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Jiangyong Jia, Giuliano Giacalone, and Chunjian Zhang

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Separating the impact of nuclear skin and nuclear deformation in high-energy isobar collisions

Jiangyong Jia,^{1,2,*} Giuliano Giacalone,^{3,†} and Chunjian Zhang¹

¹*Department of Chemistry, Stony Brook University, Stony Brook, NY 11794, USA*

²*Physics Department, Brookhaven National Laboratory, Upton, NY 11976, USA*

³*Institut für Theoretische Physik, Universität Heidelberg, Philosophenweg 16, 69120 Heidelberg, Germany*

Bulk nuclear structure properties, such as radii and deformations, leave distinct signatures in the final state of relativistic heavy-ion collisions. Isobaric collisions offer an easy route to establish explicit connections between the colliding nuclei's structure and the observable outcomes. Here, we investigate the effects of nuclear skin thickness and nuclear deformations on the elliptic flow (v_2) and its fluctuations in high-energy $^{96}\text{Ru}+^{96}\text{Ru}$ and $^{96}\text{Zr}+^{96}\text{Zr}$ collisions. Our findings reveal that the difference in skin thickness between these isobars only influences the inherent ellipticity of the collision systems, v_2^{FP} . In contrast, differences in nuclear deformations solely impact the fluctuations of v_2 around v_2^{FP} . Hence, we have identified a data-driven method to disentangle the effects of nuclear skin and nuclear deformations, marking a significant step towards assessing the consistency of nuclear phenomena across energy scales.

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The bulk properties of atomic nuclei reflect collective correlations in many-body systems held together by the strong force. Unraveling these properties and their evolution across the Segré chart constitutes a major goal in nuclear physics [1]. Traditionally, spectroscopic and scattering experiments at low energies have been employed to infer collective features of nuclei [2–4]. However, recent ultra-relativistic collision experiments have demonstrated that the dynamics of these collisions is significantly influenced by such properties [5–15]. Particularly, the angular distributions of emitted particles in high-energy collisions can be related directly to the shape of the colliding nuclei at the moment of interaction.

This connection stems from the near-ideal fluid behavior of the quark-gluon plasma (QGP) formed in high-energy collisions. In a hydrodynamic framework, anisotropies in the final-state azimuthal particle spectra emerge from spatial anisotropies in the initial conditions of the fluid expansion [16–18]. Spatial anisotropies are, in turn, sourced by the random positions of nucleons populating the colliding nuclei at the time of interaction. Unlike low-energy scattering experiments, which only provide access to average nuclear charge distributions, high-energy heavy-ion collisions can probe the spatial positions of *all* nucleons on an event-by-event basis, thus capturing multi-nucleon correlations. Experimental techniques employing multi-particle correlations routinely measure these correlations [19–21]. The crucial question is to what extent the established knowledge from low-energy nuclear physics can offer a coherent understanding of the phenomena observed at high-energy colliders. This Letter represents a significant step in addressing this question.

Although the influence of nuclear deformation is most pronounced in head-on collisions, it is possible to effectively isolate and study nuclear structure effects across

the entire centrality range by comparing two isobaric collision systems [10, 13, 15]. Isobaric nuclei have the same mass number, ensuring that any differences in observables must originate from differences in their structure, which impact the initial condition and evolution of the QGP. This argument is demonstrated clearly in $^{96}\text{Ru}+^{96}\text{Ru}$ and $^{96}\text{Zr}+^{96}\text{Zr}$ collisions at the BNL Relativistic Heavy Ion Collider, where ratios of observables between the two systems exhibit substantial and centrality-dependent deviations from unity [22].

Most models describe the nucleon density within colliding nuclei using a Woods-Saxon (WS) profile,

$$\rho(r, \theta, \phi) \propto [1 + \exp[r - R_0(1 + \beta_2 Y_2^0(\theta, \phi) + \beta_3 Y_3^0(\theta, \phi))]/a_0]^{-1}, \quad (1)$$

incorporating four structure parameters, nuclear skin a_0 , half-width radius R_0 , quadrupole deformation β_2 , and octupole deformation β_3 . Model studies have demonstrated that isobar ratios are indeed controlled by differences in these parameters, e.g., $\Delta\beta_2^2 = \beta_{2\text{Ru}}^2 - \beta_{2\text{Zr}}^2$, $\Delta\beta_3^2 = \beta_{3\text{Ru}}^2 - \beta_{3\text{Zr}}^2$, $\Delta a_0 = a_{0\text{Ru}} - a_{0\text{Zr}}$ and $\Delta R_0 = R_{0\text{Ru}} - R_{0\text{Zr}}$ [23].

