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Accelerated adiabatic passage of a single electron spin qubit in quantum dots

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Adiabatic processes can keep the quantum system in its instantaneous eigenstate, which is robust to noises and dissipation. However, it is limited by sufficiently slow evolution. Here, we experimentally demonstrate the transitionless quantum driving (TLQD) of the shortcuts to adiabaticity (STA) in gate-defined semiconductor quantum dots (QDs) to greatly accelerate the conventional adiabatic passage for the first time. For a given efficiency of quantum state transfer, the acceleration can be more than 2-fold. The dynamic properties also prove that the TLQD can guarantee fast and highfidelity quantum state transfer. In order to compensate for the diabatic errors caused by dephasing noises, the modified TLQD is proposed and demonstrated in experiment by enlarging the width of the counter-diabatic drivings. The benchmarking shows that the state transfer fidelity of 97.8% can be achieved. This work will greatly promote researches and applications about quantum simulations and adiabatic quantum computation based on the gate-defined QDs.

Introduction.— Gate-defined semiconductor quantum dots (QDs) can electrically control electron and hole states with ultra-high precision, which is one of the state-of-the-art quantum devices [1, 2]. The spin qubit of QDs is a promising candidate for fault-tolerant solidstate quantum computing due to its high-fidelity quantum operation [3–6], potential scalability [7–9], and well compatibility with manufacturing technology of semiconductor industry [10]. Recently, two-qubit gate fidelity of more than 99% have been demonstrated experimentally [11–14], crossing the well-known surface code threshold [15, 16]. Besides, QD systems are becoming emerging platforms for quantum simulations to explore strongly interacting electrons and topological phases in condensed-matter physics, such as the Fermi–Hubbard system [17], Nagaoka ferromagnetism [18], and the Su–Schrieffer–Heeger model [19].

In order to achieve the so called "quantum advantage" [20], a high-fidelity quantum processor with large enough computational space and programmable qubits is required. Meanwhile, it also needs accurate quantum control and good robustness against noises and dissipation. One possible pathway is to find a feasible quantum control theory that is applicable for the large-scale quantum processor and guarantees high-accuracy quantum operation simultaneously. It is well known that the manipulation of a quantum state using resonant pulses is sensitive to timing and pulse area errors. In contrast, adiabatic passage can always keep some properties of a dynamical quantum system invariant, ideally switch an initial state into the target state, such as the high fidelity adiabatic process demonstrated in ³¹P electron qubit of silicon QDs system [21]. This can well prevent decoherence from experimental imperfections [22]. Generally, slow enough evolution is necessary to satisfy adiabatic conditions, limiting its applications. To achieve rapid and robust quantum state manipulation, several shortcuts to adiabaticity (STA) schemes are put forward to compensate for the nonadiabatic errors [23–27], for instance the transitionless quantum driving (TLQD) and invariant-based inverse engineering. Some of them have been demonstrated in other quantum systems [28–33]. Besides, STA has significant applications in quantum simulations to greatly suppress diabatic excitations [34].

Here, we experimentally demonstrate the STA of a single spin qubit in gate-defined QDs for the first time. The experiment is based on the theory of TLQD [23], and the acceleration of quantum state transfer has been achieved. This is also verified from the dynamics of the spin state. To suppress the noises from nuclear spin fluctuations, we propose and experimentally demonstrate a modified TLQD (MOD-TLQD) by enlarging the width of the counter-diabatic pulse. The benchmarking of this MOD-TLQD demonstrates a state transfer efficiency of 97.8%. Since the gate-defined QDs are moving toward the scalable quantum processor [35], the results of this paper will greatly promote related researches about quantum control and quantum simulations.

