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Microwave Meissner Screening Properties of Proximity coupled Topological Insulator / Superconductor Bilayers

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Abstract

The proximity coupled topological insulator / superconductor (TI/SC) bilayer system is a representative system to realize topological superconductivity. In order to better understand this unique state and enable future applications of the TI/SC bilayer, a comprehensive characterization and understanding of the microscopic properties of the bilayer are required. In this work, a microwave Meissner screening study, which exploits a high-precision microwave resonator technique, is conducted on the SmB₆/YB₆ thin film bilayers as an example TI/SC system. The study reveals spatially dependent electrodynamic screening response of the TI/SC system that is not accessible to other techniques, from which the corresponding microscopic properties of a TI/SC bilayer can be obtained. The TI thickness dependence of the effective penetration depth suggests the existence of a bulk insulating region in the TI layer. The spatially dependent electrodynamic screening model analysis provides an estimate for the characteristic lengths of the TI/SC bilayer: normal penetration depth, normal coherence length, and the thickness of the surface states.

23 I. INTRODUCTION

24 The topological insulator / superconductor (TI/SC) proximity-coupled bilayer system
25 has received great attention as it has been proposed to realize topological superconductivity
26 via the proximity effect.^{1,2} With the induced topological superconductivity, the existence of
27 a Majorana bound state (MBS) is predicted in its vortex core.^{3,4} The MBS is a promising
28 qubit candidate for robust quantum computation.⁵ Naturally, it has become an important
29 goal of the physics community to verify the existence of an insulating bulk in the TI layer for
30 a given TI/SC candidate, and extract parameters which characterize the proximity induced
31 order parameter in the topological surface states (TSS).

32 There have been a number of studies on the Bi-based TI (Bi_2Se_3 , Bi_2Te_3 , etc) /SC systems
33 through point contact spectroscopy (PCS),⁶ ARPES,^{7,8} and STM⁹⁻¹¹ measurements. PCS
34 and STM probe the magnitude of the superconducting order parameter induced in the top
35 surface of the TI with a probing depth range limited to the mean free path or coherence
36 length, and cannot be applied to the case when an insulating bulk region is present. ARPES
37 studies the angle-resolved magnitude of the induced order parameter from the first few
38 atomic layers of the top surface of the TI.

39 In contrast, a microwave Meissner screening study investigates the high frequency elec-
40 tromagnetic field response. The microwave field propagates through an insulating layer and
41 penetrates inside the superconducting system to the scale of the penetration depth, which
42 is comparable to the thickness of typical thin-film bilayers (< 200 nm). Since the field
43 screening response arises throughout the entire bilayer, it can reveal more details of the
44 proximity-coupled system¹²⁻¹⁶ that are not directly available to the other techniques. It is
45 also important to note that the screening response study does not require specialized surface
46 preparation which is critical for many of the other techniques.

47 The distinct capabilities of the Meissner screening study on the proximity-coupled system
48 have been previously demonstrated on conventional normal (N) / superconductor (S) bilayer
49 systems such as **Cu (N) / Nb (S)**.^{13,17-26} It can reveal the spatial distribution of the order
50 parameter and the magnetic field profile throughout the film, as well as their evolution
51 with temperature. From such information, superconducting characteristic lengths such as
52 the normal coherence length ξ_N and normal penetration depth λ_N of the proximity-coupled
53 normal layer can be estimated. The study can also reveal thickness dependent proximity-

54 coupling behavior, which helps to estimate the thickness of the surface states (t_{TSS}) for
55 TI/SC bilayers.

56 Compared to other high frequency electromagnetic techniques such as THz optical mea-
57 surement, the advantage of the microwave Meissner screening study for investigating the
58 properties of a TI/SC bilayer is that the energy of a 1 GHz microwave photon ($\approx 4 \mu\text{eV}$) is
59 a marginal perturbation to the system. On the other hand, the energy of a 1 THz optical
60 photon ($\approx 4 \text{ meV}$) is comparable to the gap energy ($\leq 3 \text{ meV}$) of typical superconductors
61 used in TI/SC systems such as Nb, Pb, Al, NbSe₂, and YB₆.²⁷⁻²⁹ Therefore, the microwave
62 screening study is an ideal method to study details of the induced order parameter in TI/SC
63 bilayers.

64 In this article, we conduct a microwave Meissner screening study on SmB₆/YB₆: a strong
65 candidate for topological Kondo insulator / superconductor bilayer systems. The existence
66 of the insulating bulk in SmB₆ is currently under debate.³⁰⁻³⁷ From measurements of the
67 temperature dependence of the Meissner screening with a systematic variation of SmB₆
68 thickness, this study shows evidence for the presence of an insulating bulk region in the
69 SmB₆ thin films. Through a model of the electrostatics, the study also provides an
70 estimation for the characteristic lengths of the bilayer system including the thickness of the
71 surface states.

72 II. EXPERIMENT

73 A. Sample preparation

74 SmB₆/YB₆ bilayers were prepared by an in-situ sequential sputtering process (i.e., with-
75 out breaking vacuum) to secure the ideal superconducting proximity effect which is a prereq-
76 uisite for the current study and analyses.³⁸ SmB₆ and YB₆ share the same crystal structure
77 with almost the same lattice constant ($\approx 4.1 \text{ \AA}$), which allows the fabrication of bilayers by
78 sequential high-temperature growth under the same conditions. YB₆ is a superconducting
79 rare-earth hexaboride and it has been reported that slight boron deficiency improves the
80 superconducting transition temperature (T_c) of YB₆.³⁹ Thus, for this study, slightly boron
81 deficient YB₆ films (B/Y = 5.6) were used as the superconducting layers.