Experimentally, many observables have been found to exhibit sensitivity to nuclear profile parameters, such as the mean transverse momentum p_T [24], its fluctuations [15], the spectator neutron number [25], flow vector correlations [26, 27], and shape-size correlations [8, 12, 14]. In this Letter, the focus is on the elliptic flow coefficient $V_2 = v_2 e^{2i\Psi_2}$, which characterizes the quadrupole modulation of particles in the direction Ψ_2 with an amplitude v_2 . V_2 emerges as a hydrodynamic response to the elliptical shape of the region of overlap between colliding nuclei. The ratio of v_2 between $^{96}\text{Ru}+^{96}\text{Ru}$ and $^{96}\text{Zr}+^{96}\text{Zr}$ collisions exhibits a complex non-monotonic centrality dependence [22], which can be explained as a combined effect of the four WS parameters in Eq. 1 [28]. We show that the impact of the deformations parameters (β_2 and β_3) can be disentangled from that of the

radial profile parameters (a_0 and R_0), and highlight the implications of this finding.

We begin with Fig. 1, where we represent the plane transverse to the collision axis with Cartesian coordinates, with the x direction aligned with the impact parameter direction. For events at a given centrality, the joint distribution of the real and imaginary parts of V_2 , (v_{2x}, v_{2y}) , approximately follows a two-dimensional Gaussian distribution [29]

$$p(v_{2x}, v_{2y}) = \frac{1}{\pi\delta^2} \exp\left[-\frac{(v_{2x} - v_2^{\text{rp}})^2 + v_{2y}^2}{\delta^2}\right]. \quad (2)$$

The displacement along the x -axis, v_2^{rp} , corresponds to the reaction plane flow associated with the average elliptic geometry, whereas the fluctuation, δ , represents the variance of elliptic flow due to fluctuations in the positions of the colliding nucleons. Our argument is that changes in the radial profile of the nucleus via a_0 or R_0 modify v_2^{rp} , while having little impact on the flow fluctuations (Fig. 1a). Conversely, in the presence of nuclear deformations, the random orientation of the colliding nuclei results in an increase in δ , with little effect on v_2^{rp} (Fig. 1b)[30]. Since $p(V_2)$ is approximately Gaussian, the root-mean-squared elliptic flow is $v_2\{2\} = \sqrt{(v_2^{\text{rp}})^2 + \delta^2}$, while higher-order cumulants of v_2 are all identical, $v_2\{4\} = v_2\{6\} = \dots = v_2\{\infty\} = v_2^{\text{rp}}$. In this limit, the fluctuation of v_2 can be obtained as

$$\delta^2 = v_2\{2\}^2 - v_2\{4\}^2. \quad (3)$$

In the following, we demonstrate our argument regarding the sensitivity of v_2^{rp} and δ to the nuclear structure parameters using transport model calculations.

We simulate the dynamics of the QGP using the multi-phase transport model (AMPT) [31]. Specifically, we use AMPT v2.26t5 in the string-melting mode at $\sqrt{s_{\text{NN}}} = 200$ GeV with a partonic cross section of 3.0 mb [32, 33]. This model has been successful in describing the isobar ratios of v_2 , v_3 , and N_{ch} measured by the STAR collaboration [11, 23]. We simulate generic isobar collisions, $^{96}\text{X}+^{96}\text{X}$, with five different choices of nuclear structure parameters β_2 , β_3 , R_0 and a_0 , as listed in Table I. This allows us to calculate ratios that isolate the effects of these parameters step-by-step. For example, Case1/Case2 isolates the effect of β_2 , Case1/Case3 includes the effect of β_2 and β_3 , and so on. We calculate the cumulants of elliptic flow within the multi-particle cumulant framework [19, 20] for hadrons with $0.2 < p_{\text{T}} < 2$ GeV. The two-particle cumulant $v_2\{2\}$ is obtained by correlating particles in $0 < \eta < 2$ with those in $-2 < \eta < 0$ to suppress short-range correlations that do not arise from the collective expansion of the system [21]. $v_2\{4\}$, which is free from such contributions, is calculated from all particles with $|\eta| < 2$. Additionally, we calculate the true v_2^{rp} from the azimuthal correlation of particles relative to the impact parameter and the true flow fluctuation

