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Large cross-polarized Raman signal in CrI₃, first-principles study

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We find unusually large cross-polarized (and anti-symmetric) Raman signature of A_g phonon mode in CrI₃, in agreement with experiments. The signal is present only when the following three effects are considered in concert: ferromagnetism on Cr atoms, spin-orbit interaction, and resonant effects. Somewhat surprisingly, we find that the relevant spin-orbit interaction potential originates from iodine atoms, despite magnetism being mostly on chromium atoms. We analyze the Raman signature as a function of magnetic order, the direction of the magnetic moment, energy and polarization of light used for Raman scattering, as well as carrier lifetime. In addition to a strong cross-polarized Raman signal, we also find unusually strong phonon modulated magneto-optical Kerr effect (MOKE) in CrI₃.

I. INTRODUCTION

A two-dimensional magnet CrI₃ has attracted attention due to its potential applications in magneto-optoelectronic,^{1–3} spintronic devices,^{4–8} and data storage.⁹ Polarized Raman spectroscopy is a powerful and commonly used experimental tool to probe the magnetic^{10–20} and structural^{21–24} properties of CrI₃ as it is both non-invasive and extremely sensitive on the electronic and phononic structure of the material.

At low temperatures, below 210–220 K,²⁵ bulk CrI₃ crystallizes in the rhombohedral space group R $\bar{3}1'$. Point symmetries present in this phase are three-fold rotation axis, inversion symmetry, time-reversal symmetry (1'), and any combination of these symmetries taken together. Cr atoms are at Wyckoff 6c sites while I atoms are at Wyckoff 18f sites. The structure units are edge-shared CrI₆ octahedra. When the temperature is reduced further, below 68 K, the bulk CrI₃ orders ferromagnetically¹³ which breaks the time-reversal symmetry (1'). Therefore the symmetry of the system is reduced,

from R $\bar{3}1'$ to R $\bar{3}$.

In both cases, by symmetry, one expects four A_g Raman active modes in CrI₃,²⁶ however the corresponding Raman tensors are different in the magnetic and non-magnetic states. In particular, the symmetry of the non-magnetic state (R $\bar{3}1'$ symmetry) imposes that the Raman tensor has the form,²⁷

$$(\text{nonmagnetic}) \quad R\bar{3}1' \rightarrow \begin{pmatrix} a & 0 & 0 \\ 0 & a & 0 \\ 0 & 0 & c \end{pmatrix}_{A_g} \quad (1)$$

Therefore the A_g modes in the non-magnetic state of CrI₃ don't have cross-polarized I_{xy} Raman intensity, but have parallel-polarized I_{xx} intensity ($I_{xx} \sim |a|^2$). In other words, polarization of incoming and scattered light to CrI₃ is the same. However, in the ferromagnetic (FM) state of CrI₃ the symmetry dictates that the Raman ten-

sor has the following form,²⁷

$$(\text{ferromagnetic}) \quad R\bar{3} \rightarrow \begin{pmatrix} a & b & 0 \\ -b & a & 0 \\ 0 & 0 & c \end{pmatrix}_{A_g} \quad (2)$$

The presence of the anti-symmetric term b in the Raman tensor contributes to the Raman scattering intensity I_{xy} ($\sim |b|^2$) in the cross-polarized configuration, as shown in Ref. 28.

The form of Raman tensor from Eq. 2 is consistent with experiment. Furthermore, the dominant A_g mode shows an unusually high intensity in the cross-polarized (I_{xy}) configuration at 128 cm⁻¹. However, the measured intensity ratio

$$R = \frac{I_{xy}}{I_{xx}} \quad (3)$$

greatly varies from one experiment to the other. For example, in the case of CrI₃ monolayer in the FM state, Refs. 14, 15, 16 find that the intensity ratio R is 1.5, 0.5, and 0.65, respectively. While all three experiments use 633 nm laser, the temperatures are slightly different, 1.7 K, 9 K, and 15 K.

With more layers of CrI₃ the measured ratio R tends to decrease.¹⁴ For example, Ref. 21 (532 nm, 100 K) and Ref. 24 (room temperature) both report that in bulk CrI₃ the ratio R is about 0.14. Finally, both Ref. 17 (bulk, 633 nm, 300 K and 90 K) and Ref. 18 (2-4 layers and bulk, 633 nm, 10 K) find that $R \approx 0$.

One possible explanation for such a wide range of reported values of R is that R depends on the experimental conditions such as the energy of the incoming photons, quality of the sample, temperature relative to the FM phase transition, and so on. For example, the temperature in Refs. 17, 21, and 24 is above the Curie temperature (61 K), so we do not expect large R . Furthermore, Ref. 10 found a mixed state of layered anti-ferromagnetic state (AFM) on the surface and FM in the bulk. The presence of AFM state should reduce R to near zero, as in AFM state time-reversal followed by spatial inversion is a symmetry of the system, which is enough to enforce

$R = 0$. Given the uncertainties in the experimentally determined value of R , we set out to compute the Raman intensity of $128 \text{ cm}^{-1} \text{ A}_g$ mode from first-principles.

Our first-principles calculations find large cross-polarized Raman signature I_{xy} of A_g phonon mode in CrI_3 . The intensity of I_{xy} Raman signal is strongly dependent on the frequency of the incoming light. We find that the I_{xy} polarized Raman scattering is driven by ferromagnetism, spin-orbit interaction, and resonance effects. Moreover, the relevant spin-orbit interaction potential comes from iodine atoms, rather than the magnetic Cr atoms. This finding is consistent with earlier studies that also report importance of spin-orbit interaction on the nominally non-magnetic atom.^{29–33}

While in this work we focus on only one A_g mode, the one near 128 cm^{-1} , by symmetry one expects three other A_g modes in CrI_3 . However, two of the three modes (expected to be located at around 100 and 200 cm^{-1} respectively) are likely too weak to be detected experimentally.^{14,16,21} The remaining A_g mode has been measured at Raman shift of around 75 cm^{-1} . The measured ratio between I_{xy} and I_{xx} polarized intensities for this mode are 0.5,¹⁴ 0.3¹⁶ and 0.13²¹, respectively.