The acceleration of quantum state transfer.— Figure 1(a) shows a scanning electron microscope (SEM) picture of the double QDs (DQDs), which is fabricated on the GaAs/AlGaAs heterostructure. After the implemen-

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Figure 1. The device and its basic properties. (a) The falsecolored micrograph of the device. The high frequency pulses are applied through the plunger gates P1 and P2, and the MW driving is connected with P1. (b) Charge stability diagram around single electron region. The position of I, B, and O are represented by the green star, black square, and blue circle, respectively. The position of the initialization is also used for the readout. (c) The schematic of TLQD. (d) Rabi frequency $f_{\rm Rabi}$ as a function of the MW amplitude. Its maximum value is about $f_{\rm Rabi}^{\rm max} \sim 7.5$ MHz.

tation of an in-plane magnetic field B_{ext} , the qubit frequency of a single electron spin is $f_{\text{qubit}} = |g|\mu_B B/(2\pi\hbar)$, in which μ_B is the Bohr magneton, g is the Landé g-factor (~ -0.41 for this GaAs QDs), and B is the total magnetic field (consists of B_{ext} and the effective Overhauser field B_{nuc}^z). When a microwave (MW) driving is applied, the spin manipulation can be achieved using electric dipole spin resonance (EDSR) [36]. Besides, we use inter-dot tunneling to enhance the Rabi frequency [37]. We employ energy-selective readout to measure the spin state [38–40]. A nearby charge sensor provides rapid and real time detection of charge state based on the radio frequency (RF) reflectometry [41, 42].

Under the rotating frame, the interaction Hamiltonian expanded on the $|\uparrow\rangle$ and $|\downarrow\rangle$ Hilbert space is

$$\hat{H}_0 = \frac{\hbar}{2} \begin{pmatrix} -\Delta(t) & \Omega_R(t) \\ \Omega_R(t) & \Delta(t) \end{pmatrix}, \qquad (1)$$

in which $\Omega_R(t)$ is the Rabi frequency, and $\Delta(t)$ is the frequency detuning with the expression $\Delta(t) = \omega_{\text{qubit}} - \omega_{\text{MW}} - t\dot{\omega}_{\text{MW}}$. A high-fidelity quantum state transfer can occur if the evolution of this controllable parameter $\Delta(t)$ is slow enough. However, the TLQD can correct diabatic errors by adding the counter-diabatic driving \hat{H}_{CD} even though the evolution does not satisfy adiabatic conditions [23], as shown in Fig. 1(c). The TLQD can always keep the system in $|\varphi_k(t)\rangle$, the instantaneous eigenstate of \hat{H}_0 . Therefore, the time-dependent evolution operator and total Hamiltonian can be obtained. Furthermore, we can know \hat{H}_{CD} which has the expression $i\hbar \sum_k |\partial_t \varphi_k\rangle \langle \varphi_k|$. For this single electron spin system, its specific expression is $\hat{H}_{CD} = \hbar \Omega_a(t) \sigma_y/2$, in which $\Omega_a(t) = \left[\Omega_R(t) \dot{\Delta}(t) - \dot{\Omega}_R(t) \Delta(t)\right]/\Omega^2$ and $\Omega^2 = \Delta^2(t) + \Omega_R^2(t)$. Obviously, the function of \hat{H}_{CD} is to correct the diabatic errors by applying a time-dependent driving in \hat{y} -axis.

In our experiment, the electron is initialized to $|\uparrow\rangle$ state at the initialization point (I), as shown in Fig. 1(b). Then, the pulse sequences applied on plunger gates P1 and P2 deliver this electron to the intermediate transit point (B) and then to the operation point (O). After the spin manipulation at O point, this electron is delivered back to B and then to the readout point (R). Here, I and R point are the same. Our setup utilizes an arbitrary waveform generator (AWG) and an I/Q mixer to precisely tune the time-dependent terms Ω_R , Ω_a , and Δ . The relationship between Ω_R (or Ω_a) and the MW amplitude has to be characterized firstly. The Rabi frequency estimated from the Rabi oscillation and Landau-Zener transition are nearly the same. Please find more details in Section III of the Supplementary Materials. As shown in Fig. 1(d), f_{Rabi} increases linearly with larger MW amplitude. Then, it becomes saturated progressively until reaching the maximum value $f_{\text{Rabi}}^{\text{max}} \sim 7.5$ MHz because of the limitation from the trapping potentials or MW amplifiers.

