.
- Duan, Chunruo, R. E. Baumbach, Andrey Podlesnyak, Yuhang Deng, Camilla Moir, Alexander J. Breindel, M. Brian Maple, E. M. Nica, Qimiao Si, and Pengcheng Dai (2021), "Resonance from antiferromagnetic spin fluctuations for superconductivity in UTe<sub>2</sub>," Nature 600 (7890), 636–640.
- Duan, Chunruo, Kalyan Sasmal, M. Brian Maple, Andrey Podlesnyak, Jian-Xin Zhu, Qimiao Si, and Pengcheng Dai (2020), "Incommensurate spin fluctuations in the spintriplet superconductor candidate UTe<sub>2</sub>," Phys. Rev. Lett. **125**, 237003.
- Enayat, M, Z. Sun, A. Maldonado, H. Suderow, S. Seiro, C. Geibel, S. Wirth, F. Steglich, and P. Wahl (2016), "Su-

perconducting gap and vortex lattice of the heavy-fermion compound CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B **93**, 045123.

- Eremin, I, G. Zwicknagl, P. Thalmeier, and P. Fulde (2008), "Feedback spin resonance in superconducting CeCu<sub>2</sub>Si<sub>2</sub> and CeCoIn<sub>5</sub>," Phys. Rev. Lett. **101**, 187001.
- Feyerherm, R, A. Amato, C. Geibel, F. N. Gygax, P. Hellmann, R. H. Heffner, D. E. MacLaughlin, R. Müller-Reisener, G. J. Nieuwenhuys, A. Schenck, and F. Steglich (1997), "Competition between magnetism and superconductivity in CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B 56, 699–710.
- Fisher, R A, S. Kim, B. F. Woodfield, N. E. Phillips, L. Taillefer, K. Hasselbach, J. Flouquet, A. L. Giorgi, and J. L. Smith (1989), "Specific heat of UPt<sub>3</sub>: Evidence for unconventional superconductivity," Phys. Rev. Lett. 62, 1411– 1414.
- Flouquet, J, J. C. Lasjaunias, J. Peyrard, and M. Ribault (1982), "Low-temperature properties of CeAl<sub>3</sub>," J. Appl. Phys. **53** (3), 2127–2130.
- Franz, W, A Griessel, F Steglich, and D Wohlleben (1978), "Transport properties of LaCu<sub>2</sub>Si<sub>2</sub> and CeCu<sub>2</sub>Si<sub>2</sub> between 1.5K and 300K," Z. Phys. B **31** (1), 7–17.
- Friedemann, Sven, Niels Oeschler, Steffen Wirth, Cornelius Krellner, Christoph Geibel, Frank Steglich, Silke Paschen, Stefan Kirchner, and Qimiao Si (2010), "Fermi-surface collapse and dynamical scaling near a quantum-critical point," Proc. Natl. Acad. Sci. 107 (33), 14547–14551.
- Friemel, G, J. T. Park, T. A. Maier, V. Tsurkan, Yuan Li, J. Deisenhofer, H.-A. Krug von Nidda, A. Loidl, A. Ivanov, B. Keimer, and D. S. Inosov (2012), "Reciprocal-space structure and dispersion of the magnetic resonant mode in the superconducting phase of  $Rb_xFe_{2-y}Se_2$  single crystals," Phys. Rev. B 85, 140511.
- Fujiwara, K, Y. Hata, K. Kobayashi, K. Miyoshi, J. Takeuchi, Y. Shimaoka, H. Kotegawa, T. C. Kobayashi, C. Geibel, and F. Steglich (2008), "High pressure NQR measurement in CeCu<sub>2</sub>Si<sub>2</sub> up to sudden disappearance of superconductivity," J. Phys. Soc. Jpn. **77** (12), 123711.
- Fulde, P, J. Keller, and G. Zwicknagl (1988), "Theory of Heavy Fermion Systems," in *Solid State Physics*, Vol. 41, edited by Henry Ehrenreich and David Turnbull (Academic Press) pp. 1 – 150.
- Garg, Arti, Mohit Randeria, and Nandini Trivedi (2008), "Strong correlations make high-temperature superconductors robust against disorder," Nature Physics 4, 762–765.
- Gegenwart, P, C. Langhammer, C. Geibel, R. Helfrich, M. Lang, G. Sparn, F. Steglich, R. Horn, L. Donnevert, A. Link, and W. Assmus (1998), "Breakup of heavy fermions on the brink of "Phase A" in CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. 81, 1501–1504.
- Gegenwart, P, T. Westerkamp, C. Krellner, Y. Tokiwa, S. Paschen, C. Geibel, F. Steglich, E. Abrahams, and Q. Si (2007), "Multiple energy scales at a quantum critical point," Science **315** (5814), 969–971.
- Gegenwart, Philipp, Qimiao Si, and Frank Steglich (2008), "Quantum criticality in heavy-fermion metals," Nature Physics 4 (3), 186–197.
- Geibel, C, C. Schank, S. Thies, H. Kitazawa, C. D. Bredl, A. Böhm, M. Rau, A. Grauel, R. Caspary, R. Helfrich, U. Ahlheim, G. Weber, and F. Steglich (1991a), "Heavyfermion superconductivity at T<sub>c</sub>=2K in the antiferromagnet UPd<sub>2</sub>Al<sub>3</sub>," Z. Phys. B 84 (1), 1–2.
- Geibel, C, S. Thies, D. Kaczorowski, A. Mehner, A. Grauel, B. Seidel, U. Ahlheim, R. Helfrich, K. Petersen, C. D. Bredl, and F. Steglich (1991b), "A new heavy-fermion su-

perconductor: UNi<sub>2</sub>Al<sub>3</sub>," Z. Phys. B 83 (3), 305–306.

- Goremychkin, E A, and R. Osborn (1993), "Crystal-field excitations in CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B 47, 14280–14290.
- Gor'kov, L P, and E. I. Rashba (2001), "Superconducting 2D system with lifted spin degeneracy: Mixed singlet-triplet state," Phys. Rev. Lett. 87, 037004.
- Grewe, N, and F. Steglich (1991), "Heavy fermions," in *Handbook on the Physics and Chemistry of Rare Earths*, Vol. 14, edited by K. A. Gschneidner and L. Eyring (Elsevier) pp. 343–474.
- Gross, F, B. S. Chandrasekhar, K. Andres, U. Rauchschwalbe, E. Bucher, and B. Lüthi (1988), "Temperature dependence of the London penetration depth in the heavy fermion superconductors CeCu<sub>2</sub>Si<sub>2</sub> and UPt<sub>3</sub>," Physica C: Superconductivity 153, 439–440.
- Gross, F, B. S. Chandrasekhar, D. Einzel, K. Andres, P. J. Hirschfeld, H. R. Ott, J. Beuers, Z. Fisk, and J. L. Smith (1986), "Anomalous temperature dependence of the magnetic field penetration depth in superconducting UBe<sub>13</sub>," Z. Phys. B 64 (2), 175–188.
- Heffner, R H, J. L. Smith, J. O. Willis, P. Birrer, C. Baines, F. N. Gygax, B. Hitti, E. Lippelt, H. R. Ott, A. Schenck, E. A. Knetsch, J. A. Mydosh, and D. E. MacLaughlin (1990), "New phase diagram for (U,Th)Be<sub>13</sub>: A muon-spinresonance and H<sub>C1</sub> study," Phys. Rev. Lett. **65**, 2816–2819.
- Hess, D W, T. A. Tokuyasu, and J. A. Sauls (1989), "Broken symmetry in an unconventional superconductor: a model for the double transition in UPt<sub>3</sub>," J. Phys.: Condens. Matter **1** (43), 8135–8145.
- Hewson, A C (1997), The Kondo problem to heavy fermions (Cambridge university press, Cambridge).
- Hirschfeld, Peter J, and Nigel Goldenfeld (1993), "Effect of strong scattering on the low-temperature penetration depth of a *d*-wave superconductor," Phys. Rev. B **48**, 4219–4222.
- Holmes, A T, D. Jaccard, and K. Miyake (2004), "Signatures of valence fluctuations in CeCu<sub>2</sub>Si<sub>2</sub> under high pressure," Phys. Rev. B 69, 024508.
- Hu, Haoyu, Ang Cai, Lei Chen, Lili Deng, Jedediah H Pixley, Kevin Ingersent, and Qimiao Si (2021a), "Unconventional superconductivity from Fermi surface fluctuations in strongly correlated metals," arXiv preprint arXiv:2109.13224.
- Hu, Haoyu, Ang Cai, Lei Chen, and Qimiao Si (2021b), "Spin-singlet and spin-triplet pairing correlations in antiferromagnetically coupled Kondo systems," arXiv preprint arXiv:2109.12794.
- Huesges, Z, K. Schmalzl, C. Geibel, M. Brando, F. Steglich, and O. Stockert (2018), "Robustness of magnons near the quantum critical point in the heavy-fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B 98, 134425.
- Hull, G W, J. H. Wernick, T. H. Geballe, J. V. Waszczak, and J. E. Bernardini (1981), "Superconductivity in the ternary intermetallics YbPd<sub>2</sub>Ge<sub>2</sub>, LaPd<sub>2</sub>Ge<sub>2</sub>, and LaPt<sub>2</sub>Ge<sub>2</sub>," Phys. Rev. B 24, 6715–6718.
- Hunt, M, P. Meeson, P.-A. Probst, P. Reinders, M. Springford, W. Assmus, and W. Sun (1990), "Magnetic oscillations in the heavy-fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub>," J. Phys: Condens. Matter 2, 6859.
- Huy, N T, A. Gasparini, D. E. de Nijs, Y. Huang, J. C. P. Klaasse, T. Gortenmulder, A. de Visser, A. Hamann, T. Görlach, and H. v. Löhneysen (2007), "Superconductivity on the border of weak itinerant ferromagnetism in UCoGe," Phys. Rev. Lett. 99, 067006.