82 YB₆ thin films were deposited on Si(001) substrates. To remove the native oxide layer on

83 the Si substrate, we treated it with hydrofluoric acid (HF) before the thin film deposition.
 84 The base pressure of the deposition system was 2×10^{-8} Torr. The deposition process was
 85 performed at 860 °C under a pressure of 10 mTorr adjusted by Ar gas (99.999 %). The thick-
 86 ness of YB₆ layers was fixed to be 100 nm. The subsequent SmB₆ deposition was performed
 87 under the same temperature and pressure conditions, and additional sputtering of a B target
 88 was employed to compensate the B deficiency which is present in the films fabricated by
 89 the sputtering of a stoichiometric SmB₆ target.^{38,40} The compositions (i.e., stoichiometry) of
 90 YB₆ and SmB₆ thin films were examined with wavelength dispersive spectroscopy (WDS)
 91 measurements. The thicknesses of bilayers were confirmed with cross-sectional scanning
 92 electron microscopy (SEM) measurements.

93 The geometry of the bilayers is schematically shown in Fig. 1(a). The YB₆ film has a
 94 thickness of 100 nm and $T_c = 6.1$ K obtained from a DC resistance measurement.³⁹ The
 95 thickness of SmB₆ layers (t_{SmB_6}) are varied from 20 to 100 nm for systematic study. These
 96 bilayers all have $T_c = 5.8 \pm 0.1$ K without a noticeable t_{SmB_6} dependence of T_c .

97 B. Effective penetration depth measurement

98 The measurement of the effective penetration depth λ_{eff} is conducted with a dielectric
 99 resonator setup (Ref.⁴¹⁻⁴³ and Appendix B). A 3 mm diameter, 2 mm thick rutile (TiO₂)
 100 disk, which facilitates a microwave transmission resonance at 11 GHz, is placed on top of the
 101 sample mounted in a Hakki-Coleman type resonator.⁴¹ This resonator consists of niobium
 102 (top) and copper (bottom) plates to obtain a high quality factor for the dielectric resonance.
 103 The resonator is cooled down to the base temperature of 40 mK. As the temperature of the
 104 sample is increased from the base temperature, the change of the resonance frequency is
 105 measured (Appendix C 1), $\Delta f_0(T) = f_0(T) - f_0(T_{ref})$. T_{ref} here is set to 230 mK ($\approx 0.04T_c$
 106 of the bilayers), below which $f_0(T)$ of the bilayers shows saturated temperature dependence.
 107 Here, the $f_0(T)$ data in a temperature range of $T < 1.6$ K is used for this study. This
 108 is a temperature range where the niobium top plate, one of the main components of the
 109 resonator, does not show temperature dependence in its surface reactance, and hence does
 110 not affect $f_0(T)$. In this range, the temperature dependence of the resonant frequency
 111 $\Delta f_0(T)$ of the resonator can be attributed solely to that of the screening response of the
 112 sample. The $\Delta f_0(T)$ data in this range is converted to the change in the effective penetration

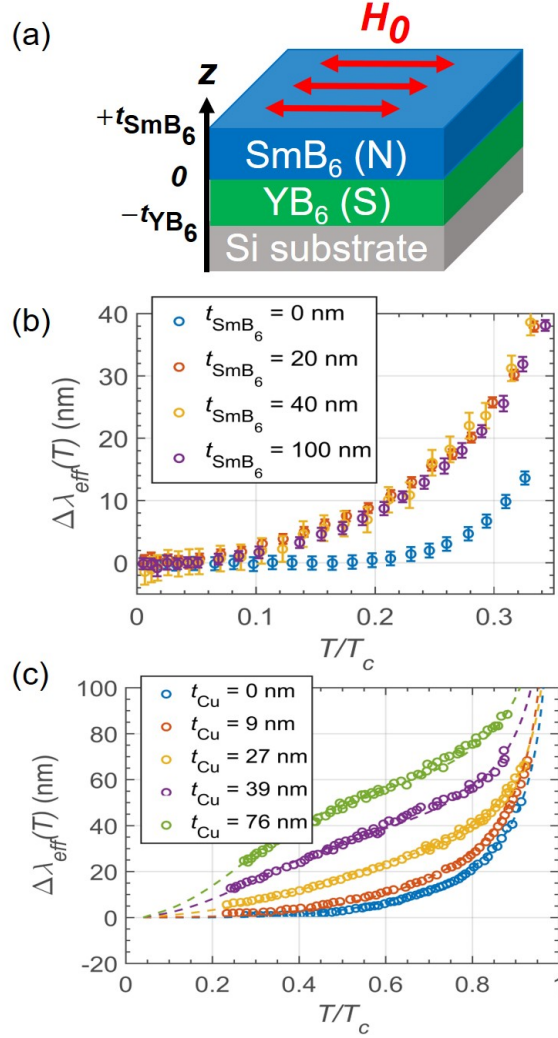


FIG. 1. (a) A schematic of the bilayer consisting of an SmB_6 film and a YB_6 film. A parallel microwave magnetic field (H_0) is applied to the top surface of the SmB_6 layer (red arrows). (b) Temperature dependence of the effective penetration depth $\Delta\lambda_{eff}(T)$ of the SmB_6/YB_6 bilayers for various SmB_6 layer thickness (t_{SmB_6}). (c) $\Delta\lambda_{eff}(T)$ of a Cu/Nb (conventional metal / superconductor) bilayers²⁴ for various Cu layer thickness (t_{Cu}). The dashed lines are the model fits.²⁴

¹¹³ depth $\Delta\lambda_{eff}(T)$ using standard cavity perturbation theory,^{44–46}

$$\Delta\lambda_{eff}(T) = \lambda_{eff}(T) - \lambda_{eff}(T_{ref}) = -\frac{G_{geo}}{\pi\mu_0} \frac{\Delta f_0(T)}{f_0^2(T)}. \quad (1)$$

