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Formation and stability of reduced TiO_x layers on anatase $TiO_2(101)$: identification of a novel Ti_2O_3 phase

Xunhua Zhao*, Sencer Selcuk, and Annabella Selloni*

Department of Chemistry, Princeton University,

Princeton, NJ 08544, USA

We use density functional theory (DFT) calculations to investigate structural models consisting of anatase TiO₂(101) slabs covered by reduced overlayers formed by (101) crystallographic shear planes (CSPs). Ab initio thermodynamics supports the stability of these structures under a wide range of experimental conditions. The overlayers are found to have Ti₂O₃ stoichiometry with a crystal structure different from the known corundum-like Ti₂O₃ (here denoted α -Ti₂O₃) phase. DFT calculations predict this new "csp-Ti₂O₃" phase to be energetically close to α -Ti₂O₃ and to have also a similar band gap. These results suggest a possible role of the csp-Ti₂O₃ phase in the properties of black TiO₂, a promising photocatalytic material made of nanoparticles with a crystalline TiO₂ core and a highly reduced TiO_x shell that is capable of absorbing the whole spectrum of visible light.

Nanomaterials of titanium dioxide (TiO₂) are of great interest in many fields, ranging from energy conversion and storage to coatings and biomedical applications [1,2]. In particular, recent research efforts have been focused on "black TiO₂", which consists of photocatalytically active core-shell nanoparticles (NPs) that absorb visible light much more efficiently than pristine TiO₂ [3,4]. It is widely accepted that the characteristic properties of black TiO₂ are due to structural changes in the outer shell of the NPs while the core maintains the crystal structure of conventional TiO₂ [3–9]. However, understanding of the detailed chemical composition and atomic structure of the outer shell has remained limited.

Independent of the synthetic procedure, a key feature of all black TiO₂ nanomaterials is that they are highly reduced (i.e. oxygen deficient), since they are prepared either by exposing the nanoparticles to a reducing atmosphere or by annealing the sample in vacuum to create oxygen vacancies [3,6]. As a prototypical reducible oxide, TiO₂ always contains a significant amount of oxygen vacancies (V_os) [10]. With increasing concentration, V_os are known to rearrange to give rise to crystallographic shear planes (CSPs) [11–13]. For example, the Magnéli phases, Ti_nO_{2n-1}, can be described as resulting from a regular arrangement of CSPs in oxygen-deficient rutile [12]. Interestingly, a recent study characterized the outer shell of black rutile TiO₂ nanoparticles as consisting of disordered α -Ti₂O₃ [6]. Similarly, based on the Ti³⁺/Ti⁴⁺ ratio of Ti ions, another study determined the black shell of anatase TiO₂ nanotubes to be amorphous Ti₄O₇ [7]. Strips of CSPs have been reported also in anatase TiO₂(001) thin films epitaxially grown on LaAlO₃ [14], where they have been attributed to anatase-derived Magnéli-like phases Ti_nO_{2n-1} (*n*=5,6,7).

In this work, we focus on anatase, the TiO_2 phase usually found in nanomaterials and most relevant in photocatalysis and photovoltaics [1,15,16], and use DFT calculations to explore the stability and properties of highly reduced TiO_x overlayers formed by CSPs on or near its most stable and frequently exposed (101) surface [10,15,17]. While ordered, these CSP structures could indirectly provide information also on the importance of structural disorder on the properties of different black TiO₂ nanomaterials. Our results show that formation of a reduced shell on the anatase surface is thermodynamically favourable under a wide range of experimental conditions. This shell has Ti₂O₃ stoichiometry and its structure is not the well-known α -Ti₂O₃ phase (the mineral "tistarite" [18]), but a novel phase that has not yet been reported. DFT calculations with various exchange-correlation functionals (see the Supplemental Material [19], for computational details) show that this new phase – here denoted csp-Ti₂O₃ – is close in stability to α -Ti₂O₃ and has also a similar band gap, which is consistent with the absorption of black TiO₂. These findings suggest the possible presence of csp-Ti₂O₃ in the outer shell of black TiO₂ nanomaterials.

Aggregation of V_{OS} and CSPs at the Anatase (101) Surface- V_{OS} at slightly or moderately reduced anatase (101) have been found to reside not at the very surface, but one or a few layers below it [20,21]. In agreement with these findings, our calculations show that a subsurface V_O (site 4 in Fig. 1) is energetically more favourable than one at a surface bridging oxygen (site 1 in Fig. 1) by 0.17 eV. Since V_Os at these sites are significantly more favourable than at any other site, we only consider such sites when studying the formation of multiple vacancies.

