



CHORUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

Mechanism of strong enhancement of anomalous Nernst effect in Fe by Ga substitution

Hiroyasu Nakayama, Keisuke Masuda, Jian Wang, Asuka Miura, Ken-ichi Uchida, Masayuki Murata, and Yuya Sakuraba

Phys. Rev. Materials **3**, 114412 — Published 25 November 2019

DOI: [10.1103/PhysRevMaterials.3.114412](https://doi.org/10.1103/PhysRevMaterials.3.114412)

1 **Mechanism of strong enhancement of anomalous Nernst effect in Fe by** 2 **Ga substitution**

3
4 Hiroyasu Nakayama^{1,2,a)}, Keisuke Masuda², Jian Wang^{1,2}, Asuka Miura², Ken-ichi
5 Uchida^{2,3,4,5}, Masayuki Murata⁶, and Yuya Sakuraba^{2,7,b)}

6
7 ¹International Center for Young Scientists, National Institute for Materials Science,
8 Tsukuba 305-0047, Japan

9 ²Research Center for Magnetic and Spintronic Materials, National Institute for
10 Materials Science, Tsukuba 305-0047, Japan

11 ³Institute for Materials Research, Tohoku University, Sendai 980-8577, Japan

12 ⁴Center for Spintronics Research Network, Tohoku University, Sendai 980-8577,
13 Japan

14 ⁵Department of Mechanical Engineering, The University of Tokyo, Tokyo
15 113-8656, Japan

16 ⁶National Institute of Advanced Industrial Science and Technology, Tsukuba
17 305-8568, Japan

18 ⁷PRESTO, Japan Science and Technology Agency, Saitama, 332-0012, Japan

19
20 a) Electronic mail: NAKAYAMA.Hiroyasu@nims.go.jp

21 b) Electronic mail: SAKURABA.Yuya@nims.go.jp

22 23 **Abstract**

24 We have investigated the anomalous Nernst effect (ANE) in Fe_{1-x}Ga_x
25 alloy films with different Ga atomic compositions ($x = 0 - 0.44$) deposited on MgO
26 (001) single crystalline substrates. We found that the magnitude of the ANE
27 increases with increasing x up to $x = 0.32$ even though the saturation magnetization
28 decreases with increasing x . The magnitude of the ANE reaches to 2.4 $\mu\text{V/K}$ in bcc
29 Fe_{0.68}Ga_{0.32} film, which is two orders of magnitude greater than that of pure Fe film.
30 The magnetotransport measurements and the first-principles calculations revealed
31 that the large ANE in bcc Fe_{1-x}Ga_x is caused by the large transverse Peltier
32 coefficient. The drastic enhancement of the transverse Peltier coefficient with
33 increasing x can be attributed to small Fermi level tuning through the electron
34 doping effect. Thus, we anticipate that our finding will provide a crucial piece of
35 information to enhance the thermopower through the ANE.

36 **Introduction**

37 Thermoelectric power generation based on the thermoelectric
38 phenomena has attracted a great deal of attention in terms of not only basic physics
39 but also application for future environmental friendly power generation
40 technologies, which aims to convert waste heat into electrical energy [1,2]. The
41 most standard method to realize the thermoelectric power generation is utilizing
42 the Seebeck effect [3,4]. The Seebeck effect converts temperature gradient to
43 electric voltage in conductive materials thorough the diffusion of charge carrier
44 [see Fig. 1(a)]. Another approach is to utilize the Nernst effect [5,6]. The Nernst
45 effect is a phenomenon that generates electric voltage along the outer product of
46 the temperature gradient and the applied magnetic field. Therefore, it is necessary
47 to apply the external magnetic field to the thermoelectric materials in order to
48 obtain the electric voltage induced by the Nernst effect. When we replace a
49 thermoelectric material into a ferromagnet, however, it is not always necessary to
50 apply the external magnetic field to obtain the magnetization direction dependent
51 thermoelectric voltage. This phenomenon is known as the anomalous Nernst effect
52 (ANE) [7–16]. The ANE is a phenomenon that generates electric voltage along the
53 outer product of the temperature gradient and the magnetization in ferromagnet
54 [see Fig. 1(b)]. The recently discovered longitudinal spin-Seebeck effect (SSE)
55 induced inverse spin-Hall effect is known to exhibit similar symmetry as the
56 ANE [17,18]. In the emerging field of spin-caloritronics, the ANE and the SSE
57 play a leading role because these phenomena offer an approach to develop
58 thermoelectric devices based on spin-heat coupling. In particular, the ANE in
59 materials with a large anisotropy between electric and thermal conductivity and
60 the SSE might go beyond the limitation of energy conversion efficiency by the
61 Wiedemann-Franz law [2,14]. Recent works demonstrate that the thermoelectric
62 voltage through the ANE and the SSE is dramatically enhanced by utilizing the
63 simple lateral thermopile structures [12,19], which will pave the way towards the
64 thermoelectric device **such as a heat flow sensor with high flexibility, low thermal**
65 **resistivity, and** low cost [14]. However, it is still necessary to explore materials
66 showing larger efficiency of thermoelectric conversion [14,20–22].

67 **In order to develop an ANE device in this direction, it** is an important
68 issue to find materials consisting of abundant and nontoxic elements that exhibits
69 large thermoelectric conversion efficiency. Therefore, the ANE in Fe-based
70 compounds and alloys are worth to be investigated. Recently, the large ANE was
71 reported in galfenol (Fe-Ga alloy) polycrystalline wire [23], **where Fe-Ga alloys**

72 are known as magnetostrictive materials. Interestingly, it shows large
73 thermopower of ANE ($\sim 3 \mu\text{V/K}$) in simple binary alloy systems although the
74 value in single crystalline bulk Fe is about $-0.1 \mu\text{V/K}$ [24]. However, the previous
75 work focused on the commercially available polycrystalline galfenol and its Ga
76 composition is fixed at $x = 0.15$. Therefore, the underlying mechanism of the
77 strong enhancement of the ANE from Fe to galfenol has not been clarified at all. In
78 this study, we investigate the ANE in epitaxial Fe-Ga thin films with different
79 compositions. We prepared $\text{Fe}_{1-x}\text{Ga}_x$ thin films on MgO (001) single crystalline
80 substrates by co-sputtering technique. We found that the magnitude of the ANE in
81 Fe-Ga alloys increases with increasing x up to $x = 0.32$ even when the crystal
82 structure is preserved in the same simple bcc structure. The magnitude of the ANE
83 reaches to $2.4 \mu\text{V/K}$ in $\text{Fe}_{0.68}\text{Ga}_{0.32}$ film, which is two orders of magnitude greater
84 than that of Fe film [16]. The systematic thermoelectric and magnetotransport
85 measurements including the Seebeck effect and the anomalous Hall effect
86 measurements revealed that the large ANE in $\text{Fe}_{1-x}\text{Ga}_x$ is mainly attributed to the
87 large transverse Peltier coefficient, which agrees with the prediction based on the
88 first-principles calculations.