Finally, we note that non-zero I_{xy} Raman signature of A_g modes could also, in principle, originate from a hypothetical breaking of a three-fold rotation axis, and not necessarily from breaking of the time-reversal symmetry.³⁴ However, there are other characteristics of the Raman signal, not only the fact that I_{xy} is non-zero, that can help distinguish between a broken three-fold rotation axis and a broken time-reversal symmetry. These differences arise from the fact that the time-reversal symmetry induces anti-symmetric off-diagonal component of the Raman tensor b while breaking of the three-fold rotation axis induces symmetric off-diagonal components,

$$\begin{pmatrix} \cdot & b & \cdot \\ b & \cdot & \cdot \\ \cdot & \cdot & \cdot \end{pmatrix}_{\text{A}_g}. \quad (4)$$

(Only two matrix elements are shown for clarity.) The first qualitative difference between the anti-symmetric (Eq. 2) and the symmetric (Eq. 4) off-diagonal Raman tensor is that in the former the Raman intensity for left and right circularly polarized light are different from each other. The second difference comes from the fact that in the case of the time-reversal symmetry breaking b is induced by the magnetic moment M , so changing the sign of M will also change the sign of b . Therefore, for example, the ratio of left and right circularly polarized Raman intensity will be inverted if the direction of the magnetic moment is changed. Third, there are also other qualitative differences, even in the case of linearly polarized Raman signal where polarization angle between incoming and outgoing light is not exactly 90° . All three of these qualitative signatures of the time-reversal symmetry breaking were found experimentally.¹⁶

This paper is organized as follows: in Sec. II we describe our approach, in Sec. III we present our results,

analysis is done in Sec. IV, and we conclude in Sec. V.

II. APPROACH

Now we discuss our approach to compute the Raman intensity in CrI_3 . By symmetry the cross-polarized term b appearing in Eq. 2 is non-zero whenever ferromagnetic order is present. However, the symmetry alone can not tell us the magnitude of b . Formally, the Raman scattering intensity for light with incoming frequency ω_I is given by the derivative of the susceptibility tensor $\chi_{\alpha\beta}(\omega_I)$ with respect to atomic displacements u .³⁵ In particular, the intensity I_{xx} is given as,

$$I_{xx}(\omega_I) \sim |a(\omega_I)|^2 \omega_I^4 \sim \left| \frac{\partial \chi_{xx}(\omega_I)}{\partial u} \right|^2 \omega_I^4, \quad (5)$$

while for the cross-polarized intensity I_{xy} we have,

$$I_{xy}(\omega_I) \sim |b(\omega_I)|^2 \omega_I^4 \sim \left| \frac{\partial \chi_{xy}(\omega_I)}{\partial u} \right|^2 \omega_I^4. \quad (6)$$

In our approach we neglect the energy of a phonon, as it is small relative to other energy scales in the problem.

Three conditions need to be met simultaneously to arrive at non-zero b for CrI_3 , and thus non-zero cross-polarized intensity I_{xy} . First, as discussed earlier, CrI_3 must be in a state with broken time-reversal symmetry, such as ferromagnetic state. Second, one needs to consider spin-orbit interaction, as otherwise electronic wavefunctions are insensitive on the overall direction of the magnetic moment, and $\chi_{xy} = 0$ regardless of atomic displacements (u), so $\frac{\partial \chi_{xy}}{\partial u}$ must be 0 as well. Third, we need to consider Raman scattering in the non-resonant limit, where the frequency of light is non-zero ($\omega_I > 0$). As is known from the theory of the anomalous Hall effect, $\chi_{xy}(\omega_I = 0)$ is quantized for an insulator, so its derivative must vanish. Therefore in the limit of zero frequency of incoming light ($\omega_I \rightarrow 0$) coefficient b must vanish in any insulator.

Earlier first-principles calculations of CrI_3 did not take into account two of three effects listed here (spin-orbit interaction and resonance), which is why theoretical studies Ref. 19 and 20 report $b = 0$ and therefore $R = 0$. We report here the first calculations of the Raman tensor in CrI_3 that includes both the spin-orbit interaction and the resonance effects. We will discuss in more detail the role of each of the three conditions in Sec. IV.

A. Computational details

For density functional theory calculations we use the Quantum Espresso package.³⁶ We use the local density approximation (LDA) along with the optimized norm-conserving Vanderbilt (ONCV) pseudopotentials which include the spin-orbit effect.³⁷ These pseudopotentials

describe the valence electrons 3s3p3d4s in Cr and 5s5p in I. In order to obtain sufficient precision, we cutoff the plane wave basis for the wavefunction at 80 Ry, and sample the electron's Brillouin zone on a $5 \times 5 \times 5$ Monkhorst-Pack grid. Given this coarse k-grid we use Wannier interpolation to calculate the susceptibility tensor χ on a grid with $30 \times 30 \times 30$ points.³⁸ We use experimental crystal structure from Ref. 39 in our calculations. For the monolayer calculation, the thickness of the unit cell perpendicular to the monolayer is 20 Å. We computed magnetic moments by integrating magnetic moment density inside a sphere of radius 1.1 Å centered on an atom.