Also in agreement with previous studies, our calculations show a slight increase of the average formation energy per V₀ with increasing number of V₀s, indicating a weakly repulsive interaction between them (Table I). However, when a full layer of subsurface oxygen atoms is removed (Fig. 1), the formation energy (E_{form}) decreases sharply by 0.28 eV compared to the value of a single, most-stable V₀. This decrease is associated to a lateral shift of the layer above the one that is removed and the formation of a (101) crystallographic shear plane; in particular, the position of O4 is taken by O5, which becomes four-coordinated and shared by the first and second layer.

To determine the relative stabilities of CSPs and disordered V₀s, the contribution of the configurational entropy per oxygen vacancy, S_{conf}, must also be included [22]. Being perfectly ordered, a CSP has S_{conf} = 0, whereas separated V₀s can have a large number of different configurations, and therefore a large value of S_{conf}. As a simple estimate, we assume the V₀s to be non-interacting, and for any given stoichiometry TiO_{2-x} we approximate S_{conf} by [k_B ln(2/x)], where 2/x is the average number of available sites per V₀. We then calculate the minimum temperature, T*, that is required for the disordered V₀s to be more stable than the CSP layer, i.e. T*·S_{conf} \geq 0.28 eV. In this way we obtain T*= 610, 425, 326 and 265 K at x= 10⁻², 10⁻³, 10⁻⁴, and 10⁻⁵, respectively, indicating that CSPs are stable at room temperature for x > 10⁻⁴. More detailed analysis of the contribution of S_{conf}, presented in the Supplemental Material [19], also supports this conclusion.

We further considered structures with several contiguous CSPs (denoted 2CSP, 3CSP, etc.) obtained by sequentially removing full layers of oxygen atoms. The average V₀ formation energy decreases with increasing number of CSPs, slowly reaching a saturation value of ~ 3.40 eV (Table I). We also investigated whether CSPs prefer to be contiguous or separated from each other, and whether they prefer to form close to the surface or in the central bulk-like region of the anatase slab. Computed formation energies for different models clearly indicate that CSPs prefer to aggregate and remain close to the surface (Fig. S3 [19]).

The densities of states (DOS) for slabs with different numbers of CSPs are shown in Fig. 2. When there is one CSP, the gap states are similar to those from isolated V_os, with some additional broadening. Two CSPs give rise to two slightly separated sets of gap states. The layer-resolved DOS reveals that the lower set is contributed mainly by Ti 3d orbitals in the second layer (Figs. S5-S7 [19]). As the number of CSPs increases to 3, the distribution of gap states becomes even broader due to the presence of many nonequivalent Ti atoms at the interface and in the central layers. As a result, the energy gap between the occupied Ti3d states and the empty states in the conduction band is only 0.2 eV. However, when the number of CSPs reaches 4 or more, the energy gap increases again to 0.66, 0.67 and 1.18 eV for n=4,5, and 6 respectively. This increase can be attributed to the formation of a new insulating phase, csp-Ti₂O₃, that is discussed below.

*A new csp-Ti*₂*O*₃ *crystal phase* - As the number of CSPs increases, the presence of a crystalline structure in the central region of the CSPs becomes evident. This structure, denoted csp-Ti₂O₃, has Ti₂O₃ stoichiometry, but is different from the usual α -Ti₂O₃ phase. csp-Ti₂O₃ is orthorombic (Fig. 3) with space group *Immm* (no. 71), and can be considered as the limiting structure of a series of Magnéli Ti_nO_{2n-1} phases (Fig. S9 [19]). The primitive unit cells of bulk csp-Ti₂O₃, α -Ti₂O₃ and anatase TiO₂ are shown in Fig. 3, while computed structural parameters are given in Tables S1 and S3 [19]. csp-Ti₂O₃ has only one type of Ti site but two inequivalent oxygen sites, both fourfold coordinated: one (O1) is at the center of a distorted tetrahedron and the other (O2) forms four O-Ti bonds in a plane. The Ti-O bonds are elongated compared to anatase, while Ti-Ti distances – one shorter than the other two in the unit cell – suggest the formation of Ti-Ti dimers as in α -Ti₂O₃.

