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Combining the AFLOW GIBBS and Elastic Libraries for efficiently and robustly screening thermo-mechanical properties of solids

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Thorough characterization of the thermo-mechanical properties of materials requires difficult and time-consuming experiments. This severely limits the availability of data and is one of the main obstacles for the development of effective accelerated materials design strategies. The rapid screening of new potential materials requires highly integrated, sophisticated and robust computational approaches. We tackled the challenge by developing an automated, integrated workflow with robust error-correction within the AFLOW framework which combines the newly developed “Automatic Elasticity Library” with the previously implemented GIBBS method. The first extracts the mechanical properties from automatic self-consistent stress-strain calculations, while the latter employs those mechanical properties to evaluate the thermodynamics within the Debye model. This new thermo-elastic workflow is benchmarked against a set of 74 experimentally characterized systems to pinpoint a robust computational methodology for the evaluation of bulk and shear moduli, Poisson ratios, Debye temperatures, Grüneisen parameters, and thermal conductivities of a wide variety of materials. The effect of different choices of equations of state and exchange-correlation functionals is examined and the optimum combination of properties for the Leibfried-Schlömann prediction of thermal conductivity is identified, leading to improved agreement with experimental results than the GIBBS-only approach. The framework has been applied to the AFLOW.org data repositories to compute the thermo-elastic properties of over 3500 unique materials. The results are now available online by using an expanded version of the REST-API described in the appendix.

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I. INTRODUCTION

Calculating the thermal and elastic properties of materials is important for predicting the thermodynamic and mechanical stability of structural phases^{1–4} and assessing their importance for a variety of applications. Elastic and mechanical properties such as the shear and bulk moduli are important for predicting the hardness of materials⁵, and thus their resistance to wear and distortion. Thermal properties, such as specific heat capacity and lattice thermal conductivity, are important for applications including thermal barrier coatings, thermoelectrics^{6–8}, and heat sinks^{9,10}.

Elasticity. There are two main methods for calculating the elastic constants, based on the response of either the stress tensor or the total energy to a set of applied strains^{11–16}. In this study, we obtain the elastic constants from the calculated stress tensors for a set of independent deformations of the crystal lattice. This method is implemented within the AFLOW framework for computational materials design^{17–19}, where it is referred to as the Automatic Elasticity Library (AEL). A similar implementation within the Materials Project¹⁴ allows extensive screening studies by combining data from these two large repositories of computational materials data.

Thermal properties. The determination of the thermal conductivity of materials from first principles re-

quires either calculation of anharmonic interatomic force constants (IFCs) for use in the Boltzmann Transport Equation (BTE)^{20–27}, or molecular dynamics simulations in combination with the Green-Kubo formula^{28,29}, both of which are highly demanding computationally even within multiscale approaches³⁰. These methods are unsuitable for rapid generation and screening of large databases of materials properties in order to identify trends and simple descriptors³¹. Previously, we have implemented the “GIBBS” quasi-harmonic Debye model^{32,33} within both the Automatic GIBBS Library (AGL)³⁴ of the AFLOW^{17,35–38} and Materials Project^{39–41} frameworks. This approach does not require large supercell calculations since it relies merely on first-principles calculations of the energy as a function of unit cell volume. It is thus much more tractable computationally and eminently suited to investigating the thermal properties of entire classes of materials in a highly-automated fashion to identify promising candidates for more in-depth experimental and computational analysis.

The data set of computed thermal and elastic properties produced for this study is available in the AFLOW³⁵ online data repository, either using the AFLOW Representational State Transfer Application Programming Interface (REST-API)³⁶ or via the `aflow.org` web portal^{35,42}.

II. THE AEL-AGL METHODOLOGY

The AEL-AGL methodology combines elastic constants calculations, in the Automatic Elasticity Library (AEL), with the calculation of thermal properties within the Automatic GIBBS Library (AGL³⁴) - ‘‘GIBBS’’³² implementation of the Debye model. This integrated software library includes automatic error correction to facilitate high-throughput computation of thermal and elastic materials properties within the AFLOW framework^{17,35–37,43–47}. The principal ingredients of the calculation are described in the following Sections.

A. Elastic properties

The elastic constants are evaluated from the stress-strain relations

$$\begin{pmatrix} s_{11} \\ s_{22} \\ s_{33} \\ s_{23} \\ s_{13} \\ s_{12} \end{pmatrix} = \begin{pmatrix} c_{11} & c_{12} & c_{13} & c_{14} & c_{15} & c_{16} \\ c_{12} & c_{22} & c_{23} & c_{24} & c_{25} & c_{26} \\ c_{13} & c_{23} & c_{33} & c_{34} & c_{35} & c_{36} \\ c_{14} & c_{24} & c_{34} & c_{44} & c_{45} & c_{46} \\ c_{15} & c_{25} & c_{35} & c_{45} & c_{55} & c_{56} \\ c_{16} & c_{26} & c_{36} & c_{46} & c_{56} & c_{66} \end{pmatrix} \begin{pmatrix} \epsilon_{11} \\ \epsilon_{22} \\ \epsilon_{33} \\ 2\epsilon_{23} \\ 2\epsilon_{13} \\ 2\epsilon_{12} \end{pmatrix} \quad (1)$$

with stress tensor elements s_{ij} calculated for a set of independent normal and shear strains ϵ_{ij} . The elements of the elastic stiffness tensor c_{ij} , written in the 6x6 Voigt notation using the mapping²: 11 \mapsto 1, 22 \mapsto 2, 33 \mapsto 3, 23 \mapsto 4, 13 \mapsto 5, 12 \mapsto 6; are derived from polynomial fits for each independent strain, where the polynomial degree is automatically set to be less than the number of strains applied in each independent direction to avoid overfitting. The elastic constants are then used to compute the bulk and shear moduli, using either the Voigt approximation

$$B_{\text{Voigt}} = \frac{1}{9} [(c_{11} + c_{22} + c_{33}) + 2(c_{12} + c_{23} + c_{13})] \quad (2)$$

for the bulk modulus, and

$$G_{\text{Voigt}} = \frac{1}{15} [(c_{11} + c_{22} + c_{33}) - (c_{12} + c_{23} + c_{13})] + \frac{1}{5} (c_{44} + c_{55} + c_{66}) \quad (3)$$

for the shear modulus; or the Reuss approximation, which uses the elements of the compliance tensor s_{ij} (the inverse of the stiffness tensor), where the bulk modulus is given by

$$\frac{1}{B_{\text{Reuss}}} = (s_{11} + s_{22} + s_{33}) + 2(s_{12} + s_{23} + s_{13}) \quad (4)$$

and the shear modulus is

$$\frac{15}{G_{\text{Reuss}}} = 4(s_{11} + s_{22} + s_{33}) - 4(s_{12} + s_{23} + s_{13}) + 3(s_{44} + s_{55} + s_{66}). \quad (5)$$

For polycrystalline materials, the Voigt approximation corresponds to assuming that the strain is uniform and that the stress is supported by the individual grains in parallel, giving the upper bound on the elastic moduli; while the Reuss approximation assumes that the stress is uniform and that the strain is the sum of the strains of the individual grains in series, giving the lower bound on the elastic moduli². The two approximations can be combined in the Voigt-Reuss-Hill (VRH)⁴⁸ averages for the bulk modulus

$$B_{\text{VRH}} = \frac{B_{\text{Voigt}} + B_{\text{Reuss}}}{2}; \quad (6)$$

and the shear modulus

$$G_{\text{VRH}} = \frac{G_{\text{Voigt}} + G_{\text{Reuss}}}{2}. \quad (7)$$

The Poisson ratio σ is then obtained by:

$$\sigma = \frac{3B_{\text{VRH}} - 2G_{\text{VRH}}}{6B_{\text{VRH}} + 2G_{\text{VRH}}} \quad (8)$$

These elastic moduli can also be used to compute the speed of sound for the transverse and longitudinal waves, as well as the average speed of sound in the material². The speed of sound for the longitudinal waves is

$$v_{\text{L}} = \left(\frac{B + \frac{4}{3}G}{\rho} \right)^{\frac{1}{2}}, \quad (9)$$

and for the transverse waves

$$v_{\text{T}} = \left(\frac{G}{\rho} \right)^{\frac{1}{2}}, \quad (10)$$

where ρ is the mass density of the material. The average speed of sound is then evaluated by

$$\bar{v} = \left[\frac{1}{3} \left(\frac{2}{v_{\text{T}}^3} + \frac{1}{v_{\text{L}}^3} \right) \right]^{-\frac{1}{3}}. \quad (11)$$

B. The AGL quasi-harmonic Debye-Grüneisen model

The Debye temperature of a solid can be written as²

$$\theta_{\text{D}} = \frac{\hbar}{k_{\text{B}}} \left[\frac{6\pi^2 n}{V} \right]^{1/3} \bar{v}, \quad (12)$$

where n is the number of atoms in the cell, V is its volume, and \bar{v} is the average speed of sound of Eq. (11). It can be shown by combining Eqs. (8), (9), (10) and (11) that \bar{v} is equivalent to²

$$\bar{v} = \sqrt{\frac{B_{\text{S}}}{\rho}} f(\sigma). \quad (13)$$

where B_s is the adiabatic bulk modulus, ρ is the density, and $f(\sigma)$ is a function of the Poisson ratio σ :

$$f(\sigma) = \left\{ 3 \left[2 \left(\frac{2}{3} \cdot \frac{1+\sigma}{1-2\sigma} \right)^{3/2} + \left(\frac{1}{3} \cdot \frac{1+\sigma}{1-\sigma} \right)^{3/2} \right]^{-1} \right\}^{1/3}, \quad (14)$$

In an earlier version of AGL³⁴, the Poisson ratio in Eq. (14) was assumed to have the constant value $\sigma = 0.25$ which is the ratio for a Cauchy solid. This was found to be a reasonable approximation, producing good correlations with experiment. The AEL approach, Eq. (8), directly evaluates σ assuming only that it is independent of temperature and pressure. Substituting Eq. (13) into Eq. (12), the Debye temperature is obtained as

$$\theta_D = \frac{\hbar}{k_B} [6\pi^2 V^{1/2} n]^{1/3} f(\sigma) \sqrt{\frac{B_s}{M}}, \quad (15)$$

where M is the mass of the unit cell. The bulk modulus B_s is obtained from a set of DFT calculations for different volume cells, either by fitting the resulting $E_{\text{DFT}}(V)$ data to a phenomenological equation of state or by taking the numerical second derivative of a polynomial fit

$$B_s(V) \approx B_{\text{static}}(\vec{x}) \approx B_{\text{static}}(\vec{x}_{\text{opt}}(V)) = V \left(\frac{\partial^2 E(\vec{x}_{\text{opt}}(V))}{\partial V^2} \right) = V \left(\frac{\partial^2 E(V)}{\partial V^2} \right). \quad (16)$$

Inserting Eq. (16) into Eq. (15) gives the Debye temperature as a function of volume $\theta_D(V)$, for each value of pressure, p , and temperature, T .

The equilibrium volume at any particular (p, T) point is obtained by minimizing the Gibbs free energy with respect to volume. First, the vibrational Helmholtz free energy, $F_{\text{vib}}(\vec{x}; T)$, is calculated in the quasi-harmonic approximation

$$F_{\text{vib}}(\vec{x}; T) = \int_0^\infty \left[\frac{\hbar\omega}{2} + k_B T \log \left(1 - e^{-\hbar\omega/k_B T} \right) \right] g(\vec{x}; \omega) d\omega, \quad (17)$$

where $g(\vec{x}; \omega)$ is the phonon density of states and \vec{x} describes the geometrical configuration of the system. In the Debye-Grüneisen model, F_{vib} can be expressed in terms of the Debye temperature θ_D

$$F_{\text{vib}}(\theta_D; T) = nk_B T \left[\frac{9}{8} \frac{\theta_D}{T} + 3 \log \left(1 - e^{-\theta_D/T} \right) - D \left(\frac{\theta_D}{T} \right) \right], \quad (18)$$

where $D(\theta_D/T)$ is the Debye integral

$$D(\theta_D/T) = 3 \left(\frac{T}{\theta_D} \right)^3 \int_0^{\theta_D/T} \frac{x^3}{e^x - 1} dx. \quad (19)$$

The Gibbs free energy is calculated as

$$G(V; p, T) = E_{\text{DFT}}(V) + F_{\text{vib}}(\theta_D(V); T) + pV, \quad (20)$$

and fitted by a polynomial of V . The equilibrium volume, V_{eq} , is that which minimizes $G(V; p, T)$.

Once V_{eq} has been determined, θ_D can be determined, and then other thermal properties including the Grüneisen parameter and thermal conductivity can be calculated as described in the following Sections.

C. Equations of State

Within AGL the bulk modulus can be determined either numerically from the second derivative of the polynomial fit of $E_{\text{DFT}}(V)$, Eq. (16), or by fitting the (p, V) data to a phenomenological equation of state (EOS). Three different analytic EOS have been implemented within AGL: the Birch-Murnaghan EOS^{2,32,49}; the Vinet EOS^{32,50}; and the Baonza-Cáceres-Núñez spinodal EOS^{32,51}.

The Birch-Murnaghan EOS is

$$\frac{p}{3f(1+2f)^{5/2}} = \sum_{i=0}^2 a_i f^i, \quad (21)$$

where p is the pressure, a_i are polynomial coefficients, and f is the ‘‘compression’’ given by

$$f = \frac{1}{2} \left[\left(\frac{V}{V_0} \right)^{-2/3} - 1 \right]. \quad (22)$$

The zero pressure bulk modulus is equal to the coefficient a_0 .

The Vinet EOS is^{32,50}

$$\log \left[\frac{px^2}{3(1-x)} \right] = \log B_0 + a(1-x), \quad (23)$$

where a and $\log B_0$ are fitting parameters and

$$x = \left(\frac{V}{V_0} \right)^{1/3}, \quad a = 3(B'_0 - 1)/2. \quad (24)$$

The isothermal bulk modulus B_T is given by^{32,50}

$$B_T = -x^{-2} B_0 e^{a(1-x)} f(x), \quad (25)$$

where

$$f(x) = x - 2 - ax(1-x).$$

The Baonza-Cáceres-Núñez spinodal equation of state has the form^{32,51}

$$V = V_{\text{sp}} \exp \left[- \left(\frac{K^*}{1-\beta} \right) (p - p_{\text{sp}})^{1-\beta} \right], \quad (26)$$

where K^* , p_{sp} and β are the fitting parameters, and V_{sp} is given by

$$V_{\text{sp}} = V_0 \exp \left[\frac{\beta}{(1-\beta) B'_0} \right],$$

where $B_0 = [K^*]^{-1} (-p_{\text{sp}})^\beta$ and $B'_0 = (-p_{\text{sp}})^{-1} \beta B_0$. The isothermal bulk modulus B_T is then given by^{32,51}

$$B_T = \frac{(p - p_{\text{sp}})^\beta}{K^*}. \quad (27)$$

Note that AGL uses B_T instead of B_s in Eq. 15 when one of these phenomenological EOS is selected. B_s can then be calculated as

$$B_s = B_T(1 + \alpha\gamma T), \quad (28)$$

where γ is the Grüneisen parameter (described in Section IID below), and α is the thermal expansion

$$\alpha = \frac{\gamma C_V}{B_T V}, \quad (29)$$

where C_V is the heat capacity at constant volume, given by

$$C_V = 3nk_B \left[4D \left(\frac{\theta_D}{T} \right) - \frac{3\theta_D/T}{\exp(\theta_D/T) - 1} \right]. \quad (30)$$

D. The Grüneisen Parameter

The Grüneisen parameter describes the variation of the thermal properties of a material with the unit cell size, and contains information about higher order phonon scattering which is important for calculating the lattice thermal conductivity^{34,52–55}, and thermal expansion^{2,32,56}. It is defined as the phonon frequencies dependence on the unit cell volume

$$\gamma_i = -\frac{V}{\omega_i} \frac{\partial \omega_i}{\partial V}. \quad (31)$$

Debye’s theory assumes that the volume dependence of all mode frequencies is the same as that of the cut-off Debye frequency, so the Grüneisen parameter can be expressed in terms of θ_D

$$\gamma = -\frac{\partial \log(\theta_D(V))}{\partial \log V}. \quad (32)$$

This macroscopic definition of the Debye temperature is a weighted average of Eq. (31) with the heat capacities for each branch of the phonon spectrum

$$\gamma = \frac{\sum_i \gamma_i C_{V,i}}{\sum_i C_{V,i}}. \quad (33)$$

Within AGL³⁴, the Grüneisen parameter can be calculated in several different ways, including direct evaluation of Eq. 32, by using the more stable Mie-Grüneisen equation²,

$$p - p_{T=0} = \gamma \frac{U_{\text{vib}}}{V}, \quad (34)$$

where U_{vib} is the vibrational internal energy³²

$$U_{\text{vib}} = nk_B T \left[\frac{9}{8} \frac{\theta_D}{T} + 3D \left(\frac{\theta_D}{T} \right) \right]. \quad (35)$$

The “Slater gamma” expression²

$$\gamma = -\frac{1}{6} + \frac{1}{2} \frac{\partial B_S}{\partial p} \quad (36)$$

is the default method in the automated workflow used for the AFLOW database.

E. Thermal conductivity

In the AGL framework, the thermal conductivity is calculated using the Leibfried-Schlömann equation^{52–54}

$$\kappa_l(\theta_a) = \frac{0.849 \times 3 \sqrt[3]{4}}{20\pi^3 (1 - 0.514\gamma_a^{-1} + 0.228\gamma_a^{-2})} \times \quad (37)$$

$$\times \left(\frac{k_B \theta_a}{\hbar} \right)^2 \frac{k_B m V^{\frac{1}{3}}}{\hbar \gamma_a^2}.$$

where V is the volume of the unit cell and m is the average atomic mass. It should be noted that the Debye temperature and Grüneisen parameter in this formula, θ_a and γ_a , are slightly different from the traditional Debye temperature, θ_D , calculated in Eq. (15) and Grüneisen parameter, γ , obtained from Eq. (36). Instead, θ_a and γ_a are obtained by only considering the acoustic modes, based on the assumption that the optical phonon modes in crystals do not contribute to heat transport⁵³. This θ_a is referred to as the “acoustic” Debye temperature^{53,54}. It can be derived directly from the phonon DOS by integrating only over the acoustic modes^{53,57}. Alternatively, it can be calculated from the traditional Debye temperature θ_D ^{53,54}

$$\theta_a = \theta_D n^{-\frac{1}{3}}. \quad (38)$$

There is no simple way to extract the “acoustic” Grüneisen parameter from the traditional Grüneisen parameter. Instead, it must be calculated from Eq. (31) for each phonon branch separately and summed over the acoustic branches^{56,58}. This requires using the quasi-harmonic phonon approximation which involves calculating the full phonon spectrum for different volumes^{56–58}, and is therefore too computationally demanding to be used for high-throughput screening, particularly for large, low symmetry systems. Therefore, we use the approximation $\gamma_a = \gamma$ in the AEL-AGL approach to calculate the thermal conductivity. The dependence of the expression in Eq. (37) on γ is weak^{34,54}, thus the evaluation of κ_l using the traditional Grüneisen parameter introduces just a small systematic error which is insignificant for screening purposes⁵⁸.

