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# Mitigating Amorphization in Superhard Boron Carbide by Microalloying Induced Stacking Faults Formation

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## Abstract

The abnormal brittle failure of superhard boron carbide ( $B_4C$ ) and other icosahedral solids arises from the shear-induced amorphization. Mitigating the amorphization in these materials remains challenging due to the lack of other deformation mechanisms such as mobile dislocations. The present study illustrates the shear induced amorphization process of  $B_4C$  from the molecular dynamics (MD) simulations using quantum mechanics derived machine-learning force field. The amorphization in  $B_4C$  initiates from the disintegration of icosahedral clusters and then this icosahedral deconstruction propagates and merges to form an amorphous region with 2~3 nm in width, leading to the following cavitation and brittle failure. More interesting, the deformation mechanism transforms from amorphization to stacking faults (SF) formation by microalloying aluminum (Al) into  $B_4C$ . This SF formation originates from the enhanced icosahedral slip as the Al is incorporated into the C-B-C chain to form C-Al-C chain. The present study illustrates a new deformation mechanism of superhard icosahedral solids and provides a new strategy for suppressing the amorphization and brittle failure of  $B_4C$ .

**Keywords:** Machine learning,  $B_4C$ , Amorphization, Microalloying, Stacking faults

## 1. Introduction

Boron carbide ( $B_4C$ ) is extremely hard with a high Hugoniot elastic limit, yet it has a low density of  $\sim 2.5 \text{ g/cm}^3$  due to the unique crystal structure consisting of  $B_{12}$ -based icosahedral motifs and three-atoms chain [1,2]. The outstanding physical properties make  $B_4C$  a promising material for personal body armor and other protection applications [3-5]. However,  $B_4C$  suffers from abnormal brittle failure just exceeding the elastic limit, preventing it from extensive engineering applications [6]. This brittle failure is directly related to the amorphous shear band formation (2~3 nm in width and several hundred nm in length), which is observed in many mechanical experiments such as hypervelocity impact [7], nanoindentation [8], shock compression [9], scratching [10], as well as ion irradiation [11]. Recent theoretical studies significantly advance the understanding of the deformation mechanism and the amorphous band formation in  $B_4C$  [12-16]. The density functional theory (DFT) simulations on the shear deformation of  $B_4C$  along 11 plausible slip systems indicated that the shear-induced failure process initiates from the deconstruction of icosahedral clusters due to the interaction of cage and C-B-C chain [12]. In the following studies, we applied reactive force field (ReaxFF) molecular dynamics (MD) simulations to demonstrate that the formation of the amorphous band arises from the deconstruction of icosahedral clusters under shear deformation [13]. The amorphous region has a higher density than the nearby crystalline region, leading to negative pressure and cavitation within the amorphous region [13]. Despite extensive experimental and theoretical studies, the amorphization process in  $B_4C$  remains not fully understood, especially the detailed propagation of amorphization along the shear band. Illustrating the amorphization process in  $B_4C$  provides an important basis for design hard yet ductile materials in the future.

The amorphization is directly related to the cavitation and brittle failure of  $B_4C$  and other icosahedral solids [12,17]. Therefore, mitigating this phase transition is essential to enhance their ductility. In order to mitigate the amorphization in  $B_4C$ , many strategies are proposed in recent studies [18] including dopant [19], B/C stoichiometry control [20], second phase addition [21], and grain boundary (GB) engineering [22]. Experimentally, Xiang *et. al.* demonstrated that doping 1~2% Si into  $B_4C$  decreases the amorphization by up to ~30% while it increases the fragmentation and microcracking [19]. Another effective approach is to increase the B/C ratio resulting in higher strength and decreased amorphization [20]. Furthermore, less fracture is observed by adding the reinforcement particles, such as SiC, TiC,  $TiB_2$ , and  $Al_2O_3$ , into  $B_4C$  [23-25]. In addition, we showed that GB sliding can improve the ductility of nanocrystalline  $B_4C$  by performing ReaxFF MD simulations on supercells of millions of atoms [22]. Besides the above approaches, an interesting strategy is proposed based on the shear-induced failure process investigated from DFT simulations [12]. The deconstruction of the icosahedral cluster initiates from the active interaction between middle B in the C-B-C chain and the icosahedral cluster under shear deformation [12]. Therefore, we suggested that replacing the 3-atom chain with a 2-atom chain can facilitate the icosahedral slip in  $B_4C$  without breaking the icosahedral cage. This modification is demonstrated to be effective using DFT simulations on  $(B_{12}P_2)$  [26] and  $(B_{11}C)Si_2$  [27]. However, it has not been demonstrated for realistic systems because of the limitation size of DFT simulations (~100 atoms) as well as the lack of temperature effects in DFT simulations.

In the present study, an accurate machine learning force field (ML-FF) is developed for both  $B_4C$  and Al-doped  $B_4C$  systems based on extensive quantum mechanics (QM) simulations. Then the amorphization and brittle failure mechanism of  $B_4C$  are illustrated from the MD simulations

using this ML-FF. The simulation results indicate that the shear-induced amorphization in  $B_4C$  arises from deconstructing icosahedra along a shear plane, yet it is confined to two icosahedral layers in the beginning. Then the amorphization propagates to two opposite directions and transforms to other neighbor icosahedral layers. Next, the propagation of amorphization along parallel icosahedral layers merges to form an amorphous region with 2~3 nm in width. Finally, a cavity is present in this region, leading to brittle failure. More important, a realistic design strategy is proposed to mitigate the amorphization and demonstrated by the ML-FF MD simulations. Substituting the C-B-C chain with the C-Al-C chain transforms the deformation mechanism from amorphization to stacking faults (SF) formation due to the enhanced icosahedral slip without disintegrating the icosahedral clusters. The present results indicate that microalloying Al is effective to activate the alternative deformation mechanism other than amorphization in  $B_4C$  and other icosahedral solids. The activation of SF formation mechanism is expected to drastically enhance the ductility of  $B_4C$ .

## **2. Computational Methods**

### **2.1 Quantum mechanics simulations**

The quantum mechanics molecular dynamics (QM-MD) simulations were performed to generate the training set for developing the ML-FF. The atomic force, the energy, and the virial stress tensor for the simulation systems were derived from the QM-MD trajectory. All QM-MD simulations were performed using VASP software based on the plane wave basis-set [28-31]. In the QM-MD simulations, the cell parameters are allowed to relax to adjust the external pressure using the isobaric-isothermic (NPT) ensemble. The temperature and pressure are controlled using the Langevin thermostat [32], and the Parrinello-Rahman barostate [33], respectively. The canonical (NVT) ensemble was adopted for the fixed volume simulations with just the Langevin

thermostat. A timestep of 1.0 fs was applied in integrating the equations of motion in all QM-MD simulations.