¹¹⁴ Here, G_{geo} is the geometric factor of the resonator.⁴³

115 III. RESULTS

116 Fig. 1(b) shows $\Delta\lambda_{eff}(T)$ for the SmB₆ (N) / YB₆ (S) bilayers for various SmB₆ layer
117 thickness t_{SmB_6} . The single layer YB₆ thin film (i.e., $t_{\text{SmB}_6} = 0$) shows temperature inde-
118 pendent behavior below $T/T_c < 0.2$. This is not only consistent with the BCS temperature
119 dependence of $\Delta\lambda(T)$ for a spatially homogeneous, fully-gapped superconductor,^{47,48} but
120 also consistent with previous observations on YB₆ single crystals.^{29,49} However, once the
121 SmB₆ layer is added, $\Delta\lambda_{eff}(T)$ clearly shows temperature dependence below $T/T_c < 0.2$.
122 Here, the important unconventional feature is that the low temperature profile of $\Delta\lambda_{eff}(T)$
123 for the SmB₆/YB₆ bilayers shows only a marginal t_{SmB_6} dependence. This is in clear con-
124 trast to the case of the Cu (N) / Nb (S) bilayers shown in Fig. 1(c). The $\Delta\lambda_{eff}(T)$ for
125 this conventional metal/superconductor bilayer system shows considerable evolution as the
126 normal layer thickness t_{Cu} increases. This evolution occurs because when the decay length
127 of the induced order parameter $\xi_N(T)$ decreases with increasing temperature, a normal layer
128 with larger (smaller) thickness undergoes a larger (smaller) change in the spatial distribu-
129 tion of the order parameter, and hence the spatial profile of the screening. Therefore, the
130 marginal t_{SmB_6} dependence of $\Delta\lambda_{eff}(T)$ for the SmB₆/YB₆ bilayer implies that even though
131 t_{SmB_6} is increased, the actual thickness of the proximity-coupled screening region in the
132 SmB₆ layer remains roughly constant. This observation provides qualitative evidence of the
133 presence of an insulating bulk which blocks the propagation of the induced order parameter
134 in the SmB₆ layer. In the following sections, the $\Delta\lambda_{eff}(T)$ data is quantitatively modeled
135 to further support this implication.

136 IV. MODEL

137 To quantitatively analyze this unconventional behavior, an electromagnetic screening
138 model for a proximity-coupled bilayer is introduced.^{13,22,24,25} The model solves Maxwell's
139 equations combined with the second London equation for the current and field inside the
140 bilayer with appropriate boundary conditions at each temperature (See Appendix D), to
141 obtain the spatial profile of the magnetic field $H(z, T)$ and the current density $J(z, T)$ as
142 a function of temperature,¹³ where z denotes the coordinate along the sample thickness
143 direction as depicted in Fig. 1(a). From the obtained field and current profiles, one can

144 obtain the total inductance $L(T)$ of the bilayer as

$$\begin{aligned}
L(T) = & \frac{\mu_0}{H_0^2} \int_{-t_S}^0 [H^2(z, T) + \lambda_S^2(T)J^2(z, T)] dz \\
& + \frac{\mu_0}{H_0^2} \int_0^{+d_N} [H^2(z, T) + \lambda_N^2(z, T)J^2(z, T)] dz \\
& + \frac{\mu_0}{H_0^2} \int_{+d_N}^{+t_N} [H^2(z)] dz,
\end{aligned} \tag{2}$$

145 from which one can obtain an effective penetration depth from the relation $L(T) =$
146 $\mu_0\lambda_{eff}(T)$. Here, H_0 is the amplitude of the applied microwave magnetic field at the
147 top surface of the normal layer (see Fig. 1(a)), λ_S (λ_N) is the local penetration depth of
148 the superconductor (normal layer), t_S is the thickness of the superconductor, t_N ($N=SmB_6$
149 or Cu) is the total thickness of the normal layer, and d_N ($\leq t_N$, integration limit of the
150 second and third terms in Eq. (2)) is the thickness of the proximity-coupled region in
151 the normal layer, which is assumed to be temperature independent. In Eq.(2), H^2 is pro-
152 portional to field stored energy and λ^2J^2 is proportional to kinetic stored energy of the
153 supercurrent. The first, second, and third integration terms come from the superconductor,
154 the proximity-coupled part of the normal layer, and the uncoupled part of the normal layer,
155 respectively.

156 A schematic view of the order parameter profile in the bilayers is shown in Fig. 2. As
157 seen in Fig. 2(a), for a conventional metal, d_N is the same as t_N since the entire normal
158 layer is uniformly susceptible to induced superconductivity, and thus the third integration
159 term in Eq. 2 becomes zero. However, as seen in Fig. 2(b), if there exists an insulating bulk
160 region blocking the propagation of the order parameter up to the top surface in the normal
161 layer (as in the case of a thick TI), only the bottom conducting surface adjacent to the
162 superconductor is proximity-coupled. In this case, d_N becomes the thickness of the bottom
163 conducting surface states (so that $d_N < t_N$). The third integration term in Eq. (2), which
164 accounts for the uncoupled portion of the normal layer, becomes non-zero. However, this
165 third term can be removed by taking $\Delta L(T)$ into account since the un-coupled SmB_6 region
166 has temperature-independent microwave properties below 3 K,⁵⁰ whereas the temperature
167 range of the measurement here extends below 2 K.

168 The spatial dependence of screening of the proximity-coupled normal layer is imposed
169 by that of the induced order parameter Δ_N (Fig. 2(a)), which can be approximated by
170 an exponential decay profile $\Delta_N(z, T) = \Delta_N(0, T)e^{-z/\xi_N(T)}$ in terms of the normal coher-