- Ikeda, H, M. T. Suzuki, and R. Arita (2015), "Emergent loopnodal  $s_{\pm}$ -wave superconductivity in CeCu<sub>2</sub>Si<sub>2</sub>: Similarities to the iron-based superconductors," Phys. Rev. Lett. **114**, 147003.
- Im, H J, T. Ito, H.-D. Kim, S. Kimura, K. E. Lee, J. B. Hong, Y. S. Kwon, A. Yasui, and H. Yamagami (2008), "Direct observation of dispersive Kondo resonance peaks in a heavy-fermion system," Phys. Rev. Lett. 100, 176402.
- Ishida, K, Y. Kawasaki, K. Tabuchi, K. Kashima, Y. Kitaoka, K. Asayama, C. Geibel, and F. Steglich (1999), "Evolution from magnetism to unconventional superconductivity in a series of  $Ce_x Cu_2Si_2$  compounds probed by Cu NQR," Phys. Rev. Lett. 82, 5353–5356.
- Ishida, K, D. Ozaki, T. Kamatsuka, H. Tou, M. Kyogaku, Y. Kitaoka, N. Tateiwa, N. K. Sato, N. Aso, C. Geibel, and F. Steglich (2002), "Spin-triplet superconductivity in UNi<sub>2</sub>Al<sub>3</sub> revealed by the <sup>27</sup>Al Knight Shift measurement," Phys. Rev. Lett. 89, 037002.
- Ishikawa, M, H. F. Braun, and J. L. Jorda (1983), "Effect of composition on the superconductivity of CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B 27, 3092–3095.
- Izawa, K, H. Yamaguchi, Yuji Matsuda, H. Shishido, R. Settai, and Y. Onuki (2001), "Angular position of nodes in the superconducting gap of quasi-2D heavy-fermion superconductor cecoin<sub>5</sub>," Phys. Rev. Lett. 87, 057002.
- Jaccard, D, K. Behnia, and J. Sierro (1992), "Pressure induced heavy fermion superconductivity of CeCu<sub>2</sub>Ge<sub>2</sub>," Phys. Lett. A **163** (5-6), 475–480.
- Jang, S Y, J. D. Denlinger, J. W. Allen, V. S. Zapf, M. B. Maple, J. N. Kim, B. G. Jang, and J. H. Shim (2020), "Evolution of the Kondo lattice electronic structure above the transport coherence temperature," Proc. Natl. Acad. Sci. 117 (1), 23467.
- Jiao, Lin, Sean Howard, Sheng Ran, Zhenyu Wang, Jorge Olivares Rodriguez, Manfred Sigrist, Ziqiang Wang, Nicholas P. Butch, and Vidya Madhavan (2020), "Chiral superconductivity in heavy-fermion metal UTe<sub>2</sub>," Nature 579 (7800), 523–527.
- Joynt, Robert, and Louis Taillefer (2002), "The superconducting phases of UPt<sub>3</sub>," Rev. Mod. Phys. **74**, 235–294.
- Kanoda, K (2008), "Mott transition and superconductivity in Q2D organic conductors," in *The Physics of Organic Superconductors and Conductors*, edited by Andrei Lebed (Springer Berlin Heidelberg, Berlin, Heidelberg) pp. 623– 642.
- Kasahara, Y, T. Iwasawa, Y. Shimizu, H. Shishido, T. Shibauchi, I. Vekhter, and Y. Matsuda (2008), "Thermal conductivity evidence for a  $d_{x^2-y^2}$  pairing symmetry in the heavy-fermion CeIrIn<sub>5</sub> superconductor," Phys. Rev. Lett. 100, 207003.
- Kasuya, Tadao (1956), "A theory of metallic ferro- and antiferromagnetism on Zener's model," Progress of Theoretical Physics 16 (1), 45–57.
- Khim, S, J. F. Landaeta, J. Banda, N. Bannor, M. Brando, P. M. R. Brydon, D. Hafner, R. Küchler, R. Cardoso-Gil, U. Stockert, A. P. Mackenzie, D. F. Agterberg, C. Geibel, and E. Hassinger (2021), "Field-induced transition within the superconducting state of CeRh<sub>2</sub>As<sub>2</sub>," Science **373** (6558), 1012–1016.
- Kitagawa, S, T. Higuchi, M. Manago, T. Yamanaka, K. Ishida, H. S. Jeevan, and C. Geibel (2017), "Magnetic and superconducting properties of an S-type single-crystal CeCu<sub>2</sub>Si<sub>2</sub> probed by <sup>63</sup>Cu nuclear magnetic resonance and nuclear quadrupole resonance," Phys. Rev. B 96, 134506.

- Kitagawa, S, G. Nakamine, K. Ishida, H. S. Jeevan, C. Geibel, and F. Steglich (2018), "Evidence for the presence of the Fulde-Ferrell-Larkin-Ovchinnikov state in CeCu<sub>2</sub>Si<sub>2</sub> revealed using <sup>63</sup>Cu NMR," Phys. Rev. Lett. **121**, 157004.
- Kittaka, S, Y. Aoki, Y. Shimura, T. Sakakibara, S. Seiro, C. Geibel, F. Steglich, H. Ikeda, and K. Machida (2014), "Multiband superconductivity with unexpected deficiency of nodal quasiparticles in CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. **112**, 067002.
- Kittaka, S, Y. Aoki, Y. Shimura, T. Sakakibara, S. Seiro, C. Geibel, F. Steglich, Y. Tsutsumi, H. Ikeda, and K. Machida (2016), "Thermodynamic study of gap structure and pair-breaking effect by magnetic field in the heavy-fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B 94, 054514.
- Knafo, W, G. Knebel, P. Steffens, K. Kaneko, A. Rosuel, J.-P. Brison, J. Flouquet, D. Aoki, G. Lapertot, and S. Raymond (2021), "Low-dimensional antiferromagnetic fluctuations in the heavy-fermion paramagnetic ladder compound UTe<sub>2</sub>," Phys. Rev. B **104**, L100409.
- Knebel, G, D. Aoki, D. Braithwaite, B. Salce, and J. Flouquet (2006), "Coexistence of antiferromagnetism and superconductivity in CeRhIn<sub>5</sub> under high pressure and magnetic field," Phys. Rev. B 74, 020501.
- Knebel, G, C. Eggert, D. Engelmann, R. Viana, A. Krimmel, M. Dressel, and A. Loidl (1996), "Phase diagram of CeCu<sub>2</sub>(Si<sub>1-x</sub>Ge<sub>x</sub>)<sub>2</sub>," Phys. Rev. B 53, 11586–11592.
- Kondo, Jun (1964), "Resistance Minimum in Dilute Magnetic Alloys," Progress of Theoretical Physics **32** (1), 37–49.
- Krimmel, A, and A. Loidl (1997), "The phase diagram of  $CeCu_2(Si_{1-x}Ge_x)_2$ ," Physica B: Condensed Matter **234**-**236**, 877 879.
- Krimmel, A, A. Loidl, H. Schober, and P. C. Canfield (1997), "Single-crystal neutron diffraction studies on CeCu<sub>2</sub>Ge<sub>2</sub> and CeCu<sub>1.9</sub>Ni<sub>0.1</sub>Ge<sub>2</sub>," Phys. Rev. B 55, 6416–6420.
- Kromer, F, R. Helfrich, M. Lang, F. Steglich, C. Langhammer, A. Bach, T. Michels, J. S. Kim, and G. R. Stewart (1998), "Revision of the phase diagram of superconducting  $U_{1-x}Th_xBe_{13}$ ," Phys. Rev. Lett. 81, 4476–4479.
- Kromer, F, M. Lang, N. Oeschler, P. Hinze, C. Langhammer, F. Steglich, J. S. Kim, and G. R. Stewart (2000), "Thermal expansion studies of superconducting  $U_{1-x}Th_xBe_{13}$  (0 < x < 0.052): Implications for the interpretation of the T - xphase diagram," Phys. Rev. B **62**, 12477–12488.
- Kuramoto, Y, and Y. Kitaoka (2012), *Dynamics of Heavy Fermions* (Oxford University Press, Oxford).
- Lambert, S E, Y. Dalichaouch, M. B. Maple, J. L. Smith, and Z. Fisk (1986), "Superconductivity under pressure in  $(U_{1-x}Th_x)Be_{13}$ : Evidence for two superconducting states," Phys. Rev. Lett. 57, 1619–1622.
- Lang, Michael, and Jens Müller (2003), "Organic superconductors," arXiv preprint arXiv:cond-mat/0302157.
- Lee, Patrick A, Naoto Nagaosa, and Xiao-Gang Wen (2006), "Doping a mott insulator: Physics of high-temperature superconductivity," Rev. Mod. Phys. 78, 17–85.
- Leggett, A J (1975), "A theoretical description of the new phases of liquid <sup>3</sup>He," Rev. Mod. Phys. 47, 331–414, Erratum: 1976, Rev. Mod. Phys. 48, 357.
- Lengyel, E, M. Nicklas, H. S. Jeevan, C. Geibel, and F. Steglich (2011), "Pressure tuning of the interplay of magnetism and superconductivity in CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. 107, 057001.
- Lévy, F, I. Sheikin, B. Grenier, and A. D. Huxley (2005), "Magnetic field-induced superconductivity in the ferromag-

net URhGe," Science 309 (5739), 1343-1346.