90 Methods

91 The samples were $\text{Fe}_{1-x}\text{Ga}_x$ thin films (Ga atomic composition $x = 0 -$
92 0.44) deposited on MgO (001) single crystalline substrates at room temperature by
93 co-sputtering technique with Fe and $\text{Fe}_{0.50}\text{Ga}_{0.50}$ sputtering targets, where a base
94 pressure was in the vicinity of 2×10^{-7} Pa. The thickness of the films was fixed at
95 40 nm , where the real thickness is determined by using the wavelength dispersive
96 X-ray fluorescence analysis (WDXRF) and X-ray diffraction (XRD). In order to
97 prevent films from oxidation, a 3-nm-thick MgO capping layer was deposited by rf
98 magnetron sputtering. The composition of the $\text{Fe}_{1-x}\text{Ga}_x$ films was measured by
99 WDXRF, where the Ga atomic composition was $x = 0.44$ when we fabricated
100 $\text{Fe}_{1-x}\text{Ga}_x$ films by a $\text{Fe}_{0.50}\text{Ga}_{0.50}$ alloy target. The magnetic properties of the
101 $\text{Fe}_{1-x}\text{Ga}_x$ films were measured with a vibrating sample magnetometer (VSM). The
102 crystal structure was investigated by XRD with a $\text{Cu } K_\alpha$ X-ray source and a
103 two-dimensional detector (PILATUS 100K/R, Rigaku Co.). Thin specimens for
104 scanning transmission electron microscope (STEM) observations were prepared
105 by the low-energy, low-angle Ar-ion milling using a precision ion polishing
106 system (PIPS, GATAN Model-691). STEM observations were performed using a
107 FEI Titan G2 80–200 STEM with a probe forming aberration corrector operated at

108 200 kV. A probe current of 100 pA was used for the STEM imaging. Element
109 mapping was carried out by means of energy-dispersive X-ray spectroscopy (EDS)
110 using an in-column symmetrically distributed four windowless silicon-drift X-ray
111 detectors (SDD) that enable a high detection efficiency at atomic resolution. The
112 Seebeck effect was measured by using the Seebeck Coefficient/Electric Resistance
113 Measurement System (ZEM-3, ADVANCE RIKO, Inc.). The substrates were
114 cleaved into a piece with a lateral dimension of $\sim 7.6 \times 10.0 \text{ mm}^2$. The films were
115 patterned into a Hall bar structure with a width of 3.0 mm and a length of 7.0 mm
116 by using photolithography and Ar ion milling. The anomalous Hall effect (AHE)
117 measurements were conducted at room temperature and 10 K with applying the
118 perpendicular magnetic field by using a Physical Property Measurement System
119 (PPMS, Quantum Design Co., Ltd.). The ANE was also measured at room
120 temperature with applying perpendicular magnetic field in PPMS. The Seebeck
121 effect was also measured simultaneously to calibrate the applied temperature
122 gradient. The relationship between the applied temperature gradient and the
123 Seebeck voltage in FeGa film was confirmed at outside of PPMS in advance by
124 utilizing an infrared thermal camera, where the sample surface is coated by black
125 ink. Then, the applied temperature gradient was calibrated through the observed
126 Seebeck voltage in PPMS. Here, the thermal conductance of the MgO substrate is
127 much greater than that of $\text{Fe}_{1-x}\text{Ga}_x$ thin films, which results in the fact that the
128 thermal conductance of $\text{Fe}_{1-x}\text{Ga}_x$ thin films does not influence the temperature
129 gradient in the films [25]. The electric resistivity was measured by a dc four-probe
130 method with a constant dc current of 300 μA . All the measurements, except for the
131 AHE measurements at 10 K, were performed at room temperature.

132

133 **Experimental results & Discussions**

134 To characterize the magnetic and structural properties of the $\text{Fe}_{1-x}\text{Ga}_x$ thin
135 films, we conducted the VSM, the XRD, and the TEM measurements. Figure 2(a)
136 shows the out-of-plane XRD pattern for $\text{Fe}_{1-x}\text{Ga}_x$ thin films. In order to clearly
137 show the diffraction peak from $\text{Fe}_{1-x}\text{Ga}_x$ thin films, we subtracted the XRD pattern
138 of a MgO (001) substrate without $\text{Fe}_{1-x}\text{Ga}_x$ thin films. As shown in Fig. 2(a), only
139 (002) peak from the simple bcc $\text{Fe}_{1-x}\text{Ga}_x$ are observed for all of the samples except
140 for $x = 0.44$. In a $\text{Fe}_{0.54}\text{Ga}_{0.44}$ film, the super lattice (001) peak of B2-FeGa is also
141 observed in the vicinity of $2\theta = 31^\circ$. These results clearly show that all the $\text{Fe}_{1-x}\text{Ga}_x$
142 thin films are epitaxially grown. Figure 2(b) shows the cross-sectional high-angle
143 annular dark-field scanning transmission electron microscopy (HAADF-STEM)

144 image and corresponding energy-dispersive X-ray spectroscopy (EDS) elemental
 145 maps of $\text{Fe}_{0.81}\text{Ga}_{0.19}$ film. In Fig. 2(b), one can find the continuous layer with flat
 146 surface and uniform Ga distribution in the $\text{Fe}_{0.81}\text{Ga}_{0.19}$ film, whereas the slight
 147 segregation of Ga exists at the surface and interface. **The slight contrast of**
 148 **HAADF-STEM image in Fig. 2(b) can be due to the surface damage caused by Ar**
 149 **ion milling using PIPS.** Figure 2(c) shows the x dependence of lattice constant
 150 determined from position of (002) peak in Fig. 2(a). In our $\text{Fe}_{1-x}\text{Ga}_x$ ($x = 0 - 0.44$)
 151 films, the (002) peak gradually shifts toward lower angle with increasing Ga, thus
 152 lattice constant almost monotonically increases with increasing x . These results
 153 indicate that Ga replaces Fe without structural transformation despite the fact that
 154 the solubility of Ga to Fe is less than 15 at.% at room temperature in the
 155 equilibrium binary phase diagram [26], suggesting that our sputtered $\text{Fe}_{1-x}\text{Ga}_x$
 156 films have the non-equilibrium bcc structure in which Ga randomly occupied Fe
 157 site up to 32 at.%. Figure 2(d) shows the Ga composition x dependence of the
 158 saturation magnetization M_s for $\text{Fe}_{1-x}\text{Ga}_x$ thin films, **where M_s is determined by**
 159 **using VSM with in-plane magnetic field along the [001] orientation for $\text{Fe}_{1-x}\text{Ga}_x$**
 160 **thin films [also see the inset of Fig. 2(d)].** The M_s decreases with increasing x ,
 161 which can be due to the replacement of Fe atoms with Ga atoms. The decreasing
 162 tendency of M_s with increasing x is consistent with the theoretically calculated M_s
 163 plotted as open circles in Fig. 2(d). **Here, the theoretically calculated M_s is**
 164 **obtained by the first-principles calculations using the Akai-KKR code [27], the**
 165 **details of which will be explained later.**