The thermal conductivity at temperatures other than θ_a is estimated by^{53–55}:

$$\kappa_l(T) = \kappa_l(\theta_a) \frac{\theta_a}{T}. \quad (39)$$

F. DFT calculations and workflow details

The DFT calculations to obtain $E(V)$ and the strain tensors were performed using the VASP software⁵⁹ with projector-augmented-wave pseudopotentials⁶⁰ and the PBE parameterization of the generalized gradient approximation to the exchange-correlation functional⁶¹, using the parameters described in the AFLOW Standard³⁷. The energies were calculated at zero temperature and pressure, with spin polarization and without zero-point motion or

lattice vibrations. The initial crystal structures were fully relaxed (cell volume and shape and the basis atom coordinates inside the cell).

For the AEL calculations, 4 strains were applied in each independent lattice direction (two compressive and two expansive) with a maximum strain of 1% in each direction, for a total of 24 configurations¹⁴. For cubic systems, the crystal symmetry was used to reduce the number of required strain configurations to 8. For each configuration, two ionic positions AFLOW Standard RELAX³⁷ calculations at fixed cell volume and shape were followed by a single AFLOW Standard STATIC³⁷ calculation. The elastic constants are then calculated by fitting the elements of stress tensor obtained for each independent strain. The stress tensor from the zero-strain configuration (i.e. the initial unstrained relaxed structure) can also be included in the set of fitted strains, although this was found to have negligible effect on the results. Once these calculations are complete, it is verified that the eigenvalues of the stiffness tensor are all positive, that the stiffness tensor obeys the appropriate symmetry rules for the lattice type³, and that the applied strain is still within the linear regime, using the method described by de Jong et al.¹⁴. If any of these conditions fail, the calculation is repeated with adjusted applied strain.

The AGL calculation of $E(V)$ is fitted to the energy at 28 different volumes of the unit cell obtained by increasing or decreasing the relaxed lattice parameters in fractional increments of 0.01, with a single AFLOW Standard STATIC³⁷ calculation at each volume. The resulting $E(V)$ data is checked for convexity and to verify that the minimum energy is at the initial volume (i.e. at the properly relaxed cell size). If any of these conditions fail, the calculation is repeated with adjusted parameters, e.g. increased k-point grid density.

G. Correlation Analysis

Pearson and Spearman correlations are used to analyze the results for entire sets of materials. The Pearson coefficient r is a measure of the linear correlation between two variables, X and Y . It is calculated by

$$r = \frac{\sum_{i=1}^n (X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^n (X_i - \bar{X})^2} \sqrt{\sum_{i=1}^n (Y_i - \bar{Y})^2}}, \quad (40)$$

where \bar{X} and \bar{Y} are the mean values of X and Y .

The Spearman coefficient ρ is a measure of the monotonicity of the relation between two variables. The raw values of the two variables X_i and Y_i are sorted in ascending order, and are assigned rank values x_i and y_i which are equal to their position in the sorted list. If there is more than one variable with the same value, the average of the position values are assigned to all duplicate entries.

The correlation coefficient is then given by

$$\rho = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}}. \quad (41)$$

It is useful for determining how well the ranking order of the values of one variable predict the ranking order of the values of the other variable.

The discrepancy between the AEL-AGL predictions and experiment is evaluated in terms normalized root-mean-square relative deviation

$$\text{RMSrD} = \sqrt{\frac{\sum_{i=1}^n \left(\frac{X_i - Y_i}{X_i} \right)^2}{N - 1}}, \quad (42)$$

In contrast to the correlations described above, lower values of the RMSrD indicate better agreement with experiment. This measure is particularly useful for comparing predictions of the same property using different methodologies that may have very similar correlations with, but different deviations from, the experimental results.

III. RESULTS

We used the AEL-AGL methodology to calculate the mechanical and thermal properties, including the bulk modulus, shear modulus, Poisson ratio, Debye temperature, Grüneisen parameter and thermal conductivity for a set of 74 materials with structures including diamond, zincblende, rocksalt, wurzite, rhombohedral and body-centred tetragonal. The results have been compared to experimental values (where available), and the correlations between the calculated and experimental values were deduced. In cases where multiple experimental values are present in the literature, we used the most recently reported value, unless otherwise specified.

In Section II A, three different approximations for the bulk and shear moduli are described: Voigt (Eqs. (2), (3)), Reuss (Eqs. (4), (5)), and the Voigt-Reuss-Hill (VRH) average (Eqs. (6), (7)). These approximations give very similar values for the bulk modulus for the set of materials included in this work, particularly those with cubic symmetry. Therefore only $B_{\text{VRH}}^{\text{AEL}}$ is explicitly cited in the following listed results (the values obtained for all three approximations are available in the AFLOW database entries for these materials). The values for the shear modulus in these three approximations exhibit larger variations, and are therefore all listed and compared to experiment. In several cases, the experimental values of the bulk and shear moduli have been calculated from the measured elastic constants using Eqs. (2) through (7), and an experimental Poisson ratio σ^{exp} was calculated from these values using Eq. (8).

As described in Section II C, the bulk modulus in AGL can be calculated from a polynomial fit of the $E(V)$ data as shown in Eq. (16), or by fitting the $E(V)$ data to one of

three empirical equations of state: Birch-Murnaghan (Eq. (21)), Vinet (Eq. (23)), and the Baonza-Cáceres-Núñez (Eq. (26)). We compare the results of these four methods, labeled $B_{\text{Static}}^{\text{AGL}}$, $B_{\text{Static}}^{\text{BM}}$, $B_{\text{Static}}^{\text{Vinet}}$, and $B_{\text{Static}}^{\text{BCN}}$, respectively, with the experimental values B^{exp} and those obtained from the elastic calculations $B_{\text{VRH}}^{\text{AEL}}$. The Debye temperatures, Grüneisen parameters and thermal conductivities depend on the calculated bulk modulus and are therefore also cited below for each of the equations of state. Also included are the Debye temperatures derived from the calculated elastic constants and speed of sound as given by Eq. (11). The Debye temperatures, $\theta_{\text{D}}^{\text{BM}}$ (Eq. (21)), $\theta_{\text{D}}^{\text{Vinet}}$ (Eq. (23)), $\theta_{\text{D}}^{\text{BCN}}$, Eq. (26)), calculated using the Poisson ratio σ^{AEL} obtained from Eq. (8), are compared to $\theta_{\text{D}}^{\text{AGL}}$, obtained from the numerical fit of $E(V)$ (Eq. (16)) using both σ^{AEL} and the approximation $\sigma = 0.25$ used in Ref. 34, to $\theta_{\text{D}}^{\text{AEL}}$, calculated with the speed of sound obtained using Eq. (11), and to the experimental values θ^{exp} . The values of the acoustic Debye temperature (θ_{a} , Eq. (38)) are shown, where available, in parentheses below the traditional Debye temperature value.

The experimental Grüneisen parameter, γ^{exp} , is compared to γ^{AGL} (Eq. (16)), obtained using the numerical polynomial fit of $E(V)$ and both values of the Poisson ratio (σ^{AEL} and the approximation $\sigma = 0.25$ from Ref. 34), and to γ^{BM} (Eq. (21)), γ^{Vinet} (Eq. (23)), and γ^{BCN} (Eq. (26)), calculated using σ^{AEL} only. Similarly, the experimental lattice thermal conductivity κ^{exp} is compared to κ^{AGL} (Eq. (16)), obtained using the numerical polynomial fit and both the calculated and approximated values of σ , and to κ^{BM} (Eq. (21)), κ^{Vinet} (Eq. (23)), and κ^{BCN} (Eq. (26)), calculated using only σ^{AEL} .

The AEL method has been previously implemented in the Materials Project framework for calculating elastic constants¹⁴. Data from the Materials Project database are included in the tables below for comparison for the bulk modulus $B_{\text{VRH}}^{\text{MP}}$, shear modulus $G_{\text{VRH}}^{\text{MP}}$, and Poisson ratio σ^{MP} .

A. Zincblende and diamond structure materials

The mechanical and thermal properties were calculated for a set of materials with the zincblende(spacegroup: $F\bar{4}3m$, #216; Pearson symbol: cF8; AFLOW prototype: AB_cF8_216_c_a⁶²⁶³) and diamond ($Fd\bar{3}m$, #227; cF8; A_cF8_227_a⁶²⁶⁴) structures. This is the same set of materials as in Table I of Ref. 34, which in turn are from Table II of Ref. 53 and Table 2.2 of Ref. 54.

The elastic properties bulk modulus, shear modulus and Poisson ratio calculated using AEL and AGL are shown in Table I and Fig. 1, together with experimental values from the literature where available. As can be seen from the results in Table I and Fig. 1(a), the $B_{\text{VRH}}^{\text{AEL}}$ values are generally closest to experiment as shown by the RMSrD value of 0.13, producing an underestimate of the order of 10%. The AGL values from both the numerical fit and the empirical equations of state are generally very similar to

each other, while being slightly less than the $B_{\text{VRH}}^{\text{AEL}}$ values.

For the shear modulus, the experimental values G^{exp} are compared to the AEL values $G_{\text{Voigt}}^{\text{AEL}}$, $G_{\text{Reuss}}^{\text{AEL}}$ and $G_{\text{VRH}}^{\text{AEL}}$. As can be seen from the values in Table I and Fig. 1(b), the agreement with the experimental values is generally good with a very low RMSrD of 0.111 for $G_{\text{VRH}}^{\text{AEL}}$, with the Voigt approximation tending to overestimate and the Reuss approximation tending to underestimate, as would be expected. The experimental values of the Poisson ratio σ^{exp} and the AEL values σ^{AEL} (Eq. (8)) are also shown in Table I and Fig. 1(c), and the values are generally in good agreement. The Pearson (i.e. linear, Eq. (40)) and Spearman (i.e. rank order, Eq. (41)) correlations between all of the AEL-AGL elastic property values and experiment are shown in Table III, and are generally very high for all of these properties, ranging from 0.977 and 0.982 respectively for σ^{exp} vs. σ^{AEL} , up to 0.999 and 0.992 for B^{exp} vs. $B_{\text{VRH}}^{\text{AEL}}$. These very high correlation values demonstrate the validity of using the AEL-AGL methodology to predict the elastic and mechanical properties of materials.

The Materials Project values of $B_{\text{VRH}}^{\text{MP}}$, $G_{\text{VRH}}^{\text{MP}}$ and σ^{MP} for diamond and zincblende structure materials are also shown in Table I, where available. The Pearson correlations values for the experimental results with the available values of $B_{\text{VRH}}^{\text{MP}}$, $G_{\text{VRH}}^{\text{MP}}$ and σ^{MP} were calculated to be 0.995, 0.987 and 0.952, respectively, while the respective Spearman correlations were 0.963, 0.977 and 0.977, and the RMSrD values were 0.149, 0.116 and 0.126. For comparison, the corresponding Pearson correlations for the same subset of materials for $B_{\text{VRH}}^{\text{AEL}}$, $G_{\text{VRH}}^{\text{AEL}}$ and σ^{AEL} are 0.997, 0.987, and 0.957 respectively, while the respective Spearman correlations were 0.982, 0.977 and 0.977, and the RMSrD values were 0.129, 0.114 and 0.108. These correlation values are very similar, and the general close agreement for $B_{\text{VRH}}^{\text{AEL}}$, $G_{\text{VRH}}^{\text{AEL}}$ and σ^{AEL} with $B_{\text{VRH}}^{\text{MP}}$, $G_{\text{VRH}}^{\text{MP}}$ and σ^{MP} demonstrate that the small differences in the parameters used for the DFT calculations make little difference to the results, indicating that the parameter set used here is robust for high-throughput calculations.

The thermal properties Debye temperature, Grüneisen parameter and thermal conductivity calculated using AGL for this set of materials are compared to the experimental values taken from the literature in Table II and are also plotted in Fig. 1. For the Debye temperature, the experimental values θ^{exp} are compared to $\theta_{\text{D}}^{\text{AGL}}$, $\theta_{\text{D}}^{\text{BM}}$, $\theta_{\text{D}}^{\text{Vinet}}$ and $\theta_{\text{D}}^{\text{BCN}}$ in Fig. 1(e), while the values for the empirical equations of state are provided in the supplementary information. Note that the θ^{exp} values taken from Ref. 53 and Ref. 54 are for θ_{a} , and generally are in good agreement with the $\theta_{\text{a}}^{\text{AGL}}$ values. The values obtained using the numerical $E(V)$ fit and the three different equations of state are also in good agreement with each other, whereas the values of $\theta_{\text{D}}^{\text{AGL}}$ calculated using different σ values differ significantly, indicating that for this property the value of σ used is far more important than the equation of state used. The correlation between θ^{exp} and the various AGL values is also very high, of the order of 0.999, and the RMSrD is low, of the order of 0.13.

TABLE I. Bulk modulus, shear modulus and Poisson ratio of zincblende (AFLOW prototype: AB_cF8_216_c.a⁶²) and diamond (A_cF8_227_a⁶²) structure semiconductors. “N/A”= Not available for that source. Units: B and G in (GPa).

| Comp. | B^{exp} | $B_{\text{VRH}}^{\text{AEL}}$ | $B_{\text{VRH}}^{\text{MP}}$ | $B_{\text{Static}}^{\text{AGL}}$ | $B_{\text{Static}}^{\text{BM}}$ | $B_{\text{Static}}^{\text{Vinet}}$ | $B_{\text{Static}}^{\text{BCN}}$ | G^{exp} | $G_{\text{Voigt}}^{\text{AEL}}$ | $G_{\text{Reuss}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{MP}}$ | σ^{exp} | σ^{AEL} | σ^{MP} |
|-------|------------------------------------------------------------------------|-------------------------------|------------------------------|----------------------------------|---------------------------------|------------------------------------|----------------------------------|---------------------------------------------|---------------------------------|---------------------------------|-------------------------------|------------------------------|-----------------------------------------------|-----------------------|----------------------|
| C | 442 ^{65,67} | 434 | N/A | 408 | 409 | 403 | 417 | 534 ^{65,67} | 520 | 516 | 518 | N/A | 0.069 ^{65,67} | 0.073 | N/A |
| SiC | 248 ⁶⁸ 211 ^{65,66} | 212 | 211 | 203 | 207 | 206 | 206 | 196 ⁶⁹ 170 ⁶⁵ | 195 | 178 | 187 | 187 | 0.145 ^{66,69} 0.183 ⁶⁵ | 0.160 | 0.16 |
| Si | 97.8 ^{65,70} 98 ⁶⁶ | 89.1 | 83.0 | 84.2 | 85.9 | 85.0 | 86.1 | 66.5 ^{65,70} | 64 | 61 | 62.5 | 61.2 | 0.223 ^{65,70} | 0.216 | 0.2 |
| Ge | 75.8 ^{65,71} 77.2 ⁶⁶ | 61.5 | 59.0 | 54.9 | 55.7 | 54.5 | 56.1 | 55.3 ^{65,71} | 47.7 | 44.8 | 46.2 | 45.4 | 0.207 ^{65,71} | 0.199 | 0.19 |
| BN | 367.0 ⁶⁶ | 372 | N/A | 353 | 356 | 348 | 359 | N/A | 387 | 374 | 380 | N/A | N/A | 0.119 | N/A |
| BP | 165.0 ^{65,66} 267 ^{65,73} 172 ^{65,72} | 162 | 161 | 155 | 157 | 156 | 157 | 136 ^{65,72} | 164 | 160 | 162 | 162 | 0.186 ^{65,72} | 0.125 | 0.12 |
| AlP | 86.0 ⁶⁶ | 82.9 | 85.2 | 78.9 | 80.4 | 79.5 | 80.4 | N/A | 48.6 | 44.2 | 46.4 | 47.2 | N/A | 0.264 | 0.27 |
| AlAs | 77.0 ⁶⁶ 74 ⁷⁴ | 67.4 | 69.8 | 63.8 | 65.1 | 64.0 | 65.3 | N/A | 41.1 | 37.5 | 39.3 | 39.1 | N/A | 0.256 | 0.26 |
| AlSb | 58.2 ^{65,66,75,76} | 49.4 | 49.2 | 46.5 | 47.8 | 46.9 | 47.8 | 31.9 ^{65,75,76} | 29.7 | 27.4 | 28.5 | 29.6 | 0.268 ^{65,75,76} | 0.258 | 0.25 |
| GaP | 88.7 ⁶⁶ 89.8 ⁷⁷ | 78.8 | 76.2 | 71.9 | 73.4 | 72.2 | 73.8 | 55.3 ⁷⁷ | 53.5 | 49.1 | 51.3 | 51.8 | 0.244 ⁷⁷ | 0.232 | 0.22 |
| GaAs | 74.8 ⁶⁶ 75.5 ⁷⁸ | 62.7 | 60.7 | 56.8 | 57.7 | 56.6 | 58.1 | 46.6 ⁷⁸ | 42.6 | 39.1 | 40.8 | 40.9 | 0.244 ⁷⁸ | 0.233 | 0.23 |
| GaSb | 57.0 ⁶⁶ 56.3 ⁷⁷ | 47.0 | 44.7 | 41.6 | 42.3 | 41.2 | 42.6 | 34.2 ⁷⁷ | 30.8 | 28.3 | 29.6 | 30.0 | 0.248 ⁷⁷ | 0.240 | 0.23 |
| InP | 71.1 ^{66,79} | 60.4 | N/A | 56.4 | 57.6 | 56.3 | 57.8 | 34.3 ⁷⁹ | 33.6 | 29.7 | 31.6 | N/A | 0.292 ⁷⁹ | 0.277 | N/A |
| InAs | 60.0 ⁶⁶ 57.9 ^{65,80} | 50.1 | 49.2 | 45.7 | 46.6 | 45.4 | 46.9 | 29.5 ^{65,80} | 27.3 | 24.2 | 25.7 | 25.1 | 0.282 ^{65,80} | 0.281 | 0.28 |
| InSb | 47.3 ^{66,81} 48.3 ^{65,82} 46.5 ⁸³ | 38.1 | N/A | 34.3 | 35.0 | 34.1 | 35.2 | 22.1 ⁸¹ 23.7 ^{65,82} | 21.3 | 19.0 | 20.1 | N/A | 0.298 ⁸¹ 0.289 ^{65,82} | 0.275 | N/A |
| ZnS | 77.1 ⁶⁶ 74.5 ⁶⁵ | 71.2 | 68.3 | 65.8 | 66.1 | 65.2 | 66.6 | 30.9 ⁶⁵ | 36.5 | 31.4 | 33.9 | 33.2 | 0.318 ⁶⁵ | 0.294 | 0.29 |
| ZnSe | 62.4 ^{66,84} | 58.2 | 58.3 | 53.3 | 53.8 | 52.8 | 54.1 | 29.1 ⁸⁴ | 29.5 | 25.6 | 27.5 | 27.5 | 0.298 ⁸⁴ | 0.296 | 0.3 |
| ZnTe | 51.0 ^{66,84} | 43.8 | 46.0 | 39.9 | 40.5 | 39.4 | 40.7 | 23.4 ⁸⁴ | 23.3 | 20.8 | 22.1 | 22.4 | 0.30 ⁸⁴ | 0.284 | 0.29 |
| CdSe | 53.0 ⁶⁶ | 46.7 | 44.8 | 41.5 | 42.1 | 41.1 | 42.3 | N/A | 16.2 | 13.1 | 14.7 | 15.3 | N/A | 0.358 | 0.35 |
| CdTe | 42.4 ⁶⁶ | 36.4 | 35.3 | 32.2 | 32.7 | 31.9 | 32.8 | N/A | 14.2 | 11.9 | 13.0 | 13.6 | N/A | 0.340 | 0.33 |
| HgSe | 50.0 ⁶⁶ 48.5 ⁸⁵ | 43.8 | 41.2 | 39.0 | 39.7 | 38.5 | 39.9 | 14.8 ⁸⁵ | 15.6 | 11.9 | 13.7 | 13.3 | 0.361 ⁸⁵ | 0.358 | 0.35 |
| HgTe | 42.3 ^{65,66,86} | 35.3 | N/A | 31.0 | 31.6 | 30.8 | 31.9 | 14.7 ^{65,86} | 14.4 | 11.6 | 13.0 | N/A | 0.344 ^{65,86} | 0.335 | N/A |

The experimental values γ^{exp} of the Grüneisen parameter are plotted against γ^{AGL} , γ^{BM} , γ^{Vinet} and γ^{BCN} in Fig. 1(f), and the values are listed in Table II and in the supplementary information. The very high RMSrD values (see Table III) show that AGL has problems accurately predicting the Grüneisen parameter for this set of materials, as the calculated value is often 2 to 3 times larger than the experimental one. Note also that there are quite large differences between the values obtained for different equations of state, with γ^{BCN} generally having the lowest values while γ^{Vinet} has the highest values. On the other hand, in contrast to the case of $\theta_{\text{D}}^{\text{AGL}}$, the value of σ used makes little difference to the value of γ^{AGL} . The correlations between γ^{exp} and the AGL values, as shown in Table III, are also quite poor, with no value higher than 0.2 for the Pearson correlations, and negative Spearman correlations.

