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Effects of intrinsic defects and alloying with Fe on the half-metallicity of Co_2MnSi

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The electronic structure and half-metallic gap of Co_2MnSi in the presence of crystallographic defects, partial Fe substitution for Mn, and thermal spin fluctuations are studied using the coherent potential approximation and the disordered local moment method. In the presence of 5% Co or Mn vacancies the Fermi level shifts down to the minority-spin valence-band maximum. In contrast to NiMnSb , both types of Mn antisite defects in Co_2MnSi are strongly exchange-coupled to the host magnetization, and thermal spin fluctuations do not strongly affect the half-metallic gap. Partial substitution of Mn by Fe results in considerable changes in the Bloch spectral function near the Fermi level, which strongly deviate from the rigid-band picture. In particular, a light band with the Fe character crosses the Fermi level at about 50% concentration. At room temperature, Fe substitution of up to 30% slightly increases the spin polarization at the Fermi level.

I. INTRODUCTION

Half-metallic ferromagnets have electronic bands in only one spin channel at the Fermi level [1, 2], which makes them attractive for applications in spintronic devices, such as magnetic tunnel junctions and spin valves [3–5]. Co_2MnSi is a full-Heusler alloy with a high Curie temperature $T_C = 985$ K [6, 7], and both density-functional and GW calculations predict it to be a half-metal with a minority-spin gap of 0.82 eV and 0.95 eV, respectively [8]. Spin polarization of 93% at room temperature was observed in Co_2MnSi thin films in ultraviolet photoemission measurements [9]. The half-metallic gap and the spin polarization can be sensitive to the presence of crystallographic defects. The effects of point defects on the half-metallic gap in full and half-Heusler alloys were studied using *ab initio* calculations [10, 11], which showed that Co_2MnSi remains half-metallic at zero temperature in the presence of four types of defects: Mn_{Co} and Mn_{Si} , Co vacancies, and Mn vacancies. Alloying with Fe on the Co sublattice also maintains the half-metallic gap at zero temperature [12].

For practical applications, it is important to consider the thermal stability of the half-metallic gap at room temperature [13, 14]. For example, for the half-Heusler NiMnSb alloy it was found [14] that the spins of Mn_{Sb} antisites are weakly coupled to the host magnetization and are, therefore, easily disordered at low temperatures. As a result, the electronic states near the valence band maximum (VBM) are strongly broadened and shifted up toward the Fermi level, which leads to a strong depolarization of NiMnSb far below room temperature. One goal of the present paper is to examine the role of thermal spin fluctuations in Co_2MnSi with intrinsic point defects.

The spin polarization of a half-metal is expected to be more robust if the Fermi level lies close to the middle of the half-metallic gap. Because the Fermi level in Co_2MnSi lies closer to the VBM [8, 15, 16], partial substitution of Fe for Mn was explored as a way to shift the Fermi level upward and enhance the magnetoresistive effects [17–20]. However, first-principles calculations, in-

cluding those in the GW approximation [8], show that the band structures of Co_2MnSi and Co_2FeSi differ by more than a rigid band shift. The second goal of this paper is to study the band structure of $\text{Co}_2\text{Mn}_{1-x}\text{Fe}_x\text{Si}$ (CMFS) and $(\text{Co}_{1-x}\text{Fe}_x)_2\text{MnSi}$ alloys as a function of Fe concentration and temperature.

II. COMPUTATIONAL METHODS

First-principles calculations were performed within the atomic sphere approximation (ASA) in the Green's function-based tight-binding linear muffin-tin orbital (GF-LMTO) method [21, 22], and substitutional alloying was described within the coherent potential approximation (CPA) [23]. The exchange and correlation were described within the generalized gradient approximation (GGA) [24]. We used the experimental lattice parameter of Co_2MnSi (5.645 Å [25]) in all calculations. Note that the lattice parameter of Co_2FeSi (5.64 Å [26]) is very similar.

To minimize the discrepancies of the ASA calculations with the reference band structure of Co_2MnSi obtained using a full-potential linear augmented plane wave calculation [27], the atomic sphere radii were optimized [28] and the magnetic part of the GGA exchange-correlation field was scaled by a factor 1.15.