- Li, Y, M. Liu, Z. Fu, X. Chen, F. Yang, and Y.-F. Yang (2018), "Gap symmetry of the heavy fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub> at ambient pressure," Phys. Rev. Lett. **120**, 217001.
- Liang, Ruixing, P. Dosanjh, D. A. Bonn, D. J. Baar, J. F. Carolan, and W. N. Hardy (1992), "Growth and properties of superconducting YBCO single crystals," Physica C: Superconductivity 195 (1), 51–58.
- Löhneysen, H v, T. Pietrus, G. Portisch, H. G. Schlager, A. Schröder, M. Sieck, and T. Trappmann (1994), "Non-Fermi-liquid behavior in a heavy-fermion alloy at a magnetic instability," Phys. Rev. Lett. **72**, 3262–3265.
- Löhneysen, Hilbert v, Achim Rosch, Matthias Vojta, and Peter Wölfle (2007), "Fermi-liquid instabilities at magnetic quantum phase transitions," Rev. Mod. Phys. 79, 1015– 1075.
- Loram, JW, K.A. Mirza, and P.F. Freeman (1990), "The electronic specific heat of  $YBa_2(Cu_{1-x}Zn_x)_3O_7$  from 1.6 K to 300 K," Physica C: Superconductivity **171** (3), 243–256.
- Lu, X F, N. Z. Wang, Hui Wu, Y. P. Wu, D. Zhao, X. Z. Zeng, X. G. Luo, T. Wu, W. Bao, G. H. Zhang, F. Q. Huang, Q. Z. Huang, and X. H. Chen (2015), "Coexistence of superconductivity and antiferromagnetism in (Li<sub>0.8</sub>Fe<sub>0.2</sub>)OHFeSe," Nature Materials 14 (3), 325–329.
- Lu, Xin, Hanoh Lee, T. Park, F. Ronning, E. D. Bauer, and J. D. Thompson (2012), "Heat-capacity measurements of energy-gap nodes of the heavy-fermion superconductor CeIrIn<sub>5</sub> deep inside the pressure-dependent dome structure of its superconducting phase diagram," Phys. Rev. Lett. **108**, 027001.
- Luke, G M, A. Keren, K. Kojima, L. P. Le, B. J. Sternlieb, W. D. Wu, Y. J. Uemura, Y. Ōnuki, and T. Komatsubara (1994), "Competition between magnetic order and superconductivity in CeCu<sub>2.2</sub>Si<sub>2</sub>," Phys. Rev. Lett. **73**, 1853– 1856.
- Luke, G M, A. Keren, L. P. Le, W. D. Wu, Y. J. Uemura, D. A. Bonn, L. Taillefer, and J. D. Garrett (1993), "Muon spin relaxation in UPt<sub>3</sub>," Phys. Rev. Lett. **71**, 1466–1469.
- Luo, X-B, Y. Zhang, Q.-Y. Chen, Q. Liu, L. Luo, S.-Y. Tan, X.-G. Zhu, and X.-C. Lai (2020), "Electronic structure evolution accompanying heavy fermion formation in CeCu<sub>2</sub>Si<sub>2</sub>," Sci. China-Phys. Mech. Astron. **63**, 287413.
- Machida, K (1983), "Note on upper critical field of heavy fermion superconductivity," J. Phys. Soc. Jpn. 52 (9), 2979–2980.
- MacLaughlin, D E, Cheng Tien, W. G. Clark, M. D. Lan, Z. Fisk, J. L. Smith, and H. R. Ott (1984), "Nuclear magnetic resonance and heavy-fermion superconductivity in (U, Th)Be<sub>13</sub>," Phys. Rev. Lett. 53, 1833–1836.
- Maple, M B (1968), "The superconducting transition temperature of  $La_{1-x}Gd_xAl_2$ ," Phys. Lett. A **26** (10), 513 514.
- Maple, M B, J. W. Chen, Y. Dalichaouch, T. Kohara, C. Rossel, M. S. Torikachvili, M. W. McElfresh, and J. D. Thompson (1986), "Partially gapped Fermi surface in the heavy-electron superconductor URu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. 56, 185–188.
- Maple, M B, W. A. Fertig, A. C. Mota, L. E. DeLong, D. Wohlleben, and R. Fitzgerald (1972), "The re-entrant superconducting-normal phase boundary of the Kondo system (La, Ce)Al<sub>2</sub>," Solid State Commun. 11 (6), 829 – 834.
  Maple, M B, P.-C. Ho, V. S Zapf, N. A. Frederick, E. D.
- Maple, M B, P.-C. Ho, V. S Zapf, N. A. Frederick, E. D. Bauer, W. M. Yuhasz, F. M. Woodward, and J. W. Lynn

(2002), "Heavy fermion superconductivity in the filled skutterudite compound  $PrOs_4Sb_{12}$ ," J. Phys. Soc. Jpn **71** (Suppl), 23–28.

- Maple, M Brian, Eric D. Bauer, Vivien S. Zapf, and Jochen Wosnitza (2004), "Unconventional superconductivity in novel materials," in *The Physics of Superconductors: Vol. II. Superconductivity in Nanostructures, High-T<sub>c</sub> and Novel Superconductors, Organic Superconductors*, edited by K. H. Bennemann and J. B. Ketterson (Springer Berlin Heidelberg, Berlin, Heidelberg) pp. 555–730.
- Mathur, N D, F. M. Grosche, S. R. Julian, I. R. Walker, D.M. Freye, R. K. W. Haswelwimmer, and G. G. Lonzarich (1998), "Magnetically mediated superconductivity in heavy fermion compounds," Nature 394, 39–31.
- Matsumoto, Yosuke, Satoru Nakatsuji, Kentaro Kuga, Yoshitomo Karaki, Naoki Horie, Yasuyuki Shimura, Toshiro Sakakibara, Andriy H. Nevidomskyy, and Piers Coleman (2011), "Quantum criticality without tuning in the mixed valence compound  $\beta$ -YbAlB<sub>4</sub>," Science **331** (6015), 316–319.
- Matthias, B T, C. W. Chu, E. Corenzwit, and D. Wohlleben (1969), "Ferromagnetism and superconductivity in uranium compounds," Proc. Natl. Acad. Sci. USA 64 (2), 459– 461.
- Matthias, B T, H. Suhl, and E. Corenzwit (1958), "Spin exchange in superconductors," Phys. Rev. Lett. 1, 92–94.
- Mazin, I I, D. J. Singh, M. D. Johannes, and M. H. Du (2008), "Unconventional superconductivity with a sign reversal in the order parameter of  $LaFeAsO_{1-x}F_x$ ," Phys. Rev. Lett. **101**, 057003.
- Meisner, G P, A. L. Giorgi, A. C. Lawson, G. R. Stewart, J. O. Willis, M. S. Wire, and J. L. Smith (1984), "U<sub>2</sub>PtC<sub>2</sub> and systematics of heavy fermions," Phys. Rev. Lett. 53, 1829–1832.
- Miyake, K, S. Schmitt-Rink, and C. M. Varma (1986), "Spinfluctuation-mediated even-parity pairing in heavy-fermion superconductors," Phys. Rev. B 34, 6554–6556.
- Mou, Daixiang, Shanyu Liu, Xiaowen Jia, Junfeng He, Yingying Peng, Lin Zhao, Li Yu, Guodong Liu, Shaolong He, Xiaoli Dong, Jun Zhang, Hangdong Wang, Chiheng Dong, Minghu Fang, Xiaoyang Wang, Qinjun Peng, Zhimin Wang, Shenjin Zhang, Feng Yang, Zuyan Xu, Chuangtian Chen, and X. J. Zhou (2011), "Distinct Fermi Surface Topology and Nodeless Superconducting Gap in a (Tl<sub>0.58</sub>Rb<sub>0.42</sub>)Fe<sub>1.72</sub>Se<sub>2</sub> Superconductor," Phys. Rev. Lett. **106**, 107001.
- Movshovich, R, T. Graf, D. Mandrus, J. D. Thompson, J. L. Smith, and Z. Fisk (1996), "Superconductivity in heavy-fermion CeRh<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B **53**, 8241–8244.
- Müller-Reisener, R (1995), Diploma thesis, TH/TU Darmstadt (unpublished).
- Mydosh, J A, P M Oppeneer, and P S Riseborough (2020), "Hidden order and beyond: an experimental – theoretical overview of the multifaceted behavior of URu<sub>2</sub>Si<sub>2</sub>," J. Phys.: Condens. Matter **32** (14), 143002.
- Nakamura, H, Y. Kitaoka, H. Yamada, and K. Asayama (1988), "Discovery of antiferromagnetic ordering above upper critical field in the heavy fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub>," J. Magn. Magn. Mater. **76-77**, 517 519.
- Nakatsuji, S, K. Kuga, Y. Machida, T. Tayama, T. Sakakibara, Y. Karaki, H. Ishimoto, S. Yonezawa, Y. Maeno, E. Pearson, G. G. Lonzarich, L. Balicas, H. Lee, and Z. Fisk (2008), "Superconductivity and quantum criticality in the heavy-fermion system  $\beta$ -YbAlB<sub>4</sub>," Nature Physics 4 (8),

603-607.