Bulk CrI₃ has significant excitonic effects, as computed in Ref. 3 from the Bethe-Salpeter equation approach (GW-BSE). The exciton absorption was calculated to start around 1.7 eV, while the bulk continuum starts above 2.0 eV. In the present work, we focus mostly on the Raman intensity ratio R , so we computed the susceptibility tensor $\chi_{\alpha\beta}(\omega_I)$ and its derivative from the approach that is less computationally demanding than the GW-BSE method. We used the Kubo formula⁴⁰ in the random phase approximation (RPA) using the density functional theory (DFT) computed eigenstates and eigenenergies,

$$\sigma_{\alpha\beta}(\omega_I) = \frac{ie^2\hbar}{VN_k} \sum_{\mathbf{k}} \sum_{nm} \frac{f_{m\mathbf{k}} - f_{n\mathbf{k}}}{\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}}} \frac{\langle \phi_{n\mathbf{k}} | v_\alpha | \phi_{m\mathbf{k}} \rangle \langle \phi_{m\mathbf{k}} | v_\beta | \phi_{n\mathbf{k}} \rangle}{\varepsilon_{m\mathbf{k}} - \varepsilon_{n\mathbf{k}} - \hbar\omega_I - i\delta/2}. \quad (7)$$

α and β denote Cartesian directions. V is the cell volume, N_k is the number of k-points, and $f_{n\mathbf{k}}$ is the Fermi-Dirac distribution function. ω_I is the optical frequency. We assume a constant lifetime of electronic states $1/\delta$ in the Kubo formula. Later we discuss our choice for parameter δ . Since DFT based RPA approach is not meant to give the correct band gap in the calculation, we applied a rigid shift to the computed spectrum to reproduce the gap onset as computed within GW-BSE. Therefore, we expect that onset of the Raman signature will be well reproduced in our calculation, but that there will be rearrangement of oscillator weight, especially in the reduced screening environment of a CrI₃ monolayer, that will not be present in our RPA approach. Therefore, while two-particle effects will redistribute some of the Raman signatures above the gap, we expect that the overall trends of the computed Raman intensities will be well reproduced, especially in bulk CrI₃.

To obtain the Raman intensity we first calculate the susceptibility tensor components $\chi_{xx}(\omega_I)$ and $\chi_{xy}(\omega_I)$ in the ground state, without any atomic displacements. Next, we displace atoms by a small finite amount and recalculate the susceptibility tensors. The calculated difference of the susceptibility tensors then gives us $\frac{\partial \chi(\omega_I)}{\partial u}$. We obtain the same numerical value of derivative if we displace atoms by either 0.01 Å or 0.02 Å. This finding confirms the linearity of $\Delta\chi$ on atom displacement.

III. RESULTS

In this study we focus on the A_g mode at frequency close to 128 cm⁻¹. While there are four A_g degrees of freedom contributing to the 128 cm⁻¹ mode, the dominant motion is coming from the movement of iodine atoms along the 3-fold rhombohedral axis (z -axis).^{14,21} Nevertheless, we also computed for completeness Raman signal of remaining three types of motions within the A_g manifold. One of these modes contributes to the displacement of Cr atoms along the $\pm z$ axis while the other two consist of in-plane (x - y) displacement of I atoms. We measured the relative importance of all four A_g degrees of freedom by computing,

$$\frac{1}{\omega_2 - \omega_1} \int_{\omega_1}^{\omega_2} \left| \frac{\partial \chi_{xy}(\omega_I)}{\partial u} \right| d\omega_I \quad (8)$$

for each mode. The average here is performed over the optical region (between 1.0 and 2.5 eV) to eliminate oscillations of $\frac{\partial \chi_{xy}(\omega_I)}{\partial u}$ in frequency. The computed average is 11 Å⁻¹ for the dominant A_g mode corresponding to the displacement of I atoms along $\pm z$ axis. The average for displacement of Cr atoms along the $\pm z$ axis is only 1.2 Å⁻¹, while averages for displacements of I atoms in the x - y plane are even smaller (0.4 Å⁻¹ and 0.3 Å⁻¹). Since the 128 cm⁻¹ is dominated by the movement of I atoms along the z -axis, and that the Raman intensity is proportional to the square of $|\frac{\partial \chi_{xy}}{\partial u}|$, we are justified in focusing only on the $\pm z$ displacement of iodine atoms in our analysis.

A. Bulk FM CrI₃

First we discuss the calculated Raman intensities I_{xx} and I_{xy} of the 128 cm⁻¹ mode in bulk CrI₃, as shown in Fig. 1. Raw data used to obtain these intensities are provided in the supplement. The DFT computed bulk bandgap is 0.79 eV, and the horizontal axis is rigidly shifted by 0.71 eV so that it matches the GW-BSE calculated optical band gap of 1.5 eV.³ While the value of electron lifetime is not known in CrI₃ we used in this calculation a conservative value of $\delta = 0.1$ eV, same as that in graphite.^{41,42} We note that in the experiment this value might depend on the sample preparation. Later in Sec. IIID we show that for an even larger δ the calculated ratio R has nearly the same shape, but is overall smoother as a function of ω_I .

Our main results for bulk CrI₃ are shown in Figs. 1 and 2. We find that the intensity ratio R varies greatly with the incoming laser energy. When the energy of the incoming photon is below the band gap (1.5 eV) the ratio R is close to 0.01. At energies close to the band gap the ratio R increases. For example, when the incident photon energy is 1.8 eV, R is about 0.5. At somewhat larger incoming photon energy of 1.92 eV ratio R is about 7.