The effects of thermal spin disorder are introduced using the vector disordered local moments (DLM) model [29–32], which assumes that the orientation of each local magnetic moment i has an independent distribution function, $p_i(\theta_i) \propto \exp(\alpha_i \cos \theta_i)$, where θ_i is the polar angle made by that local moment with the global magnetization. The parameters α_i are different for inequivalent lattice sites and for different components on the same site; they are obtained from the solution of the coupled equations of the mean-field approximation (MFA) at the given temperature with the magnetic exchange parameters calculated using the linear response technique [33].

Because the decline of the magnetization at low temperatures is too fast in MFA, we use the experimental

$M_{exp}(T)$ curve for Co_2MnSi [25] to improve the predictions for the electronic structure. Specifically, to predict the electronic properties at temperature T , we determine the temperature T' such that MFA with the calculated exchange parameters gives the magnetization $M_{\text{MFA}}(T') = M_{exp}(T)$; this conversion is illustrated in Fig. 1(a). The electronic structure obtained using the DLM method at temperature T' is then reported as corresponding to temperature T .

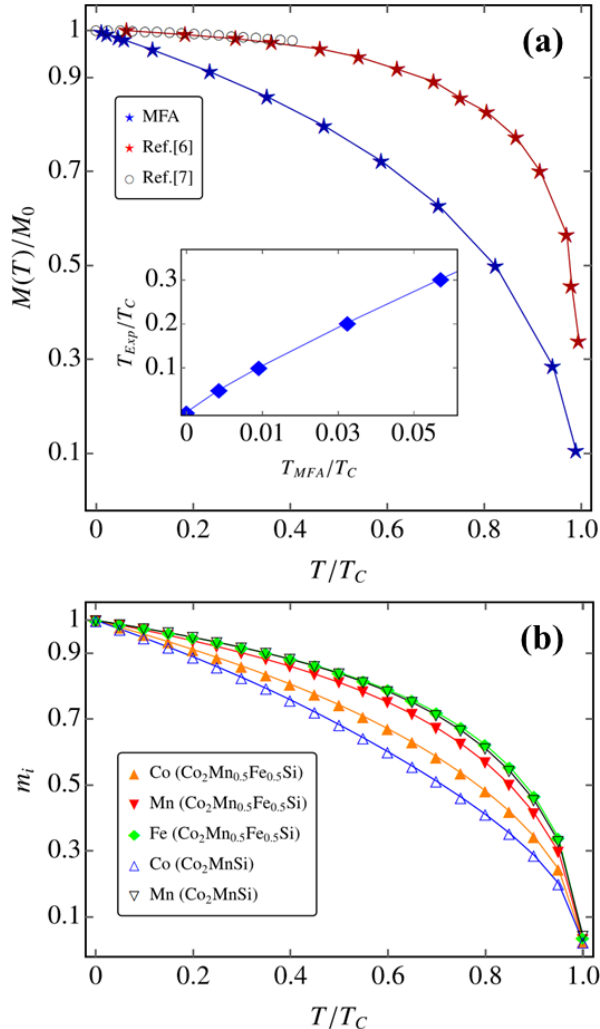


Figure 1. (a) Magnetization curve for Co_2MnSi compared with experimental data [6, 7]. Inset: conversion from T' to T using $M_{\text{MFA}}(T') = M_{exp}(T)$. (b) Reduced magnetization for each magnetic sublattice in Co_2MnSi (empty symbols) and $\text{Co}_2\text{Mn}_{0.5}\text{Fe}_{0.5}\text{Si}$ (filled symbols).

