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## Importance of Nuclear Quantum Effects on the Hydration of Chloride Ion

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Path-integral *ab initio* molecular dynamics (PI-AIMD) calculations have been employed to probe the nature of chloride ion solvation in aqueous solution. Nuclear quantum effects (NQEs) are shown to weaken hydrogen bonding between the chloride anion and the solvation shell of water molecules. As a consequence, the disruptive effect of the anion on the solvent water structure is significantly reduced compared to what is found in the absence of NQEs. The chloride hydration structure obtained from PI-AIMD agrees well with information extracted from neutron scattering data. In particular, the observed satellite peak in the hydrogen-chloride-hydrogen triple angular distribution serves as a clear signature of NQEs. The present results suggest that NQEs are likely to play a crucial role in determining the structure of saline solutions.

Hydrated chloride ions (Cl<sup>-</sup>) are ubiquitous in nature. They are essential components in the electrolytes of living systems [1]. Also, Cl<sup>-</sup> is a member of the Hofmeister series of ions [2], with important effects on protein solubility and folding. Moreover, chloride ion channels are a diverse group of anion-selective channels involved in the excitability of skeletal, cardiac, and smooth muscle cells [2]. These important biochemical and physiological roles all involve Cl<sup>-</sup> in an aqueous environment. Not surprisingly, the hydration structure of Cl<sup>-</sup>, and its impact on the hydrogen (H)-bonding network of water have been the subject of intense scientific research for decades [3– 9].

The arrangement of water around Cl<sup>-</sup> can be probed by scattering experiments [10-12], and the perturbed H-bond structure is inferable from spectroscopic measurements [13–16]. But most experiments typically vield only time-averaged structural information. At molecular level, the solvation structure of Cl<sup>-</sup> is constantly fluctuating on a sub-picosecond time scale. In this regard, ab initio molecular dynamics (AIMD) simulation [17] has already proven to be a valuable theoretical tool. In AIMD, forces needed to propagate the dynamics are generated from the instantaneous ground state of density functional theory [18]. AIMD can directly model the fast exchange of water molecules within the anions hydration shell, as well as the H-bond fluctuations in water solvent. AIMD simulations of chloride in solution,  $Cl^{-}(aq)$ , have been carried out since the 1990s [15, 19–28]. Consensus has been reached on the fact that the water structure in the first hydration shell is strongly distorted. The chloride anion, as a H-bond acceptor, is polarized in solution due to its large size [4, 16, 20, 22, 29, 30]. Therefore, the distribution of water molecules in its first coordination shell is rather inhomogeneous [22]. Such a defectlike solvation pattern around  $Cl^{-}$  is incompatible with the tetrahedral structure of water and disrupts the Hbond network in the solution. Beyond the first solvation shell, recent AIMD simulations [28] carried out using the PBE functional [31] at an elevated temperature of 400K found a well-structured second solvation shell for  $Cl^-$  and weakened H-bonds as far as the third solvation shell. These previous studies have provided important insights on  $Cl^-(aq)$ , but some issues remain unresolved. For example, one might expect that the water structure in saltwater is noticeably different from that of pure water. However, an analysis based on neutron scattering data surprisingly suggested that the disruption of the water structure by solvated  $Cl^-$  is negligible beyond the first shell [11, 12].

Rationalization of the neutron scattering data requires atomic details on the solvation structure of Cl<sup>-</sup>. In order to tackle this problem quantitatively with AIMD, one needs to employ an accurate exchange-correlation functional. Moreover, treatment of nuclear quantum effects (NQEs) associated with the systems protons is not optional, but indispensable in order to produce a liquid water structure compatible with the experimental observation [32–35]. Notably, the role of NQEs varies significantly among different types of H-bonds [36]. This new twist elevates the level of complexity in the computations. Two distinct types of H-bonds exist simultaneously in  $Cl^{-}(aq)$ , namely the water-water (W-W) and anion-water (A-W) H-bonds. The former tends to build an extended tetrahedral network [37], while the latter tends to form a tight A-W cluster surrounded by additional solvent water molecules. The resulting Cl<sup>-</sup> hydration structure reflects a delicate balance between these two competing effects. NQEs tilt the balance between these competing H-bonding forces, which in turn lead to a different hydration structure than is modeled using classical nuclei.