- Nguyen, D H, A. Sidorenko, M. Taupin, G. Knebel, G. Lapertot, E. Schuberth, and S. Paschen (2021), "Superconductivity in an extreme strange metal," Nature Communications 12, 4341.
- Nica, E M, and Q. Si (2021), "Multiorbital singlet pairing and d + d superconductivity," npj Quantum Materials 6 (1), 3.
- Nica, E M, R. Yu, and Q. Si (2017), "Orbital-selective pairing and superconductivity in iron selenides," npj Quantum Materials 2, 24.
- Norman, M R (2013), "Unconventional superconductivity," arXiv preprint arXiv:1302.3176.
- Norman, Michael R (2011), "The challenge of unconventional superconductivity," Science 332 (6026), 196–200.
- Noziéres, P (1974), "A Fermi-liquid description of the Kondo problem at low temperatures," J. Low Temp. Phys. 17 (1), 31–42.
- Oeschler, N, F. Kromer, T. Tayama, K. Tenya, P. Gegenwart, G. Sparn, F. Steglich, M. Lang, and G. R. Stewart (2003), "UBe<sub>13</sub>: Prototype of a non-Fermi-liquid superconductor," Acta Physica Polonica Series B B34, 255–274.
- Onari, Seiichiro, Hiroshi Kontani, and Masatoshi Sato (2010), "Structure of neutron-scattering peaks in both  $s_{++}$ -wave and  $s_{\pm}$ -wave states of an iron pnictide superconductor," Phys. Rev. B **81**, 060504.
- Onimaru, T, K. T. Matsumoto, Y. F. Inoue, K. Umeo, T. Sakakibara, Y. Karaki, M. Kubota, and T. Takabatake (2011), "Antiferroquadrupolar ordering in a Pr-based superconductor PrIr<sub>2</sub>Zn<sub>20</sub>," Phys. Rev. Lett. **106**, 177001.
- Ōnuki, Y, Y. Furukawa, and T. Komatsubara (1984), "Superconductivity of the Kondo lattice substance: CeCu<sub>2</sub>Si<sub>2</sub>," J. Phys. Soc. Jpn. 53 (7), 2197–2200.
- Osheroff, D D, W. J. Gully, R. C. Richardson, and D. M. Lee (1972a), "New magnetic phenomena in liquid He<sup>3</sup> below 3 mK," Phys. Rev. Lett. **29**, 920–923.
- Osheroff, D D, R. C. Richardson, and D. M. Lee (1972b), "Evidence for a new phase of solid He<sup>3</sup>," Phys. Rev. Lett. 28, 885–888.
- Ott, H R (1987), in *Progress in Low Temperature Physics*, Vol. 11, edited by D. F. Brewer (North Holland) p. 215.
- Ott, H R, H. Rudigier, Z. Fisk, and J. L. Smith (1983), "UBe<sub>13</sub>: An unconventional actinide superconductor," Phys. Rev. Lett. **50**, 1595–1598.
- Ott, H R, H. Rudigier, Z. Fisk, and J. L. Smith (1985), "Phase transition in the superconducting state of  $U_{1-x}Th_xBe_{13}$  (x=0-0.06)," Phys. Rev. B **31**, 1651(R).
- Ott, H R, H. Rudigier, T. M. Rice, K. Ueda, Z. Fisk, and J. L. Smith (1984), "*p*-wave superconductivity in UBe<sub>13</sub>," Phys. Rev. Lett. **52**, 1915–1918.
- Paglione, Johnpierre, M. A. Tanatar, D. G. Hawthorn, Etienne Boaknin, R. W. Hill, F. Ronning, M. Sutherland, Louis Taillefer, C. Petrovic, and P. C. Canfield (2003), "Field-induced quantum critical point in CeCoIn<sub>5</sub>," Phys. Rev. Lett. **91**, 246405.
- Palstra, T T M, A. A. Menovsky, J. van den Berg, A. J. Dirkmaat, P. H. Kes, G. J. Nieuwenhuys, and J. A. Mydosh (1985), "Superconducting and magnetic transitions in the heavy-fermion system URu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. 55, 2727–2730.
- Pang, G M, M. Smidman, J. L. Zhang, L. Jiao, Z. F. Weng, E. M. Nica, Y. Chen, W. B. Jiang, Y. J. Zhang, W. Xie, H. S. Jeevan, H. Lee, P. Gegenwart, F. Steglich, Q. Si, and H. Q. Yuan (2018), "Fully gapped d-wave superconductivity in CeCu<sub>2</sub>Si<sub>2</sub>," Proc. Natl. Acad. Sci. U.S.A. 115,

5343-5347.

- Park, J T, G. Friemel, Yuan Li, J.-H. Kim, V. Tsurkan, J. Deisenhofer, H.-A. Krug von Nidda, A. Loidl, A. Ivanov, B. Keimer, and D. S. Inosov (2011), "Magnetic resonant mode in the low-energy spin-excitation spectrum of superconducting Rb<sub>2</sub>Fe<sub>4</sub>Se<sub>5</sub> single crystals," Phys. Rev. Lett. 107, 177005.
- Park, T, F. Ronning, H. Q. Yuan, M. B. Salamon, R. Movshovich, J. L. Sarrao, and J. D. Thompson (2006), "Hidden magnetism and quantum criticality in the heavy fermion superconductor CeRhIn<sub>5</sub>," Nature 440 (7080), 65– 68.
- Park, W K, J. L. Sarrao, J. D. Thompson, and L. H. Greene (2008), "Andreev reflection in heavy-fermion superconductors and order parameter symmetry in CeCoIn<sub>5</sub>," Phys. Rev. Lett. **100**, 177001.
- Paschen, S, T. Lühmann, S. Wirth, P. Gegenwart, O. Trovarelli, C. Geibel, F. Steglich, P. Coleman, and Q. Si (2004), "Hall-effect evolution across a heavy-fermion quantum critical point," Nature 432 (7019), 881–885.
- Pfleiderer, C (2009), "Superconducting phases of *f*-electron compounds," Rev. Mod. Phys. **81**, 1551–1624.
- Pourovskii, L V, P. Hansmann, M. Ferrero, and A. Georges (2014), "Theoretical prediction and spectroscopic fingerprints of an orbital transition in CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. **112**, 106407.
- Proust, Cyril, and Louis Taillefer (2019), "The remarkable underlying ground states of cuprate superconductors," Annual Review of Condensed Matter Physics **10** (1), 409–429.
- Ran, S, C. Eckberg, Q.-P. Ding, Y. Furukawa, T. Metz, S. R. Saha, I.-L. Liu, M. Zic, H. S. Kim, J.-P. Paglione, and N. P. Butch (2019), "Nearly ferromagnetic spin-triplet superconductivity," Science **365** (6454), 684–687.
- Rauchschwalbe, U, U. Ahlheim, C. D. Bredl, H. M. Mayer, and F. Steglich (1987a), "Critical magnetic fields and specific heats of heavy fermion superconductors," in *Anomalous Rare Earths and Actinides*, edited by J.X. Boucherle, J. Flouquet, C. Lacroix, and J. Rossat-Mignod (Elsevier) pp. 447–454.
- Rauchschwalbe, U, W. Lieke, C. D. Bredl, F. Steglich, J. Aarts, K. M. Martini, and A. C. Mota (1982), "Critical fields of the "heavy-fermion" superconductor CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. 49, 1448–1451, Erratum: 1982, Phys. Rev. Lett. 49, 1960.
- Rauchschwalbe, U, F. Steglich, G. R Stewart, A. L Giorgi, P Fulde, and K Maki (1987b), "Lower critical field of U<sub>0.97</sub>Th<sub>0.03</sub>Be<sub>13</sub>: Evidence for two coexisting superconducting order parameters," Europhysics Letters (EPL) 3 (6), 751–756.
- Razafimandimby, H, P. Fulde, and J. Keller (1984), "On the theory of superconductivity in Kondo lattice systems," Z. Phys. B 54 (2), 111–120.
- Reinert, F, D. Ehm, S. Schmidt, G. Nicolay, S. Hüfner, J. Kroha, O. Trovarelli, and C. Geibel (2001), "Temperature dependence of the Kondo resonance and its satellites in CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. 87, 106401.
- Riblet, G, and K. Winzer (1971), "Vanishing of superconductivity below a second transition temperature in  $(La_{1-x}Ce_x)Al_2$  alloys due to the Kondo effect," Solid State Commun. 9 (19), 1663–1665.
- Rieger, W, and E. Parthé (1969), "Ternary alkaline and rare earth silicides and germanides with  $ThCr_2Si_2$  structure," Monatsh. Chem. **100**, 444.