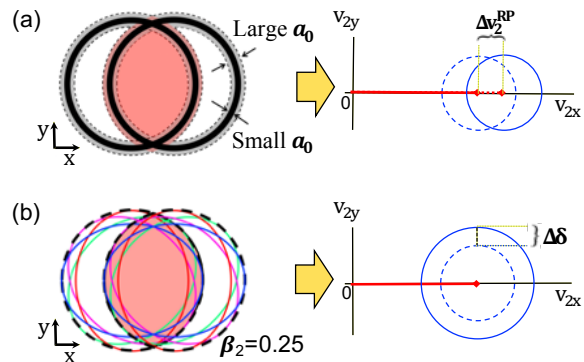


FIG. 1. (a) A schematic representation of a collision of spherical nuclei with different choices of their skin thickness, a_0 . The distribution (v_{2x}, v_{2y}) , denoted by blue circles, has a non-zero mean value along the x -direction, $\langle v_{2x} \rangle = v_2^{\text{rp}}$ indicated by red squares at the center of circles, while the variance of the distribution, corresponding to the radius of the circles, is the same along x and y . A larger skin (dashed lines) smears the elliptical shape of the QGP, resulting in a reduction of v_2^{rp} . (b) Collisions of deformed nuclei with random orientations (four for each nucleus labeled by colored lines) would lead to an increase in the width of the distribution, denoted by δ , relative to collisions of spherical nuclei.

δ_{rp} as $\delta_{\text{rp}}^2 = v_2\{2\}^2 - (v_2^{\text{rp}})^2$. The simulated events are binned into classes based on the number of participating nucleons, N_{part} .

	R_0 (fm)	a_0 (fm)	β_2	β_3
Case1 ^{96}Ru	5.09	0.46	0.162	0
Case2	5.09	0.46	0.06	0
Case3	5.09	0.46	0.06	0.20
Case4	5.09	0.52	0.06	0.20
Case5 ^{96}Zr	5.02	0.52	0.06	0.20
Ratios	Case1/Case2	Case1/Case3	Case1/Case4	Case1/Case5

TABLE I. Structure parameters used in the simulations of $^{96}\text{Ru}+^{96}\text{Ru}$ and $^{96}\text{Zr}+^{96}\text{Zr}$ collisions. Case1 and Case5 represent our full parameterizations of ^{96}Ru and ^{96}Zr , respectively.

In Fig. 2, we present our results for $v_2\{2\}$, $v_2\{4\}$, and δ , averaged over $^{96}\text{Ru}+^{96}\text{Ru}$ and $^{96}\text{Zr}+^{96}\text{Zr}$ collisions, which generally agree well with the STAR data. However, we note that the model underpredicts the value of $v_2\{4\}$ in off-central collisions while correctly reproducing the measured δ . This suggests that AMPT has a value of v_2^{rp} that is too small. This discrepancy may arise from the fact that particle production in AMPT scales with N_{part} , which is known to lead to smaller v_2^{rp} compared to other models that incorporate proper energy deposition scaling [34]. Recent calculations of $v_2\{2\}$ in isobar collisions by Nijs and van der Schee using the TREnto model do not suffer from this issue [35].