The present work focuses on probing the structure of  $Cl^{-}(aq)$  via Feynman path integral [38] *ab initio* molecular dynamics (PI-AIMD) simulations, and traditional AIMD with classical nuclei. The nuclear potential en-



FIG. 1. In PI-AIMD, the distribution of distances from the intramolecular oxygen to the MLWF centers for bonding pair electrons; vertical lines denote average positions of two types of protons bonded to solvent water or to Cl<sup>-</sup>, as shown in the inset together with density isosurfaces of MLWF for bonding pair electrons.

ergy surface is generated by employing the SCAN functional [39]. Surprisingly, NQEs tilt the balance between the competing W-W and A-W H-bonding and give rise to important changes to the anions hydration structure. Under the influence of NQEs, both types of H-bonds are weakened. However, the A-W H-bond is weakened to a greater extent than the corresponding W-W H-bond. As a result, water molecules in the first hydration shell are relatively less tightly bound by the anion, and thus more amenable to accommodating the water solvent structure. While the first hydration shell still disrupts the water structure, surprisingly the solvent partially recovers its tetrahedral order. When compared to results based on classical nuclei, the PI-AIMD simulation shows that the influence of Cl<sup>-</sup> on the water structure, beyond the first shell, is much weaker and, importantly, the solvent Hbond network is seemingly rapidly restored to its bulklike behavior. The PI-AIMD result shows excellent agreement with the experiments by Soper [11, 12]. In particular, the satellite peak of the H-Cl-H angular distribution derived from neutron scattering data only appears in the PI-AIMD simulations, and is absent in conventional AIMD. Thus, NQEs give important corrections to the computed  $Cl^{-}(aq)$  hydration structure, yielding more consistent results when compared to experiments. The present findings strongly suggest that NQEs should be included in future studies of the Hofmeister series.

All AIMD and PI-AIMD calculations were performed in the canonical ensemble at T=300K using a periodically replicated cubic box with edge length 12.42 Å. One  $Cl^-$  ion and 63 H<sub>2</sub>O molecules were included in the 0.87 M Cl<sup>-</sup> aqueous solution. AIMD and PI-AIMD pure water simulations with 64 water molecules were performed. Maximally localized Wannier Function (MLWF) [40, 41] centers were computed to study electronic properties. Supplemental Materials provide more details [42].

As already mentioned, a water molecule in the first hydration shell of  $Cl^-$  is subjected to competing forces provided by A-W and W-W H-bonds. Thus, one proton in the water molecule points towards  $Cl^-$ , while the other points to lone pair electrons of solvent water, as



FIG. 2. Spatial distributions of proton transfer coordinate  $\nu$  for water molecules in Cl<sup>-</sup>(aq) within (a) the solvent (b) anions first hydration shell from AIMD and PI-AIMD.

illustrated in the inset of Fig. 1 [42]. Furthermore, this hydration shell water molecule is polarized by this special H-bonding configuration. Under its polarizing effect, the electropositive proton and the electronegative bonding pairs are separated further apart from each other generating a larger electric dipole in the condensed phase than that in water vapor [43, 44]. However, the abilities to polarize water are different for these two types of H-bonds as determined by the electronic structural properties. The A-W H-bond has a weaker bonding strength than that of W-W, as evidenced by the shorter distance between the bonding electron pairs and the proton in Fig. 1 [45]. The relative weaker A-W bond also reduces the electric dipole of water molecules in the first hydration shell by  $\sim 3\%$  compared to that in bulk water; an effect which has been reported [46, 47].