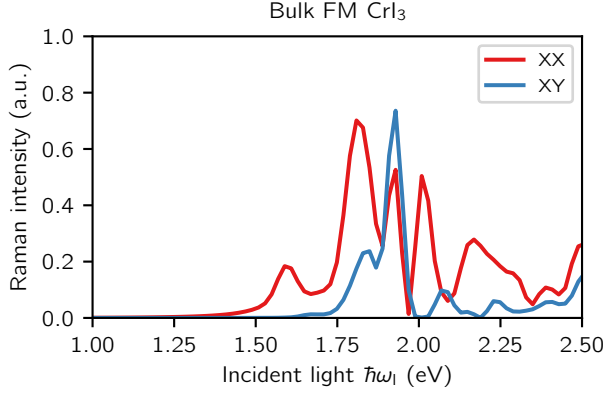


FIG. 1. The calculated Raman intensity of A_g mode in bulk ferromagnetic CrI_3 . The photon energy on the horizontal axis is shifted to reproduce the GW-BSE calculated optical bandgap onset.

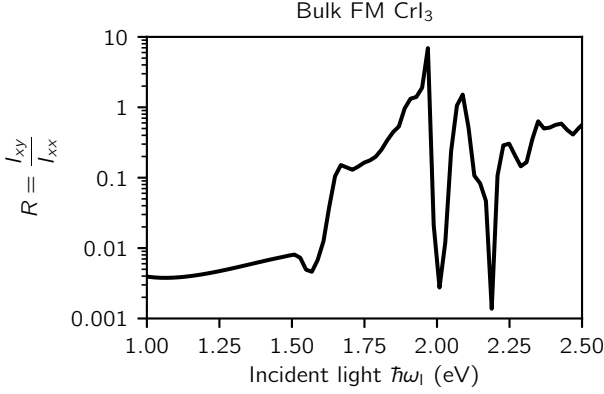


FIG. 2. The calculated ratio R of mode A_g in bulk ferromagnetic CrI_3 . (R is the ratio of blue and red curve from Fig. 1.)

At even higher incoming photon energies, above 2.1 eV, the ratio R fluctuates a lot and is on average around 0.5.

B. Monolayer FM CrI_3

Next, we discuss the calculated Raman intensities I_{xx} and I_{xy} of the 128 cm^{-1} mode in monolayer CrI_3 . The DFT computed monolayer bandgap is 0.82 eV, and the horizontal axis is shifted by 0.50 eV so that it matches the GW-BSE calculated monolayer optical band gap of 1.32 eV.³ From Fig. 3 we find, below the optical bandgap 1.32 eV, the intensities I_{xx} and I_{xy} are again small and their relative ratio is somewhat larger than in the bulk.

The main difference between monolayer and bulk occurs near the bandgap. In the monolayer both I_{xx} and I_{xy} start to increase at about 0.2 eV above the bandgap,

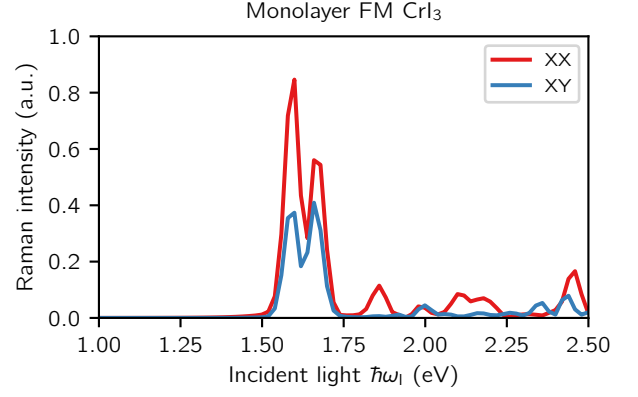


FIG. 3. The calculated Raman intensity of A_g mode in monolayer ferromagnetic CrI_3 . The photon energy on the horizontal axis is shifted to reproduce the GW-BSE calculated optical bandgap onset. The vertical scale here can't be compared with the bulk calculation from Fig. 1 due to the reduced dimensionality of the monolayer as compared to bulk.

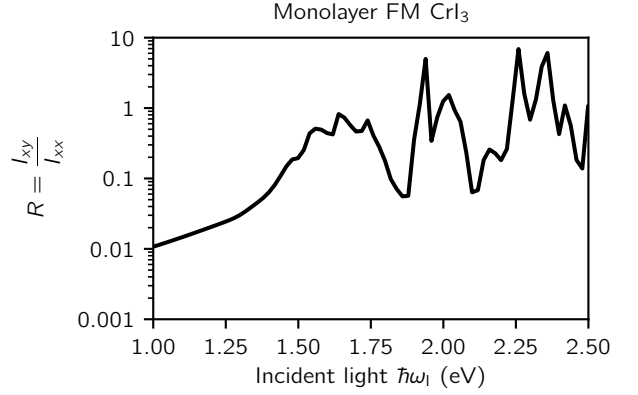


FIG. 4. The calculated ratio R of mode A_g in monolayer ferromagnetic CrI_3 . (R is the ratio of blue and red curve from Fig. 3.)

while in the bulk I_{xx} starts to increase already at the bandgap edge. The different behavior of I_{xx} in the bulk and monolayer can be explained by the band structure. Based on our band structure calculation, we find in the monolayer, both the valence band maximum (VBM) and conduction band minimum (CBM) are located at the Γ point, while in the bulk, the VBM is at the Γ point and CBM is at the T point.⁴² More importantly, the minimum direct bandgap in bulk is at the T point, rather than at the Γ point, as in the monolayer. Clearly, matrix elements for transitions at these two points are different, which leads to different Raman signatures. The transitions near the Γ point activate mostly I_{xx} while the ones near the T point activate both I_{xx} and I_{xy} .