The STAR collaboration has also measured an approximation of v_2^{rp} by correlating particles with spectator neutrons in the zero-degree calorimeters (ZDC), denoted as

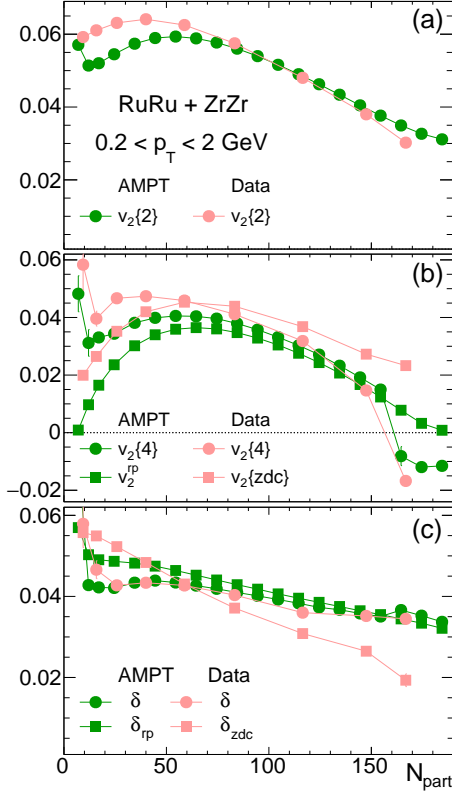


FIG. 2. Values of $v_2\{2\}$ (a), $v_2\{4\}$ and v_2^{rp} (b), δ and δ_{rp} (c) as a function of N_{part} , averaged between Ru+Ru and Zr+Zr collisions. The AMPT results are compared with the corresponding STAR data from Fig. 23 in Ref. [22]. For the STAR data, we approximate v_2^{rp} by $v_2\{zdc\}$, and δ_{rp} by δ_{zdc} , as discussed in the text.

$v_2\{zdc\}$. Figure 2(b) shows that $v_2\{zdc\}$ is smaller than $v_2\{4\}$ in peripheral collisions but is above it towards central collisions. The overall centrality-dependent trend is similar to that of AMPT's v_2^{rp} , indicating that $v_2\{zdc\}$ serves as a good proxy for v_2^{rp} , at least in peripheral and mid-central collisions. In Fig. 2(c), we also define the corresponding fluctuation δ_{zdc} as $\delta_{zdc}^2 = v_2\{2\}^2 - (v_2\{zdc\})^2$ and compare the results with the measured δ . They exhibit close agreement in peripheral collisions.

To isolate the effects of nuclear structure, we turn to isobar ratios. For an observable, \mathcal{O} , the ratio is calculated at a given N_{part} as

$$R_{\mathcal{O}}(N_{part}) = \frac{\mathcal{O}_{Ru}(N_{part})}{\mathcal{O}_{Zr}(N_{part})}. \quad (4)$$

Figure 3(a) shows the complex centrality dependence of $R_{v_2\{2\}}$, which arises from both deformation and radial profile parameters. In contrast, $R_{v_2\{4\}}$ in Fig. 3(b) is mainly sensitive to a_0 , whereas R_{δ} in Fig. 3(c) is primarily sensitive to β_2 and β_3 . Thus, the behavior of $R_{v_2\{2\}}$ can be decomposed into a part that is sensitive to the nuclear skin and a part that is sensitive to the nuclear deformations, supporting the intuition depicted in Fig. 1.