The experimental thermal conductivity κ^{exp} is compared in Fig. 1(d) to the thermal conductivities calculated with AGL using the Leibfried-Schlömann equation (Eq. (37)): κ^{AGL} , κ^{BM} , κ^{Vinet} and κ^{BCN} , while the values are listed in Table II and in the supplementary information. The absolute agreement between the AGL values and κ^{exp} is quite poor, with RMSrD values of the order of

0.8 and discrepancies of tens, or even hundreds, of percent quite common. Considerable disagreements also exist between different experimental reports of these properties, in almost all cases where they exist. Unfortunately, the scarcity of experimental data from different sources on the thermal properties of these materials prevents reaching definite conclusions regarding the true values of these properties. The available data can thus only be considered as a rough indication of their order of magnitude.

The Pearson correlations between the AGL calculated thermal conductivity values and the experimental values are high, ranging from 0.871 to 0.932, while the Spearman correlations are even higher, ranging from 0.905 to 0.954, as shown in Table III. In particular, note that using the σ^{AEL} in the AGL calculations improves the correlations by about 5%, from 0.878 to 0.927 and from 0.905 to 0.954. For the different equations of state, κ^{AGL} and κ^{BCN} appear to correlate better with κ^{exp} than κ^{BM} and κ^{Vinet} for this set of materials.

As we noted in our previous work on AGL³⁴, some of the inaccuracy in the thermal conductivity results may be due to the inability of the Leibfried-Schlömann equation to fully describe effects such as the suppression of phonon-

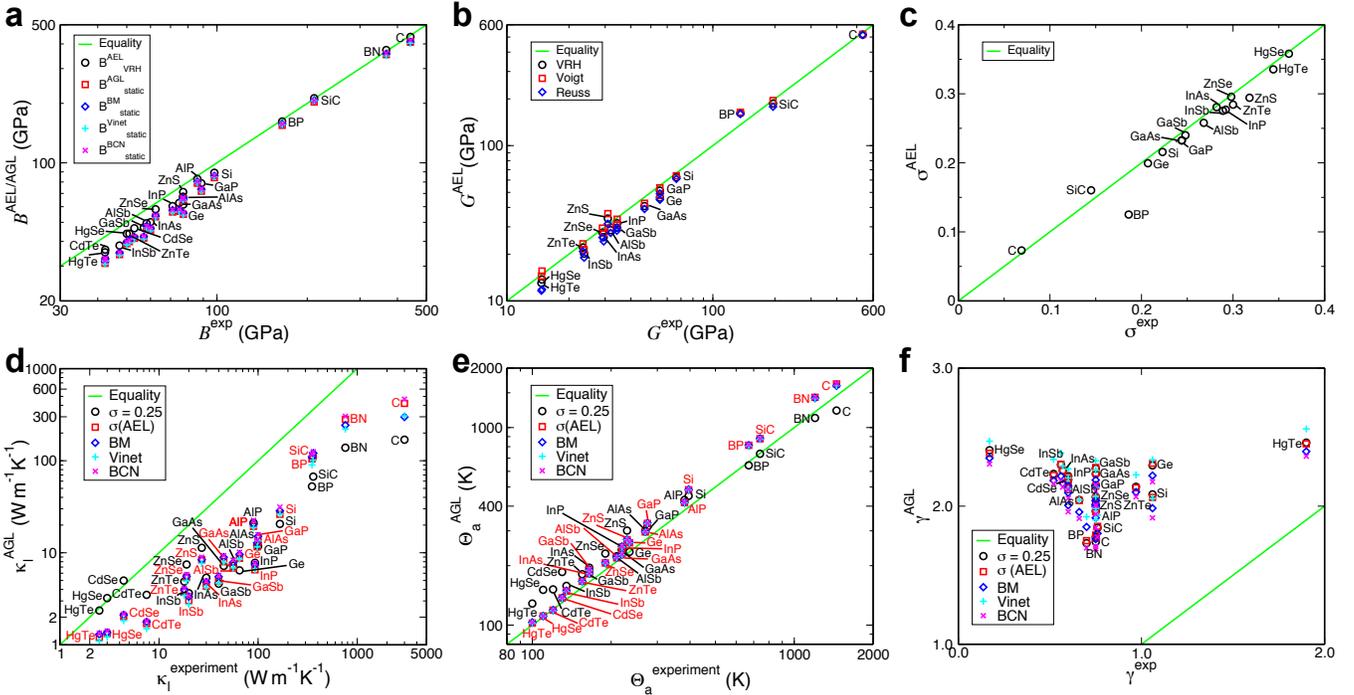


FIG. 1. (a) Bulk modulus, (b) shear modulus, (c) Poisson ratio, (d) lattice thermal conductivity at 300K, (e) acoustic Debye temperature and (f) Grüneisen parameter of zincblende (AFLOW prototype: AB.cF8.216.c.a⁶²) and diamond (A.cF8.227.a⁶²) structure semiconductors.

phonon scattering due to large gaps between the branches of the phonon dispersion²⁶. This can be seen from the thermal conductivity values shown in Table 2.2 of Ref. 54 calculated using the experimental values of θ_a and γ in the Leibfried-Schlömann equation. There are large discrepancies in certain cases such as diamond, while the Pearson and Spearman correlations of 0.932 and 0.941 respectively are very similar to the correlations we calculated using the AGL evaluations of θ_a and γ .

Thus, the unsatisfactory quantitative reproduction of these quantities by the Debye quasi-harmonic model has little impact on its effectiveness as a screening tool for identifying high or low thermal conductivity materials. The model can be used when these experimental values are unavailable to help determine the relative values of these quantities and for ranking materials conductivity.

B. Rocksalt structure materials

The mechanical and thermal properties were calculated for a set of materials with the rocksalt structure (space-group: $Fm\bar{3}m$, #225; Pearson symbol: cF8; AFLOW prototype: AB.cF8.225.a.b^{62,92}). This is the same set of materials as in Table II of Ref. 34, which in turn are from the sets in Table III of Ref. 53 and Table 2.1 of Ref. 54.

The elastic properties of bulk modulus, shear modulus and Poisson ratio, as calculated using AEL and AGL are shown in Table IV and Fig. 2, together with experimental values from the literature where available. As can be seen from the results in Table IV and Fig. 2(a), for this

set of materials the $B_{\text{VRH}}^{\text{AEL}}$ values are closest to experiment, with an RMSrD of 0.078. The AGL values from both the numerical fit and the empirical equations of state are generally very similar to each other, while being slightly less than the $B_{\text{VRH}}^{\text{AEL}}$ values.

For the shear modulus, the experimental values G^{exp} are compared to the AEL values $G_{\text{Voigt}}^{\text{AEL}}$, $G_{\text{Reuss}}^{\text{AEL}}$ and G^{AEL} . As can be seen from the values in Table IV and Fig. 2(b), the agreement with the experimental values is generally good with an RMSrD of 0.105 for $G_{\text{VRH}}^{\text{AEL}}$, with the Voigt approximation tending to overestimate and the Reuss approximation tending to underestimate, as would be expected. The experimental values of the Poisson ratio σ^{exp} and the AEL values σ^{AEL} (Eq. (8)) are also shown in Table IV and Fig. 2(c), and the values are generally in good agreement. The Pearson (i.e. linear, Eq. (40)) and Spearman (i.e. rank order, Eq. (41)) correlations between all of the the AEL-AGL elastic property values and experiment are shown in Table VI, and are generally very high for all of these properties, ranging from 0.959 and 0.827 respectively for σ^{exp} vs. σ^{AEL} , up to 0.998 and 0.995 for B^{exp} vs. $B_{\text{VRH}}^{\text{AEL}}$. These very high correlation values demonstrate the validity of using the AEL-AGL methodology to predict the elastic and mechanical properties of materials.

The values of $B_{\text{VRH}}^{\text{MP}}$, $G_{\text{VRH}}^{\text{MP}}$ and σ^{MP} for rocksalt structure materials are also shown in Table IV, where available. The Pearson correlations for the experimental results with the available values of $B_{\text{VRH}}^{\text{MP}}$, $G_{\text{VRH}}^{\text{MP}}$ and σ^{MP} were calculated to be 0.997, 0.994 and 0.890, respectively, while the respective Spearman correlations were 0.979, 0.998 and 0.817, and the RMSrD values were 0.153, 0.105 and 0.126.

TABLE II. Thermal properties lattice thermal conductivity at 300K, Debye temperature and Grüneisen parameter of zincblende (AFLOW prototype: AB_cF8_216_c_a⁶²) and diamond (A_cF8_227_a⁶²) structure semiconductors, comparing the effect of using the calculated value of the Poisson ratio to the previous approximation of $\sigma = 0.25$. The values listed for θ^{exp} are θ_a , except 141K for HgTe which is θ_D ⁸⁷. Units: κ in ($\text{W m}^{-1}\text{K}^{-1}$), θ in (K).

| Comp. | κ^{exp} | κ^{AGL} | κ^{AGL} | θ^{exp} | θ_D^{AGL} (θ_a^{AGL}) | θ_D^{AGL} (θ_a^{AGL}) | θ_D^{AEL} | γ^{exp} | γ^{AGL} | γ^{AGL} |
|-------|----------------------------------------|------------------------|-----------------------|------------------------------------------|--------------------------------------------------------|--------------------------------------------------------|-------------------------|------------------------------------------|------------------------|-----------------------|
| | | $(\sigma = 0.25)^{34}$ | | | $(\sigma = 0.25)^{34}$ | | | | $(\sigma = 0.25)^{34}$ | |
| C | 3000 ⁵⁴ | 169.1 | 419.9 | 1450 ^{53,54} | 1536 (1219) | 2094 (1662) | 2222 | 0.75 ⁵⁴ 0.9 ⁵³ | 1.74 | 1.77 |
| SiC | 360 ⁸⁸ | 67.19 | 113.0 | 740 ⁵³ | 928 (737) | 1106 (878) | 1143 | 0.76 ⁵³ | 1.84 | 1.85 |
| Si | 166 ⁵⁴ | 20.58 | 26.19 | 395 ^{53,54} | 568 (451) | 610 (484) | 624 | 1.06 ⁵⁴ 0.56 ⁵³ | 2.09 | 2.06 |
| Ge | 65 ⁵⁴ | 6.44 | 8.74 | 235 ^{53,54} | 296 (235) | 329 (261) | 342 | 1.06 ⁵⁴ 0.76 ⁵³ | 2.3 | 2.31 |
| BN | 760 ⁵⁴ | 138.4 | 281.6 | 1200 ⁵⁴ | 1409 (1118) | 1793 (1423) | 1887 | 0.7 ⁵⁴ | 1.73 | 1.75 |
| BP | 350 ⁵⁴ | 52.56 | 105.0 | 670 ^{53,54} | 811 (644) | 1025 (814) | 1062 | 0.75 ⁵⁴ | 1.78 | 1.79 |
| AlP | 90 ^{89,90} | 21.16 | 19.34 | 381 ⁵⁴ | 542 (430) | 525 (417) | 531 | 0.75 ⁵⁴ | 1.96 | 1.96 |
| AlAs | 98 ⁵⁴ | 12.03 | 11.64 | 270 ^{53,54} | 378 (300) | 373 (296) | 377 | 0.66 ^{53,54} | 2.04 | 2.04 |
| AlSb | 56 ⁵⁴ | 7.22 | 6.83 | 210 ^{53,54} | 281 (223) | 276 (219) | 277 | 0.6 ^{53,54} | 2.12 | 2.13 |
| GaP | 100 ⁵⁴ | 11.76 | 13.34 | 275 ^{53,54} | 396 (314) | 412 (327) | 423 | 0.75 ⁵⁴ 0.76 ⁵³ | 2.15 | 2.15 |
| GaAs | 45 ⁵⁴ | 7.2 | 8.0 | 220 ^{53,54} | 302 (240) | 313 (248) | 322 | 0.75 ^{53,54} | 2.23 | 2.24 |
| GaSb | 40 ⁵⁴ | 4.62 | 4.96 | 165 ^{53,54} | 234 (186) | 240 (190) | 248 | 0.75 ^{53,54} | 2.27 | 2.28 |
| InP | 93 ⁵⁴ | 7.78 | 6.53 | 220 ^{53,54} | 304 (241) | 286 (227) | 287 | 0.6 ^{53,54} | 2.22 | 2.21 |
| InAs | 30 ⁵⁴ | 5.36 | 4.33 | 165 ^{53,54} | 246 (195) | 229 (182) | 231 | 0.57 ^{53,54} | 2.26 | 2.26 |
| InSb | 20 ⁵⁴ 16.5 ⁸⁷ | 3.64 | 3.02 | 135 ^{53,54} | 199 (158) | 187 (148) | 190 | 0.56 ^{53,54} | 2.3 | 2.3 |
| ZnS | 27 ⁵⁴ | 11.33 | 8.38 | 230 ^{53,54} | 379 (301) | 341 (271) | 346 | 0.75 ^{53,54} | 2.01 | 2.00 |
| ZnSe | 19 ⁵⁴ 33 ⁸⁷ | 7.46 | 5.44 | 190 ^{53,54} | 290 (230) | 260 (206) | 263 | 0.75 ^{53,54} | 2.07 | 2.06 |
| ZnTe | 18 ⁵⁴ | 4.87 | 3.83 | 155 ^{53,54} | 228 (181) | 210 (167) | 212 | 0.97 ^{53,54} | 2.14 | 2.13 |
| CdSe | 4.4 ⁸⁷ | 4.99 | 2.04 | 130 ⁵⁴ | 234 (186) | 173 (137) | 174 | 0.6 ⁵⁴ | 2.19 | 2.18 |
| CdTe | 7.5 ⁵⁴ | 3.49 | 1.71 | 120 ^{53,54} | 191 (152) | 150 (119) | 152 | 0.52 ^{53,54} | 2.23 | 2.22 |
| HgSe | 3 ⁹¹ | 3.22 | 1.32 | 110 ⁵³ | 190 (151) | 140 (111) | 140 | 0.17 ⁵³ | 2.4 | 2.38 |
| HgTe | 2.5 ⁸⁷ | 2.36 | 1.21 | 141 ⁸⁷ (100) ⁵³ | 162 (129) | 129 (102) | 130 | 1.9 ⁸⁷ | 2.46 | 2.45 |

For comparison, the corresponding Pearson correlations for the same subset of materials for $B_{\text{VRH}}^{\text{AEL}}$, $G_{\text{VRH}}^{\text{AEL}}$ and σ^{AEL} are 0.998, 0.995, and 0.951 respectively, while the respective Spearman correlations were 0.996, 1.0 and 0.843, and the RMSrD values were 0.079, 0.111 and 0.071. These correlation values are very similar, and the general close agreement for the results for the values of $B_{\text{VRH}}^{\text{AEL}}$, $G_{\text{VRH}}^{\text{AEL}}$ and σ^{AEL} with those of $B_{\text{VRH}}^{\text{MP}}$, $G_{\text{VRH}}^{\text{MP}}$ and σ^{MP} demonstrate that the small differences in the parameters used for the DFT calculations make little difference to the results, indicating that the parameter set used here is robust for high-throughput calculations.