C. Circularly polarized Raman

Now we switch to the Raman intensity of mode A_g with circularly polarized incident light. The Raman tensor from Eq. 2 gives rise to the following Raman intensities for circularly polarized light,

$$I^{\sigma^+\sigma^+} \sim |a + ib|^2, \quad (9)$$

$$I^{\sigma^-\sigma^-} \sim |a - ib|^2, \quad (10)$$

$$I^{\sigma^+\sigma^-} = I^{\sigma^-\sigma^+} = 0. \quad (11)$$

Here σ^+ (σ^-) denote the left-handed (right-handed) circularly polarized incoming and outgoing light. Presence of an anti-symmetric b term in Eq. 2 therefore implies that intensities $I^{\sigma^+\sigma^+}$ and $I^{\sigma^-\sigma^-}$ are different from each other as long as $b \neq 0$. Furthermore, regardless of value of b intensities $I^{\sigma^+\sigma^-}$ and $I^{\sigma^-\sigma^+}$ remain zero. (In contrast, a symmetric off-diagonal Raman tensor, as would be induced by a hypothetical breaking of a 3-fold axis (as in Eq. 4), one would have $I^{\sigma^+\sigma^+} = I^{\sigma^-\sigma^-} \sim |a|^2$, independent of b . Furthermore, a symmetric off-diagonal component as in Eq. 4 would also imply that $I^{\sigma^+\sigma^-} = I^{\sigma^-\sigma^+} \sim |b|^2$.)

The calculated circularly polarized Raman intensity of bulk is shown in Fig. 5. We find when the magnetic moment is along the $+z$ direction, the Raman intensity is dominated by $\sigma^+\sigma^+$ signal. For example, $I^{\sigma^+\sigma^+}$ is more than 8 times larger than $I^{\sigma^-\sigma^-}$ when the incident light energy is between 1.65 and 1.95 eV. While when the magnetic moment flips from $+z$ direction to $-z$ direction, we confirmed that the Raman intensity is then dominated by $\sigma^-\sigma^-$ signal, as one would expect. A similar experimental result is obtained in Ref. 16: when the magnetization is along the $+z$ direction, $I^{\sigma^+\sigma^+}$ is 3.8 times larger than $I^{\sigma^-\sigma^-}$ at the 128 cm^{-1} A_g mode. By flipping the magnetization from $+z$ direction to $-z$ direction, the dominant Raman scattering changes from $\sigma^+\sigma^+$ to $\sigma^-\sigma^-$ signal.

Furthermore, we computed for completeness the circularly polarized Raman intensity of monolayer, as shown in Fig. 6. The main difference with respect to the bulk occurs near the band gap edge, which we again contribute to the different nature of optical transitions at Γ and T points.

D. Electron lifetime

Now we investigate the effect of electron lifetime on the Raman intensity. The Raman intensity ratio R with shorter electron lifetimes ($\delta=0.16 \text{ eV}$) is shown in Fig. 7. Comparing with Fig. 2 we find that a shorter electron lifetime doesn't change the overall ratio R , but that it only dampens oscillations of R with the energy of light ω_I . Therefore, the effect of increased δ is the overall reduction in both I_{xx} and I_{xy} , so that R is not changed much.

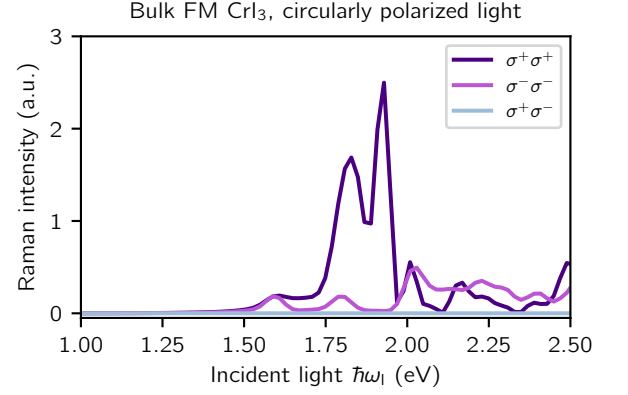


FIG. 5. The calculated circularly polarized Raman intensity of A_g mode in bulk ferromagnetic CrI_3 . The photon energy on the horizontal axis is shifted to reproduce the GW-BSE calculated optical bandgap onset.

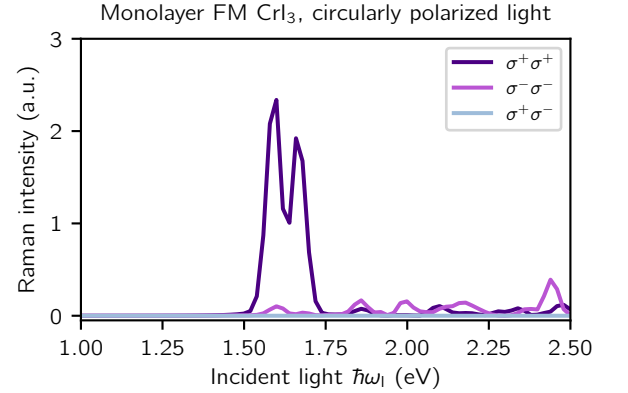


FIG. 6. The calculated circularly polarized Raman intensity of A_g mode in monolayer ferromagnetic CrI_3 . The photon energy on the horizontal axis is shifted to reproduce the GW-BSE calculated optical bandgap onset. The vertical scale here can't be compared with the bulk calculation from Fig. 5 due to the reduced dimensionality of the monolayer as compared to bulk.