The forces on each atom were calculated using the DFT. The Perdew-Burke-Ernzerhof (PBE) functional was adopted to account for the exchange-correlation interaction [34,35]. In QM-MD simulations, the energy cutoff for plane wave expansion, and the energy convergence for the self-consistent field were set up to 400 eV and  $1.0 \times 10^{-4}$  eV, respectively. The sampling of the first Brillouin zone was performed using the Gamma-point only approach. To account for the partial occupancy of electrons, the Gaussian smearing method was adopted, and the width for the smearing is 0.05 eV.

## **2.2 The development of machine learning force field**

In order to develop an accurate force field for describing both B<sub>4</sub>C and Al-doped B<sub>4</sub>C ((B<sub>12</sub>)CAIC), a large training set is generated from QM-MD simulations. Particularly, the training set includes following structures: (1) The boron carbide (B<sub>4</sub>C); (2) the (B<sub>12</sub>)CAIC; and (3) elementary boron phases such as  $\alpha$ -B<sub>12</sub> [36],  $\beta$ -B<sub>106</sub> [37],  $\beta$ -B<sub>105</sub> [37],  $\tau$ -B<sub>212</sub> [38], and  $\gamma$ -B<sub>28</sub> [39].

Extensive QM-MD data are included for the most stable configuration (B<sub>11</sub>C<sub>p</sub>)CBC. These QM data includes (1) the heating process of crystalline phase from 300 K to 4300 K within 40 ps, leading to the liquid phase; (2) The continuous quenching process of the liquid phase from 4300 K to 300 K within 40 ps, leading to the formation of amorphous phase; (3) the equation of state for both crystalline phase and amorphous phase at 300 K; equilibrium lattice parameters are compressed to 0.98, 0.96, 0.94 and 0.92, as well as are increased to 1.02 and 1.05, and then the system is equilibrated for 10 ps using NVT; (4) The crystalline phase at 300 K, 500 K, 1000 K,

1500 K, 2000 K, 2500 K, 3000 K, and 3500 K for 10 ps; (5) The liquid (or amorphous) phase at 300 K, 500 K, 1000 K, 1500 K, 2000 K, 2500 K, 3000K, 3500 K, 4000 K and 4300 K for 10 ps; and (6) The shear deformation configuration along (001)[100] slip system at 300 K for 10 ps. For the high energy configurations ( $B_{12}$ )CCC and ( $B_{11}C_e$ )CBC, the training set includes the crystal at room temperature for 10 ps, as well as the heating process from 300 K to 4300 K in 40 ps. To account for the possible twinning formation in a shear deformation, the  $\tau$ - $B_4C$  structure [40] is also included in the training set. For the asymmetric twin structure, the modified  $\tau$ - $B_4C$  with half ( $B_{11}C_p$ )CBC and half ( $B_{11}C_e$ )CBC is included. The boron-rich boron carbide ( $B_{13}C_2$ ) is also included. For the  $\tau$ - $B_4C$ , modified  $\tau$ - $B_4C$ ,  $B_{13}C_2$  and elementary boron phases ( $\alpha$ - $B_{12}$ ,  $\beta$ - $B_{106}$ ,  $\beta$ - $B_{105}$ ,  $\tau$ - $B_{212}$ ,  $\gamma$ - $B_{28}$ ), the QM-MD simulations are (1) crystal phase at 300 K for 10 ps; (2) heating from 300 K to 4300 K for 40 ps; and (3) quenching from 4300 K to 300 K for 40 ps. For the ( $B_{12}$ )CAIC, The training set includes the same QM-MD simulations as the ( $B_{11}C_p$ )CBC, which provides a good training set for an accurate description of this Al-doped  $B_4C$ .

In the ML-FF training process, a cut-off radius for neighbor searching is set up to 5.2 Å and the smoothing beginning with 5.0 Å. The size of the three layers of neural networks is all 120 in the fitting process. The learning rate varies from 0.001 to  $3.51 \times 10^{-8}$  with an exponential decay in the total of 1,000,000 training steps. The loss function is composed of energy error, force error, and virial error, and the evolution of the loss function is shown in FIG. S1 of Supplementary Materials (SM) [41].

### 2.3 Molecule dynamics simulations using ML-FF.

The MD simulations were performed using LAMMPS software [42] with the ML-FF applied to describe the interatomic interactions. The velocity Verlet algorithm is used for integrating the equations of motion with a timestep of 1.0 fs in all MD simulations. The possible surface effects

are eliminated by periodic boundary conditions (PBC) along with three directions. The NPT ensemble was applied in all simulations with the Noose-Nover thermostat and barostat for controlling the temperature and pressure, respectively. The damping constants are 0.2 ps and 2.0 ps for thermostat and barostat, respectively.

The bulk modulus and shear modulus were computed using the Voigt-Reuss-Hill average from the elastic constants  $C_{ij}$  and stiffness constants  $S_{ij}$  [43]. The lattice of the supercell is deformed elastically along possible directions to derive the elastic constant  $C_{ij}$  [44]. The inversion of the  $C_{ij}$  matrix is the  $S_{ij}$ . A  $4 \times 4 \times 4$  rhombohedral supercell with 960 atoms was used for the elastic modulus calculations for both  $(B_{11}C_p)CBC$  and  $(B_{12})CAIC$ .