Besides its impact on the electronic structure, Hbonding also affects the proton position [32]. The above effect is explored via the proton transfer coordinate  $(\nu)$ [34, 35]. The resulting distribution functions,  $P_{OH\cdots O}(\nu)$ and  $P_{OH...Cl}(\nu)$  are shown in Fig. 2(a) and (b) for water molecules in the bulk solvent as well as in the first hydration shell of Cl<sup>-</sup>, respectively. In general, two distinct features can be identified in  $P(\nu)$ . The feature at more negative  $\nu$  (around -2.2 Å in P<sub>OH··O</sub>( $\nu$ ) and -2.7 Å in  $P_{OH..Cl}(\nu)$  is contributed by the non-bonded hydrogen. Whereas, the other feature (around -0.8 Å in P<sub>OH··O</sub>( $\nu$ ) and -1.2 Å in  $P_{OH\cdots Cl}(\nu)$ , denoted as  $P_{OH\cdots O}^{B}(\nu)$  and  $P^{B}_{OH..Cl}(\nu)$ ) originates from the bonded hydrogen atoms via the W-W or the A-W H-bonds in Fig. 2(a) and (b), respectively. The shorter distance in the bonded peaks is attributed to the fact that protons are more likely to approach the acceptors, i.e. an enhanced tendency of proton transfer [34, 45], under the attractive H-bond force. As expected, peak positions of  $\mathbf{P}^{\mathrm{B}}_{\mathrm{OH} \cdots \mathrm{O}}(\nu)$  and  $\mathbf{P}^{\mathrm{B}}_{\mathrm{OH} \cdots \mathrm{Cl}}(\nu)$ 

AIMD 3 Expr. g<sub>clo</sub>(r) 2 1 (c) (a) AIMD PI-AIMD θ AIMD PI-AIMD 3 P<sub>HCIH</sub>(0)sin(0) PI-AIMD Expr. g<sub>clo</sub>(r) Expr. 1 (b) (d) 0 L 2.5 3.0 3.5 4.0 4.5 5.0 5.5 6.0 0 45 90 135 180  $\theta$ (Degree) r (Å)

FIG. 3. Cl-O RDFs in  $Cl^{-}(aq)$  from (a) AIMD and (b) PI-AIMD simulations, with neutron diffraction result [12]. (c) Isosurface of probability of finding a  $Cl^{-}$  ion first neighbor of a water molecule in AIMD and PI-AIMD simulations. The contrast level of the isosurface is set to 0.70. (d) Probability distribution of H-Cl-H angles in the first hydration shell of  $Cl^{-}$  from AIMD, PI-AIMD simulation, and neutron diffraction experiment [12]. The inset shows polarized  $Cl^{-}$  hydration structures, where water molecules in the first hydration shell are classified by bonded (orange) and non-bonded (yellow) to  $Cl^{-}$ .

are the equilibrium positions of protons determined by the average strength of H-bonds under thermal fluctuations. The different peak positions of  $P^B_{OH..O}(\nu)$  and  $P^B_{OH..Cl}(\nu)$  are mainly caused by the size difference between Cl<sup>-</sup> anion and oxygen atom [48].

Both types of H-bonds undergo notable changes when protons are treated with NQEs in PI-AIMD simulations. On the one hand, the zero-point motion significantly expands the region that protons are able to explore on the potential energy surface, which is inaccessible to classical nuclei. Therefore, both  $P_{OH\cdots O}(\nu)$  and  $P_{OH\cdots Cl}(\nu)$  show a broader distribution in PI-AIMD trajectories. On the other hand, centers of  $P^{B}_{OH\dots O}(\nu)$  and  $P^{B}_{OH\dots Cl}(\nu)$  move further away from its acceptors, which suggests that both H-bonds are weakened in PI-AIMD. The fact that Hbonding is weakened by NQEs has been recognized recently in pure water [49, 50], which yields an important refinement to theoretical descriptions of water structure. More importantly, H-bonding strength varies among different types of H-bonds. The protons are more delocalized by NQEs. However, while delocalization of the proton along the stretching direction facilitates H-bond formation, delocalization due to proton libration tends to weaken the H-bond. The result represents a delicate balance of the aforementioned opposing NQEs. A rule of thumb proposed by Michaelides et al. states that the relatively weak H-bond will become even weaker by NQEs and vice versa [36]. Indeed, a close inspection reveals that the peak position of  $P^B_{OH\dots O}(\nu)$  has a much larger shift moving away from acceptors than that of

 $\mathbf{P}^{\mathrm{B}}_{\mathrm{OH}\cdots\mathrm{Cl}}(\nu).$  Importantly, this means that the A-W H-bond becomes even weaker than the W-W H-bond under NQEs.