III. PURE Co_2MnSi AND Co_2FeSi

Spin-resolved densities of states (DOS) in Co_2MnSi and Co_2FeSi are shown in Fig. 2, and the minority-spin band structures in Fig. 3(a-b). Co_2MnSi is seen to be a half-metal with a saturated magnetic moment of $5 \mu_B$

and a half-metallic gap of 0.53 eV in GF-LMTO, which is underestimated compared to the full-potential value of 0.82 eV [8]. The half-metallic band gap is indirect and corresponds to the $\Gamma \rightarrow \text{X}$ transition energy. The direct gap at the Γ point is wider by 6 meV . On the other hand, Co_2FeSi is a ferromagnetic metal with a magnetic moment of $5.81 \mu_B$ in agreement with full-potential calculations [8]. The dispersive band with the Fe character, which was noted in Ref. 8, forms an electron pocket around the X point and is clearly seen in Fig. 3b.

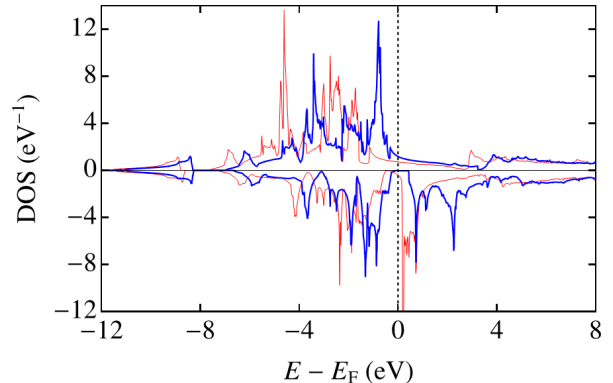


Figure 2. Density of states for majority (positive scale) and minority-spin (negative scale) electrons in Co_2MnSi (blue) and Co_2FeSi (red).

IV. VACANCIES AND ANTISITES IN Co_2MnSi

In this section we consider the spectroscopic signatures of Co and Mn vacancies (V_{Co} and V_{Mn}), Mn_{Si} and Mn_{Co} antisites, all of which preserve the half-metallic gap at zero temperature [11]. The concentrations were set to 5% and 15% for vacancies and antisites, respectively, and the resulting minority-spin Bloch spectral functions for Co_2MnSi with each type of defect are shown in Fig. 3(c-d).

The broadening of the electronic bands induced by the considered defects is fairly small even at the chosen large concentrations, and most of the bands close to the Fermi level remain well-defined. The spectral functions of Co_2MnSi with 1% Co or Mn vacancies (not shown) are virtually indistinguishable from those of pure Co_2MnSi . Note that a similar conclusion was reached for Ni and Mn vacancies in half-Heusler NiMnSb [10]. The conduction bands are almost unaffected by vacancies even at the 5% concentration. However, vacancies decrease the minority spin-flip gap, i.e., the distance between the minority-spin VBM and the Fermi level, which in our calculation goes to zero at the vacancy concentration of about 5%, as seen in Fig. 3(c-d). Thermal spin fluctuations at room temperature are expected to amplify the effect of this band shift on the spin polarization. Thus, large concentrations of Co or Mn vacancies can strongly reduce the spin polarization of Co_2MnSi .