166 To investigate the mechanism of the ANE in $\text{Fe}_{1-x}\text{Ga}_x$ thin films, we
 167 conducted the AHE measurements. Figure 3 shows the anomalous Hall resistivity
 168 ρ_{yx} plotted as a function of the magnetic field $\mu_0 H$ along the z axis in the $\text{Fe}_{1-x}\text{Ga}_x$
 169 thin films. The inset shows a schematic illustration of an experimental
 170 configuration of the AHE measurements. As one can clearly see in Fig. 3, the
 171 magnitude of the ρ_{yx} increases with increasing x . The magnetization reversal field
 172 of $\text{Fe}_{1-x}\text{Ga}_x$ thin films tends to decrease with increasing x , which corresponds to the
 173 decreasing of the demagnetization field due to the reduction of the saturation
 174 magnetization M_s in $\text{Fe}_{1-x}\text{Ga}_x$ thin films with increasing x . As shown in Figs.
 175 4(a)-4(c), the ρ_{yx} and the ρ_{xx} increase with increasing x , whereas the magnitude of
 176 $|\theta_{\text{AHE}}|$ exhibits a maximum value in the vicinity of $x = 0.16$. As shown in Fig. 4(d),
 177 the $|\sigma_{xy}|$ tends to decrease with increasing x in both 10 K and 300 K. **The inset of**
 178 **4(d) shows the $|\sigma_{xy}|$ dependence of σ_{xx} . The solid line for lower (larger) σ_{xx} is the fit**
 179 **according to the scaling relationship $|\sigma_{xy}| \propto \sigma_{xx}^n$ with $n = 1.6$ ($n = 0$), which**

180 corresponds to the scaling behavior in a dirty region (intrinsic moderately dirty
181 region).

182 In order to investigate the origin of large AHE in Fe-Ga thin films, we
183 calculated the density of states (DOS) of Fe-Ga with bcc structure by using the
184 Akai-KKR code [27] based on the density-functional theory and the
185 Korringa-Kohn-Rostoker method [28,29]. The generalized gradient
186 approximation [30] was adopted for the exchange-correlation energy and the
187 chemical disorder between Fe and Ga atoms was treated by the
188 approximation. We set the lattice constants of Fe, Fe_{0.9}Ga_{0.1}, and Fe_{0.8}Ga_{0.2} to
189 2.853, and 2.861 Å, respectively, which were determined following the Vegard's
190 law by the linear fit to the data ($x = 0 - 0.32$) of Fig. 2(c) with the fixed value of
191 ($x = 0$, $a = 2.846$ Å). In our calculations, 5832 ($= 18 \times 18 \times 18$) k points were
192 for the Brillouin-zone integration and the imaginary part of the energy was
193 as 0.001 Ry. Figure 5(a) shows the DOSs of Fe, Fe_{0.9}Ga_{0.1}, and Fe_{0.8}Ga_{0.2}, where
194 indicates the Fermi level. With increasing the Ga content, the DOS moves to
195 energies keeping the overall energy dependence; namely, the effect of the Ga
196 doping into bcc Fe can be considered as a rigid-band shift of the band structure of
197 bcc Fe. Figure 5(b) shows the projected density of state (PDOS) of Fe and
198 Fe_{0.8}Ga_{0.2}, from which we see that the energy shift of the total DOS mainly
199 from that of the Fe PDOS. Such an energy shift in the Fe PDOS can be
200 as an electron-doping effect from Ga *s* and *p* orbitals to Fe *d* orbitals. Actually, as
201 shown in Figs. 5(c) and 5(d), Ga *s* and *p* orbitals in Fe_{0.8}Ga_{0.2} have finite PDOSs
202 around ϵ_F , indicating that electrons in these orbitals can contribute to the electron
203 doping into Fe *d* orbitals. Therefore, it is reasonable to discuss a tendency of
204 and ANE against Ga concentration x based on the theoretical calculation of
205 dependence of those in pure Fe. Previously Weischenberg *et al.* performed the
206 *ab-initio* calculation of the contribution of intrinsic mechanism on AHE in Fe and
207 reported the energy dependence of σ_{xy}^{int} in Fe [31]. Thus, here we argue the
208 tendency of AHE against Ga concentration in Fe_{1-x}Ga_x films on the basis of their
209 calculation for pure Fe. In the theoretical calculation, σ_{xy}^{int} at ϵ_F in Fe is about
210 S/cm and tends to decrease with increasing ϵ to about 400 S/cm at $\epsilon_F + 0.5$
211 Experimentally observed $|\sigma_{xy}|$ shows almost monotonic reduction with x except
212 the drastic increase at $x = 0.03$ [see Fig. 4(d)], which roughly agree with the
213 dependence of the theoretical σ_{xy}^{int} . The smaller magnitude of the experimentally
214 determined $|\sigma_{xy}|$ in our epitaxial Fe_{1-x}Ga_x films with large x than that of the
215 theoretically calculated σ_{xy}^{int} can be explained by the existence of the damping

216 **the intrinsic mechanism of the AHE due to** the electron scattering at the surface
 217 and substrate interface [32]. Since we evaluated σ_{xy} using $\sigma_{xy} = \rho_{yx}/\rho_{xx}^2$ with
 218 the experimentally observed ρ_{yx} and ρ_{xx} shown in Figs. 4(a) and 4(b),
 219 abovementioned scattering that increases residual resistance causes the reduction
 220 of σ_{xy} compared with the theoretically calculated σ_{xy}^{int} , where the Berry curvature
 221 of intrinsic electronic structure determines the magnitude of σ_{xy}^{int} . Large
 222 contribution of the residual resistance in higher x region can be also confirmed by
 223 small RRR shown in Fig. 4(b). Although a mechanism of the enhancement of σ_{xy}
 224 at $x = 0.03$ shown in Fig. 4(d) has not been clarified, the contribution of extrinsic
 225 anomalous Hall effect, skew scattering, can be the possible reason. The σ_{xy} at 10
 226 K and 300 K in $\text{Fe}_{1-x}\text{Ga}_x$ film with $x = 0.03$ shown in Fig. 4(d) exhibit much
 227 larger difference than those of $\text{Fe}_{1-x}\text{Ga}_x$ films with greater x , which can be an
 228 evidence of the existence of skew scattering contribution because the skew
 229 scattering term of AHE $\sigma_{xy}^{\text{skew}}$ is proportional to σ_{xx} , i.e., $\sigma_{xy}^{\text{skew}} \propto \sigma_{xx}$ whereas
 230 σ_{xy}^{int} is independent of σ_{xx} , i.e., $\sigma_{xy}^{\text{int}} \propto \sigma_{xx}^0$ [33,34].