The most significant advantage of this TLQD is that it can always guarantee a quantum system in one of its instantaneous eigenstates and greatly accelerate the adiabatic passage. Figure 2(a) shows the final spin down probability P_{\perp} and state transfer efficiency (or fidelity) F_{flip} as a function of the total evolution time T_e . The green squares and blue circles represent the results of TLQD and conventional adiabatic evolution, respectively. The red solid line is the least-squares fitting to the Landau-Zener formula [43–45]. The experimental results show that TLQD always has higher P_{\downarrow} and F_{flip} than the conventional adiabatic passage. The differences of P_{\downarrow} (also $F_{\rm flip}$) between TLQD and adiabatic passage become smaller progressively with longer T_e (slower evolution speed). When T_e is long enough, Ω_a becomes small enough to be neglected, in analogy to the adiabatic evolution. Note that F_{flip} is evaluated from the experimental results P_{\downarrow} by taking the initialization fidelity $(F_{\text{ini}}^{\uparrow})$, spin-to-charge fidelity $(F_{\text{STC}}^{\downarrow})$ and $F_{\text{STC}}^{\uparrow}$, and charge detection fidelity (F_{E}) into consideration. Please check Section I and VI in the Supplementary Materials. Generally, the relationship $P_{\downarrow} = P_{\downarrow}^{\text{ini}=\uparrow} + P_{\downarrow}^{\text{ini}=\downarrow}$ exists, in which $P_{\downarrow}^{\text{ini}=\uparrow}$ and $P_{\downarrow}^{\text{ini}=\downarrow}$ stand for the situations with the initialization of spin to up and down state, respectively. The expression of $P_{\perp}^{\text{ini}=\uparrow}$ and $P_{\parallel}^{\text{ini}=\downarrow}$ are $F_{\text{ini}}^{\uparrow}F_{\text{flip}}F_{\text{STC}}^{\downarrow}F_{\text{E}} + F_{\text{ini}}^{\uparrow}\left(1 - F_{\text{flip}}\right)\left(1 - F_{\text{STC}}^{\uparrow}\right)F_{\text{E}}$ and $(1 - F_{\rm ini}^{\uparrow}) (1 - F_{\rm flip}) F_{\rm STC}^{\downarrow} F_{\rm E} + (1 - F_{\rm ini}^{\uparrow}) F_{\rm flip} (1 - F_{\rm STC}^{\uparrow}) F_{\rm E},$ respectively. We also make sure that the enhancement of state transfer originates from the compensation for diabatic errors instead of simply enlarging the Rabi frequency, please see Section II in the Supplementary Ma-



Figure 2. The result of TLQD. (a) The final spin down probability P_{\downarrow} as a function of the evolution time T_e using the conventional adiabatic evolution and TLQD. The red solid line is the fitting to the formula $AP_{\downarrow}^{LZ} + B$, giving the value of $\Omega_R/2\pi = 4.63$ MHz. The inset displays the speed-up factor η as functions of P_{\downarrow} and the efficiency of state transfer F_{flip} . (b) The simulation results of P_{\downarrow} and F_{flip} as a function of T_e under different variance of qubit frequency noise $\sigma \sim 0.0$ MHz (green solid line), 3.5 MHz (red dashed line), and 7.0 MHz (black dashdotted line). To better compare the simulation and experimental results, the red dashed line with $\sigma \sim 3.5$ MHz is also plotted in (a). The modulation depth is $\delta_d = 100.0$ MHz. The maximum Rabi frequency is assumed to be $f_{\text{Rabi}}^{\text{max}} = 7.5$ MHz. (c) and (d) are the experimental and simulation results of the dynamics of P_{\downarrow} , respectively. The Rabi frequency is $\Omega_R/2\pi = 4.18$ MHz.

terials. In our experiment, the maximum value of P_{\downarrow} is about 0.85, which is mainly limited by the readout fidelity. It can be improved by enhancing the relaxation time T_1 and bandwidth of the RF-reflectometry after demodulation.