For the finite shear simulations, a larger  $24 \times 24 \times 6$  supercell with 51840 atoms was used for both  $(B_{11}C_p)CBC$  and  $(B_{12})CAIC$ . The systems were equilibrated at 300 K for 100 ps before shear simulation. The temperature and atomic stress were calculated for each atom in the simulation cell during the shear simulation. The stress tensor was computed using the virial theorem as shown in Eqn. (1) where  $m$ ,  $v$ ,  $r$ , and  $f$  correspond to atomic mass, velocity, position and force, respectively [45]. Then, these physical properties were coarse-grained using  $\sim 1$  nm  $\times$  1 nm bins ( $\sim 300$  atoms) in the x-y plane to illustrate the temperature, pressure, and shear stress evolution during the amorphization. The binning analysis is along lattice “a” and “b” so that the results are rectangular meshed.

$$\sigma_{xy} = \frac{1}{V} [\sum_j m_j v_{jx} v_{jy} + \frac{1}{2} \sum_{i \neq j} r_{ijx} f_{ijy}] \quad \text{Eqn (1)}$$

### 3. Results and Discussion

#### 3.1 The validation of the ML-FF



To demonstrate the accuracy of the ML-FF, the structural and mechanical properties of B<sub>4</sub>C were computed and compared to DFT and experimental results. The ML-FF predicts the lattice parameters of  $a = 5.212 \text{ \AA}$ ,  $b = 5.069 \text{ \AA}$ ,  $c = 5.221 \text{ \AA}$ ,  $\alpha = 66.02^\circ$ ,  $\beta = 65.23^\circ$ , and  $\gamma = 65.97^\circ$  for B<sub>4</sub>C, agreeing well with the DFT values of at 0 K [12]. For (B<sub>12</sub>)CAIC, the lattice parameters are  $a=5.355 \text{ \AA}$ ,  $b=5.344 \text{ \AA}$ ,  $c=5.289 \text{ \AA}$ ,  $\alpha=64.17^\circ$ ,  $\beta=64.19^\circ$ , and  $\gamma=63.67^\circ$  from ML-FF at room temperature, which also agree well with DFT values at 0 K ( $a=b=5.347 \text{ \AA}$ ,  $c=5.261 \text{ \AA}$ ,  $\alpha=\beta=64.28^\circ, \gamma=63.56^\circ$ ). The ML-FF predicts a density of  $2.51 \text{ g/cm}^3$  for B<sub>4</sub>C at room temperature, which agrees very well with experiment ( $2.52 \text{ g/cm}^3$ ) [2] and DFT value ( $2.53 \text{ g/cm}^3$  at 0 K) [12]. In addition, the bulk modulus (K) and shear modulus (G) are predicted to be 241 GPa and 191 GPa for B<sub>4</sub>C, well consistent with experiment (K=235 GPa and G=197 GPa) and DFT values (K=238 GPa and G=199 GPa) [12]. The summary of lattice parameters and elastic constant is in Table 1 below.

**Table 1.** Lattice parameters and elastic modulus of (B<sub>11</sub>C<sub>p</sub>)CBC and (B<sub>12</sub>)CAIC from DFT and ML-FF simulations.

	(B <sub>11</sub> C <sub>p</sub> )CBC		(B <sub>12</sub> )CAIC	
	Lattice parameters	Elastic modulus	Lattice parameters	Elastic modulus
DFT (0K)	$a = 5.207 \text{ \AA}$ , $b = 5.057 \text{ \AA}$ , $c = 5.207 \text{ \AA}$ , $\alpha = 66.01^\circ$ , $\beta = 65.16^\circ$ , $\gamma = 66.01^\circ$	K=238 GPa, G=199 GPa	$a=b=5.347 \text{ \AA}$ , $c=5.261 \text{ \AA}$ , $\alpha=\beta=64.28^\circ, \gamma=63.56^\circ$	K=225 GPa, G=197 GPa
ML-FF (300K)	$a = 5.212 \text{ \AA}$ , $b = 5.069 \text{ \AA}$ , $c = 5.221 \text{ \AA}$ , $\alpha = 66.02^\circ$ , $\beta = 65.23^\circ$ , $\gamma = 65.97^\circ$	K=241 GPa, G=191 GPa	$a=5.355 \text{ \AA}$ , $b=5.344 \text{ \AA}$ , $c=5.289 \text{ \AA}$ , $\alpha=64.17^\circ$ , $\beta=64.19^\circ, \gamma=63.67^\circ$	K=233 GPa, G=181 GPa

### 3.2 Amorphization of B<sub>4</sub>C under shear deformation

The crystalline  $B_4C$  consists of icosahedral clusters connected by the three-atoms chains along  $[111]$  rhombohedral direction (FIG. 1(a)). The ground-state structure has  $(B_{11}C_p)$  icosahedra which are bonded to the C-B-C chain through equatorial (e) sites and are linked to other icosahedra via polar (p) sites [12]. The present study focuses on the finite shear deformation of the ground state structure  $(B_{11}C_p)CBC$  along the slip system  $(001)[100]$  (The 3-index rhombohedral notation is used to represent the slip plane and direction in this work). This slip system is selected because it is the most plausible slip system in  $B_4C$  from our DFT simulations on 11 plausible slip systems [12]. Therefore, it is the most plausible to be activated under applied stress conditions, leading to the amorphization. Indeed, the amorphization along this slip system was observed directly from nanoindentation and high-resolution transmission electron microscopy (HRTEM) experiments [8].

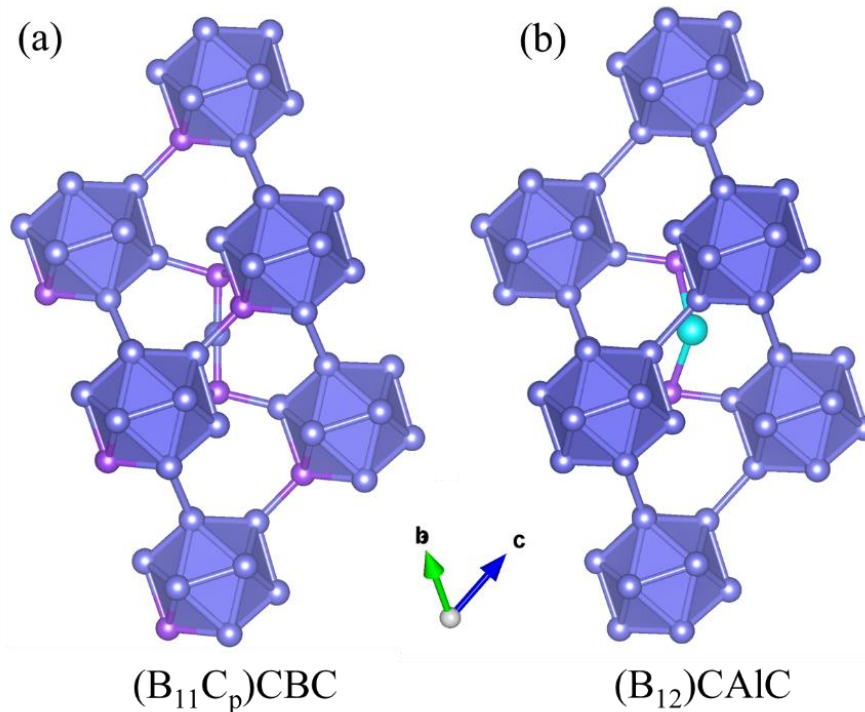


FIG 1. The atomistic structure of  $B_4C$  and Al-doped  $B_4C$ . (a) The ground state structure  $(B_{11}C_p)CBC$ , (b) the lowest energy structure  $(B_{12})CAIC$ . The B, C, and Al are represented by light blue, purple, and cyan balls, respectively.