231 Figure 6 shows the **observed** ANE voltage normalized by the width and
 232 applied temperature gradient $(V_{\text{ANE}}/w)\nabla T$ plotted as a function of the external
 233 magnetic field $\mu_0 H$ along the z axis in $\text{Fe}_{1-x}\text{Ga}_x$ thin films. **The thermopower of**
 234 **the ANE S_{ANE} corresponds to the linearly extrapolated value of $(V_{\text{ANE}}/w)\nabla T$ to**
 235 **zero magnetic field from the saturated value at high magnetic field.** The inset
 236 shows a schematic of the experimental configuration of the ANE measurements.
 237 In Fig. 6, one can clearly find that the S_{ANE} tends to increase by Ga substitution in
 238 Fe with increasing x up to $x = 0.32$. Figures 7(a)-7(b) show the x dependence of
 239 (a) the Seebeck coefficient S_{SE} , (b) the S_{ANE} . Previous studies analyzed the ANE
 240 signal by separating S_{ANE} into two components based on the following linear
 241 response equation [8,10],

$$242 \quad S_{\text{ANE}} = \rho_{xx}\alpha_{xy} + \rho_{xy}\alpha_{xx} \quad (1)$$

243 The second term $\rho_{xy}\alpha_{xx}$ (defined as S_{II} here) can be converted to $-S_{\text{SE}} \times \tan\theta_{\text{AHE}}$,
 244 thus this term can be regarded as the transverse thermopower generation from the
 245 AHE of longitudinal carrier flow induced by the Seebeck effect. On the other
 246 hand, the first term $\rho_{xx}\alpha_{xy}$ (defined as S_{I} here) can be considered as an intrinsic
 247 term of the ANE because the transverse Peltier coefficient α_{xy} gives a direct
 248 conversion of applied temperature gradient to transverse current as expressed
 249 with $j_y = \alpha_{xy}\nabla T_x$. Therefore, we also evaluate S_{I} and S_{II} contributions of the
 250 observed ANE in our $\text{Fe}_{1-x}\text{Ga}_x$ thin films as shown in Fig. 7(c). In Fig. 7(a), the
 251 $|S_{\text{SE}}|$ exhibits local maximal value in the vicinity of $x = 0.2$. The S_{SE} also exhibits

252 sign reversal in the vicinity of $x = 0.02$, which presumably due to the Fermi
 253 energy shift because the Seebeck coefficient is proportional to $dN(\epsilon)/d\epsilon$ [35]. As
 254 one can see in Fig. 7(b), the magnitude of the ANE reaches to $2.4 \mu\text{V/K}$ in
 255 $\text{Fe}_{0.68}\text{Ga}_{0.32}$ film, which is two orders of magnitude greater than that of Fe
 256 film [16]. The anomalous Nernst coefficient Q in $\text{Fe}_{0.68}\text{Ga}_{0.32}$ film is $2.2 \mu\text{VT}^{-1}\text{K}^{-1}$,
 257 which is same order of magnitude as that of polycrystalline $\text{Fe}_{0.85}\text{Ga}_{0.15}$ wire
 258 (Fe-Al thin film) reported in the previous works [16,23]. The inset of Fig. 7(b)
 259 shows the M_s dependence of the S_{ANE} , clearly indicating that the S_{ANE} decreases
 260 with increasing the M_s when $M_s > 1.1 \text{ T}$, which is completely different from the
 261 scaling behavior obtained for various ferromagnetic materials. In Fig. 7(b), the
 262 S_{ANE} increases with increasing x up to $x = 0.32$ even though the $|\theta_{\text{AHE}}|$ in $\text{Fe}_{1-x}\text{Ga}_x$
 263 thin films exhibits the largest value in the vicinity of $x = 0.16$ [also see Fig. 4(c)].
 264 This difference of Ga concentration x dependence between the AHE and the ANE
 265 can be understood by considering the possible contribution of the ANE: S_{I} and S_{II} .
 266 As shown in Fig. 7(c), the dominant contribution of the ANE switches in the
 267 vicinity of $x = 0.2$ in $\text{Fe}_{1-x}\text{Ga}_x$ films; S_{I} and S_{II} comparably appears in the films
 268 with $x < 0.2$, but the contribution of S_{I} is dominant with $x > 0.2$. These results
 269 indicate that the longitudinal resistivity ρ_{xx} and the transverse Peltier coefficient
 270 α_{xy} are critical parameters for large S_{ANE} rather than the Seebeck coefficient and
 271 the anomalous Hall angle in $\text{Fe}_{1-x}\text{Ga}_x$ thin films with $x > 0.2$. Therefore, the origin
 272 of the large ANE in $\text{Fe}_{0.68}\text{Ga}_{0.32}$ film is quite different from the case in
 273 ferromagnetic materials such as $\text{Co}_2\text{MnAl}_{1-x}\text{Si}_x$ [22] and Co_2MnGa [21] in which
 274 both S_{I} and S_{II} contribute comparably. Figure 7(d) shows the x dependence of
 275 experimentally determined transverse Peltier coefficient α_{xy} . As shown in Fig.
 276 7(d), the α_{xy} exhibits oscillation behavior with x .

277 According to the generalized Mott formula [31,36–38], the relation
 278 between the σ_{xy} and the α_{xy} at the fixed temperature T is described as

$$279 \quad \alpha_{xy} = -\frac{1}{eT} \int d\epsilon \frac{\partial f}{\partial \mu} (\epsilon - \mu) \sigma_{xy} \quad (2),$$

280 where e , f , and μ are the electronic charge ($e = -|e|$), the Fermi distribution
 281 function, and the chemical potential. In Eq. (2), the integrand becomes finite in
 282 the range of $\sim 0.1 \text{ eV}$ at 300 K due to the existence of $\partial f/\partial \mu$. Here, $\partial f/\partial \mu$ and $(\epsilon$
 283 $-\mu)$ are even and odd functions of ϵ at around μ , respectively. If σ_{xy} is odd
 284 function, the integrand in Eq. (2) becomes even function. Thus, the magnitude
 285 and the sign of the odd function in σ_{xy} at around ϵ_{F} determines the magnitude and
 286 the sign of the α_{xy} . Here we compare the experimental α_{xy} with theoretical value