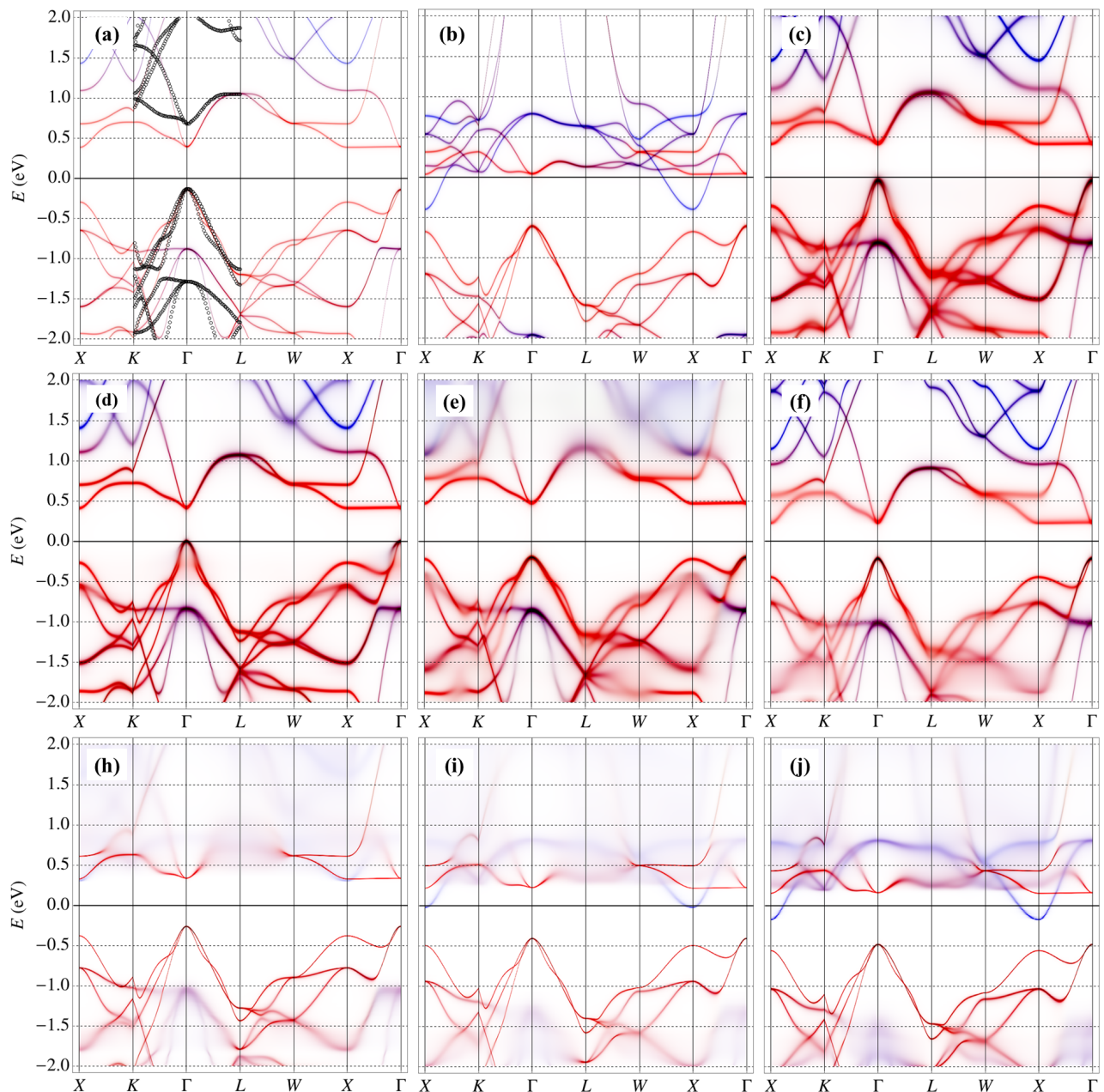


Figure 3. Minority-spin Bloch spectral functions at $T = 0$ for (a) Co_2MnSi , (b) Co_2FeSi , (c-f) Co_2MnSi with defects, including (c) 5% Co vacancies, (d) 5% Mn vacancies, (e) 15% Mn_{Si} antisites, (f) 15% Mn_{Co} antisites, (h-j) $\text{Co}_2\text{Mn}_{1-x}\text{Fe}_x\text{Si}$ at (h) $x = 0.28$, (i) $x = 0.55$, and (j) $x = 0.72$. Color reflects the spectral character Co (red), Mn and Fe (blue), and Si (green). Black circles in panel (a) show the full-potential band structure. The Fermi level is at $E = 0$.

As seen in Fig. 3(e-f), Mn_{Si} and Mn_{Co} antisites preserve the half-metallic gap even at a large concentration of 15%, in agreement with Ref. 11. Mn_{Si} antisites increase the half-metallic gap to 0.67 eV but have almost no effect on the spin-flip gap. In contrast, Mn_{Co} antisites reduce the half-metallic gap while bringing the Fermi level closer to its center. Some of the occupied bands are considerably broadened in the presence of Mn_{Si} or Mn_{Co} antisites.