Figure. 3(a) and (b), present the Cl-O radial distribution functions (RDFs)  $q_{ClO}(r)$  from the Cl<sup>-</sup>(aq) trajectories for both AIMD and PI-AIMD. For comparison, the experimental  $g_{\rm ClO}(\mathbf{r})$  derived from neutron scattering is shown. Clearly, the Cl-O interaction is overly structured in the AIMD simulation, Fig. 3(a). The artificially strengthened Cl-O attraction with classical nuclei brings the first (at 3.14 Å) and second hydration shells (at 4.91 Å) closer to the anion, relative to the experimental peaks, at 3.16 Å and 5.09 Å [42]. Moreover, the first minimum and second maximum are more prominent than those in experiment. In contrast, the more weakened A-W Hbond due to NQEs should loosen the anions hydration shell. Indeed, the Cl-O interaction is weakened in the PI-AIMD simulation, as shown in Fig. 3(b). Consistently, the center position of both first (at 3.16 Å) and second hydration shells (at 5.00 Å) increases and yields better agreements with the experiment. At the same time, the overall  $q_{ClO}(\mathbf{r})$  from PI-AIMD becomes much less structured, which then shows quantitative agreement with the experiment.

Because  $Cl^-$  is polarized in solution, bonded water molecules tend to preferentially populate one side of the anion while leaving the other half-space relatively empty, with sporadic residence of non-bonded molecules [42]. To accept a H-bond,  $Cl^-$  is located close to a proton along the bonding direction. The AIMD trajectory shows  $Cl^-$ 



FIG. 4. (a) Normalized tetrahedral structure order parameter  $\bar{Q}$  decay as a function of the distance to Cl<sup>-</sup> from AIMD and PI-AIMD. For water molecule i,  $Q_i = \frac{3}{32} \sum_{j=1}^{3} \sum_{k=j+1}^{4} (\cos\psi_{j,k} + \frac{1}{3})^2$ , where j and k are the jth and kth nearest neighbor of water molecule i, and  $\psi_{j,k}$  is the angle between molecule i, j and i, k.  $\bar{Q}$  defined by  $\langle Q_i \rangle_{\text{solution}} / \langle Q_i \rangle_{\text{water}}$ , is the averaged and normalized Q. (b) AIMD and PI-AIMD O-O RDFs within the first Cl<sup>-</sup> hydration shell computed by water bonded to Cl<sup>-</sup>, along with regular O-O RDFs of bulk water. And O-O RDFs of (c) AIMD and (d) PI-AIMD Cl<sup>-</sup>(aq) simulations, with AIMD and PI-AIMD pure water simulations, and diffraction experiment [51].

distributes within a narrow region with a double domelike shape in Fig. 3(c). The overall solvation cage, composed of both bonded and non-bonded water molecules in the first hydration shell, can be described by a polyhedron with ~7 vertices, as illustrated in the inset of Fig. 3(d). Consistent with the polyhedral geometry under thermal fluctuations, the H-Cl-H triple angular distribution  $P_{\rm HClH}(\theta)$  as plotted in Fig. 3(d) is centered at ~70° in AIMD, which is in qualitative agreement with experiment. However, a second broader peak that appears clearly in experiment around 130° is absent in the AIMD simulation.

In PI-AIMD, the solvation cage changes its geometry accordingly as a result of NQEs. Due to the weakened A-W H-bond, the average distance between the chloride ion and its bonded water molecules slightly increases from 3.235 A to 3.249 A. And the *dome-like* distribution of Cl<sup>-</sup> spreads out over a larger area due to quantum fluctuations, as shown in Fig. 3(c). Again, because of the weaker A-W bonding, Cl<sup>-</sup> can no longer bond as many water molecules as it does in the AIMD trajectory. As a consequence, the population of non-bonded water molecules largely increases by  $\sim 50\%$  from  $\sim 1.6$  in AIMD to  $\sim 2.4$ in PI-AIMD [42]. The increased number of non-bonded water in the first hydration shell can be further confirmed by the significantly increased distribution of Cl<sup>-</sup> in the region around the oxygen. With more vertices occupied by non-bonded water molecules, the solvation cage predicted by PI-AIMD has geometric characteristics different from that of AIMD. Because the bonded and nonbonded water molecules are located on opposite sides of Cl<sup>-</sup>, the triplet angular distribution  $P_{HCIH}(\theta)$  that involves a non-bonded water molecule mostly contributes to an obtuse angle as demonstrated in the insert of Fig. 3(d). As a result, the second broad peak in  $P_{HCIH}(\theta)$ centered around 130° emerges in the PI-AIMD simulation, as seen in Fig. 3(d); a finding which is in excellent agreement with experiment.