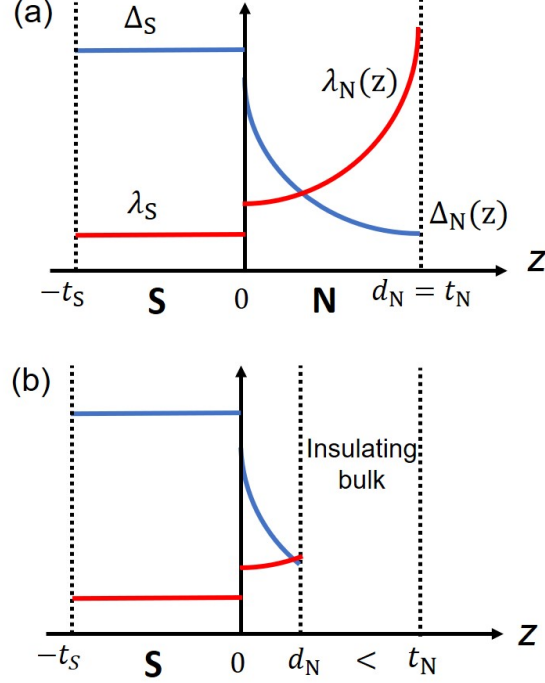


FIG. 2. (a) Schematic spatial profile of the order parameter $\Delta_{N,S}$ (blue) and the local penetration depth $\lambda_{N,S}$ (red) through the normal layer (N) / superconductor (S) bilayer sample for the case of the absence of an insulating bulk. z is the thickness direction coordinate and t_N (t_S) is the thickness of the normal layer (superconductor). The proximitized thickness d_N is equal to the normal layer thickness t_N . (b) In the presence of an insulating bulk, $d_N < t_N$ since the insulating bulk blocks propagation of the order parameter to the top surface. Note that the microwave magnetic field is applied to the right surfaces.

171 ence length $\xi_N(T)$.¹⁵ The position dependent normal penetration depth is inversely pro-
 172 portional to the order parameter $\lambda_N \sim 1/\Delta_N$ ⁵¹ so its position dependence is expressed
 173 as $\lambda_N(z, T) = \lambda_N(0, T)e^{z/\xi_N(T)}$. Here, the temperature dependence of λ_N at the inter-
 174 face is assumed to follow that of the superconductor⁵² $\lambda_N(0, T)/\lambda_N(0, 0) = \lambda_S(T)/\lambda_S(0) \cong$
 175 $1 + \sqrt{\pi\Delta_0/2k_B T} \exp(-\Delta_0/k_B T)$, which is the asymptotic behavior below $0.3T_c$ for a fully-
 176 gapped superconductor.^{47,48}

177 For the temperature dependence of the screening in the normal layer, $\xi_N(T)$ plays a
 178 crucial role since it determines the spatial distribution of $\Delta_N(z, T)$. If the sample is in
 179 the clean limit, the temperature dependence of the normal coherence length is given by
 180 $\xi_N = \hbar v_F/2\pi k_B T$, where v_F denotes the Fermi velocity of the N layer. In the dirty limit, it

181 is given by $\xi_N = \sqrt{\hbar v_F l_N / 6\pi k_B T}$,¹² where l_N denotes the mean-free path of the N layer. For
182 the model fitting, the simplified expressions $\xi_N^{clean}(T) = \xi_N^{clean}(T_0) \times T_0/T$ and $\xi_N^{dirty}(T) =$
183 $\xi_N^{dirty}(T_0) \times \sqrt{T_0/T}$ are used, with $\xi_N(T_0)$ as a fitting parameter. Here, T_0 is an arbitrary
184 reference temperature of interest. Note that the divergence of $\xi_N(T)$ as $T \rightarrow 0$ should be
185 cut off below a saturation temperature due to the finite thickness of the normal layer, which
186 is theoretically predicted,^{12,53} and also experimentally observed from magnetization studies
187 on other bilayer systems.^{20,23} In our measurements, the effect of this saturation of $\xi_N(T)$ can
188 be seen from the sudden saturation of the $\Delta\lambda_{eff}(T)$ data below $0.04T_c$ (see Fig. 1(b) and
189 Fig. 3(b-d)). Therefore, only the data obtained in a temperature range of $T/T_c \geq 0.04$ is
190 fitted, where the $\Delta\lambda_{eff}(T)$ data indicates that ξ_N is temperature dependent.

191 A given set of these parameters $\lambda_S(0)$, $\lambda_N(0,0)$, $\xi_N(T_0)$, and d_N determines a model curve
192 of $\Delta\lambda_{eff}(T)$. Therefore, by fitting the experimental data to a model curve, one can determine
193 the values of these characteristic lengths. This screening model has successfully described
194 $\Delta\lambda(T)$ behavior of various kinds of normal/superconductor bilayers.^{22,24,25}

195 V. MODEL ANALYSIS OF DATA

196 As seen in Fig. 3(a), the model is first applied to fit $\Delta\lambda_{eff}(T)$ of a single layer YB₆ thin
197 film (i.e., no SmB₆ layer on the top) to obtain $\lambda_S(0)$: the simplest case where one needs to
198 consider only the first term in Eq. (2). Here, the data in a temperature range of $T < 1.6$ K
199 ($\approx 0.28T_c$ of the SmB₆/YB₆ bilayers) is fitted due to the reason described in Sec. II B. The
200 best fit is determined by finding the fitting parameters that minimize the root-mean-square
201 error σ of $\Delta\lambda_{eff}(T)$ between the experimental data and the model fit curves. The best fit
202 gives $\lambda_S(0) = 227 \pm 2$ nm (The determination of the error bar is described in Appendix C 2).
203 A comparison between the estimated $\lambda_S(0)$ of the YB₆ thin film and that obtained in other
204 work is discussed in the Appendix A 1

205 We now fix the value of $\lambda_S(0)$ of the YB₆ layer and focus on extracting the characteristic
206 lengths of the induced superconductivity of the bilayers. Recent PCS measurements on a
207 series of SmB₆/YB₆ bilayers³⁹ help to reduce the number of fitting parameters: the point
208 contact measurement on the bilayer with $t_{SmB_6} = 20$ nm at 2 K showed perfect Andreev
209 reflection, i.e., conductance doubling at the interface between a metal tip and the top sur-
210 face of the SmB₆, indicating that the entire 20 nm thick SmB₆ layer is proximity-coupled.