E. Magnetic moment

Now we analyze the Raman signature I_{xy} of all four A_g modes from the point of view of the magnetic moment. In the limit of a weak spin-orbit coupling, the susceptibility χ_{xy} is linearly proportional to the atomic magnetic moment m on Cr. Therefore, one might expect that the derivative of the susceptibility $\frac{\partial \chi(\omega_I)}{\partial u}$ will also be proportional to the derivative of the magnetic moment, $|\frac{\partial m}{\partial u}|$. Therefore, atomic displacements that change the magnetic moment more should also give rise to a larger off-diagonal Raman intensity. To check this assumption, we computed $\frac{\partial m}{\partial u}$ for all four A_g modes. First, we calculate the magnetic moment of a single Cr atom in the ground

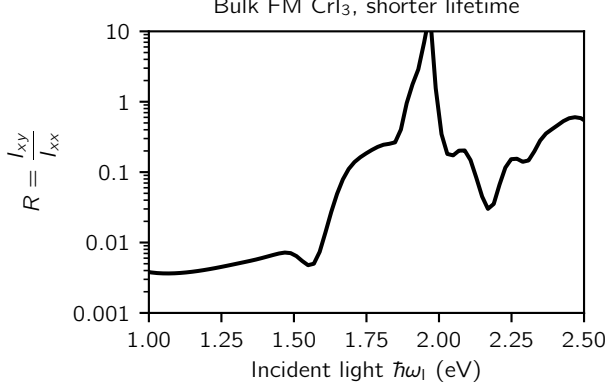


FIG. 7. The calculated ratio R in bulk ferromagnetic CrI_3 using a shorter electron lifetime, $\delta=0.16$ eV. In Fig. 2 we used $\delta=0.10$ eV.

state, without any atomic displacements. Second, we displace atoms by a small finite amount (u) and recalculate the magnetic moment of the Cr atom. This difference then gives us an estimate of $\frac{\partial m}{\partial u}$. We repeated this calculation with a range of atomic displacement magnitude (u) to confirm the linear change of m with u .

For the displacement of I atoms along the $\pm z$ axis we find that $|\frac{\partial m}{\partial u}|$ equals $0.98 \mu_B/\text{\AA}$. As expected, $|\frac{\partial m}{\partial u}|$ is smaller for the remaining three A_g modes. Specifically, for the displacement of Cr atoms along the $\pm z$ direction we find that $|\frac{\partial m}{\partial u}|$ is $0.27 \mu_B/\text{\AA}$, while for the two modes corresponding to I atom displacement in the x - y plane $|\frac{\partial m}{\partial u}|$ is only 0.06 and $0.04 \mu_B/\text{\AA}$. Comparing calculated $|\frac{\partial m}{\partial u}|$ with averages of $\frac{\partial \chi(\omega_1)}{\partial u}$ defined in Eq. 8 we indeed find that the mode that changes the magnetic moment the most has the largest off-diagonal Raman signature.

Interestingly, the dominant displacement modulating magnetic moment is coming from the displacement of nominally non-magnetic iodine atom, not from magnetic chromium atom. We discuss this in more detail in Sec. IV B where we demonstrate that the off-diagonal Raman signature here originates dominantly from the spin-orbit interaction of iodine atom.

F. Phonon modulated MOKE

Motivated by the large magnitude of $\frac{\partial m}{\partial u}$ we decided to compute the phonon modulated magneto-optical Kerr effect (MOKE), as it is often used as a signal of the magnetic moment in magnetic materials.^{1,3,42,43} We calculated the Kerr angle θ_K using,^{44,45}

$$\theta_K = -\text{Re} \left[\frac{\epsilon_{xy}}{\sqrt{\epsilon_{xx}}(\epsilon_{xx} - 1)} \right]. \quad (12)$$

We again displaced atoms and recomputed change in the Kerr angle θ_K to obtain $\frac{\partial \theta_K(\omega_1)}{\partial u}$. The results for bulk CrI_3 are shown in Fig. 8.

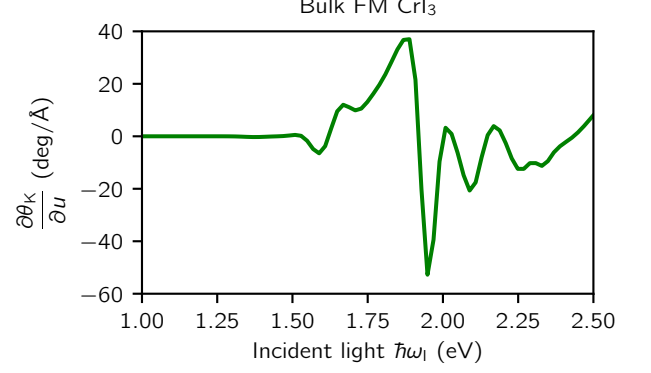


FIG. 8. The calculated phonon modulated MOKE signal in bulk ferromagnetic CrI_3 .

We find numerically that $\frac{\partial \theta_K}{\partial u}$ can be well approximated with,

$$\approx -\text{Re} \left[\frac{1}{\sqrt{\epsilon_{xx}}(\epsilon_{xx} - 1)} \frac{\partial \epsilon_{xy}}{\partial u} \right]. \quad (13)$$

Therefore, we conclude that in our case $\frac{\partial \theta_K}{\partial u}$ is approximately proportional to the coefficient b . Therefore, phonon modulated MOKE signal can be directly compared to the cross-polarized Raman signature I_{xy} , which is proportional to $|b|^2$. In particular, we find that the large positive peak in phonon modulated MOKE ($\sim 40 \text{ deg}/\text{\AA}$ at 1.86 eV) and large negative peak (about $-55 \text{ deg}/\text{\AA}$) at somewhat higher energy (1.93 eV) are in direct correspondence with two positive-definite peaks in the I_{xy} signature shown in blue in Fig. 1.

IV. ANALYSIS

The presence of I_{xy} signal in CrI_3 depends on three ingredients, as discussed earlier: broken time-reversal in ferromagnetic state, spin-orbit, and resonance. Now we analyze these conditions in more detail, one by one.