287 predicted from the $\sigma_{xy}^{\text{int}}(\varepsilon)$ in pure Fe [31]. In Fe, the $\sigma_{xy}^{\text{int}}(\varepsilon)$ was predicted to
 288 behave like the even function of the ε at around ε_{F} [31]. Therefore, even though
 289 the σ_{xy}^{int} at ε_{F} is large in Fe, the magnitude of the theoretical α_{xy} in Fe becomes
 290 very small $\sim +0.15$ A/(m·K), which shows good agreement with experimentally
 291 evaluated α_{xy} , $+0.13$ A/(m·K). By looking carefully at the theoretically calculated
 292 σ_{xy}^{int} in Fe [31], one can find that $\sigma_{xy}^{\text{int}}(\varepsilon)$ exhibits almost continuous reduction
 293 against ε from 0 to $+0.5$ eV with two shoulders at the vicinity of $\varepsilon - \varepsilon_{\text{F}} = \sim 0.08$
 294 and ~ 0.32 eV, indicating that $\alpha_{xy}(\varepsilon)$ is expected to have two peaks at around
 295 these two energies corresponding to the shoulders in pure Fe due to enhancement
 296 of $|\partial\sigma_{xy}^{\text{int}}/\partial\varepsilon|$. It is interesting to see that experimental α_{xy} in $\text{Fe}_{1-x}\text{Ga}_x$ films also
 297 shows two peaks at the vicinity of $x = 0.1$ and 0.3 in Fig. 7(d). The theoretical α_{xy}
 298 given in Ref. 31 at $\varepsilon - \varepsilon_{\text{F}} = \sim 0.08$ eV is 0.96 A/(m·K) at 300 K, which also agrees
 299 well with experimental $\alpha_{xy} \sim 1.1$ A/(m·K) in $\text{Fe}_{0.90}\text{Ga}_{0.10}$ film. Although it is
 300 difficult to strictly evaluate the actual ε_{F} shift of Fe by Ga substitution from the
 301 calculated DOS in Fig. 5, the rough evaluation gives the value of about $0.1 - 0.2$
 302 eV shift in $\text{Fe}_{0.9}\text{Ga}_{0.1}$, which almost agrees with the theoretically predicted first
 303 peak position ~ 0.08 eV for pure Fe. The deviation of the peak position of α_{xy}
 304 between experimental x dependence in $\text{Fe}_{1-x}\text{Ga}_x$ films and the theoretical
 305 predicted energy in pure Fe is more or less attributed to the slight segregation of
 306 Ga at the surface and interface as shown in Fig. 2(b). Therefore, we concluded
 307 that the enhancement of the ANE in Fe by Ga substitution originates from the
 308 enhancement of intrinsic α_{xy} because of the Fermi level shifting of Fe. It should
 309 be mentioned here that Weischenberg *et al.* has also calculated the anomalous
 310 Hall conductivity arising from the extrinsic mechanism, i.e. side jump
 311 mechanism, $\sigma_{xy}^{\text{side}}$ in Ref. 31. In Fe, $\sigma_{xy}^{\text{side}}$ was predicted to be much smaller
 312 than intrinsic σ_{xy}^{int} at ε_{F} , about 110 S/cm. In contrast to σ_{xy}^{int} , however, $\sigma_{xy}^{\text{side}}$
 313 was predicted to increase with ε and takes a peak of about 300 S/cm at the
 314 vicinity of 0.25 eV although the situation $\sigma_{xy}^{\text{int}} > \sigma_{xy}^{\text{side}}$ maintains in the range of
 315 $0 \leq \varepsilon < 0.5$ eV. It seems that our experimental result of AHE and ANE in $\text{Fe}_{1-x}\text{Ga}_x$
 316 films can be explained by the energy dependence of only σ_{xy}^{int} , suggesting that
 317 the contribution of $\sigma_{xy}^{\text{side}}$ is not remarkable in our $\text{Fe}_{1-x}\text{Ga}_x$ thin films. However,
 318 further investigation is required to consider the contribution of side jump
 319 mechanism on ANE. Here, it is also worth mentioning that one might have an
 320 interest in the relationship between the ANE and the magnetostriction of Fe-Ga.
 321 Although the magnetostriction in our $\text{Fe}_{1-x}\text{Ga}_x$ thin films has not been measured
 322 in this study, we could not find clear relationship in the Ga composition

323 dependence of the magnitude between the observed ANE and the reported
324 magnetostriction in Fe-Ga [39].
325

326

327 **Conclusion**

328 The anomalous Nernst effect (ANE) has been investigated in $\text{Fe}_{1-x}\text{Ga}_x$ alloy with
329 different Ga atomic compositions in the range of $x = 0 - 0.44$. We fabricated
330 $\text{Fe}_{1-x}\text{Ga}_x$ thin films on MgO (001) single crystalline substrates by co-sputtering
331 technique. We found that the magnitude of the ANE in $\text{Fe}_{1-x}\text{Ga}_x$ alloys increases
332 with increasing x up to $x = 0.32$, where the simple bcc crystal structure is
333 preserved in $\text{Fe}_{0.68}\text{Ga}_{0.32}$ film. The magnitude of the ANE in $\text{Fe}_{0.68}\text{Ga}_{0.32}$ film
334 reaches to $2.4 \mu\text{V/K}$, which is two orders of magnitude greater than that of Fe
335 film. The systematic magnetotransport measurements and the first-principles
336 calculations revealed that the large ANE in $\text{Fe}_{1-x}\text{Ga}_x$ is due to the large transverse
337 Peltier coefficient α_{xy} . The maximum value of the theoretically calculated α_{xy}
338 shows good agreement with the experimentally determined values in $\text{Fe}_{1-x}\text{Ga}_x$.
339 The large enhancement of the ANE in Fe by replacing Fe atoms into Ga atoms
340 can be mainly attributed to the shift of the Fermi energy, which can be
341 understood as the electron doping effect. This kind of approach based on the
342 Fermi energy engineering can be applicable to other magnetic materials.
343 Therefore, our finding will provide crucial information to enhance the
344 thermoelectric power through the ANE in various magnetic (ferro-, ferri- and
345 anti-ferromagnetic) materials and pave the way to practical applications using
346 ANE.

347

348

349 **Acknowledgments**

350 We would like to thank A. Yamamoto, K. Nawa, S. Isogami, and H. Fujita for
351 valuable discussions and N. Kojima, B. Masaoka, J. W. Jung, and W. Zhou for
352 technical supports. This work was supported in part by JSPS KAKENHI Grants
353 No. 26709045, No. 19H02585, No. 19K15297, No. 18J02115, No. 17H04808,
354 PRESTO “Scientific Innovation for Energy Harvesting
355 Technology”(JPMJPR12C1) and CREST “Creation of Innovative Core
356 technologies for nano-enabled Thermal Management”(JPMJCR1711) , and the
357 NEDO. A. M. is supported by JSPS thorough Research Fellowship for Young
358 Scientists (JP18J02115). H.N. and J.W would like to acknowledge the ICYS
359 Research Fellowship, NIMS, Japan.