The effect of Mn_{Si} and Mn_{Co} antisites on the Curie temperature T_C is shown in Fig. 4a. While T_C decreases linearly with increasing concentration of Mn_{Si} , its dependence on the concentration of Mn_{Co} is non-monotonic with a maximum at $x = 0.12$. As for the vacancies, the Curie temperature is only slightly reduced by 53 K and 23 K in Co_2MnSi with a 5% concentration of V_{Co} and V_{Mn} , respectively.

We now examine the stability of the half-metallic

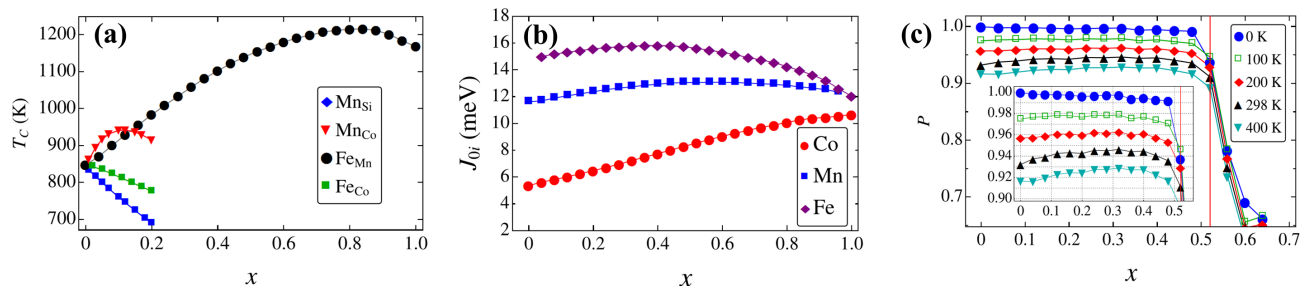


Figure 4. (a) Mean-field Curie temperature T_C for Co_2MnSi with Mn_{Si} or Mn_{Co} antisites and for the $\text{Co}_2\text{Mn}_{1-x}\text{Fe}_x\text{Si}$ and $(\text{Co}_{1-x}\text{Fe}_x)_2\text{MnSi}$ alloys. (b) Magnetic stability parameters J_{0i} for Co, Mn, and Fe atoms in $\text{Co}_2\text{Mn}_{1-x}\text{Fe}_x\text{Si}$. (c) Spin polarization P of the DOS at the Fermi level in $\text{Co}_2\text{Mn}_{1-x}\text{Fe}_x\text{Si}$ as a function of the concentration x at several temperatures. The vertical red line at $x = 0.52$ shows the point where the quasiparticle band with the Fe character crosses the Fermi level.

gap in Co_2MnSi with Mn_{Si} or Mn_{Co} antisites at *finite* temperatures. We note that Mn_{Sb} antisites in a closely related half-metallic half-Heusler alloy NiMnSb are weakly exchange-coupled to their neighbors, which leads to strong spin disorder and loss of half-metallicity at relatively low temperatures [14]. The magnetic stability of the given magnetic site i is characterized by the parameter $J_{0i} = \sum_j J_{ij}$, where J_{ij} is the pair exchange coupling.

The parameters J_{0i} calculated using the linear response theory [33] within CPA for Co_2MnSi with 15% Mn_{Si} or Mn_{Co} antisites are listed in Table I. We see that, in contrast with Mn_{Sb} antisites in NiMnSb , both types of Mn antisites in Co_2MnSi are strongly coupled to their neighbors. Therefore, thermal spin fluctuations are not expected to have a strong effect on the half-metallic gap at room temperature. Indeed, the spectral functions for Co_2MnSi with 15% Mn_{Si} or Mn_{Co} antisites calculated at room temperature using the DLM method are similar to Figs. 3e and 3f and only show a small amount of additional broadening for some bands. Thus, we conclude that even large concentrations of Mn_{Si} or Mn_{Co} antisites do not strongly affect the half-metallic gap in Co_2MnSi either in the ground state or at room temperature.