The experimentally observed amorphous shear bands in B<sub>4</sub>C are roughly 2~3 nm in width and several hundred nm in length. Simulating the formation of amorphous band formation requires a supercell with cell length ~10 nm perpendicular to the amorphous band, which is beyond the capacity of QM simulations. The intriguing bonding character in B<sub>4</sub>C and other icosahedral solids makes it challenging to develop a classical force field for them. To describe the atomistic interaction in both B<sub>4</sub>C and Al-doped B<sub>4</sub>C systems, the ML-FF is developed based on the atomic force, system energy, and virial stress obtained from extensive QM-MD simulations. The ML-FF represents the potential energy surface of atomistic systems as a sum of “atomic” that depend on the coordinates of the atoms in a symmetry-preserving way [46, 47].

In order to illustrate the shear-induced amorphization process in B<sub>4</sub>C, a supercell was constructed with the dimensions of 12.5 nm × 12.2 nm × 3.1 nm along [100], [001], and [010] lattice directions. The system was first equilibrated at room temperature for 100 ps. Then the [100] is aligned along x-direction and [001] is in the xy plane. Finally, finite shear deformation is applied in the xy plane to mimic the shear deformation along the slip system (001)[100]. The strain rate is  $5.0 \times 10^8 \text{ s}^{-1}$  that is comparable to the shock compression [9]. The initial structure for shear deformation is illustrated in FIG. S2(a) of SM [41]. During the shear deformation, the stresses along the other five directions are relaxed using the NPT ensemble to mimic the ideal shear deformation. The stress component of other five directions fluctuate around zero during the shear deformation, as shown in FIG. S3 of SM [41].

FIG. 2 displays the shear-stress-shear-strain relationship of B<sub>4</sub>C along the most plausible slip system (001)[100] (black curve). The crystalline B<sub>4</sub>C deforms elastically to ~0.15 shear strain. Then the slope of the stress-strain curve slightly decreases yet the structure does not exhibit significant change. As the shear strain increases to ~0.2, the shear stress drops abruptly from the

critical stress of  $\sim 32$  GPa to  $\sim 0$ , indicating a brittle failure in  $B_4C$ . The failed structure at 0.25 shear strain, displayed in FIG. 2, shows an amorphous shear band along the (001) shear plane, which resembles the experimental TEM observation [8]. This confirms that the amorphous shear band is the major failure mechanism of  $B_4C$  [7-16]. It is worth noting that the formed amorphous shear band in the present study is not uniformly distributed along the shear plane, as seen in FIG. 2. Some regions have only two amorphous icosahedral layers while others cross four layers. A cavity is present in the 4-layers amorphous region, suggesting a close relationship between amorphization and brittle failure. The ideal shear stress for  $B_4C$  is 32 GPa from the simulations, which is close to the critical shear stress of popping up dislocations in single crystal  $B_4C$  measured from experiments [48]. This indicates that the direct amorphization in  $B_4C$  along the slip system (001)[100] is a competitive deformation mechanism to the dislocation mediated amorphization along other slip systems [48].

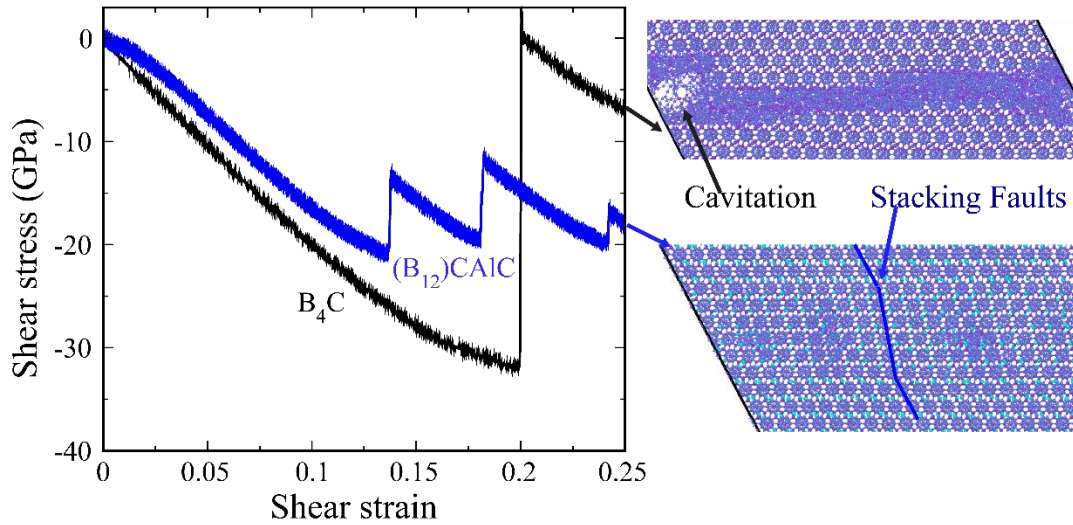


FIG. 2. Shear-stress-shear-strain curves for  $B_4C$  and  $(B_{12})CAIC$  at finite shear deformation and the atomistic structures at 0.25 shear strain. The solid blue line represents the SF layers. Only the local structures related to amorphization and SF formation are displayed here, and the detailed structure evolutions for  $B_4C$  and  $(B_{12})CAIC$  are illustrated in Fig. 3 and Fig. 4, respectively.