360

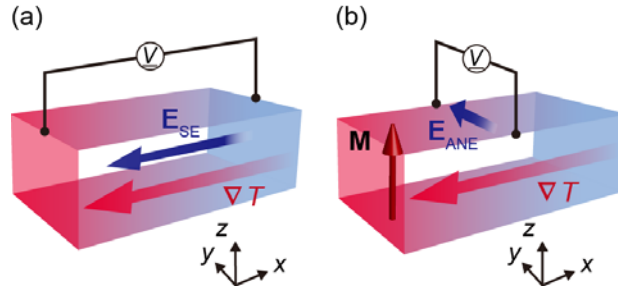
361

362 **References**

363

- 364 [1] G. E. W. Bauer, E. Saitoh, and B. J. van Wees, *Nat. Mater.* **11**, 391 (2012).
- 365 [2] K. Uchida, H. Adachi, T. Kikkawa, A. Kirihara, M. Ishida, S. Yoroazu, S.
366 Maekawa, and E. Saitoh, *Proc. IEEE* **104**, 1946 (2016).
- 367 [3] G. D. Mahan, *Solid State Phys.* **51**, 81 (1998).
- 368 [4] G. J. Snyder and E. S. Toberer, *Nat. Mater.* **7**, 105 (2008).
- 369 [5] W. Nernst, *Ann. Phys.* **267**, 760 (1887).
- 370 [6] K. Behnia, M. A. Méasson, and Y. Kopelevich, *Phys. Rev. Lett.* **98**,
371 076603 (2007).
- 372 [7] R. Suryanarayanan, V. Gasumyants, and N. Ageev, *Phys. Rev. B* **59**,
373 R9019(R) (1999).
- 374 [8] W. L. Lee, S. Watauchi, V. L. Miller, R. J. Cava, and N. P. Ong, *Phys. Rev.*
375 *Lett.* **93**, 226601 (2004).
- 376 [9] T. Miyasato, N. Abe, T. Fujii, A. Asamitsu, S. Onoda, Y. Onose, N.
377 Nagaosa, and Y. Tokura, *Phys. Rev. Lett.* **99**, 086602 (2007).
- 378 [10] Y. Pu, D. Chiba, F. Matsukura, H. Ohno, and J. Shi, *Phys. Rev. Lett.* **101**,
379 117208 (2008).
- 380 [11] M. Mizuguchi, S. Ohata, K. Uchida, E. Saitoh, and K. Takanashi, *Appl.*
381 *Phys. Express* **5**, 093002 (2012).
- 382 [12] Y. Sakuraba, K. Hasegawa, M. Mizuguchi, T. Kubota, S. Mizukami, T.
383 Miyazaki, and K. Takanashi, *Appl. Phys. Express* **6**, 033003 (2013).
- 384 [13] K. Hasegawa, M. Mizuguchi, Y. Sakuraba, T. Kamada, T. Kojima, T.
385 Kubota, S. Mizukami, T. Miyazaki, and K. Takanashi, *Appl. Phys. Lett.*
386 **106**, 252405 (2015).
- 387 [14] Y. Sakuraba, *Scr. Mater.* **111**, 29 (2016).
- 388 [15] T. C. Chuang, P. L. Su, P. H. Wu, and S. Y. Huang, *Phys. Rev. B* **96**,
389 174406 (2017).
- 390 [16] S. Isogami, K. Takanashi, and M. Mizuguchi, *Appl. Phys. Express* **10**,
391 073005 (2017).
- 392 [17] K. Uchida, H. Adachi, T. Ota, H. Nakayama, S. Maekawa, and E. Saitoh,
393 *Appl. Phys. Lett.* **97**, 172505 (2010).
- 394 [18] T. Kikkawa, K. Uchida, Y. Shiomi, Z. Qiu, D. Hou, D. Tian, H. Nakayama,
395 X. F. Jin, and E. Saitoh, *Phys. Rev. Lett.* **110**, 067207 (2013).
- 396 [19] K. Uchida, T. Nonaka, T. Yoshino, T. Kikkawa, D. Kikuchi, and E. Saitoh,
397 *Appl. Phys. Express* **5**, 093001 (2012).