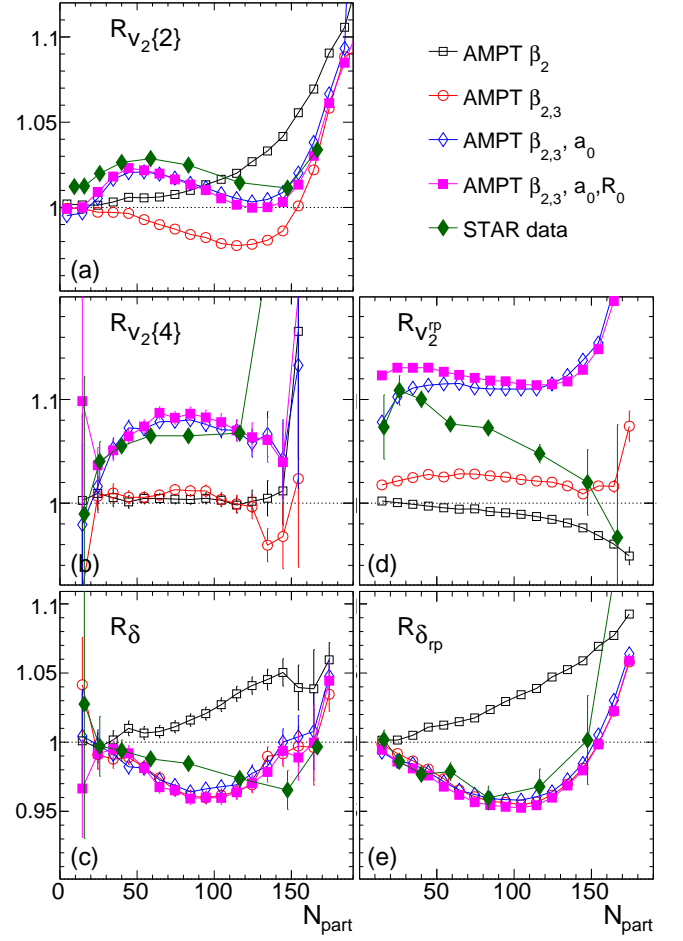


FIG. 3. Isobar ratios $R_{v_2\{2\}}$ (a), $R_{v_2\{4\}}$ (b), R_{δ} (c), $R_{v_2^{rp}}$ (d), and $R_{\delta_{rp}}$ (e) plotted as a function of N_{part} . For clarity and with reference to Tab. I, the curves labeled with “ β_2 ” correspond to Case1/Case2, where the two nuclei differ only by their value of β_2 . The curves labeled with “ $\beta_{2,3}$ ” correspond to Case1/Case3, which includes differences in both β_2 and β_3 . “ $\beta_{2,3}, a_0$ ” corresponds to Case1/Case4, adding the difference in a_0 , while “ $\beta_{2,3}, a_0, R_0$ ” corresponds to Case1/Case5, where all Woods-Saxon parameters are different. The results are compared with STAR data from Fig. 23 of Ref. [22]. Note that v_2^{rp} and δ_{rp} cannot be measured directly, and they are approximated by STAR measurements of $v_2\{zdc\}$ (d) and δ_{zdc} (e), respectively.

We establish the following identity,

$$R_{v_2\{2\}}^2 = R_{\delta}^2 + (R_{v_2\{4\}}^2 - R_{\delta}^2)r, \quad r = v_2\{4\}^2/v_2\{2\}^2 \quad (5)$$

$$R_{v_2\{2\}} \approx R_{\delta} + (R_{v_2\{4\}} - R_{\delta})r, \quad (6)$$

where the second line is obtained by assuming all ratios are close to unity. It is known that $r \sim 0$ in central collisions, and increases to around 0.8 in mid-central collisions. Consequently, the behavior of $R_{v_2\{2\}}$ in central collisions is predominantly determined by R_{δ} , while the non-monotonic behavior of $R_{v_2\{2\}}$ in mid-central collisions results from the interplay between $R_{v_2\{4\}}$ and R_{δ} .

This constitutes our main finding.

The right column of Fig. 3 presents the ratios of the true intrinsic ellipticity, $R_{v_2^{\text{rp}}}$ in Fig. 3(d), and the true flow fluctuation, $R_{\delta_{\text{rp}}}$ in Fig. 3(e), obtained from $\delta_{\text{rp}}^2 = v_2\{2\}^2 - (v_2^{\text{rp}})^2$. We observe that, for a difference in skin thickness of $a_{0\text{Ru}} - a_{0\text{Zr}} = 0.06$ fm, the value of v_2^{rp} is enhanced by about 10% in $^{96}\text{Ru}+^{96}\text{Ru}$ collisions. The impact of β_n on $R_{v_2^{\text{rp}}}$ is relatively minor, as expected. Furthermore, we observe that the values of v_2^{rp} vary more significantly compared to $v_2\{4\}$ when structure parameters are changed. As a result, $R_{\delta_{\text{rp}}}$ also exhibits a stronger dependence on these parameters than R_δ .

Note that v_2^{rp} and δ_{rp} cannot be measured directly, and therefore the ratios of these observables are approximated by the measured $R_{v_2\{\text{zdc}\}}$ in Fig. 3(d) and $R_{\delta_{\text{rp}}}$ in Fig. 3(e), respectively. The STAR data agree with AMPT $R_{v_2^{\text{rp}}}$ in peripheral collisions but gradually deviate and lose sensitivity to the WS parameters in more central collisions. This discrepancy could be attributed to a strong decorrelation between the spectator plane and the reaction plane [36] when the number of spectator neutrons is small. In contrast, STAR $R_{\delta_{\text{zdc}}}$ demonstrates good agreement with AMPT $R_{\delta_{\text{rp}}}$ in Fig. 3(e).