We find that P_{\downarrow} and $F_{\rm flip}$ of TLQD decrease more rapidly when $T_e < 0.4 \ \mu s$. This originates from the saturation of Ω_a (because of the large compensation for diabatic errors and the limited value of $f_{\rm Rabi}^{\rm max}$). Please find the simulation results without considering the limitation of $f_{\rm Rabi}^{\rm max}$ in Fig. S13 of the Supplementary Materials. When $T_e > 0.4 \ \mu s$, there is a tiny increase of P_{\downarrow} and $F_{\rm flip}$. As you can see in Section II of the Supplementary Materials, the TLQD has the highest efficiency of state transfer when $f_{\rm qubit} = f_{\rm MW}^c$ ($f_{\rm MW}^c$ is the center frequency of the MW). The dephasing noises (mainly from the Overhauser field) would cause the fluctuations of $B_{\rm nuc}^z$ and degrade the performance of TLQD.

The simulation after taking dephasing noises and saturation of Rabi frequency into consideration is also performed. For the GaAs QDs [46, 47], the coherence time is dominated by the quasistatic (or low-frequency) noises with a spectral distribution $S(f) \propto 1/f^{\beta}$. For simplicity, β is set to be 2, i.e., $S(f) = A^2/f^2$. The variance of the qubit frequency σ can be estimated as $\sigma^2 = 2 \int_{f_c}^{1/t} S(f) df = 2A^2 (1/f_c - t)$. Here, f_c and 1/tare low and high cutoff frequencies, respectively. The value of A can be calculated from the Ramsey pattern. Using the relationship $1/T_2^* = \sqrt{2}\pi\sigma$, we know $1/T_2^* = 2\pi A \sqrt{1/f_c - t}$. Please find more details in Section V of the Supplementary Materials. Here, the saturation value of total Rabi frequency is $f_{\text{Rabi}}^{\text{max}} = 7.5 \text{ MHz}$, i.e., $\Omega(t)$ is set as 7.5 MHz if $\Omega(t) > f_{\text{Rabi}}^{\text{max}}$. The value of σ is about 3.5 MHz. The simulation result is plotted as the red dashed line in both Fig. 2(a) and (b), which can well reproduce experimental results qualitatively. For GaAs QDs, β may range between 1 and 3. This just changes the value of A without changing the estimation of σ too much. In our simulation, we generate 2000 random values of δf_{qubit} (the shift of the qubit frequency) with the variance σ . For each δf_{qubit} , we can know F_{flip} (also P_{\downarrow} based on the relationship with $F_{\rm flip}$) by solving the Schrödinger equation of $H_0 + H_{CD}$. The average values of F_{flip} and P_{\downarrow} are the simulation results.

Generally, the TLQD consumes less time compared with conventional adiabatic evolution for a given state transfer efficiency. This acceleration can be characterized quantitatively by the time ratio $\eta = T_{\rm adia}/T_{\rm TLQD}$, in which $T_{\rm TLQD}$ and $T_{\rm adia}$ represent the time using the TLQD and conventional adiabatic passage, respectively. The result is shown in the inset of Fig. 2(a), in which an acceleration of more than 2-fold can be achieved. The value of η becomes flat when $P_{\downarrow} < 0.65$, which is due to the limitation of $f_{\rm Rabi}^{\rm max}$. Note that $T_{\rm TLQD}$ is estimated from the polynomial fitting to the experimental results of TLQD, and $T_{\rm adia}$ is deduced from the fitting to the