The thermal properties of Debye temperature,

Grüneisen parameter and thermal conductivity calculated using AGL are compared to the experimental values taken from the literature in Table V and are also plotted in Fig. 2. For the Debye temperature, the experimental values θ^{exp} are compared to θ_D^{AGL} , θ_D^{BM} , θ_D^{Vinet} and θ_D^{BCN} in Fig. 2(e), while the actual values for the empirical equations of state are provided in the supplementary information. Note that the θ^{exp} values taken from Ref. 53 and Ref. 54 are for θ_a , and generally are in good agreement with the θ_a^{AGL} values. The values obtained using the numerical $E(V)$ fit and the three different equations of state are also in good agreement with each other, whereas the values of θ_D^{AGL} calculated using

TABLE IV. Mechanical properties bulk modulus, shear modulus and Poisson ratio of rocksalt (AFLOW Prototype: AB_cf8_225_a.b⁶²) structure semiconductors. “N/A” = Not available for that source. Units: B and G in (GPa).

| Comp. | B^{exp} | $B_{\text{VRH}}^{\text{AEL}}$ | $B_{\text{VRH}}^{\text{MP}}$ | $B_{\text{Static}}^{\text{AGL}}$ | $B_{\text{Static}}^{\text{BM}}$ | $B_{\text{Static}}^{\text{Vinet}}$ | $B_{\text{Static}}^{\text{BCN}}$ | G^{exp} | $G_{\text{Voigt}}^{\text{AEL}}$ | $G_{\text{Reuss}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{MP}}$ | σ^{exp} | σ^{AEL} | σ^{MP} |
|-------|------------------------|-------------------------------|------------------------------|----------------------------------|---------------------------------|------------------------------------|----------------------------------|------------------------|---------------------------------|---------------------------------|-------------------------------|------------------------------|-------------------------|-----------------------|----------------------|
| LiH | 33.7 ⁹³ | 37.7 | 36.1 | 29.5 | 29.0 | 27.7 | 31.4 | 36.0 ⁹³ | 43.4 | 42.3 | 42.8 | 42.9 | 0.106 ⁹³ | 0.088 | 0.07 |
| LiF | 69.6 ⁹⁴ | 70.4 | 69.9 | 58.6 | 59.9 | 57.5 | 61.2 | 48.8 ⁹⁴ | 46.4 | 45.8 | 46.1 | 50.9 | 0.216 ⁹⁴ | 0.231 | 0.21 |
| NaF | 48.5 ⁹⁴ | 46.9 | 47.6 | 38.7 | 38.6 | 36.8 | 39.3 | 31.2 ⁹⁴ | 29.5 | 28.4 | 28.9 | 30.0 | 0.236 ⁹⁴ | 0.244 | 0.24 |
| NaCl | 25.1 ⁹⁴ | 24.9 | 22.6 | 20.0 | 20.5 | 19.2 | 20.7 | 14.6 ⁹⁴ | 14.0 | 12.9 | 13.5 | 14.3 | 0.255 ⁹⁴ | 0.271 | 0.24 |
| NaBr | 20.6 ⁹⁴ | 20.5 | 27.1 | 16.3 | 16.9 | 15.7 | 16.9 | 11.6 ⁹⁴ | 11.0 | 9.9 | 10.4 | 11.6 | 0.264 ⁹⁴ | 0.283 | 0.31 |
| NaI | 15.95 ⁹⁴ | 16.4 | 15.8 | 12.6 | 13.2 | 12.2 | 13.1 | 8.59 ⁹⁴ | 8.35 | 7.31 | 7.83 | 8.47 | 0.272 ⁹⁴ | 0.295 | 0.27 |
| KF | 31.6 ⁹⁴ | 29.9 | 28.9 | 25.1 | 24.2 | 22.9 | 24.7 | 16.7 ⁹⁴ | 16.5 | 15.4 | 15.9 | 16.5 | 0.275 ⁹⁴ | 0.274 | 0.26 |
| KCl | 18.2 ⁹⁴ | 16.7 | 15.8 | 13.8 | 13.7 | 12.7 | 13.6 | 9.51 ⁹⁴ | 10.1 | 8.51 | 9.30 | 9.24 | 0.277 ⁹⁴ | 0.265 | 0.26 |
| KBr | 15.4 ⁹⁴ | 13.8 | 21.6 | 11.1 | 11.4 | 10.5 | 11.2 | 7.85 ⁹⁴ | 8.14 | 6.46 | 7.30 | 7.33 | 0.282 ⁹⁴ | 0.276 | 0.35 |
| KI | 12.2 ⁹⁴ | 10.9 | 9.52 | 8.54 | 9.03 | 8.28 | 8.84 | 5.96 ⁹⁴ | 6.05 | 4.39 | 5.22 | 5.55 | 0.290 ⁹⁴ | 0.294 | 0.26 |
| RbCl | 16.2 ⁹⁴ | 14.3 | 14.6 | 12.1 | 11.8 | 11.0 | 11.8 | 7.63 ⁹⁴ | 8.06 | 6.41 | 7.24 | 7.67 | 0.297 ⁹⁴ | 0.284 | 0.28 |
| RbBr | 13.8 ⁹⁴ | 12.6 | 13.8 | 10.3 | 9.72 | 9.06 | 9.67 | 6.46 ⁹⁴ | 7.12 | 5.24 | 6.18 | 6.46 | 0.298 ⁹⁴ | 0.289 | 0.3 |
| RbI | 11.1 ⁹⁴ | 9.90 | 9.66 | 8.01 | 7.74 | 7.12 | 7.54 | 5.03 ⁹⁴ | 5.50 | 3.65 | 4.57 | 4.63 | 0.303 ⁹⁴ | 0.300 | 0.29 |
| AgCl | 44.0 ⁹⁵ | 40.6 | N/A | 33.7 | 34.1 | 33.0 | 34.7 | 8.03 ⁹⁵ | 8.68 | 8.66 | 8.67 | N/A | 0.414 ⁹⁵ | 0.400 | N/A |
| MgO | 164 ⁹⁶ | 152 | 152 | 142 | 142 | 140 | 144 | 131 ⁹⁶ | 119 | 115 | 117 | 119 | 0.185 ⁹⁶ | 0.194 | 0.19 |
| CaO | 113 ⁹⁷ | 105 | 105 | 99.6 | 100 | 98.7 | 101 | 81.0 ⁹⁷ | 73.7 | 73.7 | 73.7 | 74.2 | 0.210 ⁹⁷ | 0.216 | 0.21 |
| SrO | 91.2 ⁹⁷ | 84.7 | 87.4 | 80.0 | 80.2 | 79.1 | 80.8 | 58.7 ⁹⁷ | 55.1 | 55.0 | 55.1 | 56.0 | 0.235 ⁹⁷ | 0.233 | 0.24 |
| BaO | 75.4 ⁹⁷ | 69.1 | 68.4 | 64.6 | 64.3 | 63.0 | 64.6 | 35.4 ⁹⁷ | 36.4 | 36.4 | 36.4 | 37.8 | 0.297 ⁹⁷ | 0.276 | 0.27 |
| PbS | 52.9 ^{65,98} | 53.5 | N/A | 49.9 | 50.8 | 50.0 | 51.0 | 27.9 ^{65,98} | 34.0 | 26.8 | 30.4 | N/A | 0.276 ^{65,98} | 0.261 | N/A |
| PbSe | 54.1 ^{65,99} | 47.7 | N/A | 43.9 | 44.8 | 43.9 | 44.9 | 26.2 ^{65,99} | 31.7 | 23.6 | 27.6 | N/A | 0.291 ^{65,99} | 0.257 | N/A |
| PbTe | 39.8 ^{65,100} | 39.5 | N/A | 36.4 | 36.6 | 35.8 | 36.8 | 23.1 ^{65,100} | 28.7 | 19.8 | 24.3 | N/A | 0.256 ^{65,100} | 0.245 | N/A |
| SnTe | 37.8 ^{65,101} | 40.4 | 39.6 | 38.1 | 38.4 | 37.6 | 38.6 | 20.8 ^{65,101} | 31.4 | 22.0 | 26.7 | 27.6 | 0.267 ^{65,101} | 0.229 | 0.22 |

0.445 to 0.556. In particular, note that using the σ^{AEL} in the AGL calculations improves the correlations by about 2% to 8%, from 0.910 to 0.932 and from 0.445 to 0.528. For the different equations of state, the results for κ^{BM} appear to correlate best with κ^{exp} for this set of materials.

As in the case of the diamond and zinblende structure materials discussed in the previous Section, Ref. 54 includes values of the thermal conductivity at 300K for rocksalt structure materials, calculated using the experimental values of θ_a and γ in the Leibfried-Schlömann equation, in Table 2.1. The correlation values of 0.986 and 0.761 with experiment are better than those obtained for the AGL results by a larger margin than for the zinblende materials. Nevertheless, the Pearson correlation between the calculated and experimental conductivities is high in both calculations, indicating that the AGL approach may be used as a screening tool for high or low conductivity compounds in cases where gaps exist in the experimental data for these materials.

C. Hexagonal structure materials

The experimental data for this set of materials appears in Table III of Ref. 34, taken from Table 2.3 of Ref. 54. Most of these materials have the wurtzite structure ($P6_3mc$, #186; Pearson symbol: hP4; AFLOW prototype: AB_hP4_186_b.b^{62,103}) except InSe which is $P6_3mmc$, #194, Pearson symbol: hP8.

The calculated elastic properties are shown in Table VII and Fig. 3. The bulk moduli values obtained from a direct calculation of the elastic tensor, $B_{\text{VRH}}^{\text{AEL}}$, are usually slightly

higher than those obtained from the $E(V)$ curve and are also closer to experiment (Table VII and Fig. 3(a)), with the exception of InSe where it is noticeably lower.

For the shear modulus, the experimental values G^{exp} are compared to the AEL values $G_{\text{Voigt}}^{\text{AEL}}$, $G_{\text{Reuss}}^{\text{AEL}}$ and $G_{\text{VRH}}^{\text{AEL}}$. As can be seen in Table VII and Fig. 3(b), the agreement with the experimental values is very good. Similarly good agreement is obtained for the Poisson ratio of most materials (Table VII and Fig. 3(c)), with a single exception for InSe where the calculation deviates significantly from the experiment. The Pearson (i.e. linear, Eq. (40)) and Spearman (i.e. rank order, Eq. (41)) correlations between the calculated elastic properties and their experimental values are generally quite high (Table IX), ranging from 0.851 and 0.893 respectively for σ^{exp} vs. σ^{AEL} , up to 0.998 and 1.0 for G^{exp} vs. $G_{\text{VRH}}^{\text{AEL}}$.

The Materials Project values of $B_{\text{VRH}}^{\text{MP}}$, $G_{\text{VRH}}^{\text{MP}}$ and σ^{MP} for hexagonal structure materials are also shown in Table VII, where available. The Pearson correlations values for the experimental results with the available values of $B_{\text{VRH}}^{\text{MP}}$, $G_{\text{VRH}}^{\text{MP}}$ and σ^{MP} were calculated to be 0.984, 0.998 and 0.993, respectively, while the respective Spearman correlations were 0.943, 1.0 and 0.943, and the RMSrD values were 0.117, 0.116 and 0.034. For comparison, the corresponding Pearson correlations for the same subset of materials for $B_{\text{VRH}}^{\text{AEL}}$, $G_{\text{VRH}}^{\text{AEL}}$ and σ^{AEL} are 0.986, 0.998, and 0.998 respectively, while the respective Spearman correlations were 0.943, 1.0 and 1.0, and the RMSrD values were 0.100, 0.091 and 0.036. These correlation values are very similar, and the general close agreement for the results for the values of $B_{\text{VRH}}^{\text{AEL}}$, $G_{\text{VRH}}^{\text{AEL}}$ and σ^{AEL} with those of $B_{\text{VRH}}^{\text{MP}}$, $G_{\text{VRH}}^{\text{MP}}$ and σ^{MP} demonstrate that the small differences in

TABLE V. Thermal properties lattice thermal conductivity at 300K, Debye temperature and Grüneisen parameter of rocksalt structure (AFLOW Prototype: AB.cF8.225_a.b⁶²) semiconductors, comparing the effect of using the calculated value of the Poisson ratio to previous approximation of $\sigma = 0.25$. The values listed for θ^{exp} are θ_a , except 155K for SnTe which is θ_D ⁸⁷. “N/A” = Not available for that source. Units: κ in ($\text{W m}^{-1}\text{K}^{-1}$), θ in (K).

| Comp. | κ^{exp} | κ^{AGL} | κ^{AGL} | θ^{exp} | θ_D^{AGL} (θ_a^{AGL}) | θ_D^{AGL} (θ_a^{AGL}) | θ_D^{AEL} | γ^{exp} | γ^{AGL} | γ^{AGL} |
|-------|-----------------------|------------------------|-----------------------|-----------------------|--------------------------------------------------------|--------------------------------------------------------|-------------------------|------------------------|-----------------------|-----------------------|
| | | $(\sigma = 0.25)^{34}$ | | | $(\sigma = 0.25)^{34}$ | | | $(\sigma = 0.25)^{34}$ | | |
| LiH | 15 ⁵⁴ | 8.58 | 18.6 | 615 ^{53,54} | 743 (590) | 962 (764) | 1175 | 1.28 ^{53,54} | 1.62 | 1.66 |
| LiF | 17.6 ⁵⁴ | 8.71 | 9.96 | 500 ^{53,54} | 591 (469) | 617 (490) | 681 | 1.5 ^{53,54} | 2.02 | 2.03 |
| NaF | 18.4 ⁵⁴ | 4.52 | 4.67 | 395 ^{53,54} | 411 (326) | 416 (330) | 455 | 1.5 ^{53,54} | 2.2 | 2.21 |
| NaCl | 7.1 ⁵⁴ | 2.43 | 2.12 | 220 ^{53,54} | 284 (225) | 271 (215) | 289 | 1.56 ^{53,54} | 2.23 | 2.23 |
| NaBr | 2.8 ⁵⁴ | 1.66 | 1.33 | 150 ^{53,54} | 203 (161) | 188 (149) | 198 | 1.5 ^{53,54} | 2.22 | 2.22 |
| NaI | 1.8 ⁵⁴ | 1.17 | 0.851 | 100 ^{53,54} | 156 (124) | 140 (111) | 147 | 1.56 ^{53,54} | 2.23 | 2.23 |
| KF | N/A | 2.68 | 2.21 | 235 ^{53,54} | 305 (242) | 288 (229) | 309 | 1.52 ^{53,54} | 2.29 | 2.32 |
| KCl | 7.1 ⁵⁴ | 1.4 | 1.25 | 172 ^{53,54} | 220 (175) | 213 (169) | 226 | 1.45 ^{53,54} | 2.38 | 2.40 |
| KBr | 3.4 ⁵⁴ | 1.0 | 0.842 | 117 ^{53,54} | 165 (131) | 156 (124) | 162 | 1.45 ^{53,54} | 2.37 | 2.37 |
| KI | 2.6 ⁵⁴ | 0.72 | 0.525 | 87 ^{53,54} | 129 (102) | 116 (92) | 120 | 1.45 ^{53,54} | 2.35 | 2.35 |
| RbCl | 2.8 ⁵⁴ | 1.09 | 0.837 | 124 ^{53,54} | 168 (133) | 155 (123) | 160 | 1.45 ^{53,54} | 2.34 | 2.37 |
| RbBr | 3.8 ⁵⁴ | 0.76 | 0.558 | 105 ^{53,54} | 134 (106) | 122 (97) | 129 | 1.45 ^{53,54} | 2.40 | 2.43 |
| RbI | 2.3 ⁵⁴ | 0.52 | 0.368 | 84 ^{53,54} | 109 (87) | 97 (77) | 102 | 1.41 ^{53,54} | 2.47 | 2.47 |
| AgCl | 1.0 ^{89,102} | 2.58 | 0.613 | 124 ⁵³ | 235 (187) | 145 (115) | 148 | 1.9 ⁵³ | 2.5 | 2.49 |
| MgO | 60 ⁵⁴ | 31.9 | 44.5 | 600 ^{53,54} | 758 (602) | 849 (674) | 890 | 1.44 ^{53,54} | 1.95 | 1.96 |
| CaO | 27 ⁵⁴ | 19.5 | 24.3 | 450 ^{53,54} | 578 (459) | 620 (492) | 638 | 1.57 ^{53,54} | 2.07 | 2.06 |
| SrO | 12 ⁵⁴ | 12.5 | 13.4 | 270 ^{53,54} | 399 (317) | 413 (328) | 421 | 1.52 ^{53,54} | 2.09 | 2.13 |
| BaO | 2.3 ⁵⁴ | 8.88 | 7.10 | 183 ^{53,54} | 305 (242) | 288 (229) | 292 | 1.5 ^{53,54} | 2.09 | 2.14 |
| PbS | 2.9 ⁵⁴ | 6.48 | 6.11 | 115 ^{53,54} | 226 (179) | 220 (175) | 221 | 2.0 ^{53,54} | 2.02 | 2.00 |
| PbSe | 2.0 ⁵⁴ | 4.88 | 4.81 | 100 ⁵⁴ | 197 (156) | 194 (154) | 196 | 1.5 ⁵⁴ | 2.1 | 2.07 |
| PbTe | 2.5 ⁵⁴ | 4.15 | 4.07 | 105 ^{53,54} | 170 (135) | 172 (137) | 175 | 1.45 ^{53,54} | 2.04 | 2.09 |
| SnTe | 1.5 ⁸⁷ | 4.46 | 5.24 | 155 ⁸⁷ | 202 (160) | 210 (167) | 212 | 2.1 ⁸⁷ | 2.15 | 2.11 |

the parameters used for the DFT calculations make little difference to the results, indicating that the parameter set used here is robust for high-throughput calculations.

The thermal properties calculated using AGL are compared to the experimental values in Table VIII and are also plotted in Fig. 3. For the Debye temperature, the θ^{exp} values taken from Ref. 54 are for θ_a , and are mostly in good agreement with the calculated θ_a^{AGL} values. As in

the case of the other materials sets, the values obtained using the numerical $E(V)$ fit and the three different equations of state are very similar to each other, whereas θ_D^{AGL} calculated using $\sigma = 0.25$ differs significantly. In fact, the values of θ_D^{AGL} calculated with σ^{AEL} have a lower the correlation with θ^{exp} than the values calculated with $\sigma = 0.25$ do, although the RMSrD values are lower when σ^{AEL} is used. However, most of this discrepancy appears to be

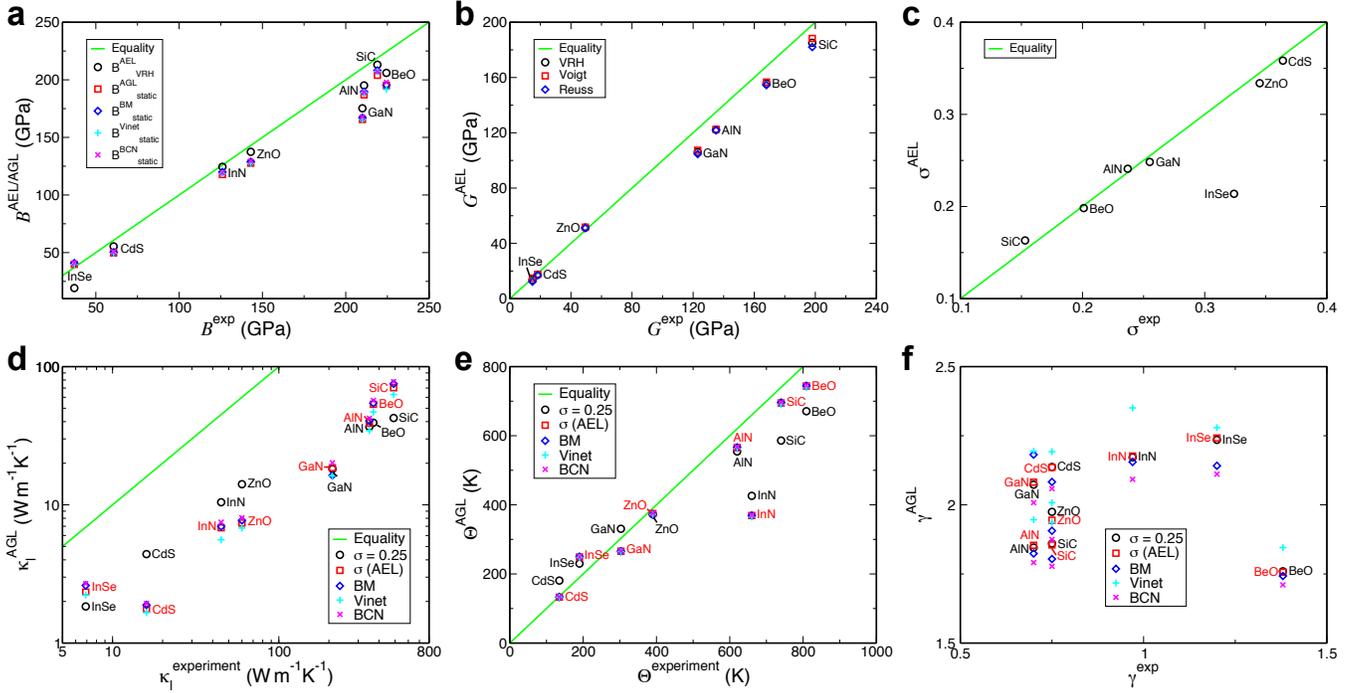


FIG. 3. (a) Bulk modulus, (b) shear modulus, (c) Poisson ratio, (d) lattice thermal conductivity, (e) Debye temperature and (f) Grüneisen parameter of hexagonal structure semiconductors. The Debye temperatures plotted in (e) are θ_a , except for InSe and InN where θ_D values are quoted in Refs. 87, 88, and 113.