In order to illustrate the amorphization and failure mechanism of  $B_4C$ , the detailed analyses on the MD trajectory were performed from 0.199 to 0.2015 shear strain. FIG. 3(a) displays the stress-strain relationship in this strain interval. The strain at 0.199 strain does not show obvious bond breaking, as shown in FIG. 3(b). As the shear strain increases to 0.19945, the icosahedral-icosahedral B-C bonds break among a few icosahedra in two adjacent layers (FIG. 3(c)), yet this does not cause a significant drop of shear stress. The initial icosahedral-icosahedral B-C bond breaking is consistent with our previous DFT simulations [12], demonstrating the accuracy of this ML-FF. Then the icosahedra start to collapse and the amorphization propagates along opposite directions in the two adjacent layers at 0.1996 shear strain (FIG. 3(d)). Next, the propagation of amorphization in the upper layer stops after deconstructing a couple of icosahedra and transforms to the above icosahedral layer. Similarly, the amorphization in the lower layer extends to the below icosahedral layer without further deconstructing icosahedra in the initial layer. This leads to the presence of disintegrated icosahedra in four layers, as shown in FIG. 3(e). This propagation of amorphization only leads to a small drop of shear stress to  $\sim 25$  GPa. Due to the periodic boundary condition in the MD supercell, the upper amorphous layers meet the lower amorphous layers at 0.200 strain, causing the deconstruction of icosahedral in all four layers (FIG. 3(f)). This makes the shear stress drop to  $\sim 15$  GPa. Finally, a cavity forms in the 4-layer amorphous region at 0.2005 strain (FIG. 3(g)), relaxing the shear stress quickly to  $\sim 0$  GPa. The structure remains unchanged up to 0.2015 shear strain, as shown in FIG. 3(h). The movie showing the detailed amorphization and failure process can be found in SM [41].

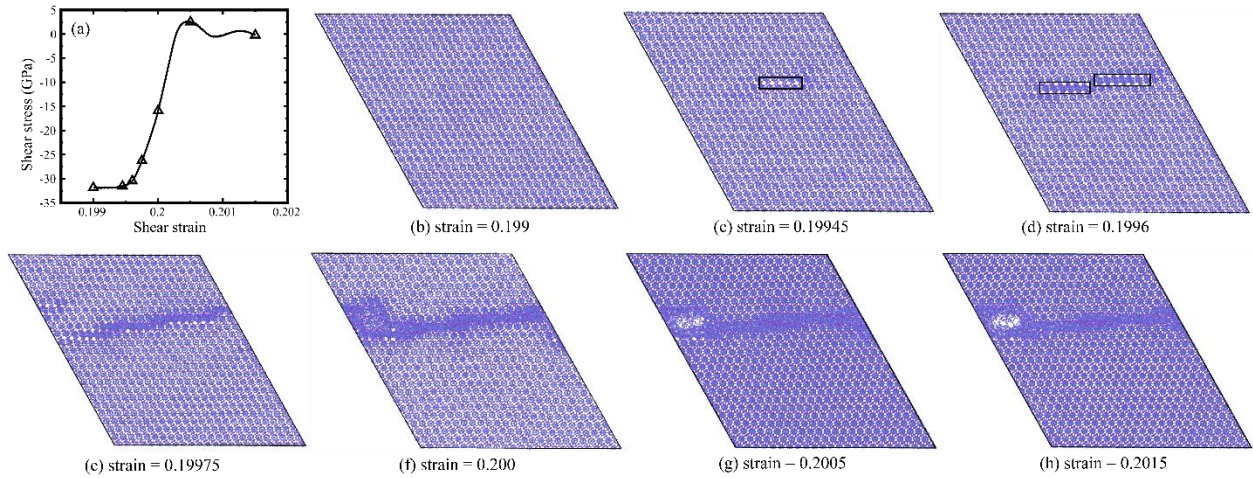


FIG 3. The amorphization and failure mechanism of  $B_4C$  from 0.199 to 0.2015 shear strain. (a) The shear-stress-shear-strain relationship and the following examined structures labeled with triangle symbols. (b) The structure at 0.199 strain without obvious bond breaking. (c) The initial bond breaking at 0.19945 strain displayed in the rectangular region. (d) The structure at 0.1996 strain showing the propagation of amorphization along opposite directions in the rectangular region. (e) The structure at 0.19975 strain displaying the amorphization transforms to other icosahedral layers. (f) The structure at 0.2 strain showing the formation of an amorphous region across 4 icosahedral layers. (g) Cavitation formation in the amorphous region at 0.2005 strain. (h) The amorphous band at 0.2015 strain similar to (g).

To investigate the temperature, pressure, and shear stress evolution during the amorphization, a binning analysis was performed, and the results are displayed in FIGs.S4-S6 of SM [41]. FIG. S4(a) shows that the temperature does not significantly increase as the initial deconstruction of icosahedra. As the amorphization propagates across the whole simulation cell, the temperature significantly increases to  $\sim 2200$  K, as shown in FIG. S4(b) of SM [41]. Then the temperature drops along the amorphous region since the temperature is controlled by a thermostat (FIG. S4(c)). It is worth noting that the melting temperature of  $B_4C$  is  $\sim 2700$  K [1], which is higher than the increased temperature in the present study. This suggests that the failure process in the present work is the mechanical stress induced amorphization. However, the increased temperature during the amorphization softens the bonding in  $B_4C$ , may promote cavitation and failure in the amorphous region. The shear stress profile, displayed in FIG. S5 of SM [41],

indicates that the amorphization causes the relaxation of shear stress. In addition, the pressure in the amorphous region increases in the amorphous region (FIG. S6 of SM [41]), which is consistent with the fact that the amorphous has a higher density than the crystalline region.

### 3.3 Shear deformation of Al-doped B<sub>4</sub>C

A recent experimental study suggested that 1~5 at. % Al can be incorporated into boron carbide through arc-melting, leading to a similar crystal structure as B<sub>4</sub>C and lattice expansion [49]. But the structure of the Al-doped BC system is not well characterized, in contrast to extensive studies on B<sub>4</sub>C. Several possible structures are examined in the present work based on previous studies [50,51]: (B<sub>12</sub>)CAIC, (B<sub>12</sub>)CAIB, and (B<sub>11</sub>C)CAIC. The DFT simulations indicated that (B<sub>12</sub>)CAIC is the most plausible structure with the heat of formation of 1.28 eV taking fcc Al,  $\alpha$ -B<sub>12</sub>, and graphite crystal as the reference structures. For comparison, the (B<sub>12</sub>)CAIB and (B<sub>11</sub>C)CAIC structures have a smaller heat of formation of 0.82 and 0.24 eV, respectively. Therefore, the (B<sub>12</sub>)CAIC structure (FIG. 1(b)) is selected for the finite shear deformation along the same slip system as B<sub>4</sub>C. It is worth noting the B/C ratio in (B<sub>12</sub>)CAIC is 6.0 which is higher than 4.0 in B<sub>4</sub>C, which is consistent with the experimental observation that Al can only be incorporated into B<sub>4</sub>C with the addition of B [49]. The (B<sub>12</sub>)CAIC is relaxed at room temperature and then is sheared along the same slip system (001)[100], as displayed in FIG. S2(b) of SM [41].