The presence of Cl<sup>-</sup> disrupts the H-bond network, and distortions are expected around the solvated ion. Fig. 4(a) presents the normalized tetrahedral structure order parameter,  $\bar{Q}$  [52] of water solvent in different hydration shells, as computed from both AIMD and PI-AIMD trajectories. Noting that  $\bar{Q}$  shows the anions disruptive effect on the tetrahedral structure of pure water [42]. Not surprisingly, the most abrupt distortion takes place in the first hydration shell because the solvation cage polyhedron is intrinsically different from a tetrahedron. Consistently, the first peak of  $g_{OO}^{1st}(\mathbf{r})$ , the O-O RDF computed by only water molecules in the first hydration shell, is also drastically different from bulk water as shown in Fig. 4(b). Away from the solvated anion, the degree of distortion on H-bond network decays, and the tetrahedral water structure gradually recovers to its bulk value in the second hydration shell and beyond as shown in Fig. 4(a). In AIMD, the remaining distortion is non-negligible for solvent structure in the second and third hydration shells. As a result, the overall  $q_{00}(\mathbf{r})$ 

of AIMD is softened as compared to that in bulk water modeled by AIMD. This effect has been attributed to a long-range structural disturbance on the underlying H-bond network by  $Cl^{-}$  [25, 28].

Interestingly, the inclusion of NQEs in PI-AIMD lessens the impact of anion on the underlying H-bond network. A water molecule in  $Cl^{-}(aq)$  is attracted by two competing forces from the Cl<sup>-</sup> anion and the solvent water. The aforementioned more weakened A-W H-bond makes it easier for water molecules to attract each other and restore the tetrahedral liquid structure. Indeed, the facilitated water structure can already be seen in the first hydration shell [42]. As shown in Fig. 4(b), the H-bond network is still largely disrupted in the first coordination shell. However, it becomes more structured; this can be seen by the decreased distance of the first peak, as well as the appearance of a second peak around 4.5 Å, which coincides with the peak position of the second hydration shell of  $g_{OO}(\mathbf{r})$  in bulk water. Clearly, this indicates a partial recovery of the solvent water structure. By the same token, the normalized structural order parameter Q recovers more quickly its bulk value in the PI-AIMD simulation in Fig. 4(a). The resulting overall  $g_{OO}(\mathbf{r})$  of the solvent in PI-AIMD is also very close to that in bulk water in Fig. 4(d). The relatively small impact on the water structure caused by Cl<sup>-</sup>, as modeled by including NQEs, agrees well with the conclusions based on analysis of neutron scattering data [12] and terahertz absorption spectroscopy [53]. Notably, inclusion of NQEs not only gives a more accurate description of  $Cl^{-}(aq)$  but also play an essential role in describing the bulk water structure more accurately. The computed  $g_{OO}(\mathbf{r})$  via PI-AIMD greatly helps to improve the agreement between theory and experiment.

In conclusion, NQEs have a surprisingly large influence on the hydration structure of  $Cl^{-}(aq)$ . Specifically, the interaction between water and  $Cl^{-}$  is weakened, so that the anions disruptive effect on the solvent H-bond network of solvent water is reduced. The predicted hydration properties computed via PI-AIMD agree well with experiments. In particular, the emergence of the satellite peak in the H-Cl-H triangular distribution function in the PI-AIMD trajectory is a clear signature of NQEs. The present results highlight the important role played by NQEs in ionic solutions involving the Hofmeister series. Complementary studies of NQEs on hydration of cations, such as  $Na^+(aq)$  and  $K^+(aq)$ , should be interesting. Unlike Cl<sup>-</sup>, these cations are not H-bonded to water in solution, and only the underlying water solvent will be affected by NQEs. Therefore, distinct corrections by NQEs are expected.

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