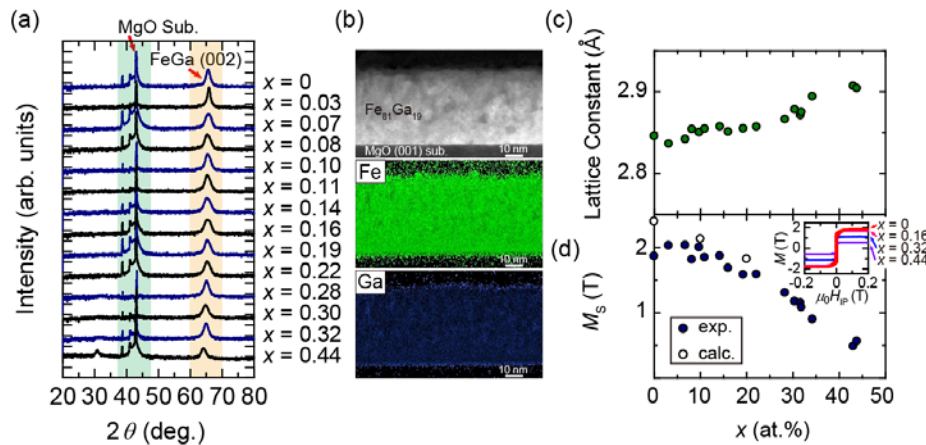
- 398 [20] M. Ikhlas, T. Tomita, T. Koretsune, M. T. Suzuki, D. Nishio-Hamane, R.
399 Arita, Y. Otani, and S. Nakatsuji, Nat. Phys. **13**, 1085 (2017).
- 400 [21] A. Sakai, Y. P. Mizuta, A. A. Nugroho, R. Sihombing, T. Koretsune, M. T.
401 Suzuki, N. Takemori, R. Ishii, D. Nishio-Hamane, R. Arita, P. Goswami,
402 and S. Nakatsuji, Nat. Phys. **14**, 1119 (2018).
- 403 [22] Y. Sakuraba, K. Hyodo, A. Sakuma, and S. Mitani, ArXiv :1807.02209
404 (2018).
- 405 [23] Z. Yang, E. A. Codecido, J. Marquez, Y. Zheng, J. P. Heremans, and R. C.
406 Myers, AIP Adv. **7**, 095017 (2017).
- 407 [24] S. J. Watzman, R. A. Duine, Y. Tserkovnyak, S. R. Boona, H. Jin, A.
408 Prakash, Y. Zheng, and J. P. Heremans, Phys. Rev. B **94**, 144407 (2016).
- 409 [25] C. Fang, C. H. Wan, Z. H. Yuan, L. Huang, X. Zhang, H. Wu, Q. T. Zhang,
410 and X. F. Han, Phys. Rev. B **93**, 054420 (2016).
- 411 [26] H. Okamoto, J. Phase Equilibria Diffus. **25**, 100 (2004).
- 412 [27] H. Akai, <http://kkriissp.u> (2002).
- 413 [28] J. Koringa, Physica **13**, 392 (1947).
- 414 [29] W. Kohn and N. Rostoker, Phys. Rev. **94**, 1111 (1954).
- 415 [30] J. P. Perdew, K. Burke, and M. Ernzerhof, Phys. Rev. Lett. **77**, 3865
416 (1996).
- 417 [31] J. Weischenberg, F. Freimuth, S. Blügel, and Y. Mokrousov, Phys. Rev. B
418 **87**, 060406(R) (2013).
- 419 [32] S. Sangiao, L. Morellon, G. Simon, J. M. De Teresa, J. A. Pardo, J. Arbiol,
420 and M. R. Ibarra, Phys. Rev. B **79**, 014431 (2009).
- 421 [33] J. Smit, Physica **21**, 877 (1955).
- 422 [34] S. Onoda, N. Sugimoto, and N. Nagaosa, Phys. Rev. B **77**, 165103 (2008).
- 423 [35] F. J. Blatt, P. A. Schroeder, C. L. Foiles, and D. Greig, *Thermoelectric*
424 *Power of Metals*, Plenum Press, New York (1976).
- 425 [36] L. Smrčka and P. Streda, J. Phys. C **10**, 2153 (1977).
- 426 [37] M. Jonson and G. D. Mahan, Phys. Rev. B **21**, 4223 (1980).
- 427 [38] M. J. Kearney and P. N. Butcher, J. Phys. C **21**, L265 (1988).
- 428 [39] J. B. Restorff, M. Wun-Fogle, K. B. Hathaway, A. E. Clark, T. A.
429 Lograsso, and G. Petculescu, J. Appl. Phys. **111**, 023905 (2012).
- 430
- 431
- 432



433

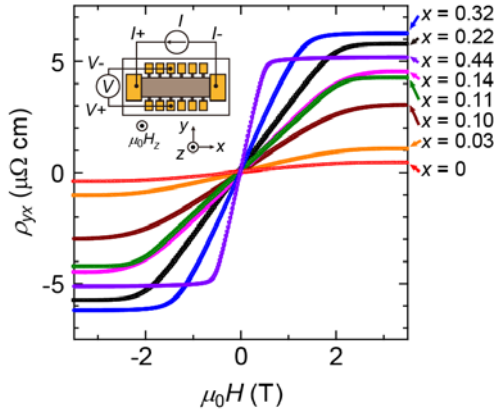
434 FIG. 1. Schematic of experimental configuration for (a) the Seebeck effect and
 435 (b) the anomalous Nernst effect (ANE) measurements. E_{SE} , E_{ANE} , M , and ∇T
 436 denote the electric field induced by the Seebeck effect and the ANE, the
 437 magnetization vector of the ferromagnets, and the applied temperature gradient,
 438 respectively.

439



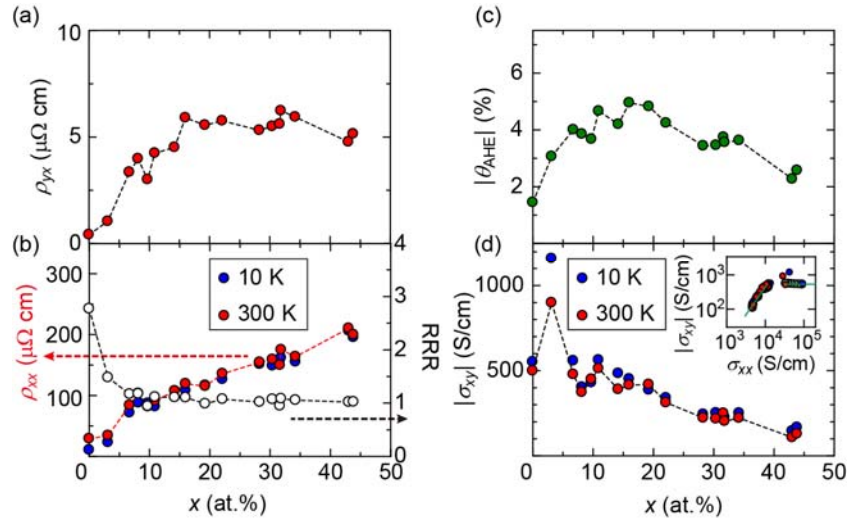
440

441 FIG. 2. (a) Out-of-plane XRD pattern for $Fe_{1-x}Ga_x$ thin films. In order to clearly
 442 show XRD pattern for $Fe_{1-x}Ga_x$ thin films, we subtracted the XRD pattern of
 443 MgO (001) a substrate without $Fe_{1-x}Ga_x$ thin films. Because the subtraction was
 444 conducted for two-dimensional diffraction images of the substrate with and
 445 without films, the slight difference of the tilting of the substrate between two
 446 measurements causes a variation of remaining intensity from the MgO substrate
 447 in the vicinity of $2\theta = 42^\circ$. (b) Cross-sectional HAADF-STEM images and
 448 corresponding EDS maps for $Fe_{0.81}Ga_{0.19}$ film. (c) Ga composition x dependence
 449 of lattice constant determined from position of (002) peak. (d) x dependence of
 450 saturation magnetization M_s for $Fe_{1-x}Ga_x$ thin films, where the open circles are the
 451 theoretically calculated values for Fe, $Fe_{0.9}Ga_{0.1}$, and $Fe_{0.8}Ga_{0.2}$. **The inset shows**
 452 **the in-plane magnetic field along [001] orientation $\mu_0 H_{IP}$ dependence of the**
 453 **magnetization M for $Fe_{1-x}Ga_x$ thin films.**