The deformation mechanism for (B<sub>12</sub>)CAIC is drastically in contrast with B<sub>4</sub>C. In contrast to B<sub>4</sub>C, the shear-stress-shear-strain relationship of (B<sub>12</sub>)CAIC (blue curve in FIG. 2) exhibits a different behavior – the shear stress only drops from critical stress of ~20 GPa to ~13 GPa while it continuously increases to ~20 GPa with the same stress-strain slope as the perfect crystal. This suggests that (B<sub>12</sub>)CAIC does not lose the shear strength at finite shear deformation. Up to 0.25

strain, the shear stress drops and increases three times, but no amorphous shear band is present in  $(B_{12})CAIC$  at 0.25 shear strain (FIG. 2). Instead, a stacking faults layer is present across 6 icosahedral layers, suggesting that the relaxation of the shear stress is accomplished through stacking faults formation in  $(B_{12})CAIC$ , quite distinct from the amorphization in  $B_4C$ .

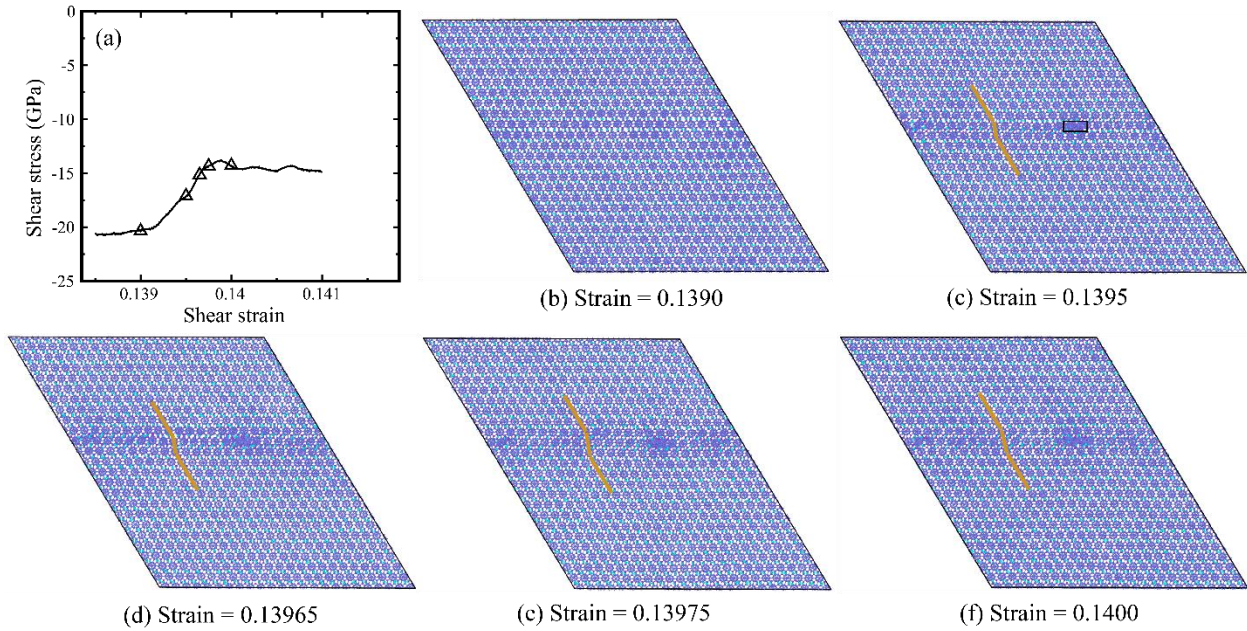


FIG. 4. The formation of stacking faults in  $(B_{12})CAIC$  from 0.1385 to 0.141 shear strain. (a) The shear-stress-shear-strain relationship and the examined structures are labeled with the triangle. (b) The structure at 0.139 strain without obvious bond breaking. (c) The initiation of the icosahedral slip at 0.1395 strain with two adjacent icosahedra deconstructed in the rectangular region. (d) The structure at 0.13965 strain showing one additional icosahedral layer slips. (e) The structure at 0.13975 strain displaying the formation of 3-layers SF structure. (f) The SF structure remains stable at 0.1400 strain. The solid yellow lines represent the SF structures.

FIG. 4 illustrates the detailed deformation process of forming SF in the shear strain ranging from 0.1385 to 0.141. The shear-stress-shear-strain relationship, displayed in FIG. 4(a), shows the shear stress relaxation from  $\sim 21$  to  $\sim 14$  GPa in this process. The structure at 0.139 shear strain is elastically deformed from the perfect crystal without bond breaking, as shown in FIG. 4(b). When the shear strain increases to 0.1395, one icosahedral layer slips relative to its adjacent layers (FIG. 4(c)), releasing the shear stress from  $\sim 21$  GPa to  $\sim 17.5$  GPa. Since the C-Al-C chain



is weaker than the bonding in  $(B_{12})$  icosahedron, the icosahedral slip is observed in  $(B_{12})CAIC$  system rather than the disintegration of icosahedra. Two adjacent icosahedra along the slip layer are deconstructed while the cage collapse is confined to this very local region. Then, an additional icosahedral layer above the SF layer starts to slip, forming a 3-layer SF structure FIG. 4(d,e), relaxing the shear stress to  $\sim 14$  GPa. Finally, the SF structure remains stable with the increased shear strain (FIG. 4(f)). More SF layers form with the further increased strain, leading to a total of six SF layers at 0.25 shear strain (FIG. 2). The detailed process of SF formation can be found in the movie of SM [41].

The SF formation due to the icosahedral slip under high strain rate deformation has significant implication on materials design to improve the ductility of superhard  $B_4C$  [18]. The icosahedral slip is facilitated in  $(B_{12})CAIC$  system because of the relative weak C-Al chain compared to the cage bonding. The modification of chain structure changes the deformation mechanism from amorphization in  $B_4C$  to SF formation in  $(B_{12})CAIC$ . It is expected that the ductility of  $B_4C$  will be significantly improved through Al doping that is achievable experimentally [49]. The present study suggests that future materials design can focus on increasing the icosahedral slip to improve the ductility of boron carbide and related icosahedral solids.