System	Atom	J_0 (meV)
Pure Co_2MnSi	Co	5.2
	Mn	11.5
15% Mn_{Si}	Co	7.4
	Mn	12.6
	Mn_{Si}	31.9
15% Mn_{Co}	Co	6.6
	Mn	12.0
	Mn_{Co}	9.7

Table I. Magnetic stability parameters J_{0i} for Co_2MnSi with Mn_{Si} and Mn_{Co} antisites.

V. $\text{Co}_2\text{Mn}_{1-x}\text{Fe}_x\text{Si}$ AND $(\text{Co}_{1-x}\text{Fe}_x)_2\text{MnSi}$ ALLOYS

Alloying with Fe on the Mn sublattice shifts the Fermi energy in Co_2MnSi upward, which brings the Fermi level closer to the middle of the half-metallic gap, which is expected to be favorable for applications [17–20]. In addition, alloying with Fe increases T_C which is also favorable; in fact, Co_2FeSi has the highest T_C of any Heusler alloy [34]. In this section, we examine the evolution of the electronic structure of the CMFS alloy with increasing concentration x . We also consider the effects of the unavoidable Fe dopants on the Co sublattice.

Figure 3(h-j) shows the minority-spin spectral functions of the CMFS alloy at $x = 0.28, 0.55,$ and 0.72 , which can be compared with those for $x = 0$ in Fig. 3a and $x = 1$ in Fig. 3b. Because Fe has an extra valence electron compared to Mn, its addition increases the band filling, shifting the Fermi level upward. As seen in Fig. 3h, the Fermi level lies close to the middle of the gap at $x = 0.28$. However, in addition to the band filling trend, the band structure also undergoes drastic changes with increasing x . The failure of the rigid-band model is already obvious from the fact that the band structure of the unoccupied states is very different in Co_2MnSi and Co_2FeSi ; see Figs. 3a and 3b. The most important change in the band structure is the formation of a light band with the Fe character, which drops below the Mn-dominated unoccupied bands and crosses the Fermi level at the X point at $x \approx 0.52$, as seen in Fig. 3(h-j).

The magnetic stability parameters J_{0i} for Co, Mn, and Fe atoms in CMFS are shown in Fig. 4b. At small concentrations of Fe, the exchange coupling of Mn and Fe atoms to their neighbors is similar and about twice stronger compared to Co. As x increases from 0 to 1, the $J_{0,\text{Co}}$ parameter increases by a factor of 2 and nearly reaches those of Mn and Fe, which pass through a broad maximum and then decline somewhat. As seen in Fig. 4a, the Curie temperature increases up to $x \approx 0.8$ where it is about 40% larger compared to Co_2MnSi . As seen in Fig. 1b, the enhancement of $J_{0,\text{Co}}$ by alloying with Fe slightly increases the magnetic order parameter for Co

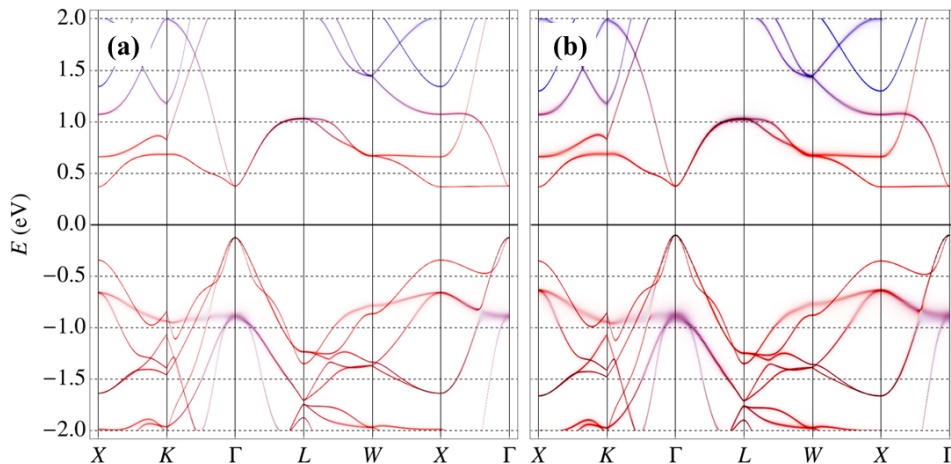


Figure 5. Minority-spin Bloch spectral functions in $(\text{Co}_{1-x}\text{Fe}_x)_2\text{MnSi}$ at (a) $x = 0.1$ and (b) $x = 0.2$, both at $T = 0$. The color scheme is the same as in Fig. 3.

while other sublattices are essentially unaffected.