- Rotundu, C R, H. Tsujii, Y. Takano, B. Andraka, H. Sugawara, Y. Aoki, and H. Sato (2004), "High magnetic field phase diagram of PrOs<sub>4</sub>Sb<sub>12</sub>," Phys. Rev. Lett. **92**, 037203.
- Ruderman, M A, and C. Kittel (1954), "Indirect exchange coupling of nuclear magnetic moments by conduction electrons," Phys. Rev. 96, 99–102.
- Rueff, J-P, J. M. Ablett, F. Strigari, M. Deppe, M. W. Haverkort, L. H. Tjeng, and A. Severing (2015), "Absence of orbital rotation in superconducting CeCu<sub>2</sub>Ge<sub>2</sub>," Phys. Rev. B **91**, 201108.
- Sachdev, Subir (2011), *Quantum Phase Transitions*, 2nd ed. (Cambridge University Press).
- Sakai, A, K. Kuga, and S. Nakatsuji (2012), "Superconductivity in the ferroquadrupolar state in the quadrupolar Kondo lattice PrTi<sub>2</sub>Al<sub>20</sub>," J. Phys. Soc. Jpn 81 (8), 083702.
  Sales, B C, and R. Viswanathan (1976), "Demagnetization
- Sales, B C, and R. Viswanathan (1976), "Demagnetization due to interconfiguration fluctuations in the RE-Cu<sub>2</sub>Si<sub>2</sub> compounds," J. Low Temp. Phys. 23 (3), 449–467.
- Sarrao, J L, L. A. Morales, J. D. Thompson, B. L. Scott, G. R. Stewart, F. Wastin, J. Rebizant, P. Boulet, E. Colineau, and G. H. Lander (2002), "Plutonium-based superconductivity with a transition temperature above 18 K," Nature 420 (6913), 297–299.
- Sarrao, J L, and J. D. Thompson (2007), "Superconductivity in cerium- and plutonium-based '115' materials," J. Phys. Soc. Jpn. 76 (5), 051013.
- Sato, N K, K. Aso, N. Miyake, R. Shiina, P. Thalmeier, G. Varelogiannis, C. Geibel, F. Steglich, Fulde P., and T. Komatsubara (2001), "Strong coupling between local moments and superconducting heavy electrons in UPd<sub>2</sub>Al<sub>3</sub>," Nature **410**, 340–343.
- Saxena, S S, P. Agarwal, K. Ahilan, F. M. Grosche, R. K. W. Haselwimmer, M. J. Steiner, E. Pugh, I. R. Walker, S. R. Julian, P. Monthoux, G. G. Lonzarich, A. Huxley, I. Sheikin, D. Braithwaite, and J. Flouquet (2000), "Superconductivity on the border of itinerant-electron ferromagnetism in UGe<sub>2</sub>," Nature **406** (6796), 587–592.
- Scalapino, D J (2012), "A common thread: The pairing interaction for unconventional superconductors," Rev. Mod. Phys. 84, 1383–1417.
- Scalapino, D J, E. Loh, and J. E. Hirsch (1986), "d-wave pairing near a spin-density-wave instability," Phys. Rev. B 34, 8190–8192.
- Scalapino, DJ (1995), "The case for  $d_{x^2-y^2}$  pairing in the cuprate superconductors," Physics Reports **250** (6), 329–365.
- Schemm, E R, R. E. Baumbach, P. H. Tobash, F. Ronning, E. D. Bauer, and A. Kapitulnik (2015), "Evidence for broken time-reversal symmetry in the superconducting phase of URu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B **91**, 140506.
- Schemm, E R, W. J. Gannon, C. M. Wishne, W. P. Halperin, and A. Kapitulnik (2014), "Observation of broken timereversal symmetry in the heavy-fermion superconductor UPt<sub>3</sub>," Science **345** (6193), 190–193.
- Schlabitz, W, J. Baumann, J. Diesing, W. Krause, G. Neumann, C. D. Bredl, U. Ahlheim, H. M. Mayer, and U. Rauchschwalbe (1984), "Heavy-fermion superconductivity in URu<sub>2</sub>Si<sub>2</sub>," Poster presented at the 4th Int. Conf. on Valence Fluctuations (Cologne, Germany).
- Schlabitz, W, J. Baumann, B. Pollit, U. Rauchschwalbe, H. M. Mayer, U. Ahlheim, and C. D. Bredl (1986), "Superconductivity and magnetic order in a strongly interacting Fermi-system: URu<sub>2</sub>Si<sub>2</sub>," Z. Phys. B **62**, 171–177.

- Schneider, H, Z. Kletowski, F. Oster, and D. Wohlleben (1983), "Transport properties of single crystals of CeCu<sub>2</sub>Si<sub>2</sub> and CeNi<sub>2</sub>Ge<sub>2</sub>," Solid State Commun. 48 (12), 1093–1097.
- Schotte, KD, and U. Schotte (1975), "Interpretation of Kondo experiments in a magnetic field," Phys. Lett. A 55 (1), 38– 40.
- Schröder, A, G. Aeppli, R. Coldea, M. Adams, O. Stockert, H. v. Löhneysen, E. Bucher, R. Ramazashvili, and P. Coleman (2000), "Onset of antiferromagnetism in heavyfermion metals," Nature 407 (6802), 351–355.
- Schuberth, Erwin, Marc Tippmann, Lucia Steinke, Stefan Lausberg, Alexander Steppke, Manuel Brando, Cornelius Krellner, Christoph Geibel, Rong Yu, Qimiao Si, and Frank Steglich (2016), "Emergence of superconductivity in the canonical heavy-electron metal YbRh<sub>2</sub>Si<sub>2</sub>," Science **351** (6272), 485–488.
- Schuberth, Erwin, Steffen Wirth, and Frank Steglich (2022), "Nuclear-order-induced quantum criticality and heavyfermion superconductivity at ultra-low temperatures in YbRh<sub>2</sub>Si<sub>2</sub>," Front. Electron. Mater. 2, 869495.
- Seiro, S, M. Deppe, H. Jeevan, U. Burkhardt, and C. Geibel (2010), "Flux crystal growth of CeCu<sub>2</sub>Si<sub>2</sub>: Revealing the effect of composition," physica status solidi (b) **247** (3), 614–616.
- Senthil, T, Matthias Vojta, and Subir Sachdev (2004), "Weak magnetism and non-Fermi liquids near heavy-fermion critical points," Phys. Rev. B 69, 035111.
- Shan, Z Y, M. Smidman, O. Stockert, Y. Liu, H. Q. Yuan, P. J. Sun, S. Wirth, E. Schuberth, and F. Steglich (2022), "CeCu<sub>2</sub>Si<sub>2</sub> and YbRh<sub>2</sub>Si<sub>2</sub>: Strange cases of heavy-fermion superconductivity," arXiv:2208.14663 10.48550/arXiv.2208.14663.
- Shen, Bin, Yongjun Zhang, Yashar Komijani, Michael Nicklas, Robert Borth, An Wang, Ye Chen, Zhiyong Nie, Rui Li, Xin Lu, Hanoh Lee, Michael Smidman, Frank Steglich, Piers Coleman, and Huiqiu Yuan (2020), "Strange metal behavior in a pure ferromagnetic Kondo lattice," Nature 579 (7797), 51–55.
- Shishido, Hiroaki, Rikio Settai, Hisatomo Harima, and Yoshichika Ōnuki (2005), "A drastic change of the Fermi surface at a critical pressure in CeRhIn<sub>5</sub>: dHvA study under pressure," J. Phys. Soc. Jpn. **74** (4), 1103–1106.
- Shoenberg, David (2009), Magnetic oscillations in metals (Cambridge University Press, Cambridge).
- Si, Q, S. Rabello, K. Ingersent, and J. L. Smith (2001), "Locally critical quantum phase transitions in strongly correlated metals," Nature 413, 804–808.
- Si, Q, R. Yu, and E. Abrahams (2016), "High-temperature superconductivity in iron pnictides and chalcogenides," Nature Reviews Materials 1, 16017.
- Si, Qimiao, and Frank Steglich (2010), "Heavy fermions and quantum phase transitions," Science **329** (5996), 1161– 1166.
- Sidis, Y, S. Pailhes, B. Keimer, P. Bourges, C. Ulrich, and L. P. Regnault (2004), "Magnetic resonant excitations in high- $T_c$  superconductors," physica status solidi (b) **241** (6), 1204–1210.
- Smidman, M, M. B. Salamon, H. Q. Yuan, and D. F. Agterberg (2017), "Superconductivity and spin-orbit coupling in non-centrosymmetric materials: a review," Rep. Prog. Phys. 80 (3), 036501.
- Smidman, M, O. Stockert, J. Arndt, G. M. Pang, L. Jiao, H. Q. Yuan, H. A. Vieyra, S. Kitagawa, K. Ishida, K. Fujiwara, T. C. Kobayashi, E. Schuberth, M. Tippmann,

L. Steinke, S. Lausberg, A. Steppke, M. Brando, H. Pfau, U. Stockert, P. Sun, S. Friedemann, S. Wirth, C. Krellner, S. Kirchner, E. M. Nica, R. Yu, Q. Si, and F. Steglich (2018), "Interplay between unconventional superconductivity and heavy-fermion quantum criticality: CeCu<sub>2</sub>Si<sub>2</sub> versus YbRh<sub>2</sub>Si<sub>2</sub>," Phil. Mag. **98** (32), 2930–2963.