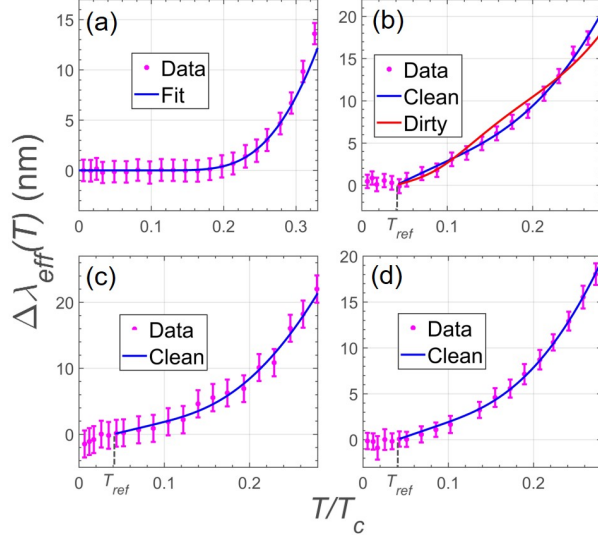


FIG. 3. $\Delta\lambda_{eff}(T)$ vs. T/T_c data and fits for SmB_6/YB_6 bilayers at low temperature, $T/T_c < 0.3$. (a) The single layer YB_6 (100 nm) ($t_{\text{SmB}_6} = 0$ nm). The magenta points are data, and the blue line is a fit from the electromagnetic screening model. (b) The bilayer with $t_{\text{SmB}_6} = 20$ nm. The blue line is a fit with the clean limit temperature dependence of $\xi_N(T)$, and the red line is a fit with the dirty limit temperature dependence. (c) and (d) The bilayers with $t_{\text{SmB}_6} = 40$ nm and 100 nm, respectively.

211 Therefore, d_N is fixed to 20 nm when fitting the $\Delta\lambda_{eff}(T)$ data of the bilayer with $t_{\text{SmB}_6} = 20$
 212 nm.

213 The fitting is conducted with the clean and the dirty limit temperature dependence of
 214 $\xi_N(T)$ as shown in Fig. 3(b). The clean limit fit (blue) gives $\xi_N^{clean}(2\text{K}) = 52 \pm 1$ nm,
 215 $\lambda_N(0, 0) = 340 \pm 2$ nm with σ of 0.237. On the other hand, the dirty limit fit (red) gives
 216 $\xi_N^{dirty}(2\text{K}) = 262 \pm 180$ nm, $\lambda_N(0, 0) = 505 \pm 7$ nm with σ of 0.780. According to the fitting
 217 result, not only does the dirty limit fit apparently deviate from the data points, but also
 218 the σ of the dirty limit fit is three times larger than that of the clean limit fit, implying
 219 that the clean limit is more appropriate for describing $\xi_N(T)$ of the SmB_6 layer. Henceforth,
 220 the $\Delta\lambda_{eff}(T)$ data for the bilayers with other t_{SmB_6} is fit using the clean limit temperature
 221 dependence of ξ_N . Also, the obtained value of $\xi_N(2\text{K}) = 52$ nm will be used when the data
 222 of the bilayers with other t_{SmB_6} is fitted, as the Fermi velocity of the surface bands, which
 223 determines the value of ξ_N , does not have a clear TI layer thickness dependence.⁸

224 For the bilayers with $t_{\text{SmB}_6} = 40$ and 100 nm, d_N is now set to be a free fitting parameter.

Characteristic lengths	SmB ₆ layer thickness		
	20 nm	40 nm	100 nm
$\xi_N(2K)$ (nm)	52 ± 1	52*	52*
d_N (nm)	20*	8 ± 2	10 ± 1
$\lambda_N(0, 0)$ (nm)	340 ± 2	159 ± 2	207 ± 2

TABLE I. Summary of the extracted characteristic lengths from the electrodynamic screening model for TI/SC bilayers for different SmB₆ layer thickness. All fits on the bilayers assume $\lambda_S(0) = 227$ nm which is obtained from the fitting on the single layer YB₆. Note that the values with an asterisk are fixed when the fitting is conducted. d_N (the proximitized thickness) of the thin SmB₆ layer (20 nm) is larger than that of the thick SmB₆ layers (40, 100 nm) because of the slight overlap in the wavefunction between the top and bottom surface states in the 20 nm SmB₆ layer. A detailed discussion of the values of the fitting parameters can be found in Sec. VI.

225 As seen from Fig. 3(c) and (d), the resulting fit line gives $d_N = 8 \pm 2$ nm, $\lambda_N(0, 0) = 159 \pm 2$
226 nm for the bilayer with $t_{\text{SmB}_6} = 40$ nm, and $d_N = 10 \pm 1$ nm, $\lambda_N(0, 0) = 207 \pm 2$ nm for
227 the bilayer with $t_{\text{SmB}_6} = 100$ nm. The estimated $d_N \approx 9$ nm is much smaller than t_{SmB_6} ,
228 which is consistent with the absence of induced order parameter in the top surface of 40
229 and 100 nm thick SmB₆ layers measured by point contact spectroscopy.³⁹ A summary of the
230 estimated characteristic lengths $\xi_N(2K)$, d_N , and $\lambda_N(0, 0)$ for the case of 20, 40, and 100 nm
231 thick SmB₆ layers on top of YB₆ is presented in Table. I.

232 VI. DISCUSSION

233 We now discuss the implications of these results and propose a microscopic picture for the
234 proximity coupled bilayers. The important implication of the above results is the absence
235 of Meissner screening in the bulk of proximity-coupled SmB₆, which is consistent with the
236 existence of an insulating bulk region inside the SmB₆ layer. If the entire SmB₆ layer is
237 conducting without an insulating bulk inside, the proximity-coupled thickness d_N should be
238 equal to t_{SmB_6} for thicker films too, considering the long normal coherence length of ≈ 52
239 nm. In that case, as t_{SmB_6} increases, one would expect a continuous evolution of stronger
240 $\Delta\lambda(T)$ as seen in the Cu/Nb system (Fig. 1(c)), which is not observed in Fig. 1(b). Also,