Figure 3. The result of MOD-TLQD. (a) The enhancement of spin flip probability ΔP_{\downarrow} as a function of α under different T_e . The markers are experimental data, and the lines represent simulation results. The variance of qubit frequency is $\sigma \sim 2.9$ MHz. The traces are shifted vertically for clarity. (b) The enhancement of spin flip probability $\Delta P'_{\downarrow}$ as a function of T_e . The width factor is set to be $\alpha = 2.5$. The Rabi frequency in (a) and (b) is $\Omega_R/2\pi \sim 4.0$ MHz. (c) The benchmarking of the efficiency of state transfer using the MOD-TLQD, giving the value of $p = 0.978 \pm 0.01$. The inset corresponds to the result of conventional adiabatic evolution, which has the oscillation instead of an exponential decay. (d) The schematic of pulse sequences to benchmark the spin flip fidelity.

Landau-Zener formula. We believe that the acceleration would be much faster for QDs with longer coherence time, e.g., silicon QDs [48]. The green solid line in Fig. 2(b) shows the simulation results if $\sigma = 0.0$ MHz. When the evolution time $T_e > 0.4 \ \mu$ s, P_{\downarrow} and $F_{\rm flip}$ can always keep the highest value. Furthermore, an acceleration of $\eta > 6$ can be achieved from our rough estimation. In contrast, large noises would greatly lower the efficiency of state transfer, represented by the black dashdotted line.

The dynamic properties of TLQD and adiabatic evolution are also investigated experimentally, as shown in Fig. 2(c). The blue line with circle dots and red line with square dots represent the results of TLQD and conventional adiabatic evolution, respectively. Here, we just show the results starting from the time 0.3 T_e , i.e., the relative time t' has a shift of 0.3 T_e with respect to the real time. Simulation results are displayed in Fig. 2(d), which can well reproduce experimental results. The experimental and simulation results show that this TLQD can always keep highest P_{\downarrow} (also F_{flip}) after spin flip under various T_e ranging from 0.4 μ s to 1.2 μ s. In contrast, P_{\downarrow} (also $F_{\rm flip}$) would increase gradually with longer T_e for the conventional adiabatic evolution. Meanwhile, its P_{\parallel} has much larger amplitude of oscillation compared with TLQD after the spin flip because its quantum state is not the eigenstate of this system.

Compensation for dephasing noises. — For an ideal case, the efficiency of state transfer using TLQD can be up to 100%. There are two main reasons that make it difficult to realize such high efficiency. The first comes from charge noises, which may cause a shift of the O point and Ω_R , leading to the over or under estimated value of Ω_a . The second is the nuclear spin fluctuations which can cause the shift of qubit frequency and significant dephasing in GaAs QDs. Here, we propose a feasible and simple method through pulse optimization to greatly compensate for dephasing noises.

In the TLQD experiment demonstrated above, Ω_R is kept as a constant and Δ is modulated linearly. Therefore, Ω_a has a Gaussian envelope, i.e., $\Omega_a(t) \propto$ $\left(\Delta^2 + \Omega_R^2\right)^{-1}$. In order to compensate for the dephasing noises, we can enlarge the width of this Gaussian envelope without changing the maximum value of Ω_a . This modified pulse is $\Omega_a^{\text{MOD}}(t) = \alpha^2 \Omega_R \dot{\Delta} \left(\Delta^2 + \alpha^2 \Omega_R^2 \right)^{-1}$. Here, α is the width factor, and this optimization makes the pulse width to be $\alpha \Omega_R$. The enhancement of P_{\perp} , with the definition $\Delta P_{\downarrow}(\alpha) = P_{\downarrow}(\alpha) - P_{\downarrow}(\alpha = 1.0)$, as a function of α under various T_e is shown in Fig. 3(a). It shows that P_{\perp} would increase with α firstly and reach the maximum when α ranges from 2.5 to 3.0. If $T_e < 0.6 \ \mu s$, there is a clear drop of ΔP_{\downarrow} when $\alpha > 2.5$, which may be due to the over compensation for diabatic errors. In contrast, ΔP_{\downarrow} is nearly flat when $\alpha > 2.5$ for the situation of $T_e > 0.6 \ \mu$ s. The reason is that Ω_a becomes smaller and the effect of over compensation is not obvious any more. The simulation results shown as the dashed lines can well reproduce our experimental results. We also note that the simulation result of $T_e = 0.4 \ \mu s$ is much smaller than the experimental result, which may be due to the under estimated value of $f_{\text{Rabi}}^{\text{max}}$ in our calculation.