The present study focuses on the amorphization process of  $B_4C$  under ideal shear deformation, as well as the suppression of local amorphization by Al dopant. The deformation mechanism under more complex situation will be explored in the future, practically under shock compression.

#### **4. Conclusion**

In summary, the present study illustrates the amorphization and failure process of  $B_4C$  under finite shear deformation from the ML-FF MD simulations. The amorphous band initiates from

the deconstruction of icosahedra in two adjacent layers and then it propagates to other neighbor layers, leading to the formation of a 4-layer amorphous band. Finally, a cavity is present in the amorphous band, releasing the shear strength and leading to brittle failure. In contrast, the (B<sub>12</sub>)CAIC system exhibits a different deformation mechanism in which the icosahedral slip causes the formation of SF, releasing the shear strength without deconstructing the icosahedral clusters. This newly identified deformation mechanism in (B<sub>12</sub>)CAIC suggests that adding Al into B<sub>4</sub>C can significantly improve the ductility.

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### **References**

- [1] V. Domnich, S. Reynaud, R. A. Haber, and M. Chhowalla, Boron Carbide: Structure, Properties, and Stability under Stress, *J. Am. Ceram. Soc.* **94**, 3605 (2011).
- [2] F. Thevenot, Boron Carbide — A Comprehensive Review, *J. Eur. Ceram. Soc.* **6**, 205 (1990).
- [3] J. L. Hoard and R. E. Hughes, in *The Chemistry of Boron and Its Compounds* edited by E. L. Muetterties (Wiley, New York, 1967).
- [4] A. K. Suri, C. Subramanian, J. K. Sonber, and T. S. R. Ch. Murthy, Synthesis and Consolidation of Boron Carbide: A Review, *Int. Mater. Rev.* **55**, 4 (2010).

- [5] J. Deng, Erosion Wear of Boron Carbide Ceramic Nozzles by Abrasive Air-Jets, *Mater. Sci. Eng. A* **408**, 227 (2005).
- [6] D. E. Grady, Hugoniot Equation of State and Dynamic Strength of Boron Carbide, *J. Appl. Phys.* **117**, 165904 (2015).
- [7] M. W. Chen, J. W. McCauley, and K. J. Hemker, Shock-Induced Localized Amorphization in Boron Carbide, *Science* **299**, 1563 (2003).
- [8] K. M. Reddy, P. Liu, A. Hirata, T. Fujita, and M. W. Chen, Atomic Structure of Amorphous Shear Bands in Boron Carbide, *Nat. Commun.* **4**, 2483 (2013).
- [9] S. T. Zhao, B. Kada, B. A. Remington, J. C. LaSalviac, C. E. Wehrenberg, K. D. Behler, and M. A. Meyers, Directional Amorphization of Boron Carbide Subjected to Laser Shock Compression, *Proc. Natl. Acad. Sci. U.S.A.* **113**, 12088 (2016).
- [10] M. W. Chen and J. W. McCauley, Mechanical Scratching Induced Phase Transitions and Reactions of Boron Carbide, *J. Appl. Phys.* **100**, 123517 (2006).
- [11] D. Gosset, S. Miro, S. Doriot, G. Victor, and V. Motte, Evidence of Amorphisation of B<sub>4</sub>C Boron Carbide under Slow, Heavy Ion Irradiation, *Nucl. Instrum. Methods Phys. Res., Sect. B* **365**, 300 (2015).
- [12] Q. An and W. A. Goddard III, Atomistic Explanation of Shear-Induced Amorphous Band Formation in Boron Carbide, *Phys. Rev. Lett.* **113**, 095501 (2014).
- [13] Q. An and W. A. Goddard III, Atomistic Origin of Brittle Failure of Boron Carbide from Large-Scale Reactive Dynamics Simulations: Suggestions toward Improved Ductility, *Phys. Rev. Lett.* **115**, 105501 (2015).

- [14] G. Fanchini, J. W. McCauley, and M. Chhowalla, Behavior of Disordered Boron Carbide under Stress, *Phys. Rev. Lett.* **97**, 035502 (2006).
- [15] D. E. Taylor, J. W. McCauley, and T. W. Wright, The Effects of Stoichiometry on the Mechanical Properties of Icosahedral Boron Carbide under Loading, *J. Phys.: Condens. Matter* **24**, 505402 (2012).
- [16] J. Li, S. Xu, J. Zhang, and L. Liu, First-Principles Predicting Improved Ductility of Boron Carbide through Element Doping, *J. Phys. Chem. C* **125**, 11591 (2021).
- [17] Q. An, K. M. Reddy, J. Qian, K. J. Hemker, M. W. Chen, and W. A. Goddard III. Nucleation of Amorphous Shear Bands at Nanotwins in Boron Suboxide, *Nat. Commun.* **7**, 11001 (2016).
- [18] Y. Shen, J. Fuller, and Q. An, Mitigating the Formation of Amorphous Shear Band in Boron Carbide, *J. Appl. Phys.* **129**, 140902 (2021).
- [19] S. Xiang, L. Ma, B. Yang, Y. Dieudonne, G. M. Pharr, J. Lu, D. Yadav, C. Hwang, J. C. LaSalvia, R. A. Haber, K. J. Hemker, and K. Y. Xie, Tuning the Deformation Mechanisms of Boron Carbide via Silicon Doping, *Sci. Adv.* **5**, eaay0352 (2019).
- [20] A. Chauhan, M. C. Schaefer, R. A. Haber, and K. J. Hemker, Experimental Observations of Amorphization in Stoichiometric and Boron-Rich Boron Carbide, *Acta. Mater.* **181**, 207 (2019).
- [21] K. Y. Xie, K. Kuwelkar, R. A. Haber, J. C. LaSalvia, K. J. Hemker, and R. Hay, Microstructural Characterization of a Commercial Hot-Pressed Boron Carbide Armor Plate, *J. Am. Ceram. Soc.* **99**, 2834 (2016)
- [22] D. Guo, S. Song, R. Luo, W. A. Goddard, M. Chen, K. M. Reddy, and Q. An, Grain Boundary Sliding and Amorphization are Responsible for the Reverse Hall-Petch