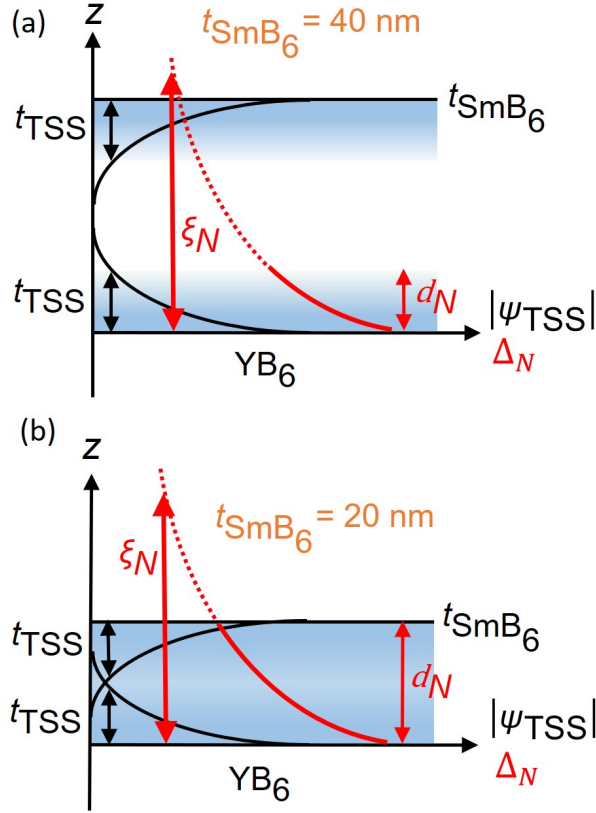


FIG. 4. Schematic view (not to scale) of the proposed position dependence of the surface states wavefunction $|\psi_{\text{TSS}}(z)|$ (black) and induced order parameter $\Delta_N(z)$ (red) in the SmB₆/YB₆ bilayer for the case of $t_{\text{SmB}_6} =$ (a) 40 nm, and (b) 20 nm. The $|\psi_{\text{TSS}}(z)|$ is also visualized by the blue gradations in the SmB₆ layer. The sketches are based on the estimated normal coherence length $\xi_N(2\text{K}) = 52 \text{ nm}$ and the surface state thickness $t_{\text{TSS}} \approx 9 \text{ nm}$. In a thick SmB₆ layer (a), only the bottom surface is proximitized so that $d_N = t_{\text{TSS}} = 9 \text{ nm}$. In a thin SmB₆ layer (b), through the wavefunction overlap between the top and bottom surface states, the entire SmB₆ layer is proximitized so that $d_N = t_{\text{SmB}_6} = 20 \text{ nm}$.

241 the estimated $d_N \approx 9 \text{ nm}$ for the bilayers with $t_{\text{SmB}_6} = 40$ and 100 nm is much smaller than
 242 half of t_{SmB_6} . As illustrated in Fig. 4(a), this situation can only be explained if a thick
 243 insulating bulk region of $t_{\text{bulk}} \approx 22$ and 82 nm exist in the bilayers with $t_{\text{SmB}_6} = 40$ and 100
 244 nm respectively.

245 This thick insulating bulk provides a spatial separation between the top and bottom
 246 surface conducting states, not allowing the order parameter to propagate to the top surface.
 247 Thus, only the bottom surface states are proximitized in the $t_{\text{SmB}_6} = 40$ and 100 nm cases,

248 and hence one can conclude that the proximitized thickness $d_N \approx 9$ nm in these cases equals
 249 the thickness of the surface states t_{TSS} . Note that this confirmation of the presence of the
 250 insulating bulk in the TI layer cannot be made solely from the PCS study. Even if the PCS
 251 study observed the absence of the order parameter on the top surface of the TI layer (SmB₆
 252 in this case), it could be either due to an insulating bulk, or due to a short normal coherence
 253 length $\xi_N < t_{\text{SmB}_6}$. The large value of $\xi_N = 52$ nm, which is larger than $t_{\text{SmB}_6} = 40$ nm,
 254 rules out the latter scenario and confirms the presence of an insulating bulk inside the SmB₆
 255 layers.

256 This picture is also consistent with the observation that the entire SmB₆ layer with
 257 $t_{\text{SmB}_6} = 20$ nm is proximity-coupled (Fig. 4(b)); the top and the bottom conducting surface
 258 state wavefunctions are likely to be weakly overlapped based on $2t_{\text{TSS}} \approx t_{\text{SmB}_6}$ through the
 259 exponentially decaying profile (Fig. 4(b)). Thus the induced order parameter is able to
 260 reach to the top surface states, giving $d_N = 20$ nm for this case. Although such overlap is
 261 expected to open a hybridization gap in the surface states, the fact that 20 nm SmB₆ on YB₆
 262 is entirely proximity-coupled implies that the opened gap is much smaller than the energy
 263 difference between the Fermi level of SmB₆ and the Dirac point. Note that topological
 264 protection might not be affected by such weak hybridization, provided that the Fermi level
 265 is sufficiently far away from the Dirac point present in thick SmB₆.⁸

266 Note that crystalline disorder in the SmB₆ thin film layer, such as dislocations or grain
 267 boundaries, may create conduction paths and lead to the propagation of superconducting
 268 order parameter through the bulk.⁵⁴ However, if such disorder creates significant conduction
 269 paths, the proximity coupled thickness in 40 and 100 nm thick SmB₆ layer are expected to
 270 be inconsistent with each other and much longer than the value (≈ 9 nm) we estimated here.
 271 Therefore, we believe possible propagation of superconducting order parameter through the
 272 bulk in the 40 and 100 nm thick SmB₆ layer is negligible.