In order to well demonstrate the performance of this width optimization method, the enhancement of P_{\downarrow} defined as $\Delta P'_{\downarrow} = \Delta P_{\downarrow}$ ($\alpha = 2.5$) as a function of T_e is displayed in Fig. 3(b). There is a clear enhancement under various T_e . Thus, the degradation of state transfer caused by the dephasing noises can be greatly compensated using the MOD-TLQD. Meanwhile, $\Delta P'_{\downarrow}$ becomes smaller progressively with longer T_e because of the negligible Ω_a . When $T_e > 1.1 \ \mu s$, $\Delta P'_{\downarrow}$ is nearly zero. Besides, the optimal value of α will become smaller with larger Ω_R because we have to keep $\alpha \Omega_R$ comparable with the dephasing noises. Please see more data in Section VIII of the Supplementary Materials.

Finally, the performance of this MOD-TLQD is characterized quantitatively. The probability P_{\downarrow} as a function of the spin flip number $n_{\rm flip}$ is measured, as shown in Fig. 3(c). The evolution time is $T_e = 0.6 \ \mu$ s, and a waiting time $\tau_{\rm wait} = 0.2 \ \mu$ s is added after each spin flip process to reduce the thermal heating, as shown in Fig. 3(d). The repeated sequences represent two flips in a row to keep the spin up state. After fitting to the formula $P_{\downarrow} = Ap^{n_{\rm flip}} + B$, the fidelity $p = 0.978 \pm 0.01$ is obtained. The relationship between $n_{\rm flip}$ and the number of this repeated sequences $n_{\rm seq}$ is $n_{\rm flip} = 2n_{\rm seq} + 1$. In contrast, the conventional adiabatic evolution has a clear oscillation for $T_e = 0.6 \ \mu$ s, as shown in the inset of Fig. 3(c). Only when T_e is large enough (larger than 1.1 μ s), the exponential decay can be observed. More data can be found in Fig. S12 of the Supplementary Materials. If we perform the spin flip using Rabi oscillation under the same conditions with Fig. 3(a), i.e., $\Omega_R/2\pi = 4.0$ MHz and $\sigma = 2.9$ MHz, the spin flip fidelity is less than 65.6%. Therefore, MOD-TLQD has higher fidelity, although it takes longer time.

Conclusion and outlook. — The STA is experimentally demonstrated in gate-defined QDs for the first time based on the TLQD protocol. Furthermore, the optimization by enlarging the width of counter-diabatic driving can achieve the efficiency of state transfer as high as 97.8%. The acceleration of quantum state transfer would be much better in Si or Ge QDs with longer coherence time. We also find that the experimental method in our pa-

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per can be directly used in the invariant-based inverse engineering [25], which also needs the precise control of time-dependent terms $\Delta(t)$, $\Omega_R(t)$, and $\Omega_a(t)$. Besides, for the cases that the input is a superposition state, i.e., $(|\uparrow\rangle + |\downarrow\rangle)/\sqrt{2}$, the output state would become $(|\uparrow\rangle - |\downarrow\rangle)/\sqrt{2}$. It means a π rotation along the \hat{z} -axis for this superposition state. Meanwhile, the TLQD may be used in other single-qubit operations and adiabatic passages of the QDs system. However, it still needs more researches both in theory and experiment.

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