- Relation in Superhard Nanocrystalline Boron Carbide, *Phys. Rev. Lett.* **121**, 145504 (2018).
- [23] Y. Gu, J. X. Liu, F. Xu, and G. J. Zhang, Pressureless Sintering of Titanium Carbide Doped with Boron or Boron Carbide, *J. Eur. Ceram. Soc.* **37**, 539 (2017).
- [24] L. Yang, G. Min, H. Yu, J. Han, and Y. B. Paderno, Densification and Mechanical Properties of  $\text{CaB}_6$  with Nickel as a Sintering Aid, *Ceram. Int.* **31**, 271 (2005).
- [25] L. S. Sigl, Processing and Mechanical Properties of Boron Carbide Sintered with TiC, *J. Eur. Ceram. Soc.* **18**, 1521 (1998).
- [26] Q. An and W. A. Goddard III, Ductility in Crystalline Boron Subphosphide ( $\text{B}_{12}\text{P}_2$ ) for Large Strain Indentation, *J. Phys. Chem. C* **121**, 16644 (2017).
- [27] Q. An and W. A. Goddard III, Microalloying Boron Carbide with Silicon to Achieve Dramatically Improved Ductility, *J. Phys. Chem. Lett.* **5**, 4169 (2014).
- [28] G. Kresse and J. Hafner, *Ab Initio* Molecular Dynamics for Liquid Metals, *Phys. Rev. B* **47**, 558 (1993).
- [29] G. Kresse and J. Furthmüller, Efficiency of *Ab Initio* Total Energy Calculations for Metals and Semiconductors Using a Plane-Wave Basis Set, *Comput. Mater. Sci.* **6**, 15 (1996).
- [30] G. Kresse and J. Furthmüller, Efficient Iterative Schemes for *Ab Initio* Total-Energy Calculations Using a Plane-Wave Basis Set, *Phys. Rev. B* **54**, 11169 (1996).
- [31] G. Kresse and D. Joubert, From Ultrasoft Pseudopotentials to the Projector Augmented-Wave Method, *Phys. Rev. B* **59**, 1758 (1999).
- [32] W. G. Hoover, A. J. C. Ladd, and B. Moran, High-Strain-Rate Plastic Flow Studied via Nonequilibrium Molecular Dynamics, *Phys. Rev. Lett.* **48**, 1818 (1982)

- [33] M. Parrinello and A. Rahman, Crystal Structure and Pair Potentials: A Molecular-Dynamics Study, *Phys. Rev. Lett.* **45**, 1196 (1980).
- [34] J. P. Perdew, K. Burke, and M. Ernzerhof, Generalized Gradient Approximation Made Simple, *Phys. Rev. Lett.* **77**, 3865 (1996).
- [35] J. P. Perdew, K. Burke, and M. Ernzerhof, Erratum: Generalized Gradient Approximation Made Simple, *Phys. Rev. Lett.* **78**, 1396 (1997).
- [36] A. R. Oganov and V. L. Solozhenko, Boron: A hunt for Superhard Polymorphs, *J. Superhard Mater.* **31**, 285 (2009).
- [37] R. E. Hughes, C. H. L. Kennard, D. B. Sullenger, H. A. Weakliem, D. Sands, and J. L. Hoard, The Structure of  $\beta$ -Rhombohedral Boron, *J. Am. Chem. Soc.* **85**, 361 (1963).
- [38] Q. An, K. M. Reddy, K. Y. Xie, K. J. Hemker, and W. A. Goddard III, New Ground-State Crystal Structure of Elemental Boron, *Phys. Rev. Lett.* **117**, 085501 (2016).
- [39] A. R. Oganov, J. Chen, C. Gatti, Y. Ma, Y. Ma, C. W. Glass, Z. Liu, T. Yu, O. O. Kurakevych, and V. L. Solozhenko, Ionic High-Pressure Form of Elemental Boron, *Nature (London)* **457**, 863 (2009).
- [40] Q. An, Prediction of Superstrong  $\tau$ -Boron Carbide Phase from Quantum Mechanics, *Phys. Rev. B* **95**, 100101 (2017).
- [41] See Supplemental Material at [URL will be inserted by publisher] for Figure S1-S6 and two movies displaying the amorphization in  $B_4C$  (0.199~0.201 shear strain) and stacking faults formation in  $(B_{12})CAIC$  (0.139~0.140 shear strain), respectively.
- [42] S. Plimpton, Fast Parallel Algorithms for Short-Range Molecular Dynamics, *J. Comp. Phys.* **117**, 1 (1995).

- [43] R. Hill, The Elastic Behaviour of a Crystalline Aggregate, Proc. Phys. Soc., London, Sect. A **65**, 349 (1952).
- [44] Y. Le Page and P. Saxe, Symmetry-General Least-Squares Extraction of Elastic Data for Strained Materials from *Ab Initio* Calculations of Stress, Phys. Rev. B **65**, 104104 (2002).
- [45] D. C. Rapaport, *The Art of Molecular Dynamics Simulation* (Cambridge University Press 1995)
- [46] L. Zhang, J. Han, H. Wang, R. Car, and E. Weinan, Deep Potential Molecular Dynamics: A Scalable Model with the Accuracy of Quantum Mechanics, Phys. Rev. Lett. **120**, 143001 (2018).
- [47] J. Han, L. Zhang, R. Car, and E. Weinan, Deep Potential: A General Representation of a Many-Body Potential Energy Surface, Commun. Comput. Phys. **23**, 629 (2018).
- [48] K. M. Reddy, D. Guo, S. Song, C. Cheng, J. Han, X. Wang, Q. An, and M.-W. Chen, Dislocation-Mediated Shear Amorphization in Boron Carbide, Sci. Adv. **7**, eabc6714 (2021).
- [49] S. Xiang, Q. Yang, H.M. Lien, K. Shial, E. Grounske, R. Haber, and K.Y. Xie, The Effect of Boron and Aluminum Additions on the Microstructure of Arc-Melted Boron Carbide, J. Am. Ceram. Soc. **103**, 3453 (2020).
- [50] H. Neidhard, R. Mattes, and H. Becher, The Production and Structure of a Boron Carbide Containing Aluminum, Acta Crystallogr., Sect. B: Struct. Sci., Cryst. Eng. Mater., **26**, 315 (1970).
- [51] R. Schmechel, H. Werheit, K. Robberding, T. Lundström, and H. Bolmgren, IR Active Phonon Spectra of B–C–Al Compounds with Boron Carbide Structure, J. Solid State Chem. **133**, 254 (1997).