273 Besides confirming the existence of an insulating bulk in the SmB₆ layer, the extracted
 274 fitting parameters based on the electromagnetic model provide an estimate for the charac-
 275 teristic lengths such as ξ_N , λ_N , and t_{TSS} , as seen from Sec. V. ξ_N provides information on
 276 the spatial distribution of the induced order parameter in the TI layer. λ_N dictates elec-
 277 trodynamic screening response of the TI/SC bilayer system. t_{TSS} determines a minimum
 278 required thickness of the TI layer to maintain its topological properties. For example, if
 279 the thickness of the device is too thin ($t_{\text{SmB}_6} \sim t_{\text{TSS}}$), the wavefunction overlap between the

280 top and bottom surface states becomes significant, which opens a large hybridization gap
281 up to the Fermi level. As a result, the surface states lose not only electrical conduction but
282 also lose the spin-momentum locking property,⁸ which is a key element of the topological
283 phenomenon observed in this bilayer system.³⁹

284 VII. CONCLUSION

285 In summary, a microwave Meissner screening study is introduced and utilized to in-
286 vestigate the spatially dependent electrodynamic screening response and the corresponding
287 properties of the TI/SC bilayers. The advantages of the study in investigating the properties
288 of a TI/SC system is demonstrated by the measurement and modeling of the temperature
289 dependence of the screening with systematic TI-layer thickness variation. The study goes
290 beyond the surface response to examine the screening properties of the entire TI layer, and
291 uncovers the existence of an insulating bulk in the TI layer conclusively. Also, the study
292 provides an estimate for characteristic lengths of the TI/SC bilayer, which sheds light on
293 the microscopic details of the induced superconductivity in the proximity coupled TI layer.

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301 Appendix A: Validity of the extracted sample properties

302 1. Validity of the estimated magnetic penetration depth of the YB₆ thin film

303 In the main text (Fig. 2(a)), the model fit gives $\lambda_S(0) = 227 \pm 2$ nm (and $2\Delta(0)/k_B T_c =$
304 3.66 ± 0.01) for the YB₆ thin film with thickness of 100 nm. This estimate is larger than
305 the value $\lambda_S(0) \approx 134$ nm measured by muon spin rotation study from a single crystal YB₆

	This work	previous work
v_F	8.5	$4^{60,61}$ (ARPES)
(10^4 m/s)		9^{38} (transport)
		0.6^{57} (STM)
		0.4^{62} (theory)
t_{TSS} (nm)	≈ 9	6^{38} (transport)
		32^{63} (spin pumping)

TABLE II. v_F for SmB₆ derived from the estimated ξ_N from the microwave Meissner screening study for the comparison to the results from the other techniques. The estimated t_{TSS} is also compared to that from the previous works.

sample²⁹ with higher $T_c = 6.94$ K (and $2\Delta(0)/k_B T_c = 3.67$). This is reasonable considering that the higher T_c implies a longer mean free path l_{mfp} ,⁵⁵ and shorter $\lambda_S(0)$ through the relation $\lambda_S(0) = \lambda_L(0)\sqrt{1 + \xi_0/l_{mfp}}$ ⁵⁶ where $\lambda_L(0)$ is London penetration depth at $T = 0$ K and ξ_0 is BCS coherence length of the superconductor.

2. Validity of the extracted characteristic lengths of the SmB₆/YB₆ bilayers

To confirm the validity of the estimated values of the characteristic lengths of the SmB₆/YB₆ bilayers obtained in Sec. V, one of the parameters ξ_N is converted to the Fermi velocity v_F , whose value has been reported from other measurements on SmB₆. From the clean limit relation $\xi_N = \hbar v_F/2\pi k_B T$, one arrives at $v_F = 8.5 \times 10^4$ m/s. As seen from Table. II, this value is similar to the values obtained from the ARPES and DC transport measurements. However, the v_F values from theory and STM are an order of magnitude smaller. Recent DFT calculation accompanied by STM measurements^{57,58} and an independent theoretical calculation⁵⁹ show that the discrepancy can be explained by termination-dependent band bending at the surface of SmB₆.

Appendix B: Dielectric resonator setup

The dielectric resonator setup was originally developed to study dielectric properties of materials⁴¹ and subsequently used to characterize microwave properties of high- T_c cuprate

323 films.^{42,44,64} The comprehensive details of the dielectric resonator used in this work can be
 324 found in Ref.⁴³ Here, a summary of the key features is introduced for the reader's con-
 325 venience. The resonator consists of a top and bottom metallic plate which confine the
 326 microwave field inside the resonator just as in a cavity (Fig. 5). A disk with high dielectric
 327 constant, which is placed on top of a superconducting thin film sample, concentrates the
 328 incident microwave fields injected from the excitation loop (p1 of Fig. 5) in the disk and
 329 generates a microwave resonance at certain frequencies f_0 . These resonant frequencies f_0 are
 330 determined mainly by the dimension and the dielectric constant of the disk. In our setup,
 331 a 3 mm diameter, 2 mm height rutile (TiO_2) disk is used as the dielectric disk. Rutile is
 332 chosen as the dielectric material for the resonator because it has very high dielectric constant
 333 ($\epsilon_c > 250$, $\epsilon_{a,b} > 120$ where a, b are the in-plane crystallographic axes and c is the out-of-
 334 plane axis) compared to those of sapphire ($\epsilon_{a,b,c} \sim 10$) or other dielectric materials. The
 335 high dielectric constant of the rutile helps to minimize the size of the disk, while maintaining
 336 the resonant frequencies in the microwave regime. The smaller the measurement area is,
 337 the more likely the sample will have homogeneous properties. Among the resonant modes
 338 generated by the dielectric resonator, the TE_{011} mode (~ 11 GHz) induces a radial magnetic
 339 field and a circulating screening current on the sample surface. This circulating current
 340 helps to support the microwave transmission resonance. If there occurs any change of the
 341 sample properties such as superfluid density, that change can be studied through the change
 342 of the microwave transmission resonance. Note that the typical value of the quality factor
 343 of the TE_{011} mode in this work is on the order of 10^4 . The simulated (HFSS) microwave
 344 magnetic field at the surface of the sample for the TE_{011} mode is $\approx 8\mu\text{T}$ when the input
 345 microwave power P_{in} is -20 dBm. In this range of P_{in} , the resonance frequency does not
 346 show P_{in} dependence, showing that the sample is in the linear response regime in terms of
 347 the microwave magnetic field.

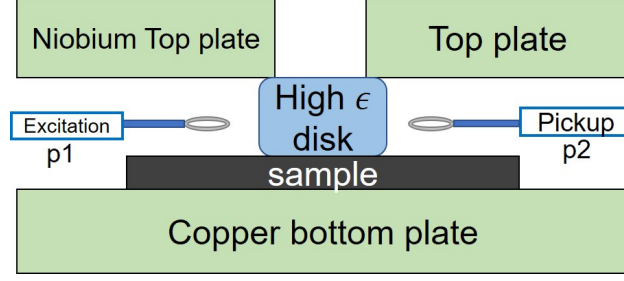


FIG. 5. Schematic cross-section diagram of the dielectric resonator setup for a microwave transmission resonance with a sample.