It is interesting to compare the relative stabilities of csp-Ti₂O₃ and α -Ti₂O₃. To address this question we performed DFT+U [23] calculations with the Perdew-Burke-Ernzerhof (PBE) [24] functional and on-site Coulomb repulsion U on the Ti 3d orbitals, considering 10 different U values in the range between 0 and 5 eV, which includes the values typically used for Ti⁴⁺ and Ti³⁺ ions in titanium oxides [25,26]. As a further check, we also used the hybrid HSE06 functional [27], which is known to work well for many oxides including TiO₂ [28]. Experimentally, α -Ti₂O₃ is observed to be a small band gap insulator with no long-range magnetic ordering at room

temperature.[29,30] We found that both α -Ti₂O₃ and csp-Ti₂O₃ are metallic and either nonmagnetic or with a small absolute magnetization (Table S5 [19]) for $U \le 1.5$ eV, whereas they are insulating and antiferromagnetic (AFM) for larger U and with HSE06 as well. For comparison, α -Ti₂O₃ was found to be AFM and insulating (with band gap E_g = 0.59 eV) in a recent study using self-consistent hybrid functionals [31], and nonmagnetic and insulating (with E_g = 0.22-0.57 eV) in studies employing screened exchange and modified (LDA-based) HSE06 hybrid functionals [32,33].

Computed values of the total energy difference between α -Ti₂O₃ and csp-Ti₂O₃ are reported in Fig. 4 (see also Table S4 [19]). Two different choices of lattice parameters were considered. As experimental lattice parameters are not available for csp-Ti₂O₃, we used the lattice parameters optimized with HSE06, which are very close to the experimental ones in the case of α -Ti₂O₃ and anatase TiO₂ (Table S1 [19]). We further computed PBE+*U* energy differences using the lattice parameters also optimized with PBE+*U*, which tend to deviate significantly from experiment, especially for large *U* [25]. From Fig. 4, it is evident that the results obtained with the two choices of geometries are quite different, as PBE+ *U* predicts csp-Ti₂O₃ to be more (less) stable than α -Ti₂O₃ for *U* > 2 (*U* > 1.5) when HSE06 (PBE+*U*) optimized geometries are used. Interestingly, the small range of *U* values, 1.5 \leq *U* \leq 2 eV, for which the relative stability of the two phases is independent of the choice of the lattice constant is located around the transition between metallic and insulating behaviour, where the computed band gap for α -Ti₁O₁(on the insulating side) is close to the experimental value (see Table S4 [19] and below) and the reduction energy of TiO, to Ti₁O, is also in good agreement with experiment [25] (see also Fig. S1 [19]). Here, csp-Ti₁O, is predicted to be less stable than α -Ti₁O, as one would expect, but only by a small amount.

The electronic DOS of csp-Ti₂O₃ and α -Ti₂O₃ computed at the PBE+*U* (*U*=1.75 and 3 eV), and HSE06 levels are shown in Fig. 5 (see also Figs. S10 and S11 [19]). Results for the two phases are

similar despite their significant structural differences. In particular, U=1.75 eV gives $E_g = 0.30$ eV for α -Ti₂O₃, close to experimental value of 0.1-0.2 eV [34,35], while HSE06 predicts much larger band gaps of 1.90 eV and 1.82 eV for α -Ti₂O₃, and csp-Ti₂O₃, respectively. For comparison, Table S4 [19] reports also the computed band gap of anatase, which is in the range 2.2-3.7 eV with PBE+*U* and HSE06. Independent of the approach, all methods predict that the band gap of csp-Ti₂O₃ is close to that of α -Ti₂O₃ and about 1-2 eV smaller than the band gap of anatase TiO₂.

Stability Diagrams - To evaluate the relative stabilities of the csp-Ti₂O₃/TiO₂ structures with different degrees of reduction, Gibbs free energies of formation are calculated in either O₂ or H_2/H_2O atmosphere [36,37]. We used a 7-layer pristine anatase TiO₂(101) slab as the reference, and considered the slab models listed in Table I as well as bulk csp-Ti₂O₃. Based on the results in Fig. 6(a), formation of CSPs in a TiO₂ slab or formation of bulk csp-Ti₂O₃ from bulk TiO₂ (see inset) in a pure O₂ atmosphere requires the O₂ pressure to be well below the pressures that can be achieved in ultra-high vacuum experiments.