A. Anti-ferromagnetic order

First to further confirm the importance of the ferromagnetic order for non-zero b , we computed Raman intensity in the antiferromagnetic (AFM) state of CrI_3 . If we assume that FM and AFM states have the same crystal structure, but that only the atomic magnetic moments point in different directions, we infer that the magnetic space group of AFM state is $R\bar{3}'$. This space group consists of a 3-fold rotation, as well as inversion followed by time-reversal. The inversion operation, or time-reversal operation, on their own are not symmetries in the AFM state.

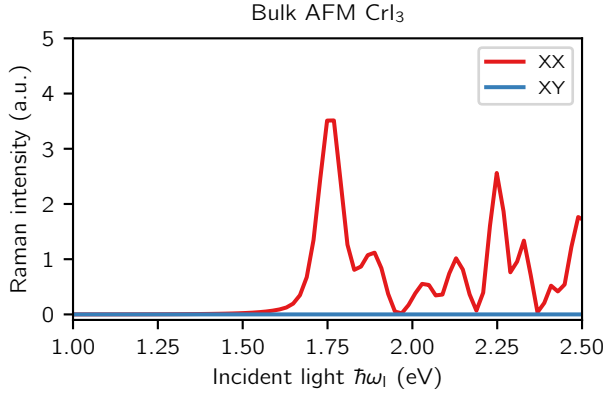


FIG. 9. The calculated Raman intensity of A_g mode in bulk CrI_3 in the anti-ferromagnetic state, showing no I_{xy} intensity.

Therefore the symmetry analysis in this case gives that the Raman signature should not have the cross-polarized signal b and that therefore $R = 0$. This is exactly what we find in our calculation, as shown in Fig. 9. While the I_{xx} intensities are of similar structure in the AFM and FM state, we find that the I_{xy} intensity is exactly zero in the AFM state, as expected from the symmetry arguments.

Furthermore, we investigate the Raman intensity in the FM state when the magnetic moment is along the x direction. Walker¹⁵ found when the applied magnetic field was parallel to the monolayer and the magnetic field was large enough ($B = 6$ T), the CrI_3 layers had a magnetic moment in the x - y plane. Therefore, we decided to repeat our calculation with the magnetic moment along the x direction, and the calculated Raman intensity of mode A_g is shown in Fig. 10. We find the I_{xy} intensity is almost zero, and we observe a strong I_{yz} intensity which is comparable to I_{xx} . For example, when the incoming photon energy is 1.91 eV, I_{yz} is about half of I_{xx} and ten times larger than I_{xy} .

B. Spin-orbit interaction

Second, we consider the importance of the spin-orbit interaction. We confirmed that if spin-orbit is excluded from the calculation that we obtain $b = 0$, as expected. However, we can take this analysis one step further. The pseudopotentials for Cr and I in our calculation were constructed by solving the relativistic Dirac equation separately on Cr and I. Therefore, this gives us a possibility to perform a calculation where spin-orbit is turned on selectively on either Cr or I atom. The results of such calculations are shown in Fig. 11. As can be seen from the middle panel of the figure, if spin-orbit interaction is included only on Cr atoms we get nearly negligible I_{xy} intensity. This is a somewhat surprising result, as one might naively assume that locality of the spin-orbit interaction poten-

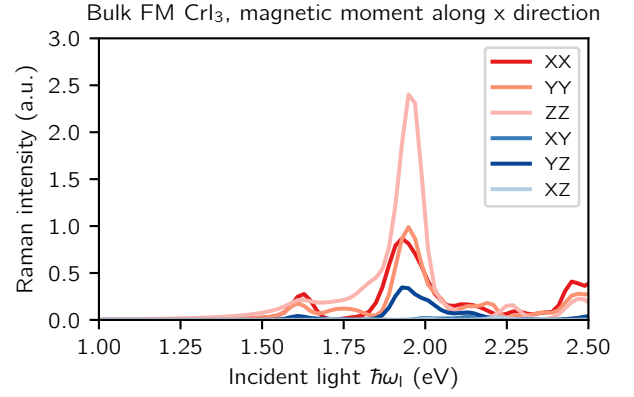


FIG. 10. The calculated Raman intensity of A_g mode in bulk ferromagnetic CrI_3 with magnetic moment pointing along the in-plane x -axis direction, showing large cross-polarized I_{yz} intensity.

tial implies that the only relevant spin-orbit interaction is the one on the magnetic atom. Clearly, there must therefore be some significant spillover of the dominantly chromium atomic-like orbitals onto iodine atoms.

Given this insight we then repeated calculation with spin-orbit interaction present only on the iodine atom (right panel of Fig. 11). We find that the calculated Raman signature is nearly indistinguishable from that in the full Raman calculation. Therefore, we conclude that the spin-orbit on iodine atom is almost exclusively responsible for calculated I_{xy} intensity. This observation is again consistent with our earlier finding that the largest change of the magnetic moment ($\frac{\partial m}{\partial u}$) comes from the displacement of I atom, not Cr atom. Finally, our findings are also consistent with the results in Refs. 29–33.

C. Resonance

Third, we discuss the importance of resonance. As can be seen from Fig. 2 the I_{xy} intensity is already two orders of magnitude smaller than I_{xx} at low energy. We find that I_{xy} vanishes in the $\omega_I = 0$ limit, as is expected in an insulator based on our earlier analysis. Therefore, without taking into consideration ω_I dependence of χ the I_{xy} intensity would be zero.