348 Appendix C: Measurement of the effective penetration depth

349 1. Determining resonance frequency and corresponding effective penetration 350 depth

351 Microwave transmission data $S_{21}(f)$ near the resonance is fitted with the phase versus
352 frequency fitting procedure,⁶⁵ to precisely determine the resonance frequency f_0 . Measure-
353 ment and fitting of $S_{21}(f)$ data are repeated for different temperatures. From this, the
354 temperature dependence $\Delta f_0(T) = f_0(T) - f_0(T_{ref})$ can be acquired. This temperature
355 dependence of the resonance frequency can be converted to that of the effective penetration
356 depth of a superconducting thin film sample by^{45,46,66}

$$\Delta\lambda_{eff}(T) = -\frac{G_{geo}}{\pi\mu_0} \frac{\Delta f_0(T)}{f_0^2(T)}. \quad (C1)$$

357 Here, $G_{geo} = \omega\mu_0 \int_V dV |H(x, y, z)|^2 / \int_S dS |H(x, y)|^2 = 225.3 \Omega$ is the geometric factor
358 calculated numerically using the field solution inside the resonator for TE₀₁₁ mode derived
359 by Hakki et al.⁴¹

360 2. Determining error bars for the effective penetration depth and estimated fit 361 parameters

362 The error bar in the effective penetration depth $\Delta\lambda_{eff}(T)$ is determined by the error bar
363 of determination of the resonance frequency $f_0(T)$. The error bar of the f_0 is determined
364 by a deviation of f_0 from the estimated value, which increases the root-mean-square error
365 σ of the fit by 5%. The main source of the error bar of f_0 is the noise in $S_{21}(f)$ data. If

366 the signal to noise ratio of S_{21} is large (small) which makes the $S_{21}(f)$ curve well- (poorly-)
 367 defined, f_0 can have a narrower (wider) range of values while giving fits with similar values
 368 of σ . Once the error bar of f_0 is determined, with the standard error propagation from the
 369 relation between $\Delta\lambda_{eff}(T)$ and $f_0(T)$, the error bar in the $\Delta\lambda_{eff}(T)$ data is estimated. The
 370 error bar for the estimated fit parameters ($\xi_N(T_0)$, $\lambda_N(0,0)$, and d_N) obtained from fitting
 371 $\Delta\lambda_{eff}(T)$ data are determined by a deviation from the estimated value which increases σ
 372 by 5%.

373 Appendix D: Further remarks on the electromagnetic screening model

374 1. Boundary conditions

375 Although explained in detail in Ref.¹³ for the reader's convenience, the equation and the
 376 boundary conditions for the magnetic field inside a proximity-coupled bilayer are described
 377 below. First, by combining Maxwell's equations with London's equation, one can obtain an
 378 equation for the tangential magnetic field for the bilayer

$$\frac{d^2 H(z)}{dz^2} + \frac{2}{\lambda_{N,S}(z)} \frac{d\lambda_{N,S}(z)}{dz} \frac{dH(z)}{dz} - \frac{1}{\lambda_{N,S}^2(z)} H(z) = 0. \quad (\text{D1})$$

The boundary conditions for the tangential magnetic field for the geometry shown in Fig. 1
 of the main article are as follows,

$$H(d_N) = H_0, \text{ (top surface)} \quad (\text{D2})$$

$$H(-d_S) = 0, \text{ (bottom surface)} \quad (\text{D3})$$

$$H(0^+) = H(0^-), \text{ (interface)} \quad (\text{D4})$$

$$\lambda_N^2(0, T) \frac{dH(z)}{dz} \Big|_{z=0^+} = \lambda_S^2(0, T) \frac{dH(z)}{dz} \Big|_{z=0^-}, \quad (\text{D5})$$

379 where $d_N \leq t_{SmB_6}$ is the proximity-coupled thickness of the normal layer and $d_S = t_{YB_6}$
 380 is the thickness of the parent superconductor. The last boundary condition is a continuity
 381 condition for the superfluid velocity at the interface.

382 2. Field solutions

With Eq.(D1) and the approximated spatial profile of the induced order parameter in the
 normal layer $\Delta_N(z, T) = \Delta_N(0, T)e^{-z/\xi(T)}$ and the normal penetration depth $\lambda_N(z, T) =$

$\lambda_N(0, T)e^{+z/\xi_N(T)}$, one can obtain the spatial profile of the magnetic field in the normal and superconducting layer as follows:¹³

$$H_N(z, T) = ApI_1(p) + BpK_1(p), \quad (0 \leq z \leq d_N) \quad (\text{D6})$$

$$H_S(z, T) = Ce^{z/\lambda_S} + De^{-z/\lambda_S}, \quad (-d_S \leq z \leq 0), \quad (\text{D7})$$

383 Here, the parameter p is defined as $p(z, T) = (\xi_N(T)/\lambda_N(z, T))e^{-z/\xi_N(T)}$ and I_1, K_1 are
 384 the modified Bessel functions of the first, second kind. The coefficients A, B, C, D can be
 385 calculated using the boundary conditions. The corresponding spatial profile of the current
 386 density can be obtained from z derivative of the magnetic field profile. After all the coef-
 387 ficients are obtained, the spatial profiles of the magnetic field and the current density of a
 388 normal/superconductor bilayer are fully determined. When calculating the inductance, the
 389 microwave loss is ignored so that the supercurrent density of the bilayer is approximated as
 390 the total current density $J_s \simeq J$. This is a valid approximation since the temperature range
 391 of the measurement ($0 \sim 1.6$ K) is well below T_c of the bilayer (~ 5.86 K) and the microwave
 392 photon energy (~ 0.044 meV) is much lower than the zero temperature superconducting gap
 393 of the YB_6 (> 1 meV).²⁹

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