TABLE VI. Correlations between experimental values and AEL and AGL results for elastic and thermal properties for rocksalt structure semiconductors.

| Property | Pearson (Linear) | Spearman (Rank Order) | RMSrD |
|---------------------------------------------------------------------------------------|---------------------|--------------------------|-------|
| κ^{exp} vs. κ^{AGL} ($\sigma = 0.25$) ³⁴ | 0.910 | 0.445 | 1.093 |
| κ^{exp} vs. κ^{AGL} | 0.932 | 0.528 | 1.002 |
| κ^{exp} vs. κ^{BM} | 0.940 | 0.556 | 1.038 |
| κ^{exp} vs. κ^{Vinet} | 0.933 | 0.540 | 0.920 |
| κ^{exp} vs. κ^{BCN} | 0.930 | 0.554 | 1.082 |
| θ_a^{exp} vs. θ_a^{AGL} ($\sigma = 0.25$) ³⁴ | 0.985 | 0.948 | 0.253 |
| θ_a^{exp} vs. θ_a^{AGL} | 0.978 | 0.928 | 0.222 |
| θ_a^{exp} vs. θ_a^{BM} | 0.980 | 0.926 | 0.222 |
| θ_a^{exp} vs. θ_a^{Vinet} | 0.979 | 0.925 | 0.218 |
| θ_a^{exp} vs. θ_a^{BCN} | 0.978 | 0.929 | 0.225 |
| γ^{exp} vs. γ^{AGL} ($\sigma = 0.25$) ³⁴ | 0.118 | -0.064 | 0.477 |
| γ^{exp} vs. γ^{AGL} | 0.036 | -0.110 | 0.486 |
| γ^{exp} vs. γ^{BM} | -0.019 | -0.088 | 0.462 |
| γ^{exp} vs. γ^{Vinet} | -0.098 | -0.086 | 0.591 |
| γ^{exp} vs. γ^{BCN} | 0.023 | -0.110 | 0.443 |
| B^{exp} vs. $B^{\text{AEL}}_{\text{VRH}}$ | 0.998 | 0.995 | 0.078 |
| B^{exp} vs. $B^{\text{AGL}}_{\text{Static}}$ | 0.998 | 0.993 | 0.201 |
| B^{exp} vs. $B^{\text{BM}}_{\text{Static}}$ | 0.997 | 0.993 | 0.199 |
| B^{exp} vs. $B^{\text{Vinet}}_{\text{Static}}$ | 0.997 | 0.990 | 0.239 |
| B^{exp} vs. $B^{\text{BCN}}_{\text{Static}}$ | 0.998 | 0.993 | 0.197 |
| C^{exp} vs. $C^{\text{AEL}}_{\text{VRH}}$ | 0.994 | 0.997 | 0.105 |
| C^{exp} vs. C^{Voigt} | 0.991 | 0.990 | 0.157 |
| C^{exp} vs. $C^{\text{AEL}}_{\text{Reuss}}$ | 0.995 | 0.995 | 0.142 |
| σ^{exp} vs. σ^{AEL} | 0.959 | 0.827 | 0.070 |

due to the clear outlier value for the material InN. When the values for this material are removed from the data set, the Pearson correlation values become very similar when both the $\sigma = 0.25$ and $\sigma = \sigma^{\text{AEL}}$ values are used,

increasing to 0.995 and 0.994 respectively.

The experimental and calculated values of the Grüneisen parameter are listed in Table VIII and in the supplementary information, and are plotted in Fig. 3(f). Again, the Debye model does not reproduce the experimental data, as the calculated values are often 2 to 3 times too large and the RMSrD is larger than 1.5. The corresponding correlation, shown in Table IX, are also quite poor, with no value higher than 0.160 for the Spearman correlations, and negative values for the Pearson correlations.

The comparison between the experimental thermal conductivity κ^{exp} and the calculated values is also quite poor (Fig. 3(d) and Table VIII), with RMSrD values of the order of 0.9. Considerable disagreements also exist between different experimental reports for most materials. Nevertheless, the Pearson correlations between the AGL calculated thermal conductivity values and the experimental values are high, ranging from 0.974 to 0.980, while the Spearman correlations are even higher, ranging from 0.976 to 1.0.

As for the rocksalt and zincblende material sets, Ref. 54 (Table 2.3) includes values of the thermal conductivity at 300K for wurzite structure materials, calculated using the experimental values of the Debye temperature and Grüneisen parameter in the Leibfried-Schlömann equation. The Pearson and Spearman correlations are 0.996 and 1.0 respectively, which are slightly higher than the correlations obtained using the AGL calculated quantities. The difference is insignificant since all of these correlations are very high and could reliably serve as a screening

TABLE VII. Bulk modulus, shear modulus and Poisson ratio of hexagonal structure semiconductors. “N/A” = Not available for that source. Units: B and G in (GPa).

| Comp. | B^{exp} | $B_{\text{VRH}}^{\text{AEL}}$ | $B_{\text{VRH}}^{\text{MP}}$ | $B_{\text{Static}}^{\text{AGL}}$ | $B_{\text{Static}}^{\text{BM}}$ | $B_{\text{Static}}^{\text{Vinet}}$ | $B_{\text{Static}}^{\text{BCN}}$ | G^{exp} | $G_{\text{Voigt}}^{\text{AEL}}$ | $G_{\text{Reuss}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{MP}}$ | σ^{exp} | σ^{AEL} | σ^{MP} |
|-------|------------------------|-------------------------------|------------------------------|----------------------------------|---------------------------------|------------------------------------|----------------------------------|------------------------|---------------------------------|---------------------------------|-------------------------------|------------------------------|-------------------------|-----------------------|----------------------|
| SiC | 219 ¹⁰⁴ | 213 | 213 | 204 | 208 | 207 | 207 | 198 ¹⁰⁴ | 188 | 182 | 185 | 187 | 0.153 ¹⁰⁴ | 0.163 | 0.16 |
| AlN | 211 ^{89,105} | 195 | 194 | 187 | 190 | 189 | 189 | 135 ^{89,105} | 123 | 122 | 122 | 122 | 0.237 ^{89,105} | 0.241 | 0.24 |
| | 200 ¹⁰⁶ | | | | | | | 130 ¹⁰⁶ | | | | | 0.234 ¹⁰⁶ | | |
| GaN | 195 ^{65,107} | 175 | 172 | 166 | 167 | 166 | 168 | 51.6 ^{65,107} | 107 | 105 | 106 | 105 | 0.378 ^{65,107} | 0.248 | 0.25 |
| | 210 ¹⁰⁸ | | | | | | | 123 ¹⁰⁸ | | | | | 0.255 ¹⁰⁸ | | |
| ZnO | 143 ^{65,109} | 137 | 130 | 128 | 129 | 127 | 129 | 49.4 ^{65,109} | 51.7 | 51.0 | 51.4 | 41.2 | 0.345 ^{65,109} | 0.334 | 0.36 |
| BeO | 224.4 ¹¹⁰ | 206 | 208 | 195 | 195 | 192 | 198 | 168 ¹¹⁰ | 157 | 154 | 156 | 156 | 0.201 ¹¹⁰ | 0.198 | 0.2 |
| CdS | 60.7 ^{65,109} | 55.4 | 53.3 | 49.7 | 50.3 | 49.4 | 50.6 | 18.2 ^{65,109} | 17.6 | 17.0 | 17.3 | 17.6 | 0.364 ^{65,109} | 0.358 | 0.35 |
| InSe | 37.1 ¹¹¹ | 19.2 | N/A | 39.8 | 40.8 | 39.7 | 41.0 | 14.8 ¹¹¹ | 14.9 | 12.3 | 13.6 | N/A | 0.324 ¹¹¹ | 0.214 | N/A |
| InN | 126 ¹¹² | 124 | N/A | 118 | 120 | 119 | 119 | N/A | 55.4 | 54.4 | 54.9 | N/A | N/A | 0.308 | N/A |

TABLE VIII. Lattice thermal conductivity, Debye temperature and Grüneisen parameter of hexagonal structure semiconductors, comparing the effect of using the calculated value of the Poisson ratio to previous approximation of $\sigma = 0.25$. The values listed for θ^{exp} are θ_a , except 190K for InSe⁸⁷ and 660K for InN^{88,113} which are θ_D . “N/A” = Not available for that source. Units: κ in ($\text{W m}^{-1}\text{K}^{-1}$), θ in (K).

| Comp. | κ^{exp} | κ^{AGL} | κ^{AGL} | θ^{exp} | θ_D^{AGL} | θ_D^{AGL} | θ_D^{AEL} | γ^{exp} | γ^{AGL} | γ^{AGL} |
|-------|-----------------------|------------------------|-----------------------|-----------------------|-------------------------|-------------------------|-------------------------|----------------------------|------------------------|-----------------------|
| | | $(\sigma = 0.25)^{34}$ | | | $(\sigma = 0.25)^{34}$ | | | | $(\sigma = 0.25)^{34}$ | |
| SiC | 490 ⁵⁴ | 42.49 | 70.36 | 740 ⁵⁴ | 930 | 1103 | 1138 | 0.75 ⁵⁴ | 1.86 | 1.86 |
| | | | | | (586) | (695) | | | | |
| AlN | 350 ⁵⁴ | 36.73 | 39.0 | 620 ⁵⁴ | 880 | 898 | 917 | 0.7 ⁵⁴ | 1.85 | 1.85 |
| | | | | | (554) | (566) | | | | |
| GaN | 210 ⁵⁴ | 18.17 | 18.54 | 390 ⁵⁴ | 592 | 595 | 606 | 0.7 ⁵⁴ | 2.07 | 2.08 |
| | | | | | (373) | (375) | | | | |
| ZnO | 60 ⁵⁴ | 14.10 | 7.39 | 303 ⁵⁴ | 525 | 422 | 427 | 0.75 ⁵⁴ | 1.97 | 1.94 |
| | | | | | (331) | (266) | | | | |
| BeO | 370 ⁵⁴ | 39.26 | 53.36 | 809 ⁵⁴ | 1065 | 1181 | 1235 | 1.38 ^{54,110,114} | 1.76 | 1.76 |
| | | | | | (671) | (744) | | | | |
| CdS | 16 ⁵⁴ | 4.40 | 1.76 | 135 ⁵⁴ | 287 | 211 | 213 | 0.75 ⁵⁴ | 2.14 | 2.14 |
| | | | | | (181) | (133) | | | | |
| InSe | 6.9 ⁸⁷ | 1.84 | 2.34 | 190 ⁸⁷ | 230 | 249 | 168 | 1.2 ⁸⁷ | 2.24 | 2.24 |
| | | | | | (115) | (125) | | | | |
| InN | 45 ^{88,113} | 10.44 | 6.82 | 660 ^{88,113} | 426 | 369 | 370 | 0.97 ¹¹³ | 2.17 | 2.18 |
| | | | | | (268) | (232) | | | | |

tool of the thermal conductivity. However, as we noted in our previous work on AGL³⁴, the high correlations calculated with the experimental θ_a and γ were obtained using $\gamma = 0.75$ for BeO. Table 2.3 of Ref. 54 also cites an alternative value of $\gamma = 1.38$ for BeO (Table VIII). Using this outlier value would severely degrade the results down to 0.7, for the Pearson correlation, and 0.829, for the Spearman correlation. These values are too low for a reliable screening tool. This demonstrates the ability of the AEL-AGL calculations to compensate for anomalies in the experimental data when they exist and still provide a reliable screening method for the thermal conductivity.

D. Rhombohedral materials

The elastic properties of a few materials with rhombohedral structures (spacegroups: $R\bar{3}mR$, #166, $R\bar{3}mH$, #166; Pearson symbol: hR5; AFLOW prototype: A2B3-hR5.166_c.ac⁶²¹¹⁵; and spacegroup: $R\bar{3}cH$,

#167; Pearson symbol: hR10; AFLOW prototype: A2B3.hR10.167_c.e⁶²¹¹⁶) are shown in Table X (we have left out the material Fe_2O_3 which was included in the data set in Table IV of Ref. 34, due to convergence issues with some of the strained structures required for the calculation of the elastic tensor). The comparison between experiment and calculation is qualitatively reasonable, but the scarcity of experimental results does not allow for a proper correlation analysis.

The thermal properties calculated using AGL are compared to the experimental values in Table XI and the thermal conductivity is also plotted in Fig. 4(a). The experimental Debye temperatures are θ_D for Bi_2Te_3 and Sb_2Te_3 , and θ_a for Al_2O_3 . The values obtained using the numerical $E(V)$ fit and the three different equations of state (see supplementary material) are very similar, but just roughly reproduce the experiments.

The calculated Grüneisen parameters are about 50% larger than the experimental ones, and the value of σ used makes a little difference in the calculation. The absolute

TABLE IX. Correlations between experimental values and AEL and AGL results for elastic and thermal properties for hexagonal structure semiconductors.

| Property | Pearson (Linear) | Spearman (Rank Order) | RMSrD |
|---------------------------------------------------------------------------------------|---------------------|--------------------------|-------|
| κ^{exp} vs. κ^{AGL} ($\sigma = 0.25$) ³⁴ | 0.977 | 1.0 | 0.887 |
| κ^{exp} vs. κ^{AGL} | 0.980 | 0.976 | 0.911 |
| κ^{exp} vs. κ^{BM} | 0.974 | 0.976 | 0.904 |
| κ^{exp} vs. κ^{Vinet} | 0.980 | 0.976 | 0.926 |
| κ^{exp} vs. κ^{BCN} | 0.980 | 0.976 | 0.895 |
| θ_a^{exp} vs. θ_a^{AGL} ($\sigma = 0.25$) ³⁴ | 0.960 | 0.976 | 0.233 |
| θ_a^{exp} vs. θ_a^{AGL} | 0.921 | 0.929 | 0.216 |
| θ_a^{exp} vs. θ_a^{BM} | 0.921 | 0.929 | 0.217 |
| θ_a^{exp} vs. θ_a^{Vinet} | 0.920 | 0.929 | 0.218 |
| θ_a^{exp} vs. θ_a^{BCN} | 0.921 | 0.929 | 0.216 |
| γ^{exp} vs. γ^{AGL} ($\sigma = 0.25$) ³⁴ | -0.039 | 0.160 | 1.566 |
| γ^{exp} vs. γ^{AGL} | -0.029 | 0.160 | 1.563 |
| γ^{exp} vs. γ^{BM} | -0.124 | -0.233 | 1.547 |
| γ^{exp} vs. γ^{Vinet} | -0.043 | 0.012 | 1.677 |
| γ^{exp} vs. γ^{BCN} | -0.054 | 0.098 | 1.467 |
| B^{exp} vs. $B^{\text{AEL}}_{\text{VRH}}$ | 0.990 | 0.976 | 0.201 |
| B^{exp} vs. $B^{\text{AGL}}_{\text{Static}}$ | 0.990 | 0.976 | 0.138 |
| B^{exp} vs. $B^{\text{BM}}_{\text{Static}}$ | 0.988 | 0.976 | 0.133 |
| B^{exp} vs. $B^{\text{Vinet}}_{\text{Static}}$ | 0.988 | 0.976 | 0.139 |
| B^{exp} vs. $B^{\text{BCN}}_{\text{Static}}$ | 0.990 | 0.976 | 0.130 |
| G^{exp} vs. $G^{\text{AEL}}_{\text{VRH}}$ | 0.998 | 1.0 | 0.090 |
| G^{exp} vs. $G^{\text{AEL}}_{\text{Voigt}}$ | 0.998 | 1.0 | 0.076 |
| G^{exp} vs. $G^{\text{AEL}}_{\text{Reuss}}$ | 0.998 | 1.0 | 0.115 |
| σ^{exp} vs. σ^{AEL} | 0.851 | 0.893 | 0.143 |

agreement between the AGL values and κ^{exp} is also quite poor (Fig. 4(a)). However, despite all these discrepancies, the Pearson correlations between the calculated thermal conductivities and the experimental values are all high, of the order of 0.998, while the Spearman correlations range from 0.7 to 1.0, with all of the different equations of state having very similar correlations with experiment. Using the calculated σ^{AEL} , vs. the rough Cauchy approximation, improves the Spearman correlation from 0.7 to 1.0.

E. Body-centred tetragonal materials

The mechanical properties of the body-centred tetragonal materials (spacegroup: $I\bar{4}2d$, #122; Pearson symbol: tI16; AFLOW prototype: ABC2_tI16_122_a_b_d⁶²¹²²) of Table V of Ref. 34 are reported in Table XIII. The calculated bulk moduli miss considerably the few available experimental results, while the shear moduli are well reproduced. Reasonable estimates are also obtained for the Poisson ratio.

The thermal properties are reported in Table XIV and Fig. 4(b). The θ^{exp} values are all for θ_D , and in most cases are in good agreement with the values obtained with the AEL calculated σ . The values from the numerical $E(V)$ fit and the three different equations of state are again very similar, but differ significantly from θ_D^{AGL} calculated with $\sigma = 0.25$.