D. Relevant atomic-like orbitals

The Wannier interpolation³⁸ method that we used to compute optical response allows us to analyze the results in more detail. For this purpose, we analyzed the exact tight-binding parameters we obtained from Wannier interpolation. If we look at the on-site and hopping energies in the case of undistorted CrI_3 , we find that the dominant energy scale near the Fermi level is the split-

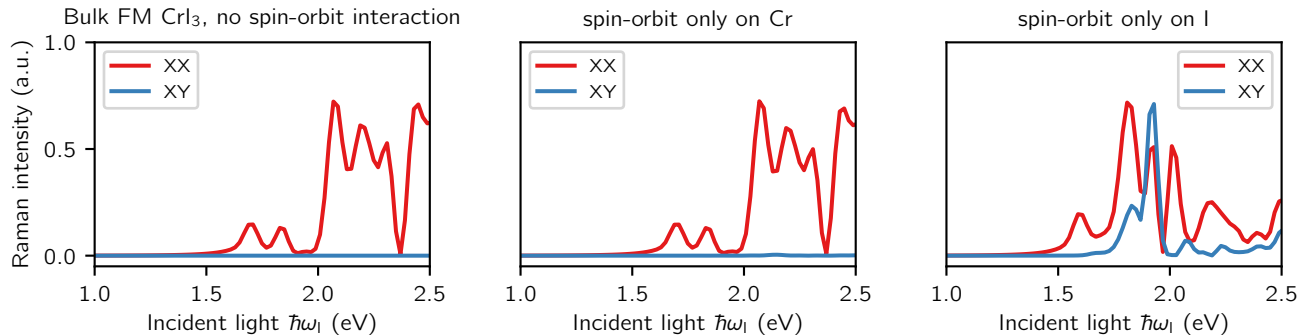


FIG. 11. The calculated Raman intensity of mode A_g in the bulk ferromagnetic CrI_3 . The left panel shows result without spin-orbit interaction. The middle panel shows the result with spin-orbit interaction on only Cr atoms. The right panel shows the result with spin-orbit interaction on only I atoms (nearly the same as that in a calculation where spin-orbit is included on all atoms, see Fig. 1.)

ting of the minority and majority spin states on Cr atoms. Therefore, we can for simplicity consider only the majority spins, as the gap to the minority spins is about 2 eV. Focusing on the five majority spin d -like states we find that they are split into three t_{2g} -like states and two e_g -like states, as expected in the octahedral environment. The splitting between t_{2g} and e_g states is about 0.5 eV. The electron bands formed by the t_{2g} -like states are fully occupied, while e_g -like bands are empty, as would be expected for spin-polarized nominally Cr^{3+} state in CrI_3 .

Next we displace the I atoms along the $\pm z$ -axis, corresponding to the A_g phonon mode. If we repeat our Wannier analysis on the distorted structure we find that this displacement of I atoms dominantly results in modulation of the crystal field splitting between t_{2g} and e_g states. This is to be expected from a simplified crystal field theory, as this particular mode modulates all Cr-I bond lengths in the octahedron. The calculated magnitude of the splitting is about 2 eV/Å. We also checked that the onsite energies are not changed as much. The largest change in the hopping term is -0.9 eV/Å.

Therefore, the dominant role of the displacement of I atoms along the $\pm z$ -axis is to rigidly shift the unoccupied e_g bands relative to the occupied t_{2g} bands. Therefore, if we consider derivative of Eq. 7 with respect to atom displacement u , we find that in this simplified picture of rigid displacement of bands, the following approximation holds,

$$I \sim \left| \frac{\partial \chi}{\partial u} \right|^2 \sim \left| \frac{\partial \chi}{\partial \omega_I} \right|^2. \quad (14)$$

We confirmed this by an explicit numerical calculation. Figure 12 shows calculated $\left| \frac{\partial \chi}{\partial \omega_I} \right|^2 \omega_I^4$ as a function of photon energy. As can be seen from the figure, the Raman intensity is in good qualitative agreement with full calculation, where intensity is computed from $\frac{\partial \chi}{\partial u}$ (see Fig. 1). As one would expect, the agreement is better in the region just above the band gap edge. Therefore, we con-

clude that the main origin of the Raman signature in our calculations is the rigid shifts in the band structure due to the displacement of iodine atoms along the $\pm z$ -axis.

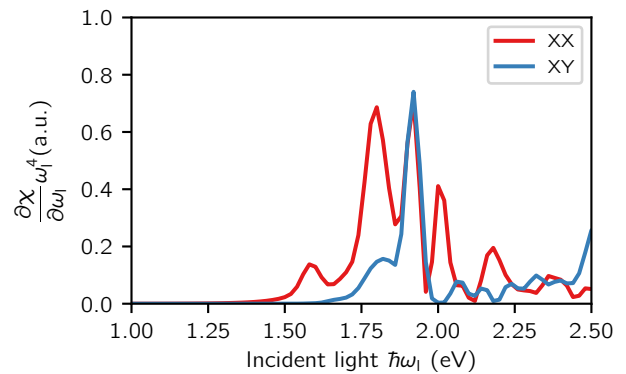


FIG. 12. Approximate Raman intensity one would get by assuming that dominant atomic motions modulate the t_{2g} – e_g crystal field splitting in CrI_3 . See text for details. The photon energy on the horizontal axis is shifted to reproduce the GW-BSE calculated optical bandgap onset.

V. CONCLUSION

In conclusion, our calculations show strong Raman scattering in CrI_3 driven by ferromagnetism, spin-orbit interaction, and resonance effects. The strong I_{xy} polarized Raman scattering comes from the spin-orbit effect of I atoms, rather than the metal Cr atoms. We speculate that our findings open up the possibility that strong spin orbit effects in materials need not come from the magnetic ion, but could instead be driven by non-magnetic ion, as in this case. Therefore, it might be possible to find other materials with strong spin-orbit interaction,

even when magnetism originates from atoms with small spin-orbit interaction, such as Cr, Mn, Fe, Co, or Ni.

cluster at UCR.

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