- Song, Y, J. Van Dyke, I. K. Lum, B. D. White, S.-Y. Jang, D.-G. Yazici, L. Shu, A. Schneidewind, P. Čermák, Y. Qiu, M. B. Maple, D. K. Morr, and P. C. Dai (2016), "Robust upward dispersion of the neutron spin resonance in the heavy fermion superconductor Ce<sub>1-x</sub>Yb<sub>x</sub>CoIn<sub>5</sub>," Nature Communications 7, 12774.
- Song, Y, W. Y. Wang, C. D. Cao, Z. Yamani, Y. J. Xu, Y. T. Sheng, W. Löser, Y. M. Qiu, Y.-F. Yang, R. J. Birgeneau, and P. C. Dai (2021), "High-energy magnetic excitations from heavy quasiparticles in CeCu<sub>2</sub>Si<sub>2</sub>," npj Quantum Materials 6 (1), 60.
- Song, Yu, Weiyi Wang, John S Van Dyke, Naveen Pouse, Sheng Ran, Duygu Yazici, Astrid Schneidewind, Petr Čermák, Yiming Qiu, M. B. Maple, Dirk K. Morr, and Pengcheng Dai (2020), "Nature of the spin resonance mode in CeCoIn<sub>5</sub>," Communications Physics **3** (1), 1–8.
- Spille, H, U. Rauchschwalbe, and F. Steglich (1983), "Superconductivity in CeCu<sub>2</sub>Si<sub>2</sub>: Dependence of  $T_c$  on alloying and stoichiometry," Helv. Phys. Acta **56** (1-3), 165–177.
- Steglich, F (1990), "Superconductivity of strongly correlated electrons: Heavy-fermion systems," Springer Series in Solid State Sciences 90, 306–325.
- Steglich, F, J. Aarts, C. D. Bredl, W. Lieke, D. Meschede, W. Franz, and H. Schäfer (1979), "Superconductivity in the presence of strong Pauli paramagnetism: CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. 43, 1892–1896.
- Steglich, F, U. Ahlheim, J.J.M. Franse, N. Grewe, D. Rainer, and U. Rauchschwalbe (1985a), "CeCu<sub>2</sub>Si<sub>2</sub> and UPt<sub>3</sub>: Two different cases of heavy fermion superconductivity," J. Magn. Magn. Mater. **52** (1), 54–60.
- Steglich, F, and H. Armbrüster (1974), "Evidence for intermediate temperature superconductivity as a bulk effect," Solid State Communications 14 (10), 903–906.
- Steglich, F, P. Gegenwart, C. Geibel, R. Helfrich, P. Hellmann, M. Lang, A. Link, R. Modler, G. Sparn, N. Büttgen, and A. Loidl (1996), "New observations concerning magnetism and superconductivity in heavy-fermion metals," *Physica B: Condensed Matter* 223-224, 1–8.
- Steglich, F, P. Gegenwart, C. Geibel, P. Hinze, M. Lang, C. Langhammer, G. Sparn, T. Tayama, O. Trovarelli, N. Sato, T. Dahm, and G. Varelogiannis (2001), "Superconductivity and magnetism in heavy-fermions," in *More is Different: Fifty Years of Condensed Matter Physics* (Princeton University Press) pp. 191–210.
- Steglich, F, U. Rauchschwalbe, U. Gottwick, H. M. Mayer, G. Sparn, N. Grewe, U. Poppe, and J. J. M. Franse (1985b), "Heavy fermions in Kondo lattice compounds," J. Appl. Phys. 57 (8), 3054–3059.
- Steglich, F, and S. Wirth (2016), "Foundations of heavyfermion superconductivity: Lattice Kondo effect and Mott physics," Rep. Prog. Phys. **79** (8), 084502.
- Steppke, A, R. Küchler, S. Lausberg, E. Lengyel, L. Steinke, R. Borth, T. Lühmann, C. Krellner, M. Nicklas, C. Geibel, F. Steglich, and M. Brando (2013), "Ferromagnetic quantum critical point in the heavy-fermion metal YbNi<sub>4</sub>(P<sub>1-x</sub>As<sub>x</sub>)<sub>2</sub>," Science **339** (6122), 933–936.
- Stewart, G R (1984), "Heavy-fermion systems," Rev. Mod. Phys. 56, 755–787.

- Stewart, G R (2001), "Non-Fermi-liquid behavior in *d* and *f*-electron metals," Rev. Mod. Phys. **73**, 797–855.
- Stewart, G R (2006), "Addendum: Non-Fermi-liquid behavior in d- and f-electron metals," Rev. Mod. Phys. 78, 743– 753.
- Stewart, G R (2011), "Superconductivity in iron compounds," Rev. Mod. Phys. 83, 1589–1652.
- Stewart, G R (2017), "Unconventional superconductivity," Advances in Physics 66 (2), 75–196.
- Stewart, G R, Z. Fisk, and J. O. Willis (1983), "Characterization of single crystals of CeCu<sub>2</sub>Si<sub>2</sub>. A source of new perspectives," Phys. Rev. B 28, 172–177.
- Stewart, G R, Z. Fisk, J. O. Willis, and J. L. Smith (1984), "Possibility of coexistence of bulk superconductivity and spin fluctuations in UPt<sub>3</sub>," Phys. Rev. Lett. **52**, 679–682.
- Stockert, O, D. Andreica, A. Amato, H. S. Jeevan, C. Geibel, and F. Steglich (2006), "Magnetic order and superconductivity in single-crystalline CeCu<sub>2</sub>Si<sub>2</sub>," Physica B: Condensed Matter **374-375**, 167 – 170, Proceedings of the Tenth International Conference on Muon Spin Rotation, Relaxation and Resonance.
- Stockert, O, J. Arndt, E. Faulhaber, C. Geibel, H. S. Jeevan, S. Kirchner, M. Loewenhaupt, K. Schmalzl, W. Schmidt, Q. Si, and F. Steglich (2011), "Magnetically driven superconductivity in CeCu<sub>2</sub>Si<sub>2</sub>," Nature Physics 7 (2), 119–124.
- Stockert, O, J. Arndt, A. Schneidewind, H. Schneider, H. S. Jeevan, C. Geibel, F. Steglich, and M. Loewenhaupt (2008), "Magnetism and superconductivity in the heavy-fermion compound CeCu<sub>2</sub>Si<sub>2</sub> studied by neutron scattering," Physica B: Condensed Matter **403** (5), 973 976.
- Stockert, O, M. Deppe, E. Faulhaber, H. S. Jeevan, R. Schneider, N. Stusser, C. Geibel, M. Loewenhaupt, and F. Steglich (2005), "Antiferromagnetism in  $CeCu_2(Si_{1-x}Ge_x)_2$ : nature of the A phase," Physica B: Condensed Matter **359-361**, 349 – 356, Proceedings of the International Conference on Strongly Correlated Electron Systems (SCES 2005), Vienna (Austria).
- Stockert, O, M. Deppe, C. Geibel, F. Steglich, D. Hohlwein, and R. Schneider (2003), "Neutron diffraction study of the magnetism in single-crystalline  $\text{CeCu}_2(\text{Si}_{1-x}\text{Ge}_x)_2$ ," Acta Physica Polonica B **34**, 963.
- Stockert, O, E. Faulhaber, G. Zwicknagl, N. Stüßer, H. S. Jeevan, M. Deppe, R. Borth, R. Küchler, M. Loewenhaupt, C. Geibel, and F. Steglich (2004), "Nature of the A phase in CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. **92**, 136401.
- Stockert, Oliver, Stefan Kirchner, Frank Steglich, and Qimiao Si (2012), "Superconductivity in Ce- and U-based heavyfermion compounds," J. Phys. Soc. Jpn. 81 (1), 011001.
- Sun, P, and F. Steglich (2013), "Nernst effect: Evidence of local Kondo scattering in heavy fermions," Phys. Rev. Lett. 110, 216408.
- Tachiki, M, and S. Maekawa (1984), "Superconductivity in the Kondo lattice," Phys. Rev. B **29**, 2497–2502.
- Taillefer, L, and G. G. Lonzarich (1988), "Heavy-fermion quasiparticles in UPt<sub>3</sub>," Phys. Rev. Lett. **60**, 1570–1573.
- Takenaka, T, Y. Mizukami, J. A. Wilcox, M. Konczykowski, S. Seiro, C. Geibel, Y. Tokiwa, Y. Kasahara, C. Putzke, Y. Matsuda, A. Carrington, and T. Shibauchi (2017), "Fullgap superconductivity robust against disorder in heavyfermion CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. **119**, 077001.
- Tayama, T, M. Lang, T. Lühmann, F. Steglich, and W. Assmus (2003), "High-resolution magnetization studies of the heavy-fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub> at very low temperatures and in high magnetic fields," Phys. Rev. B 67,

214504.