The comparison of the experimental thermal conductivity κ^{exp} to the calculated values, in Fig. 4(b), shows poor reproducibility. The available data can thus only be

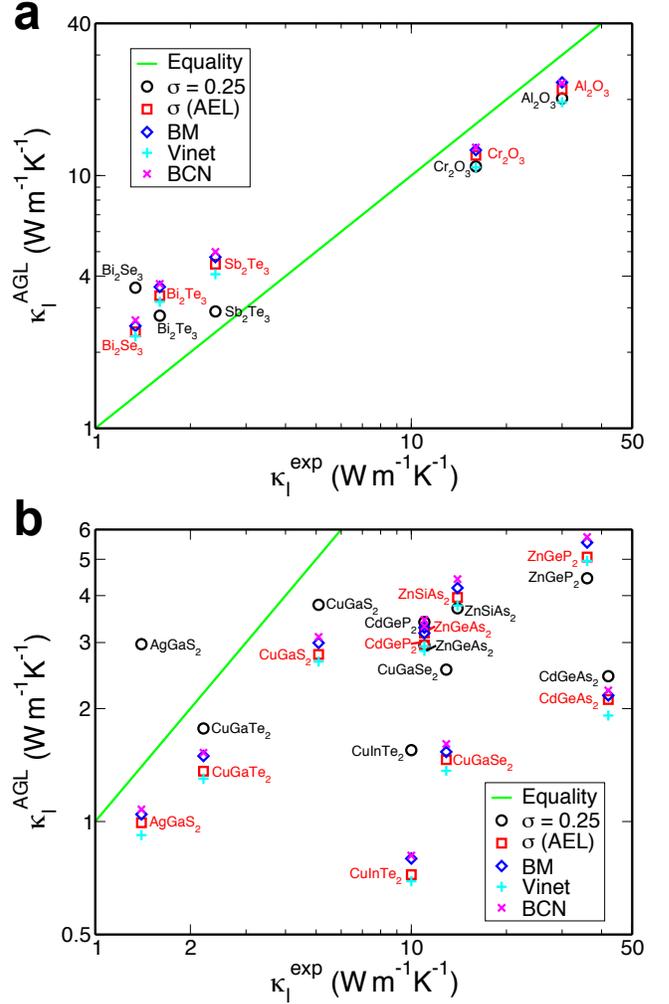


FIG. 4. (a) Lattice thermal conductivity of rhombohedral semiconductors at 300K. (b) Lattice thermal conductivity of body-centred tetragonal semiconductors at 300K.

considered a rough indication of their order of magnitude. The Pearson and Spearman correlations are also quite low for all types of calculation, but somewhat better when the calculated σ^{AEL} is used instead of the Cauchy approximation.

F. Miscellaneous materials

In this Section we consider materials with various other structures, as in Table VI of Ref. 34: CoSb_3 and IrSb_3 (spacegroup: $Im\bar{3}$, #204; Pearson symbol: cI32; AFLOW prototype: A3B_cI32_204_g_c⁶²¹³⁵), ZnSb ($Pbca$, #61; oP16; AFLOW prototype: AB_oP16_61_c_c⁶²¹³⁶), Sb_2O_3 ($Pccn$, #56; oP20), InTe ($Pm\bar{3}m$, #221; cP2; AFLOW prototype: AB_cP2_221_b_a⁶²¹³⁷), and $I4/mcm$, #140; tI16), Bi_2O_3 ($P121/c1$, #14; mP20); and SnO_2 ($P42/mnm$, #136; tP6; A2B_tP6_136_f_a⁶²¹³⁸). Two different structures are listed for InTe . In Ref. 34, we considered its simple cubic structure, but this is a high-pressure phase¹³⁹, while the ambient pressure phase is

TABLE X. Bulk modulus, shear modulus and Poisson ratio of rhombohedral semiconductors. “N/A” = Not available for that source. Units: B and G in (GPa).

| Comp. | B^{exp} | $B_{\text{VRH}}^{\text{AEL}}$ | $B_{\text{VRH}}^{\text{MP}}$ | $B_{\text{Static}}^{\text{AGL}}$ | $B_{\text{Static}}^{\text{BM}}$ | $B_{\text{Static}}^{\text{Vinet}}$ | $B_{\text{Static}}^{\text{BCN}}$ | G^{exp} | $G_{\text{Voigt}}^{\text{AEL}}$ | $G_{\text{Reuss}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{MP}}$ | σ^{exp} | σ^{AEL} | σ^{MP} |
|---------------------------------|------------------------|-------------------------------|------------------------------|----------------------------------|---------------------------------|------------------------------------|----------------------------------|------------------------|---------------------------------|---------------------------------|-------------------------------|------------------------------|-------------------------|-----------------------|----------------------|
| Bi ₂ Te ₃ | 37.0 ^{65,117} | 28.8 | 15.0 | 43.7 | 44.4 | 43.3 | 44.5 | 22.4 ^{65,117} | 23.5 | 16.3 | 19.9 | 10.9 | 0.248 ^{65,117} | 0.219 | 0.21 |
| Sb ₂ Te ₃ | N/A | 22.9 | N/A | 45.3 | 46.0 | 45.2 | 46.0 | N/A | 20.6 | 14.5 | 17.6 | N/A | N/A | 0.195 | N/A |
| Al ₂ O ₃ | 254 ¹¹⁸ | 231 | 232 | 222 | 225 | 224 | 224 | 163.1 ¹¹⁸ | 149 | 144 | 147 | 147 | 0.235 ¹¹⁸ | 0.238 | 0.24 |
| Cr ₂ O ₃ | 234 ¹¹⁹ | 203 | 203 | 198 | 202 | 201 | 201 | 129 ¹¹⁹ | 115 | 112 | 113 | 113 | 0.266 ¹¹⁹ | 0.265 | 0.27 |
| Bi ₂ Se ₃ | N/A | 93.9 | N/A | 57.0 | 57.5 | 56.4 | 57.9 | N/A | 53.7 | 28.0 | 40.9 | N/A | N/A | 0.310 | N/A |

TABLE XI. Lattice thermal conductivity, Debye temperatures and Grüneisen parameter of rhombohedral semiconductors, comparing the effect of using the calculated value of the Poisson ratio to previous approximation of $\sigma = 0.25$. The experimental Debye temperatures are θ_{D} for Bi₂Te₃ and Sb₂Te₃, and θ_{a} for Al₂O₃. “N/A” = Not available for that source. Units: κ in ($\text{W m}^{-1}\text{K}^{-1}$), θ in (K).

| Comp. | κ^{exp} | κ^{AGL} | κ^{AGL} | θ^{exp} | $\theta_{\text{D}}^{\text{AGL}}$ ($\theta_{\text{a}}^{\text{AGL}}$) | $\theta_{\text{D}}^{\text{AGL}}$ ($\theta_{\text{a}}^{\text{AGL}}$) | $\theta_{\text{D}}^{\text{AEL}}$ | γ^{exp} | γ^{AGL} | γ^{AGL} |
|---------------------------------|-----------------------|------------------------|-----------------------|-----------------------|--------------------------------------------------------------------------|--------------------------------------------------------------------------|----------------------------------|------------------------|-----------------------|-----------------------|
| | | $(\sigma = 0.25)^{34}$ | | | $(\sigma = 0.25)^{34}$ | | | $(\sigma = 0.25)^{34}$ | | |
| Bi ₂ Te ₃ | 1.6 ⁸⁷ | 2.79 | 3.35 | 155 ⁸⁷ | 191 (112) | 204 (119) | 161 | 1.49 ⁸⁷ | 2.13 | 2.14 |
| Sb ₂ Te ₃ | 2.4 ⁸⁷ | 2.90 | 4.46 | 160 ⁸⁷ | 217 (127) | 243 (142) | 170 | 1.49 ⁸⁷ | 2.2 | 2.11 |
| Al ₂ O ₃ | 30 ¹²⁰ | 20.21 | 21.92 | 390 ⁵³ | 927 (430) | 952 (442) | 975 | 1.32 ⁵³ | 1.91 | 1.91 |
| Cr ₂ O ₃ | 16 ^{89,121} | 10.87 | 12.03 | N/A | 733 (340) | 717 (333) | 720 | N/A | 2.26 | 2.10 |
| Bi ₂ Se ₃ | 1.34 ⁸⁹ | 3.60 | 2.41 | N/A | 223 (130) | 199 (116) | 241 | N/A | 2.08 | 2.12 |

TABLE XII. Correlations between experimental values and AEL and AGL results for elastic and thermal properties for rhombohedral structure semiconductors.

| Property | Pearson (Linear) | Spearman (Rank Order) | RMSrD |
|-----------------------------------------------------------------------------------|---------------------|--------------------------|-------|
| κ^{exp} vs. κ^{AGL} ($\sigma = 0.25$) ³⁴ | 0.997 | 0.7 | 0.955 |
| κ^{exp} vs. κ^{AGL} | 0.998 | 1.0 | 0.821 |
| κ^{exp} vs. κ^{BM} | 0.997 | 1.0 | 0.931 |
| κ^{exp} vs. κ^{Vinet} | 0.998 | 1.0 | 0.741 |
| κ^{exp} vs. κ^{BCN} | 0.997 | 1.0 | 1.002 |

body-centred tetragonal. It appears that the thermal conductivity results should be for the body-centred tetragonal phase⁹⁰, therefore both sets of results are reported here. The correlation values shown in the tables below were calculated for the body-centred tetragonal structure.

The elastic properties are shown in Table XVI. Large discrepancies appear between the results of all calculations and the few available experimental results.

The thermal properties are compared to the experimental values in Table XVII. The experimental Debye temperatures are for θ_{D} , except ZnSb for which it is θ_{a} . Good agreement is found between calculation and the few available experimental values. Again, the numerical $E(V)$ fit and the three different equations of state give similar results. For the Grüneisen parameter, experiment and calculations again differ considerably, while the changes due to the different values of σ used in the calculations are negligible.

The experimental thermal conductivity κ^{exp} is com-

pared in Table XVII to the thermal conductivity calculated with AGL using the Leibfried-Schlömann equation (Eq. (37)) for κ^{AGL} , while the values obtained for κ^{BM} , κ^{Vinet} and κ^{BCN} are listed in the supplementary information. The absolute agreement between the AGL values and κ^{exp} is quite poor. The scarcity of experimental data from different sources on the thermal properties of these materials prevents reaching definite conclusions regarding the true values of these properties. The available data can thus only be considered as a rough indication of their order of magnitude.

For these materials, the Pearson correlation between the calculated and experimental values of the thermal conductivity ranges from 0.438 to 0.937, while the corresponding Spearman correlations range from -0.143 to 0.071 . In this case, using σ^{AEL} in the AGL calculations does not improve the correlations, instead actually lowering the values somewhat. However, it should be noted that the Pearson correlation is heavily influenced by the values for SnO₂. When this entry is removed from the list, the Pearson correlation values fall to -0.471 and -0.466 when the $\sigma = 0.25$ and $\sigma = \sigma^{\text{AEL}}$ values are used, respectively. The low correlation values, particularly for the Spearman correlation, for this set of materials demonstrates the importance of the information about the material structure when interpreting results obtained using the AGL method in order to identify candidate materials for specific thermal applications. This is partly due to the fact that the Grüneisen parameter values tend to be similar for materials with the same structure. Therefore, the effect of the

TABLE XIII. Bulk modulus, shear modulus and Poisson ratio of body-centred tetragonal semiconductors. Note that there appears to be an error in Table 1 of Ref. 123 where the bulk modulus values are stated to be in units of 10^{12} Pa. This seems unlikely, as that would give a bulk modulus for CuInTe₂ an order of magnitude larger than that for diamond. Also, units of 10^{12} Pa would be inconsistent with the experimental results listed in Ref. 124, so therefore it seems that these values are in units of 10^{10} Pa, which are the values shown here. “N/A” = Not available for that source. Units: B and G in (GPa).

| Comp. | B^{exp} | $B_{\text{VRH}}^{\text{AEL}}$ | $B_{\text{VRH}}^{\text{MP}}$ | $B_{\text{Static}}^{\text{AGL}}$ | $B_{\text{Static}}^{\text{BM}}$ | $B_{\text{Static}}^{\text{Vinet}}$ | $B_{\text{Static}}^{\text{BCN}}$ | G^{exp} | $G_{\text{Voigt}}^{\text{AEL}}$ | $G_{\text{Reuss}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{MP}}$ | σ^{exp} | σ^{AEL} | σ^{MP} |
|---------------------|--------------------------------------------|-------------------------------|------------------------------|----------------------------------|---------------------------------|------------------------------------|----------------------------------|---------------------|---------------------------------|---------------------------------|-------------------------------|------------------------------|-----------------------|-----------------------|----------------------|
| CuGaTe ₂ | N/A | 47.0 | N/A | 42.5 | 43.2 | 42.0 | 43.5 | N/A | 25.1 | 22.1 | 23.6 | N/A | N/A | 0.285 | N/A |
| ZnGeP ₂ | N/A | 73.1 | 74.9 | 70.1 | 71.1 | 70.0 | 71.4 | N/A | 50.5 | 46.2 | 48.4 | 48.9 | N/A | 0.229 | 0.23 |
| ZnSiAs ₂ | N/A | 67.4 | 65.9 | 63.4 | 64.3 | 63.1 | 64.6 | N/A | 44.4 | 40.4 | 42.4 | 42.2 | N/A | 0.240 | 0.24 |
| CuInTe ₂ | 36.0 ¹²⁴ 45.4 ¹²³ | 53.9 | N/A | 38.6 | 39.2 | 38.2 | 39.4 | N/A | 20.4 | 17.2 | 18.8 | N/A | 0.313 ¹²³ | 0.344 | N/A |
| AgGaS ₂ | 67.0 ¹²⁵ | 70.3 | N/A | 56.2 | 57.1 | 56.0 | 57.4 | 20.8 ¹²⁵ | 20.7 | 17.4 | 19.1 | N/A | 0.359 ¹²⁵ | 0.375 | N/A |
| CdGeP ₂ | N/A | 65.3 | 65.2 | 60.7 | 61.6 | 60.4 | 61.9 | N/A | 37.7 | 33.3 | 35.5 | 35.0 | N/A | 0.270 | 0.27 |
| CdGeAs ₂ | 69.9 ¹²⁶ | 52.6 | N/A | 49.2 | 49.6 | 48.3 | 49.9 | 29.5 ¹²⁶ | 30.9 | 26.2 | 28.6 | N/A | 0.315 ¹²⁶ | 0.270 | N/A |
| CuGaS ₂ | 94.0 ¹²⁷ | 73.3 | N/A | 69.0 | 69.9 | 68.7 | 70.6 | N/A | 37.8 | 32.4 | 35.1 | N/A | N/A | 0.293 | N/A |
| CuGaSe ₂ | N/A | 69.9 | N/A | 54.9 | 55.6 | 54.4 | 56.0 | N/A | 30.3 | 26.0 | 28.1 | N/A | N/A | 0.322 | N/A |
| ZnGeAs ₂ | N/A | 59.0 | N/A | 56.2 | 56.7 | 55.5 | 57.1 | N/A | 39.0 | 35.6 | 37.3 | N/A | N/A | 0.239 | N/A |

TABLE XIV. Lattice thermal conductivity at 300K, Debye temperatures and Grüneisen parameter of body-centred tetragonal semiconductors, comparing the effect of using the calculated value of the Poisson ratio to previous approximation of $\sigma = 0.25$. “N/A” = Not available for that source. Units: κ in ($\text{W m}^{-1}\text{K}^{-1}$), θ in (K).

| Comp. | κ^{exp} | κ^{AGL} | κ^{AGL} | θ^{exp} | $\theta_{\text{D}}^{\text{AGL}}$ | $\theta_{\text{D}}^{\text{AGL}}$ | $\theta_{\text{D}}^{\text{AEL}}$ | γ^{exp} | γ^{AGL} | γ^{AGL} |
|---------------------|--------------------------------------------------------------------------|------------------------|-----------------------|------------------------------------------------|----------------------------------|----------------------------------|----------------------------------|-----------------------|------------------------|-----------------------|
| | | $(\sigma = 0.25)^{34}$ | | | $(\sigma = 0.25)^{34}$ | | | | $(\sigma = 0.25)^{34}$ | |
| CuGaTe ₂ | 2.2 ⁸⁷ | 1.77 | 1.36 | 226 ⁸⁷ | 234 (117) | 215 (108) | 218 | 1.46 ⁸⁷ | 2.32 | 2.32 |
| ZnGeP ₂ | 35 ^{89,128} 36 ^{89,128} 18 ^{89,130,131} | 4.45 | 5.07 | 500 ⁸⁹ 428 ¹²⁹ | 390 (195) | 408 (204) | 411 | N/A | 2.13 | 2.14 |
| ZnSiAs ₂ | 14 ^{89,130,131} | 3.70 | 3.96 | 347 ^{89,132} | 342 (171) | 350 (175) | 354 | N/A | 2.15 | 2.15 |
| CuInTe ₂ | 10 ^{89,133} | 1.55 | 0.722 | 185 ^{89,133} 195 ^{89,134} | 215 (108) | 166 (83) | 185 | 0.93 ¹³³ | 2.33 | 2.32 |
| AgGaS ₂ | 1.4 ^{89,128} | 2.97 | 0.993 | 255 ^{89,129} | 324 (162) | 224 (112) | 237 | N/A | 2.20 | 2.20 |
| CdGeP ₂ | 11 ^{89,130,131} | 3.40 | 2.96 | 340 ^{89,129} | 335 (168) | 320 (160) | 324 | N/A | 2.20 | 2.21 |
| CdGeAs ₂ | 42 ^{89,130} | 2.44 | 2.11 | 241 ¹³² | 266 (133) | 254 (127) | 255 | N/A | 2.20 | 2.20 |
| CuGaS ₂ | 5.09 ⁸⁹ | 3.78 | 2.79 | 356 ^{89,129} | 387 (194) | 349 (175) | 349 | N/A | 2.24 | 2.24 |
| CuGaSe ₂ | 12.9 ^{89,133} | 2.54 | 1.46 | 262 ^{89,134} | 294 (147) | 244 (122) | 265 | N/A | 2.27 | 2.26 |
| ZnGeAs ₂ | 11 ^{89,130} | 2.95 | 3.18 | N/A | 299 (150) | 307 (154) | 308 | N/A | 2.16 | 2.17 |

TABLE XV. Correlations between experimental values and AEL and AGL results for elastic and thermal properties for body-centred tetragonal structure semiconductors.

| Property | Pearson (Linear) | Spearman (Rank Order) | RMSrD |
|-----------------------------------------------------------------------------------|---------------------|--------------------------|-------|
| κ^{exp} vs. κ^{AGL} ($\sigma = 0.25$) ³⁴ | 0.265 | 0.201 | 0.812 |
| κ^{exp} vs. κ^{AGL} | 0.472 | 0.608 | 0.766 |
| κ^{exp} vs. κ^{BM} | 0.467 | 0.608 | 0.750 |
| κ^{exp} vs. κ^{Vinet} | 0.464 | 0.608 | 0.778 |
| κ^{exp} vs. κ^{BCN} | 0.460 | 0.608 | 0.741 |

Grüneisen parameter on the ordinal ranking of the lattice thermal conductivity of materials with the same structure

is small.