Figure 4c shows the spin polarization $P = [N_{\uparrow}(E_F) - N_{\downarrow}(E_F)]/[N_{\uparrow}(E_F) + N_{\downarrow}(E_F)]$ of the density of states (DOS) $N_{\sigma}(E)$ at the Fermi level calculated using the DLM method in the range of temperatures from 0 to 400 K. The precipitous drop of the spin polarization at $x \approx 0.52$ is caused by the light Fe band crossing the Fermi level. The deviation of P from 1 at smaller concentrations of Fe reflects the effect of spin fluctuations without any quasiparticle bands appearing at the Fermi level. At room temperature P starts at about 0.93 at $x = 0$, increases almost to 0.95 at about $x \approx 0.30$, and then declines back to 0.93 at $x = 0.5$. This behavior is due to the competition of several factors: the upward shift of the Fermi level relative to the half-metallic gap, the increase in band broadening due to substitutional disorder, and the rearrangement of the band structure with the lowering of the light Fe band toward the Fermi level. Thus, there is an optimal concentration of about 30% of Fe at which CMFS exhibits the maximum spin polarization at room temperature.

Fe atoms substituting on the Co sublattice in Co_2MnSi have a small magnetic moment of about $0.2 \mu_B$. Such small magnetic moments should be regarded as being induced by the neighboring magnetic atoms, and the DLM spin fluctuation model is inapplicable to them. The minority-spin spectral functions of Co_2MnSi with 10 or 20% of Co atoms substituted by Fe are shown in Fig. 5. It is seen that Fe substitution for Co shifts the Fermi level downward toward the VBM but only slightly. This is because the reduction in band filling is accompanied by the reduction in the exchange splitting in the alloy where Fe is essentially non-magnetic. Aside from the small Fermi level shift, there are no substantial changes in the band structure. Electronic states near the Γ point at about -1 eV have a mixed Co-Fe and Mn character and are broadened by alloying with Fe, but they are far from the Fermi energy and do not affect the half-metallic gap,

which is essentially unchanged even at $x = 0.2$. Thus, partial substitution of Fe on the Co sublattice is not expected to have a significant effect on the spin polarization of the alloy, either at zero or at room temperature.

The Curie temperature is reduced by about 70 K when 20% Fe substitutes for Co. Thus, if a substantial fraction of Fe atoms substitutes on the Co sublattice, the increasing T_C trend seen in Fig. 4a for CMFS may be weakened.

VI. CONCLUSIONS

We have examined the electronic structure of Co_2MnSi in the presence of vacancies and Mn antisites, as well as those of the $\text{Co}_2\text{Mn}_{1-x}\text{Fe}_x\text{Si}$ and $(\text{Co}_{1-x}\text{Fe}_x)_2\text{MnSi}$ alloys, paying special attention to the effects of thermal spin fluctuations treated within the DLM approximation. Although small concentrations of Co or Mn vacancies do not destroy the half-metallic gap, they can lead to a considerable downward shift of the Fermi level, which crosses the VBM at about 5% concentration. On the other hand, even large concentrations of Mn_{Si} and Mn_{Co} antisites do not strongly affect the half-metallic gap at room temperature. In the CMFS alloy, substitution of Mn by Fe shifts the Fermi level away from the VBM, but it also pulls down a light minority-spin band with the Fe character, which crosses the Fermi level and forms an electron pocket at about 50% substitution. The spin polarization of DOS at the Fermi level has a broad maximum at about 30% concentration at room temperature, increasing by about 0.02 from its value in pure Co_2MnSi . Fe atoms substituting on the Co sublattice are essentially non-magnetic; this substitution tends to shift the Fermi level slightly toward the VBM but otherwise does not affect the electronic states near the Fermi level.

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