- Tazai, Rina, and Hiroshi Kontani (2018), "Fully gapped swave superconductivity enhanced by magnetic criticality in heavy-fermion systems," Phys. Rev. B 98, 205107.
- Tazai, Rina, and Hiroshi Kontani (2019), "Hexadecapole fluctuation mechanism for s-wave heavy fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub>: Interplay between intra- and inter-orbital Cooper pairs," J. Phys. Soc. Jpn. 88 (6), 063701.
- Thalmeier, P, G. Zwicknagl, O. Stockert, G. Sparn, and F. Steglich (2005), "Frontiers in superconducting materials," Chap. Superconductivity in Heavy Fermion Compounds (Springer-Berlin, Heidelberg) pp. 109–182.
- Thomas, F, J. Thomasson, C. Ayache, C. Geibel, and F. Steglich (1993), "Precise determination of the pressure dependence of  $T_c$  in the heavy-fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub>," Physica B: Condensed Matter **186-188**, 303 306.
- Thomas, S M, F. B. Santos, M. H. Christensen, T. Asaba, F. Ronning, J. D. Thompson, E. D. Bauer, R. M. Fernandes, G. Fabbris, and P. F. S. Rosa (2020), "Evidence for a pressure-induced antiferromagnetic quantum critical point in intermediate-valence UTe<sub>2</sub>," Science Advances 6 (42), eabc8709.
- Thompson, J D, and Z. Fisk (2012), "Progress in heavyfermion superconductivity: Cel15 and related materials," J. Phys. Soc. Jpn 81 (1), 011002.
- Tou, H, Y. Kitaoka, K. Ishida, K. Asayama, N. Kimura, Y. Ōnuki, E. Yamamoto, Y. Haga, and K. Maezawa (1998), "Nonunitary spin-triplet superconductivity in UPt<sub>3</sub>: Evidence from <sup>195</sup>Pt Knight shift study," Phys. Rev. Lett. 80, 3129–3132.
- Triplett, B B, and Norman E. Phillips (1971), "Calorimetric evidence for a singlet ground state in CuCr and CuFe," Phys. Rev. Lett. 27, 1001–1004.
- Tsujimoto, Masaki, Yosuke Matsumoto, Takahiro Tomita, Akito Sakai, and Satoru Nakatsuji (2014), "Heavy-fermion superconductivity in the quadrupole ordered state of PrV<sub>2</sub>Al<sub>20</sub>," Phys. Rev. Lett. **113**, 267001.
- Ueda, K, Y. Kitaoka, H. Yamada, Y. Kohori, T. Kohara, and K. Asayama (1987), <sup>"29</sup>Si Knight shift in the heavy-fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub>," J. Phys. Soc. Jpn. **56** (3), 867–870.
- Uemura, Y J, W. J. Kossler, X. H. Yu, H. E. Schone, J. R. Kempton, C. E. Stronach, S. Barth, F. N. Gygax, B. Hitti, A. Schenck, C. Baines, W. F. Lankford, Y. Ōnuki, and T. Komatsubara (1988), "Static magnetic ordering of CeCu<sub>2.1</sub>Si<sub>2</sub> found by muon spin relaxation," Physica C: Superconductivity **153-155**, 455 – 456.
- Uemura, Y J, W. J. Kossler, X. H. Yu, H. E. Schone, J. R. Kempton, C. E. Stronach, S. Barth, F. N. Gygax, B. Hitti, A. Schenck, C. Baines, W. F. Lankford, Y. Ōnuki, and T. Komatsubara (1989), "Coexisting static magnetic order and superconductivity in CeCu<sub>2.1</sub>Si<sub>2</sub> found by muon spin relaxation," Phys. Rev. B **39**, 4726–4729.
- Vieyra, H A (2012), Dissertation, TU Dresden.
- Vieyra, H A, N. Oeschler, S. Seiro, H. S. Jeevan, C. Geibel, D. Parker, and F. Steglich (2011), "Determination of gap symmetry from angle-dependent  $H_{c2}$  measurements on CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. **106**, 207001.
- Vollhardt, D, and P. Wölfle (1990), The Superfluid Phases of Helium 3 (Taylor and Francis, London).
- Vorontsov, A B, and I. Vekhter (2007), "Unconventional superconductors under a rotating magnetic field. I. Density of states and specific heat," Phys. Rev. B 75, 224501.

- Wang, Qing-Yan, Zhi Li, Wen-Hao Zhang, Zuo-Cheng Zhang, Jin-Song Zhang, Wei Li, Hao Ding, Yun-Bo Ou, Peng Deng, Kai Chang, Jing Wen, Can-Li Song, Ke He, Jin-Feng Jia, Shuai-Hua Ji, Ya-Yu Wang, Li-Li Wang, Xi Chen, Xu-Cun Ma, and Qi-Kun Xue (2012a), "Interface-induced hightemperature superconductivity in single unit-cell FeSe films on SrTiO<sub>3</sub>," Chinese Physics Letters **29** (3), 037402.
- Wang, X-P, T. Qian, P. Richard, P. Zhang, J. Dong, H.-D. Wang, C.-H. Dong, M.-H. Fang, and H. Ding (2011), "Strong nodeless pairing on separate electron Fermi surface sheets in (Tl, K)Fe<sub>1.78</sub>Se<sub>2</sub> probed by ARPES," Europhys. Lett. **93** (5), 57001.
- Wang, X-P, P. Richard, X. Shi, A. Roekeghem, Y.-B. Huang, E. Razzoli, T. Qian, E. Rienks, S. Thirupathaiah, H.-D. Wang, C.-H. Dong, M.-H. Fang, M. Shi, and H. Ding (2012b), "Observation of an isotropic superconducting gap at the Brillouin zone centre of Tl<sub>0.63</sub>K<sub>0.37</sub>Fe<sub>1.78</sub>Se<sub>2</sub>," Europhys. Lett. **99** (6), 67001.
- Wastin, F, P. Boulet, J. Rebizant, E. Colineau, and G. H. Lander (2003), "Advances in the preparation and characterization of transuranium systems," J. Phys.: Condens. Matter 15 (28), S2279.
- Weickert, F, P. Gegenwart, C. Geibel, W. Assmus, and F. Steglich (2018), "Observation of two critical points linked to the high-field phase B in CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. B 98, 085115.
- Wu, Y, Y. J. Zhang, F. Du, B. Shen, H. Zheng, Y. Fang, M. Smidman, C. Cao, F. Steglich, H. Q. Yuan, J. D. Denlinger, and Y. Liu (2021a), "Anistropic c - f hybridization in the ferromagnetic quantum critical metal CeRh<sub>6</sub>Ge<sub>4</sub>," Phys. Rev. Lett. **126**, 216406.
- Wu, Z, Y. Fang, H. Su, W. Xie, P. Li, Y. B. Huang, D. W. Shen, B. Thiagarajan, J. Adell, C. Cao, H. Q. Yuan, F. Steglich, and Y. Liu (2021b), "Revealing the heavy quasiparticles in the heavy-fermion superconductor CeCu<sub>2</sub>Si<sub>2</sub>," Phys. Rev. Lett. **127**, 067002.
- Xiao, Gang, M. Z. Cieplak, A. Gavrin, F. H. Streitz, A. Bakhshai, and C. L. Chien (1988), "High-temperature superconductivity in tetragonal perovskite structures: Is oxygen-vacancy order important?" Phys. Rev. Lett. 60, 1446-1449.
- Xu, M, Q. Q. Ge, R. Peng, Z. R. Ye, Juan Jiang, F. Chen, X. P. Shen, B. P. Xie, Y. Zhang, A. F. Wang, X. F. Wang, X. H. Chen, and D. L. Feng (2012), "Evidence for an s-wave superconducting gap in K<sub>x</sub>Fe<sub>2-y</sub>Se<sub>2</sub> from angle-resolved photoemission," Phys. Rev. B 85, 220504.

- Yamashita, T, T. Takenaka, Y. Tokiwa, J. A. Wilcox, Y. Mizukami, D. Terazawa, Y. Kasahara, S. Kittaka, T. Sakakibara, M. Konczykowski, S. Seiro, H. S. Jeevan, C. Geibel, C. Putzke, T. Onishi, H. Ikeda, A. Carrington, T. Shibauchi, and Y. Matsuda (2017), "Fully gapped superconductivity with no sign change in the prototypical heavyfermion CeCu<sub>2</sub>Si<sub>2</sub>," Science Advances **3** (6), 10.1126/sciadv.1601667.
- Yosida, Kei (1957), "Magnetic properties of Cu-Mn alloys," Phys. Rev. 106, 893–898.
- Yu, G, Y. Li, E. M. Motoyama, and M. Greven (2009), "A universal relationship between magnetic resonance and superconducting gap in unconventional superconductors," Nature Physics 5 (12), 873–875.
- Yuan, H Q, F. M. Grosche, M. Deppe, C. Geibel, G. Sparn, and F. Steglich (2003), "Observation of two distinct superconducting phases in CeCu<sub>2</sub>Si<sub>2</sub>," Science **302** (5653), 2104–2107.
- Yuan, H Q, F. M. Grosche, M. Deppe, C. Geibel, G. Sparn, and F. Steglich (2004), "Effect of impurity scattering on the superconductivity of CeCu<sub>2</sub>Si<sub>2</sub>," New Journal of Physics 6 (1), 132.
- Yuan, H Q, F. M. Grosche, M. Deppe, G. Sparn, C. Geibel, and F. Steglich (2006), "Non-Fermi liquid states in the pressurized  $\text{CeCu}_2(\text{Si}_{1-x}\text{Ge}_x)_2$  system: Two critical points," Phys. Rev. Lett. **96**, 047008.
- Zhang, F C, and T. M. Rice (1988), "Effective hamiltonian for the superconducting Cu oxides," Phys. Rev. B 37, 3759– 3761.
- Zhou, Brian B, Shashank Misra, Eduardo H. da Silva Neto, Pegor Aynajian, Ryan E. Baumbach, J. D. Thompson, Eric D. Bauer, and Ali Yazdani (2013), "Visualizing nodal heavy fermion superconductivity in CeCoIn<sub>5</sub>," Nature Physics 9 (8), 474–479.
- Zwicknagl, G (1992), "Quasi-particles in heavy fermion systems," Adv. Phys. 41 (3), 203–302.
- Zwicknagl, G (2007), "Kondo effect and antiferromagnetism in CeCu<sub>2</sub>Ge<sub>2</sub>: An electronic structure study," J. Low Temp. Phys. **147** (3), 123–134.
- Zwicknagl, G (2016), "The utility of band theory in strongly correlated electron systems," Rep. Prog. Phys. 79 (12), 124501.
- Zwicknagl, G, and U. Pulst (1993), "CeCu<sub>2</sub>Si<sub>2</sub>: Renormalized band structure, quasiparticles and co-operative phenomena," Physica B: Condensed Matter 186-188, 895 – 898.