G. Thermomechanical properties from LDA

The thermomechanical properties of a randomly-selected subset of the materials investigated in this work were calculated using LDA in order to check the impact of the choice of exchange-correlation functional on the results. For the LDA calculations, all structures were first re-relaxed using the LDA exchange-correlation functional with VASP using the appropriate parameters and potentials as described in the AFLOW standard³⁷, and then

TABLE XVI. Bulk modulus, shear modulus and Poisson ratio of materials with various structures. “N/A” = Not available for that source. Units: B and G in (GPa).

| Comp. | Pearson | B^{exp} | $B_{\text{VRH}}^{\text{AEL}}$ | $B_{\text{VRH}}^{\text{MP}}$ | $B_{\text{Static}}^{\text{AGL}}$ | $B_{\text{Static}}^{\text{BM}}$ | $B_{\text{Static}}^{\text{Vinet}}$ | $B_{\text{Static}}^{\text{BCN}}$ | G^{exp} | $G_{\text{Voigt}}^{\text{AEL}}$ | $G_{\text{Reuss}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{AEL}}$ | $G_{\text{VRH}}^{\text{MP}}$ | σ^{exp} | σ^{AEL} | σ^{MP} |
|--------------------------------|-------------|---------------------|-------------------------------|------------------------------|----------------------------------|---------------------------------|------------------------------------|----------------------------------|--------------------|---------------------------------|---------------------------------|-------------------------------|------------------------------|-----------------------|-----------------------|----------------------|
| CoSb ₃ | <i>cI32</i> | N/A | 78.6 | 82.9 | 75.6 | 76.1 | 75.1 | 76.3 | N/A | 57.2 | 55.1 | 56.2 | 57.0 | N/A | 0.211 | 0.22 |
| IrSb ₃ | <i>cI32</i> | N/A | 97.5 | 98.7 | 94.3 | 94.8 | 93.8 | 95.5 | N/A | 60.9 | 59.4 | 60.1 | 59.7 | N/A | 0.244 | 0.25 |
| ZnSb | <i>oP16</i> | N/A | 47.7 | 47.8 | 46.7 | 47.0 | 46.0 | 47.7 | N/A | 29.2 | 27.0 | 28.1 | 28.2 | N/A | 0.253 | 0.25 |
| Sb ₂ O ₃ | <i>oP20</i> | N/A | 16.5 | 19.1 | 97.8 | 98.7 | 97.8 | 98.7 | N/A | 22.8 | 16.4 | 19.6 | 20.4 | N/A | 0.0749 | 0.11 |
| InTe | <i>cP2</i> | 90.2 ¹³⁹ | 41.7 | N/A | 34.9 | 34.4 | 33.6 | 34.7 | N/A | 8.41 | 8.31 | 8.36 | N/A | N/A | 0.406 | N/A |
| InTe | <i>tI16</i> | 46.5 ¹³⁹ | 20.9 | N/A | 32.3 | 33.1 | 32.2 | 33.2 | N/A | 13.4 | 13.0 | 13.2 | N/A | N/A | 0.239 | N/A |
| Bi ₂ O ₃ | <i>mP20</i> | N/A | 48.0 | 54.5 | 108 | 110 | 109 | 109 | N/A | 30.3 | 25.9 | 28.1 | 29.9 | N/A | 0.255 | 0.27 |
| SnO ₂ | <i>tP6</i> | 212 ¹⁴⁰ | 159 | N/A | 158 | 162 | 161 | 161 | 106 ¹⁴⁰ | 86.7 | 65.7 | 76.2 | N/A | 0.285 ¹⁴⁰ | 0.293 | N/A |

TABLE XVII. Lattice thermal conductivity at 300K, Debye temperatures and Grüneisen parameter of materials with various structures, comparing the effect of using the calculated value of the Poisson ratio to previous approximation of $\sigma = 0.25$. The experimental Debye temperatures are θ_{D} , except ZnSb for which it is θ_{a} . “N/A” = Not available for that source. Units: κ in ($\text{W m}^{-1}\text{K}^{-1}$), θ in (K).

| Comp. | Pearson | κ^{exp} | κ^{AGL} | κ^{AGL} | θ^{exp} | $\theta_{\text{D}}^{\text{AGL}}$ | $\theta_{\text{D}}^{\text{AGL}}$ | $\theta_{\text{D}}^{\text{AEL}}$ | γ^{exp} | γ^{AGL} | γ^{AGL} |
|--------------------------------|-------------|----------------------------------------|------------------------|-----------------------|-----------------------|------------------------------------|------------------------------------|----------------------------------|------------------------|------------------------|-----------------------|
| | | | $(\sigma = 0.25)^{34}$ | | | $(\sigma = 0.25)^{34}$ | | | | $(\sigma = 0.25)^{34}$ | |
| | | | | | | $(\theta_{\text{a}}^{\text{AGL}})$ | $(\theta_{\text{a}}^{\text{AGL}})$ | | | | |
| CoSb ₃ | <i>cI32</i> | 10 ⁸⁷ | 1.60 | 2.60 | 307 ⁸⁷ | 284 | 310 | 312 | 0.95 ⁸⁷ | 2.63 | 2.33 |
| | | | | | | (113) | (123) | | | | |
| IrSb ₃ | <i>cI32</i> | 16 ⁸⁷ | 2.64 | 2.73 | 308 ⁸⁷ | 283 | 286 | 286 | 1.42 ⁸⁷ | 2.34 | 2.34 |
| | | | | | | (112) | (113) | | | | |
| ZnSb | <i>oP16</i> | 3.5 ^{55,141} | 1.24 | 1.23 | 92 ⁵⁵ | 244 | 242 | 237 | 0.76 ^{55,141} | 2.24 | 2.23 |
| | | | | | | (97) | (96) | | | | |
| Sb ₂ O ₃ | <i>oP20</i> | 0.4 ⁸⁹ | 3.45 | 8.74 | N/A | 418 | 572 | 238 | N/A | 2.13 | 2.12 |
| | | | | | | (154) | (211) | | | | |
| InTe | <i>cP2</i> | N/A | 3.12 | 0.709 | N/A | 191 | 113 | 116 | N/A | 2.28 | 2.19 |
| | | | | | | (152) | (90) | | | | |
| InTe | <i>tP16</i> | 1.7 ^{87,90} | 1.32 | 1.40 | 186 ⁸⁷ | 189 | 193 | 150 | 1.0 ⁸⁷ | 2.23 | 2.24 |
| | | | | | | (95) | (97) | | | | |
| Bi ₂ O ₃ | <i>mP20</i> | 0.8 ⁸⁹ | 3.04 | 2.98 | N/A | 345 | 342 | 223 | N/A | 2.10 | 2.10 |
| | | | | | | (127) | (126) | | | | |
| SnO ₂ | <i>tP6</i> | 98 ¹⁴² 55 ¹⁴² | 9.56 | 6.98 | N/A | 541 | 487 | 480 | N/A | 2.48 | 2.42 |
| | | | | | | (298) | (268) | | | | |

TABLE XVIII. Correlations between experimental values and AEL and AGL results for elastic and thermal properties for materials with miscellaneous structures.

| Property | Pearson | Spearman | RMSrD |
|-----------------------------------------------------------------------------------|----------|--------------|-------|
| | (Linear) | (Rank Order) | |
| κ^{exp} vs. κ^{AGL} ($\sigma = 0.25$) ³⁴ | 0.937 | 0.071 | 3.38 |
| κ^{exp} vs. κ^{AGL} | 0.438 | -0.143 | 8.61 |
| κ^{exp} vs. κ^{BM} | 0.498 | -0.143 | 8.81 |
| κ^{exp} vs. κ^{Vinet} | 0.445 | 0.0 | 8.01 |
| κ^{exp} vs. κ^{BCN} | 0.525 | -0.143 | 9.08 |

the appropriate strained structures were calculated using LDA. These calculations were restricted to a subset of materials to limit the total number of additional first-principles calculations required, and the materials were selected randomly from each of the sets in the previous sections so as to cover as wide a range of different structure types as possible, given the available experimental data. Results for elastic properties obtained using LDA, GGA and experimental measurements are shown in Table XIX, while the thermal properties are shown in Table XX. All thermal properties listed in Table XX were calculated

using σ^{AEL} in the expression for the Debye temperature.

In general, the LDA values for elastic and thermal properties are slightly higher than the GGA values, as would be generally expected due to their relative tendencies to overbind and underbind, respectively^{143,144}. The correlations and RMSrD of both the LDA and GGA results with experiment for this set of materials are listed in Table XXI. The Pearson and Spearman correlation values for LDA and GGA are very close to each other for most of the listed properties. The RMSrD values show greater differences, although it isn’t clear that one of the exchange-correlation functionals consistently gives better predictions than the other. Therefore, the choice of exchange-correlation functional will make little difference to the predictive capability of the workflow, so we choose to use GGA-PBE as it is the functional used for performing the structural relaxation for the entries in the AFLOW data repository.

TABLE XIX. Bulk modulus, shear modulus and Poisson ratio of a subset of the materials investigated in this work, comparing the effect of using different exchange-correlation functionals. “N/A”= Not available for that source. Units: B and G in (GPa).

| Comp. | B^{exp} | $B_{\text{VRH}}^{\text{GGA}}$ | $B_{\text{VRH}}^{\text{LDA}}$ | $B_{\text{Static}}^{\text{GGA}}$ | $B_{\text{Static}}^{\text{LDA}}$ | G^{exp} | $G_{\text{Voigt}}^{\text{GGA}}$ | $G_{\text{Voigt}}^{\text{LDA}}$ | $G_{\text{Reuss}}^{\text{GGA}}$ | $G_{\text{Reuss}}^{\text{LDA}}$ | $G_{\text{VRH}}^{\text{GGA}}$ | $G_{\text{VRH}}^{\text{LDA}}$ | σ^{exp} | σ^{GGA} | σ^{LDA} |
|--------------------------------|------------------------|-------------------------------|-------------------------------|----------------------------------|----------------------------------|------------------------|---------------------------------|---------------------------------|---------------------------------|---------------------------------|-------------------------------|-------------------------------|-------------------------|-----------------------|-----------------------|
| Si | 97.8 ^{65,70} | 89.1 | 96.9 | 84.2 | 92.1 | 66.5 ^{65,70} | 64 | 65 | 61 | 61.9 | 62.5 | 63.4 | 0.223 ^{65,70} | 0.216 | 0.231 |
| BN | 367.0 ⁶⁶ | 372 | 402 | 353 | 382 | N/A | 387 | 411 | 374 | 395 | 380 | 403 | N/A | 0.119 | 0.124 |
| GaSb | 57.0 ⁶⁶ | 47.0 | 58.3 | 41.6 | 52.3 | 34.2 ⁷⁷ | 30.8 | 35.3 | 28.3 | 32.2 | 29.6 | 33.7 | 0.248 ⁷⁷ | 0.240 | 0.258 |
| InAs | 60.0 ⁶⁶ | 50.1 | 62.3 | 45.7 | 57.4 | 29.5 ^{65,80} | 27.3 | 30.1 | 24.2 | 26.4 | 25.7 | 28.2 | 0.282 ^{65,80} | 0.281 | 0.303 |
| ZnS | 77.1 ⁶⁶ | 71.2 | 88.4 | 65.8 | 83.3 | 30.9 ⁶⁵ | 36.5 | 42.1 | 31.4 | 35.7 | 33.9 | 38.9 | 0.318 ⁶⁵ | 0.294 | 0.308 |
| NaCl | 25.1 ⁹⁴ | 24.9 | 33.3 | 20.0 | 27.6 | 14.6 ⁹⁴ | 14.0 | 19.8 | 12.9 | 16.6 | 13.5 | 18.2 | 0.255 ⁹⁴ | 0.271 | 0.269 |
| KI | 12.2 ⁹⁴ | 10.9 | 16.3 | 8.54 | 13.3 | 5.96 ⁹⁴ | 6.05 | 9.39 | 4.39 | 5.3 | 5.22 | 7.35 | 0.290 ⁹⁴ | 0.294 | 0.305 |
| RbI | 11.1 ⁹⁴ | 9.90 | 14.8 | 8.01 | 12.1 | 5.03 ⁹⁴ | 5.50 | 8.54 | 3.65 | 3.94 | 4.57 | 6.24 | 0.303 ⁹⁴ | 0.300 | 0.315 |
| MgO | 164 ⁹⁶ | 152 | 164 | 142 | 163 | 131 ⁹⁶ | 119 | 138 | 115 | 136 | 117 | 137 | 0.185 ⁹⁶ | 0.194 | 0.173 |
| CaO | 113 ⁹⁷ | 105 | 129 | 99.6 | 122 | 81.0 ⁹⁷ | 73.7 | 87.4 | 73.7 | 86.3 | 73.7 | 86.9 | 0.210 ⁹⁷ | 0.216 | 0.225 |
| GaN | 195 ^{65,107} | 175 | 202 | 166 | 196 | 51.6 ^{65,107} | 107 | 116 | 105 | 113 | 106 | 114 | 0.378 ^{65,107} | 0.248 | 0.262 |
| | 210 ¹⁰⁸ | | | | | 123 ¹⁰⁸ | | | | | | | 0.255 ¹⁰⁸ | | |
| CdS | 60.7 ^{65,109} | 55.4 | 68.2 | 49.7 | 64.1 | 18.2 ^{65,109} | 17.6 | 18.4 | 17.0 | 17.8 | 17.3 | 18.1 | 0.364 ^{65,109} | 0.358 | 0.378 |
| Al ₂ O ₃ | 254 ¹¹⁸ | 231 | 259 | 222 | 250 | 163.1 ¹¹⁸ | 149 | 166 | 144 | 163 | 147 | 165 | 0.235 ¹¹⁸ | 0.238 | 0.238 |
| CdGeP ₂ | N/A | 65.3 | 78.4 | 60.7 | 74.5 | N/A | 37.7 | 42.1 | 33.3 | 36.8 | 35.5 | 39.4 | N/A | 0.270 | 0.285 |
| CuGaSe ₂ | N/A | 69.9 | 76.4 | 54.9 | 72.1 | N/A | 30.3 | 34.7 | 26.0 | 30.0 | 28.1 | 32.3 | N/A | 0.322 | 0.315 |
| CoSb ₃ | N/A | 78.6 | 99.6 | 75.6 | 96.1 | N/A | 57.2 | 67.1 | 55.1 | 64.2 | 56.2 | 65.7 | N/A | 0.211 | 0.23 |

TABLE XX. Thermal properties lattice thermal conductivity at 300K, Debye temperature and Grüneisen parameter of a subset of materials, comparing the effect of using different exchange-correlation functionals. The values listed for θ^{exp} are θ_a , except 340K for CdGeP₂^{89,129}, 262K for CuGaSe₂^{89,134} and 307K for CoSb₃⁸⁷ which are θ_D . Units: κ in (W m⁻¹K⁻¹), θ in (K).

| Comp. | κ^{exp} | κ^{GGA} | κ^{LDA} | θ^{exp} | θ_D^{GGA} (θ_a^{GGA}) | θ_D^{LDA} (θ_a^{LDA}) | γ^{exp} | γ^{GGA} | γ^{LDA} |
|--------------------------------|--------------------------|-----------------------|-----------------------|-----------------------|--------------------------------------------------------|--------------------------------------------------------|------------------------------------------|-----------------------|-----------------------|
| Si | 166 ⁵⁴ | 26.19 | 27.23 | 395 ^{53,54} | 610 (484) | 614 (487) | 1.06 ⁵⁴ 0.56 ⁵³ | 2.06 | 2.03 |
| BN | 760 ⁵⁴ | 281.6 | 312.9 | 1200 ⁵⁴ | 1793 (1423) | 1840 (1460) | 0.7 ⁵⁴ | 1.75 | 1.72 |
| GaSb | 40 ⁵⁴ | 4.96 | 5.89 | 165 ^{53,54} | 240 (190) | 254 (202) | 0.75 ^{53,54} | 2.28 | 2.25 |
| InAs | 30 ⁵⁴ | 4.33 | 4.92 | 165 ^{53,54} | 229 (182) | 238 (189) | 0.57 ^{53,54} | 2.26 | 2.22 |
| ZnS | 27 ⁵⁴ | 8.38 | 9.58 | 230 ^{53,54} | 341 (271) | 363 (288) | 0.75 ^{53,54} | 2.00 | 2.02 |
| NaCl | 7.1 ⁵⁴ | 2.12 | 2.92 | 220 ^{53,54} | 271 (215) | 312 (248) | 1.56 ^{53,54} | 2.23 | 2.29 |
| KI | 2.6 ⁵⁴ | 0.525 | 0.811 | 87 ^{53,54} | 116 (92) | 137 (109) | 1.45 ^{53,54} | 2.35 | 2.37 |
| RbI | 2.3 ⁵⁴ | 0.368 | 0.593 | 84 ^{53,54} | 97 (77) | 115 (91) | 1.41 ^{53,54} | 2.47 | 2.45 |
| MgO | 60 ⁵⁴ | 44.5 | 58.4 | 600 ^{53,54} | 849 (674) | 935 (742) | 1.44 ^{53,54} | 1.96 | 1.95 |
| CaO | 27 ⁵⁴ | 24.3 | 28.5 | 450 ^{53,54} | 620 (492) | 665 (528) | 1.57 ^{53,54} | 2.06 | 2.09 |
| GaN | 210 ⁵⁴ | 18.54 | 21.34 | 390 ⁵⁴ | 595 (375) | 619 (390) | 0.7 ⁵⁴ | 2.08 | 2.04 |
| CdS | 16 ⁵⁴ | 1.76 | 1.84 | 135 ⁵⁴ | 211 (133) | 217 (137) | 0.75 ⁵⁴ | 2.14 | 2.14 |
| Al ₂ O ₃ | 30 ¹²⁰ | 21.92 | 25.36 | 390 ⁵³ | 952 (442) | 1002 (465) | 1.32 ⁵³ | 1.91 | 1.91 |
| CdGeP ₂ | 11 ^{89,130,131} | 2.96 | 3.47 | 340 ^{89,129} | 320 (160) | 337 (169) | N/A | 2.21 | 2.18 |
| CuGaSe ₂ | 12.9 ^{89,133} | 1.46 | 2.23 | 262 ^{89,134} | 244 (122) | 281 (141) | N/A | 2.26 | 2.23 |
| CoSb ₃ | 10 ⁸⁷ | 2.60 | 3.25 | 307 ⁸⁷ | 310 (123) | 332 (132) | 0.95 ⁸⁷ | 2.33 | 2.28 |

H. AGL predictions for thermal conductivity

The AEL-AGL methodology has been applied for high-throughput screening of the elastic and thermal properties of over 3000 materials included in the AFLOW database³⁶. Tables XXII and XXIII list those found to have the high-

est and lowest thermal conductivities, respectively. The high conductivity list is unsurprisingly dominated by various phases of elemental carbon, boron nitride, boron carbide and boron carbon nitride, while all other high-conductivity materials also contain at least one of the elements C, B or N. The low thermal conductivity list tends

TABLE XXI. Correlations between experimental values and AEL and AGL results for elastic and thermal properties comparing the LDA and GGA exchange-correlation functionals for this subset of materials.