454

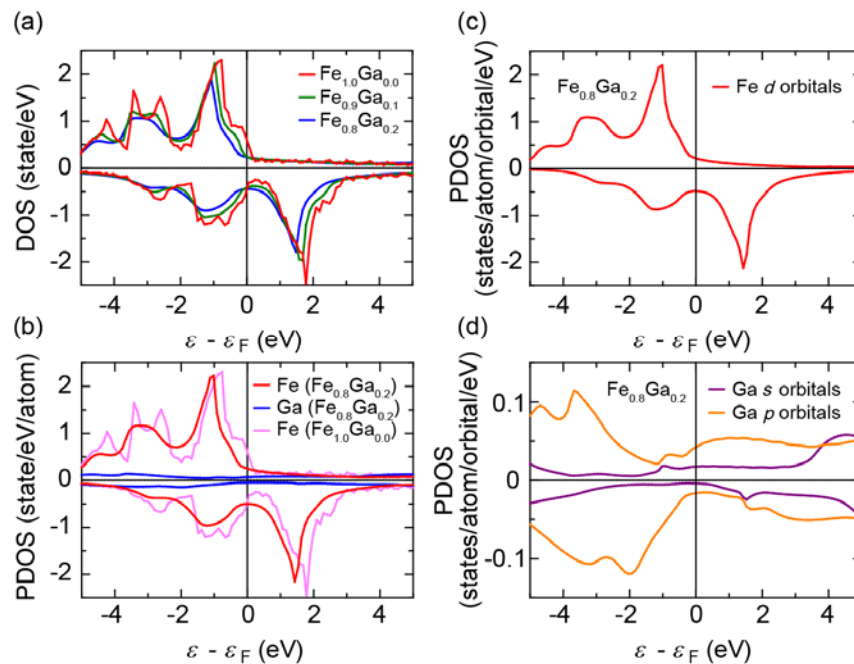
455 FIG. 3. The anomalous Hall resistivity plotted as a function of the magnetic field
 456 $\mu_0 H$ along the z axis in the $\text{Fe}_{1-x}\text{Ga}_x$ thin films. The inset shows a schematic of the
 457 experimental configuration of the anomalous Hall effect (AHE) measurements.
 458



459

460 FIG. 4. The Ga composition x dependence of (a) the anomalous Hall resistivity
 461 ρ_{yx} , (b) the longitudinal resistivity ρ_{xx} (red and blue plots) and the residual
 462 resistivity ratio RRR (open circles) defined as $\rho_{xx}(300\text{ K})/\rho_{xx}(10\text{ K})$, (c) the
 463 anomalous Hall angle $|\theta_{\text{AHE}}| (= |\rho_{yx}/\rho_{xx}|)$, and (d) the anomalous Hall conductivity
 464 $|\sigma_{xy}|$ (red and blue plots) in $\text{Fe}_{1-x}\text{Ga}_x$ thin films, where the blue (red) plot in Figs.
 465 4(b) and 4(d) are measured at 10 K (300 K). **The inset shows the $|\sigma_{xy}|$ dependence**
 466 **of the electrical conductivity σ_{xx} , where the solid line for lower (larger) σ_{xx}**
 467 **corresponds to the fit according to the scaling relationship $|\sigma_{xy}| \propto \sigma_{xx}^n$ with $n =$**
 468 **1.6 ($n = 0$).**
 469

470

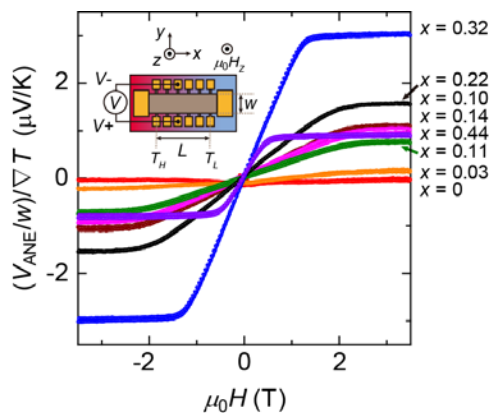


471

472 FIG. 5. (a) The DOSs of Fe, $\text{Fe}_{0.9}\text{Ga}_{0.1}$, and $\text{Fe}_{0.8}\text{Ga}_{0.2}$, where ε_F is the Fermi level.
 473 (b) The PDOSs of Fe and $\text{Fe}_{0.8}\text{Ga}_{0.2}$. (c) and (d) The orbital-resolved PDOSs in
 474 Fe d and Ga s and p orbitals of $\text{Fe}_{0.8}\text{Ga}_{0.2}$.

475

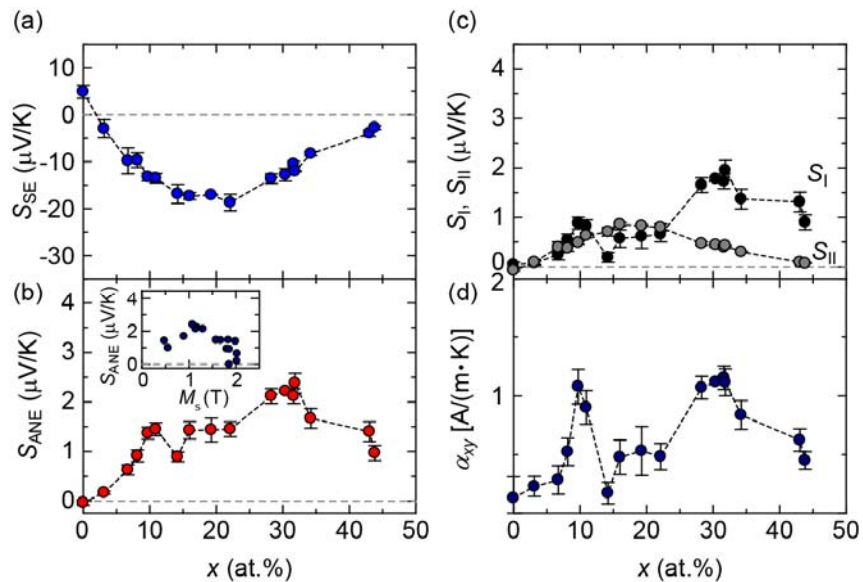
476



477

478 FIG. 6. The μ_0H dependence of the observed ANE voltage V_{ANE} along the y axis
 479 normalized by the width of the Hall bar structure w and the applied temperature
 480 gradient ∇T along the x axis for $\text{Fe}_{1-x}\text{Ga}_x$ thin films. The inset shows a schematic
 481 of the experimental configuration of the ANE measurements.

482



484

485 FIG. 7. The Ga composition x dependence of (a) the Seebeck coefficient S_{SE} , (b)
 486 the magnitude of the ANE S_{ANE} in $Fe_{1-x}Ga_x$ thin films. The inset shows M_s
 487 dependence of the S_{ANE} . x dependence of (c) S_I and S_{II} , where $S_I = \alpha_{xy}\rho_{xx}$ and $S_{II} =$
 488 $-S_{SE} \times \tan\theta_{AHE}$ in $Fe_{1-x}Ga_x$ thin films, and (d) the transverse Peltier coefficient α_{xy}
 489 in $Fe_{1-x}Ga_x$ thin films.

490

491

492

493