TABLE I Chronology of discoveries and early studies on heavy fermions, heavy-fermion superconductivity, and related topics (1969-1989). The following abbreviations are used: PM: paramagnetic, AF(O): antiferromagnetic (order), SDW: spin-density wave, CDW: charge-density wave, MF: mean field, FL: Fermi liquid, HF: heavy fermion, KE: Kondo effect, RLM: resonance level model (Schotte and Schotte, 1975), I: interpretation.

Year	Discovery/Achievement	Material	Reference
1969	First synthesis	$CeCu_2Si_2$	Rieger and Parthé, 1969
1969	Superconductivity, $T_c = 1.47$ K	$U_2PtC_2$	Matthias <i>et al.</i> , 1969
1971	Fe/Cr-derived specific heat $\Delta C(T) = \gamma T$ at $T \ll T_{\rm K}, \gamma \approx 1(16)$ J/mol K <sup>2</sup>	<b>Cu</b> (Fe,Cr) 80 (20-50) ppm	Triplett and Phillips, 1971
1972	Superfluidity	Liquid <sup>3</sup> He	Osheroff <i>et al.</i> , 1972a,b
1974	Theory of local FL of $S = \frac{1}{2}$ Kondo ion	Liquia IIo	Noziéres, 1974
1975	Superconducting transition at $T_c = 0.97$ K $T_c$ decreases by 30% in $B = 6$ T. I: due to U - filaments	UBe <sub>13</sub>	Bucher et al., 1975
1975	Heavy FL; $\gamma = 1.62 \text{ J/mol K}^2$ I: due to $4f$ -virtual bound state	$CeAl_3$	Andres et al., 1975
1975	Theory of superfluid phases	Liquid <sup>3</sup> He	Leggett, 1975
1976	Magnetic properties I: Intermediate-valence compound	CeCu <sub>2</sub> Si <sub>2</sub>	Sales and Viswanathan, 1976
1978	$T_{\rm K} = 5 \text{ K}, T_{\rm N} = 3.9 \text{ K}, \gamma_{\rm AF} = 0.135 \text{ J/mol } \text{K}^2$ KE/AFO treated by RLM/MF: $\gamma_{\rm PM} = 1.7 \text{ J/mol } \text{K}^2$	$CeAl_2$	Bredl <i>et al.</i> , 1978
1978	Superconducting transition at $T_c \approx 0.5$ K in resistivity and susceptibility <b>I</b> : due to spurious phase(s)	$CeCu_2Si_2$	Franz et al., 1978
1979	Bulk superconductivity, $T_c \approx 0.6$ K (first HF superconductor) $\gamma \approx 1$ J/mol K <sup>2</sup> , heavy fermions (introduction of the term "HF")	$\mathrm{CeCu}_2\mathrm{Si}_2$	Steglich et al., 1979
1982	Lower and upper critical fields Meissner effect, strong Pauli limiting, <b>I</b> : even-parity pairing	$\rm CeCu_2Si_2$	Rauchschwalbe et al., 1982
1983	HF superconductivity ( $T_{\rm c} \approx 0.85$ K, $\gamma \approx 1.1$ J/mol K <sup>2</sup> )	$UBe_{13}$	Ott et al., 1983
1983	Suppression of superconductivity by $\approx 1\%$ impurity substitution I: Unconventional superconductivity	$CeCu_2Si_2$	Spille et al., 1983
1984	HF superconductivity in single crystals	$CeCu_2Si_2$	Assmus <i>et al.</i> , 1984 Ōnuki <i>et al.</i> , 1984
1984	Hump in $C(T)/T$ , <b>I</b> : due to Kondo lattice coherence	CeCu <sub>2</sub> Si <sub>2</sub> /CeAl <sub>3</sub>	Bredl et al., 1984
1984	$C(T) \sim T^3(T \ll T_c)$	UBe <sub>13</sub>	Ott et al., 1984
	I: gap point nodes, $p$ -wave superconductivity		
1984	NMR: $1/T_1 \sim T^3$ , <b>I</b> : gap line nodes	$(\mathrm{U}_{1-x}\mathrm{Th}_x)\mathrm{Be}_{13}$	MacLaughlin et al., 1984
1984	Theory of superconductivity in Kondo lattice by Grüneisen-parameter coupling		Razafimandimby et al., 1984
1984	Theory of triplet pairing in HF superconductors		Anderson, 1984
1984	HF superconductivity ( $T_{\rm c} \approx 1.5 \text{ K}, \gamma \approx 0.075 \text{ J/mol K}^2$ )	$U_2PtC_2$	Meisner <i>et al.</i> , 1984
1984	HF superconductivity ( $T_c \approx 0.8 - 1.5 \text{ K}, \gamma \approx 0.07 \text{ J/mol K}^2$ ) MF-type transition at $T_0 = 17.5 \text{ K}$ , I: into SDW/CDW	$\mathrm{URu}_2\mathrm{Si}_2$	Schlabitz et al., 1984, 1986 Palstra et al., 1985 Maple et al., 1986
1985	dc-Josephson effect across CeCu <sub>2</sub> Si <sub>2</sub> /Al weak link: ordinary critical pair current size	$CeCu_2Si_2$	Steglich et al., 1985b
1985	Second transition below $T_c$ , I: Unconventional superconductivity	$(\mathrm{U}_{1-x}\mathrm{Th}_x)\mathrm{Be}_{13}$	Ott et al., 1985
1985	Second transition below $T_c$ , I: SDW transition	$(U_{1-x}Th_x)Be_{13}$	Batlogg et al., 1985
1986	Evidence for two superconducting states	$(U_{1-x}Th_x)Be_{13}$	Lambert et al., 1986
1986	Penetration depth: $\lambda(T) \sim T^2(T \ll T_c)$ , <b>I</b> : gap point nodes	UBe <sub>13</sub>	Gross et al., 1986
1986	Theory of even-parity pairing caused by spin fluctuations		Miyake <i>et al.</i> , 1986
1986	Theory of <i>d</i> -wave pairing near an SDW instability		Scalapino et al., 1986
1987	Evidence for two coexisting superconducting order parameters	$(\mathrm{U}_{1-x}\mathrm{Th}_x)\mathrm{Be}_{13}$	Rauchschwalbe et al., 1987b
1988	dHvA oscillations: direct observation of HFs	$UPt_3$	Taillefer and Lonzarich, 1988
1988	Penetration depth: $\lambda(T) \sim T^2(T \ll T_c)$ , I: gap nodes	$UPt_3$ , $CeCu_2Si_2$	Gross et al., 1988
1989	Second transition below $T_c$ , I: Unconventional superconductivity	$UPt_3$	Fisher et al., 1989
1989 1989	Weak AFO, decrease of magnetic Bragg intensity below $T_c$ Theory on broken symmetry in an unconventional superconductor	$UPt_3$	Aeppli <i>et al.</i> , 1989 Hess <i>et al.</i> , 1989
1909	model for double transition in $UPt_3$		11055 <i>et ut.</i> , 1909

Experiments			
Probe	Results	Interpretation	Reference
Resistivity under field	Paramagnetic limiting of $B_{c2}$	Singlet pairing	Assmus et al., 1984
Specific heat	$C \sim T^3$	_	Steglich et al., 1985a
NMR Knight shift	Knight shift decrease below $T_{\rm c}$	Singlet pairing	Ueda <i>et al.</i> , 1987
Penetration depth	$\lambda \sim T^2$	Gap nodes	Gross <i>et al.</i> , 1988
Point contact spectroscopy	Flat $dV/dI$	Nodeless gap	De Wilde et al., 1994
Cu-NQR	$1/T_1 \sim T^3$	Gap line nodes	Ishida <i>et al.</i> , 1999 Fujiwara <i>et al.</i> , 2008
Inelastic neutron scattering	Peak in magnetic response below $T_{\rm c}$	Sign-changing order parameter	Stockert et al., 2011
Field angle dependent resistivity	4-fold $B_{c2}(\phi)$	$d_{xy}$ state	Vieyra et al., 2011
Specific heat $(T < 0.1 \text{ K})$	Exponential $C(T)$ as $T \to 0$	Two nodeless gaps	Kittaka <i>et al.</i> , 2014, 2016
Scanning tunneling microscopy	Spectra analysis	Nodal + nodeless gaps	Enayat et al., 2016
Penetration depth ( $T < 0.1$ K)	Exponential $\lambda(T)$ as $T \to 0$	Nodeless gap	Yamashita et al., 2017 Takenaka et al., 2017 Pang et al., 2018
Thermal conductivity ( $T < 0.1$ K)	Vanishing $\kappa/T$ as $T \to 0$	Nodeless gap	Yamashita et al., 2017
Cu-NQR $(T<0.1~{\rm K})$	Exponential $1/T_1$ as $T \to 0$	Nodeless gap	Kitagawa et al., 2017
Small angle neutron scattering	Form factor analysis	Two nodeless gaps	Campillo et al., 2021

TABLE II A summary of experimental probes of the superconducting gap structure of  $CeCu_2Si_2$ , together with proposed theories for the superconducting pairing state.

Theory			
Theory	Gap structure	Sign-change?	Reference
Loop nodal $s_{+-}$ state	Nodal	$\checkmark$ (interband)	Ikeda et al., 2015
d + d pairing	Nodeless	$\checkmark$ (intraband)	Nica et al., 2017 Nica and Si, 2021
Multipole mediated $s$ -wave	Nodeless	×	Tazai and Kontani, 2018, 2019 Tazai and Kontani, 2019
$s_{+-}$ state	Nodal, nodeless	$\checkmark$ (interband)	Li et al., 2018