Alternatively, one of the common procedures for preparing black TiO₂ is by reducing anatase powders under H₂ atmosphere. This reduction proceeds according to H₂+O_s \rightarrow H₂O + V₀, where O_s is a surface oxygen atom [4,38,39]. We thus evaluated the thermodynamics of forming *n*CPSs@TiO₂ and bulk csp-Ti₂O₃ from anatase TiO₂ in the presence of a mixed H₂/H₂O environment, where the reduction of TiO₂ is driven by the formation of water. Phase stability diagrams as a function of the H chemical potential ($\Delta \mu_{\rm H}$) with H₂O at high (ambient condition) and low partial pressures are shown in Fig. 6(b) and Fig. S8 [19]. In the mixed H₂/H₂O atmosphere, formation of the reduced structures becomes favorable at values of the chemical potentials that are well accessible experimentally. Although this thermodynamic analysis only predicts the preferred state at infinitely long time, without taking into account the kinetics that could actually play a critical role, e.g. in determining the thickness of the reduced layer, it is evident that the combination of oxygen from TiO_2 with hydrogen in the surrounding environment provides a strong driving force toward the formation of CSPs and eventually of the csp- Ti_2O_3 phase on the anatase surface.

In summary, based on DFT calculations, we have identified a new metastable csp-Ti₂O₃ phase that results from aggregation of CSPs on anatase TiO₂(101) and is close in stability to α -Ti₂O₃. Structures consisting of a csp-Ti₂O₃ overlayer on crystalline anatase are thermodynamically stable in reducing atmosphere and, depending on the thickness of the overlayer, have energy gaps in the range 0.2 ~ 1.2 eV, consistent with the photoabsorption of black TiO₂. Besides representing viable models for black TiO₂ nanomaterials, such structures might be relevant for understanding recent experimental observations on anatase (101) chemically doped with oxygen vacancies [40], and for describing the reduced surface region of nanomaterials of other metal oxides as well [41,42].

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* aselloni@princeton.edu

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TABLE I: Formation energy per oxygen vacancy E_{form} (eV), computed using PBE+U with U=3.0 eV, for different model systems: one and two vacancies in a 7 layer anatase (101) slab, $n\text{CSP}@(7-n)\text{TiO}_2$ (n = 1-6) with n CSPs in a 7 layer (101) slab, and bulk csp-Ti₂O₃ (last column). For the latter, E_{form} is computed from the reaction $2\text{TiO}_2 \rightarrow \text{Ti}_2\text{O}_3 + \frac{1}{2}\text{O}_2$.

Model	Vo	2Vo	1CSP	2CSP	3CSP	4CSP	5CSP	6CSP	csp-Ti ₂ O ₃
$E_{\rm form}$	3.92	3.94	3.65	3.51	3.46	3.44	3.42	3.44	3.39



FIG. 1: Formation of a CSP parallel to the (101) surface (schematic). O atoms removed upon CSP formation are yellow, all other O atoms are red, Ti atoms are grey. Five non-equivalent oxygen atoms are indicated. The part within bracket is the top layer of TiO₂; the arrow shows the direction of shear.



FIG. 2: Electronic densities of states of $nCSP@(7-n)TiO_2$ (n=0-6), computed using PBE+U with U = 3.0 eV. Solid and dashed lines refer to spin up and spin down states. Blue and red bars indicate valence and conduction band edges, respectively. The zero of energy is set at the vacuum level (see Fig. S4 [19])



FIG. 3: Primitive unit cells of (a) anatase TiO_2 , (b) csp- Ti_2O_3 and (c) α - Ti_2O_3 . Oxygen atoms are red, titanium atoms are grey.



FIG. 4 Total energy difference per formula unit between csp-Ti₂O₃ and α -Ti₂O₃, computed using PBE+*U* with different *U* values, and two different choices of lattice parameters. In the region 1 < U < 2 eV (darker shading), the magnetic moment of Ti³⁺ ions increases from 0 to nearly 1 μ_B (Table S5 [19]). The horizontal dashed-dotted line indicates HSE06 results.



FIG. 5: Density of states of bulk csp-Ti₂O₃ (solid lines) and α -Ti₂O₃ (dashed lines), computed using PBE+U (U=1.75 and 3.0 eV) and hybrid HSE06. The Fermi level is at the top of the occupied states. DOS curves for spin-up and spin-down states are identical.



FIG. 6: Formation free energy (ΔG) for the structures in Table I as function of: (a) O chemical potential (relative to 1/2 O₂), and (b) H chemical potential (relative to 1/2 H₂), with H₂O at T = 800 K and $p_{\text{H2O}} = 10^{-2}$ bar; the two dashed vertical lines mark the region of H chemical potential typical of black TiO₂ synthesis. The insets show the phase diagram for bulk csp-Ti₂O₃ and TiO₂ as a function of temperature (T) and O₂(a) or H₂(b) pressure. ΔG for nV_0 @7TiO₂ (n=1,2) do not include the configurational entropy discussed in the text.