| Property | Pearson (Linear) | Spearman (Rank Order) | RMSrD |
|-------------------------------------------------------|---------------------|--------------------------|-------|
| κ^{exp} vs. κ^{GGA} | 0.963 | 0.867 | 0.755 |
| κ^{exp} vs. κ^{LDA} | 0.959 | 0.848 | 0.706 |
| θ^{exp} vs. θ^{GGA} | 0.996 | 0.996 | 0.119 |
| θ^{exp} vs. θ^{LDA} | 0.996 | 0.996 | 0.174 |
| γ^{exp} vs. γ^{GGA} | 0.172 | 0.130 | 1.514 |
| γ^{exp} vs. γ^{LDA} | 0.265 | 0.296 | 1.490 |
| B^{exp} vs. $B_{\text{VRH}}^{\text{GGA}}$ | 0.995 | 1.0 | 0.111 |
| B^{exp} vs. $B_{\text{VRH}}^{\text{LDA}}$ | 0.996 | 1.0 | 0.185 |
| B^{exp} vs. $B_{\text{Static}}^{\text{GGA}}$ | 0.996 | 1.0 | 0.205 |
| B^{exp} vs. $B_{\text{Static}}^{\text{LDA}}$ | 0.998 | 1.0 | 0.072 |
| G^{exp} vs. $G_{\text{VRH}}^{\text{GGA}}$ | 0.999 | 0.993 | 0.108 |
| G^{exp} vs. $G_{\text{VRH}}^{\text{LDA}}$ | 0.997 | 0.986 | 0.153 |
| G^{exp} vs. $G_{\text{Voigt}}^{\text{GGA}}$ | 0.998 | 0.993 | 0.096 |
| G^{exp} vs. $G_{\text{Voigt}}^{\text{LDA}}$ | 0.996 | 0.986 | 0.315 |
| G^{exp} vs. $G_{\text{Reuss}}^{\text{GGA}}$ | 0.999 | 0.993 | 0.163 |
| G^{exp} vs. $G_{\text{Reuss}}^{\text{LDA}}$ | 0.997 | 0.993 | 0.111 |
| σ^{exp} vs. σ^{GGA} | 0.982 | 0.986 | 0.037 |
| σ^{exp} vs. σ^{LDA} | 0.983 | 0.993 | 0.052 |

TABLE XXII. Materials from AFLOW database with the highest thermal conductivities as predicted using the AEL-AGL methodology. Units: κ in ($\text{W m}^{-1}\text{K}^{-1}$).

| Comp. | Pearson | Space Group | # | κ^{AGL} |
|----------------------------------------------|---------|-------------|-----|-----------------------|
| C | cF8 | 227 | 420 | |
| BN | cF8 | 216 | 282 | |
| C | hP4 | 194 | 272 | |
| C | tI8 | 139 | 206 | |
| BC ₂ N | oP4 | 25 | 188 | |
| BN | hP4 | 186 | 178 | |
| C | hP8 | 194 | 167 | |
| C | cI16 | 206 | 162 | |
| C | oS16 | 65 | 147 | |
| C | mS16 | 12 | 145 | |
| BC ₇ | tP8 | 115 | 145 | |
| BC ₅ | oI12 | 44 | 137 | |
| Be ₂ C | cF12 | 225 | 129 | |
| CN ₂ | tI6 | 119 | 127 | |
| C | hP12 | 194 | 127 | |
| BC ₇ | oP8 | 25 | 125 | |
| B ₂ C ₄ N ₂ | oP8 | 17 | 120 | |
| MnB ₂ | hP3 | 191 | 117 | |
| C | hP4 | 194 | 117 | |
| SiC | cF8 | 216 | 113 | |
| TiB ₂ | hP3 | 191 | 110 | |
| AlN | cF8 | 225 | 107 | |
| BP | cF8 | 216 | 105 | |
| C | hP16 | 194 | 105 | |
| VN | hP2 | 187 | 101 | |

to contain materials with large unit cells and heavier elements such as Hg, Tl, Pb and Au.

By combining the AFLOW search for thermal conductivity values with other properties such as chemical, electronic or structural factors, candidate materials for specific engineering applications can be rapidly identified for further in-depth analysis using more accurate computa-

TABLE XXIII. Materials from AFLOW database with the lowest thermal conductivities as predicted using the AEL-AGL methodology. Units: κ in ($\text{W m}^{-1}\text{K}^{-1}$).

| Comp. | Pearson | Space Group | # | κ^{AGL} |
|---------------------------------------------------|---------|-------------|--------|-----------------------|
| Hg ₃₃ Rb ₃ | cP36 | 221 | 0.0113 | |
| Hg ₃₃ K ₃ | cP36 | 221 | 0.0116 | |
| Cs ₆ Hg ₄₀ | cP46 | 223 | 0.0136 | |
| Ca ₁₆ Hg ₃₆ | cP52 | 215 | 0.0751 | |
| CrTe | cF8 | 216 | 0.081 | |
| Hg ₄ K ₂ | oI12 | 74 | 0.086 | |
| Sb ₆ Tl ₂₁ | cI54 | 229 | 0.089 | |
| Se | cF24 | 227 | 0.093 | |
| Cs ₈ I ₂₄ Sn ₄ | cF36 | 225 | 0.104 | |
| Ag ₂ Cr ₄ Te ₈ | cF56 | 227 | 0.107 | |
| AsCdLi | cF12 | 216 | 0.116 | |
| Au ₃₆ In ₁₆ | cP52 | 215 | 0.117 | |
| Cd ₃ In | cP4 | 221 | 0.128 | |
| AuLiSb | cF12 | 216 | 0.130 | |
| K ₅ Pb ₂₄ | cI58 | 217 | 0.135 | |
| K ₈ Sn ₄₆ | cP54 | 223 | 0.142 | |
| Au ₇ Cd ₁₆ Na ₆ | cF116 | 225 | 0.145 | |
| Cs | cI2 | 229 | 0.148 | |
| Cs ₈ Pb ₄ Cl ₂₄ | cF36 | 225 | 0.157 | |
| Au ₄ In ₈ Na ₁₂ | cF96 | 227 | 0.158 | |
| SeTl | cP2 | 221 | 0.164 | |
| Cd ₃₃ Na ₆ | cP39 | 200 | 0.166 | |
| Au ₁₈ In ₁₅ Na ₆ | cP39 | 200 | 0.168 | |
| Cd ₂₆ Cs ₂ | cF112 | 226 | 0.173 | |
| Ag ₂ I ₂ | hP4 | 186 | 0.192 | |

tional methods and for experimental examination. The full set of thermomechanical properties calculated using AEL-AGL for over 3500 entries can be accessed online at aflow.org¹⁴⁵, which incorporates search and sort functionality to generate customized lists of materials.

IV. CONCLUSIONS

We have implemented the “Automatic Elasticity Library” framework for *ab-initio* elastic constant calculations, and integrated it with the “Automatic GIBBS Library” implementation of the GIBBS quasi-harmonic Debye model within the AFLOW and Materials Project ecosystems. We used it to automatically calculate the bulk modulus, shear modulus, Poisson ratio, thermal conductivity, Debye temperature and Grüneisen parameter of materials with various structures and compared them with available experimental results.

A major aim of high-throughput calculations is to identify useful property descriptors for screening large datasets of structures³¹. Here, we have examined whether the *inexpensive* Debye model, despite its well known deficiencies, can be usefully leveraged for estimating thermal properties of materials by analyzing correlations between calculated and corresponding experimental quantities.

It is found that the AEL calculation of the elastic moduli reproduces the experimental results quite well, within 5% to 20%, particularly for materials with cubic and hexag-

onal structures. The AGL method, using an isotropic approximation for the bulk modulus, tends to provide a slightly worse quantitative agreement but still reproduces trends equally well. The correlations are very high, often above 0.99. Using different values of the Poisson ratio mainly affects Debye temperatures, while having very little effect on Grüneisen parameters. Several different numerical and empirical equations of state have also been investigated. The differences between the results obtained from them are small, but in some cases they are found to introduce an additional source of error compared to a direct evaluation of the bulk modulus from the elastic tensor or from the $E(V)$ curve. Using the different equations of state has very little effect on Debye temperatures, but has more of an effect on Grüneisen parameters. Currently, the values for AGL properties available in the AFLOW repository are those calculated by numerically fitting the $E_{\text{DFT}}(V)$ data and calculating the bulk modulus using Eq. (16). The effect of using different exchange-correlation functionals was investigated for a subset of 16 materials. The results showed that LDA tended to overestimate thermomechanical properties such as bulk modulus or Debye temperature, compared to GGA’s tendency to underestimate. However, neither functional was consistently better than the other at predicting trends. We therefore use GGA-PBE for the automated AEL-AGL calculations in order to maintain consistency with the rest of the AFLOW data.

The AEL-AGL evaluation of the Debye temperature provides good agreement with experiment for this set of materials, whereas the predictions of the Grüneisen parameter are quite poor. However, since the Grüneisen parameter is slowly varying for materials sharing crystal structures, the AEL-AGL methodology provides a reliable screening tool for identifying materials with very high or very low thermal conductivity. The correlations between the experimental values of the thermal conductivity and those calculated with AGL are summarized in Table XXIV. For the entire set of materials examined we find high values of the Pearson correlation between κ^{exp} and κ^{AGL} , ranging from 0.880 to 0.933. It is particularly high, above 0.9, for materials with high symmetry (cubic, hexagonal or rhombohedral) structures, but significantly lower for anisotropic materials. In our previous work on AGL³⁴, we used an approximated the value of $\sigma = 0.25$ in Eq. (14). Using instead the Poisson ratio calculated in AEL, σ^{AEL} , the overall correlations are improved by about 5%, from 0.880 to 0.928, in the agreement with previous work on metals¹⁴⁶. The correlations for anisotropic materials, such as the body-centred tetragonal set examined here, improved even more, demonstrating the significance of a direct evaluation of the Poisson ratio. This combined algorithm demonstrates the advantage of an integrated high-throughput materials design framework such as AFLOW, which enables the calculation of interdependent properties within a single automated workflow.

A direct AEL evaluation of the Poisson ratio, instead of assuming a simple approximation, e.g. a Cauchy solid

TABLE XXIV. Correlations between experimental values and AEL and AGL results for elastic and thermal properties for the entire set of materials.

| Property | Pearson (Linear) | Spearman (Rank Order) | RMSrD |
|-----------------------------------------------------------------------------------|---------------------|--------------------------|-------|
| κ^{exp} vs. κ^{AGL} ($\sigma = 0.25$) ³⁴ | 0.880 | 0.752 | 1.293 |
| κ^{exp} vs. κ^{AGL} | 0.928 | 0.720 | 2.614 |
| κ^{exp} vs. κ^{BM} | 0.879 | 0.735 | 2.673 |
| κ^{exp} vs. κ^{Vinet} | 0.912 | 0.737 | 2.443 |
| κ^{exp} vs. κ^{BCN} | 0.933 | 0.733 | 2.751 |

with $\sigma = 0.25$, consistently improves the correlations of the AGL-Debye temperatures with experiments. However, it has very little effect on the values obtained for the Grüneisen parameter. Simple approximations lead to more numerically-robust and better system-size scaling calculations, as they avoid the complications inherent in obtaining the elastic tensor. Therefore, AGL could also be used on its own for initial rapid screening, with AEL being performed later for potentially interesting materials to increase the accuracy of the results.

With respect to rapid estimation of thermal conductivities, the approximations in the Leibfried-Schlömann formalism miss some of the details affecting the lattice thermal conductivity, such as the suppression of phonon-phonon scattering due to large gaps between the branches of the phonon dispersion²⁶. Nevertheless, the high correlations between κ^{exp} and κ^{AGL} found for most of the structure families in this study demonstrate the utility of the AEL-AGL approach as a screening method for large databases of materials where experimental data is lacking or ambiguous. Despite its intrinsic limitations, the synergy presented by the AEL-AGL approach provides the right balance between accuracy and complexity in identifying materials with promising properties for further investigation.

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Appendix A: AFLOW AEL-AGL REST-API

The AEL-AGL methodology described in this work is being used to calculate the elastic and thermal properties

of materials in a high-throughput fashion by the AFLOW consortium. The results are now available on the AFLOW

database^{35,145} via the AFLOW REST-API³⁶. The following optional materials keywords have now been added to the AFLOW REST-API to facilitate accessing this data.

-
- `ael_bulk_modulus_reuss`
 - *Description.* Returns AEL bulk modulus as calculated using the Reuss average.
 - *Type.* number.
 - *Units.* GPa.
 - *Example.* `ael_bulk_modulus_reuss=105.315`.
 - *Request syntax.* `$aurl/?ael_bulk_modulus_reuss`.
 - `ael_bulk_modulus_voigt`
 - *Description.* Returns AEL bulk modulus as calculated using the Voigt average.
 - *Type.* number.
 - *Units.* GPa.
 - *Example.* `ael_bulk_modulus_voigt=105.315`.
 - *Request syntax.* `$aurl/?ael_bulk_modulus_voigt`.
 - `ael_bulk_modulus_vrh`
 - *Description.* Returns AEL bulk modulus as calculated using the Voigt-Reuss-Hill (VRH) average.
 - *Type.* number.
 - *Units.* GPa.
 - *Example.* `ael_bulk_modulus_vrh=105.315`.
 - *Request syntax.* `$aurl/?ael_bulk_modulus_vrh`.
 - `ael_elastic_anisotropy`
 - *Description.* Returns AEL elastic anisotropy.
 - *Type.* number.
 - *Units.* dimensionless.
 - *Example.* `ael_elastic_anisotropy=0.000816153`.
 - *Request syntax.* `$aurl/?ael_elastic_anisotropy`.
 - `ael_poisson_ratio`
 - *Description.* Returns AEL Poisson ratio.
 - *Type.* number.
 - *Units.* dimensionless.
 - *Example.* `ael_poisson_ratio=0.21599`.
 - *Request syntax.* `$aurl/?ael_poisson_ratio`.
 - `ael_shear_modulus_reuss`
 - *Description.* Returns AEL shear modulus as calculated using the Reuss average.
 - *Type.* number.
 - *Units.* GPa.
 - *Example.* `ael_shear_modulus_reuss=73.7868`.
 - *Request syntax.* `$aurl/?ael_shear_modulus_reuss`.
 - `ael_shear_modulus_voigt`

- *Description.* Returns AEL shear modulus as calculated using the Voigt average.
 - *Type.* number.
 - *Units.* GPa.
 - *Example.* `ael_shear_modulus_voigt=73.7989`.
 - *Request syntax.* `$aurl/?ael_shear_modulus_voigt`.
- `ael_shear_modulus_vrh`
 - *Description.* Returns AEL shear modulus as calculated using the Voigt-Reuss-Hill (VRH) average.
 - *Type.* number.
 - *Units.* GPa.
 - *Example.* `ael_shear_modulus_vrh=73.7929`.
 - *Request syntax.* `$aurl/?ael_shear_modulus_vrh`.
- `ael_speed_of_sound_average`
 - *Description.* Returns AEL average speed of sound calculated from the transverse and longitudinal speeds of sound.
 - *Type.* number.
 - *Units.* m/s.
 - *Example.* `ael_speed_of_sound_average=500.0`.
 - *Request syntax.* `$aurl/?ael_speed_of_sound_average`.
- `ael_speed_of_sound_longitudinal`
 - *Description.* Returns AEL speed of sound in the longitudinal direction.
 - *Type.* number.
 - *Units.* m/s.
 - *Example.* `ael_speed_of_sound_longitudinal=500.0`.
 - *Request syntax.* `$aurl/?ael_speed_of_sound_longitudinal`.
- `ael_speed_of_sound_transverse`
 - *Description.* Returns AEL speed of sound in the transverse direction.
 - *Type.* number.
 - *Units.* m/s.
 - *Example.* `ael_speed_of_sound_transverse=500.0`.
 - *Request syntax.* `$aurl/?ael_speed_of_sound_transverse`.
- `agl_acoustic_debye`
 - *Description.* Returns AGL acoustic Debye temperature.
 - *Type.* number.
 - *Units.* K.
 - *Example.* `agl_acoustic_debye=492`.
 - *Request syntax.* `$aurl/?agl_acoustic_debye`.
- `agl_bulk_modulus_isothermal_300K`
 - *Description.* Returns AGL isothermal bulk modulus at 300K and zero pressure.
 - *Type.* number.
 - *Units.* GPa.
 - *Example.* `agl_bulk_modulus_isothermal_300K=96.6`.

- *Request syntax.* \$aurl/?agl_bulk_modulus_isothermal_300K.
- agl_bulk_modulus_static_300K
 - *Description.* Returns AGL static bulk modulus at 300K and zero pressure.
 - *Type.* number.
 - *Units.* GPa.
 - *Example.* agl_bulk_modulus_static_300K=99.59.
 - *Request syntax.* \$aurl/?agl_bulk_modulus_static_300K.
- agl_debye
 - *Description.* Returns AGL Debye temperature.
 - *Type.* number.
 - *Units.* K.
 - *Example.* agl_debye=620.
 - *Request syntax.* \$aurl/?agl_debye.
- agl_gruneisen
 - *Description.* Returns AGL Grüneisen parameter.
 - *Type.* number.
 - *Units.* dimensionless.
 - *Example.* agl_gruneisen=2.06.
 - *Request syntax.* \$aurl/?agl_gruneisen.
- agl_heat_capacity_Cv_300K
 - *Description.* Returns AGL heat capacity at constant volume (C_V) at 300K and zero pressure.
 - *Type.* number.
 - *Units.* k_B /cell.
 - *Example.* agl_heat_capacity_Cv_300K=4.901.
 - *Request syntax.* \$aurl/?agl_heat_capacity_Cv_300K.
- agl_heat_capacity_Cp_300K
 - *Description.* Returns AGL heat capacity at constant pressure (C_p) at 300K and zero pressure.
 - *Type.* number.
 - *Units.* k_B /cell.
 - *Example.* agl_heat_capacity_Cp_300K=5.502.
 - *Request syntax.* \$aurl/?agl_heat_capacity_Cp_300K.
- agl_poisson_ratio_source
 - *Description.* Returns source of Poisson ratio used to calculate Debye temperature in AGL. Possible sources include ael_poisson_ratio_<value>, in which case the Poisson ratio was calculated from first principles using AEL; empirical_ratio_<value>, in which case the value was taken from the literature; and Cauchy_ratio_0.25, in which case the default value of 0.25 of the Poisson ratio of a Cauchy solid was used.
 - *Type.* string.
 - *Example.* agl_poisson_ratio_source=ael_poisson_ratio_0.193802.
 - *Request syntax.* \$aurl/?agl_poisson_ratio_source.
- agl_thermal_conductivity_300K
 - *Description.* Returns AGL thermal conductivity at 300K.

- *Type. number.*
- *Units.* W/m*K.
- *Example.* `agl_thermal_conductivity_300K=24.41`.
- *Request syntax.* `$curl/?agl_thermal_conductivity_300K`.

- `agl_thermal_expansion_300K`

- *Description.* Returns AGL thermal expansion at 300K and zero pressure.
- *Type. number.*
- *Units.* 1/K.
- *Example.* `agl_thermal_expansion_300K=4.997e-05`.
- *Request syntax.* `$curl/?agl_thermal_expansion_300K`.

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