It is worth noting that elliptic flow emerges event-by-event as a response to the initial ellipticity of the system, denoted by \mathcal{E}_2 . This response follows a linear scaling, $V_2 \propto \mathcal{E}_2$ [37]. Therefore, the ratios of observables analyzed in Fig. 3 can be estimated solely based on knowledge of \mathcal{E}_2 and its fluctuations. In the supplemental material, we demonstrate that the observed behaviors in Fig. 3 largely originate from the initial state.

Our analysis does not rely exclusively on the Gaussian Ansatz in Eq. (2) for the distribution of v_2 . In fact, the fluctuations of v_2 are non-Gaussian, especially in peripheral collisions where v_2^{rp} is large and one becomes sensitive to the bound $v_2 < 1$ [38, 39]. It would be interesting to extend this study to higher-order cumulants, $v_2\{4, 6, 8\}$, and investigate how nuclear structure affects these quantities in isobar collisions [40]. In the supplemental material, we provide results for $R_{v_2\{4\}}$, $R_{v_2\{6\}}$ and $R_{v_2\{8\}}$, and also explore the fine splitting of these cumulants in terms of eccentricity fluctuations. Our preliminary findings, limited by AMPT statistics, indicate that there is no apparent separation of nuclear structure effects [41].

In summary, we have discovered that the nuclear radial profile parameters, i.e., nuclear skin thickness, a_0 , and half-density radius, R_0 , predominantly influence the magnitude of v_2 along the impact parameter direction captured by $v_2\{4\}$. In contrast, the nuclear deformations, β_n , primarily affect the fluctuation of elliptic flow, δ . We find that the measured isobar ratio of $v_2\{4\}$ is determined by $a_{0\text{Ru}} - a_{0\text{Zr}}$, while the measured isobar ratio of δ arises from the interplay between $\beta_{2\text{Ru}}^2 - \beta_{2\text{Zr}}^2$ and $\beta_{3\text{Ru}}^2 - \beta_{3\text{Zr}}^2$. Our results, combined with the previous finding that the isobar ratio of triangular flow is dominated

by $\beta_{3\text{Ru}}^2 - \beta_{3\text{Zr}}^2$ [23, 35], provide separate constraints on three key properties of the colliding nuclei: Δa_0 , $\Delta\beta_2^2$, and $\Delta\beta_3^2$.

The skin thickness as a property of the radial structure of nuclei is determined by the frame-independent one-body density of the nuclei. In contrast, deformations are defined in the intrinsic frame of nuclei and can only be captured by two- and many-body densities. Thus, separating skin and deformation effects implies that we have found an experimental method to discern the impact of one-body distribution from that of many-body correlations within nuclei. To our knowledge, such a clean separation of one-body and many-body effects is difficult to achieve in traditional low-energy nuclear structure experiments due to the larger time scales involved. Therefore, our result opens a new opportunity for nuclear structure research based on high-energy nuclear collisions.

On the side of heavy ion physics, our results can aid in the characterization of the QGP from data, which is currently limited by uncertainties in the QGP initial condition [42, 43]. Reducing these uncertainties requires improving our understanding of the role of the low-energy structure of nuclei in these processes. While flow observables are very sensitive to structure parameters between isobars—up to 10% for two-particle observables [22] and even larger for higher-order correlations as seen in Fig. 2 of [44]—the influences of different structure parameters are often entangled for most observables. Our technique, which separates the effects of nuclear radial parameters from nuclear shape parameters, represents a significant step towards refining the initial condition. This reinforces the scientific case for using isobar collisions to elucidate the influence of bulk nuclear structure properties in high-energy collisions, as extensively discussed in Ref. [44]. We hope that it will stimulate further investigations using selected isobar pairs at the LHC [45].

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* Correspond to jiangyong.jia@stonybrook.edu

† Correspond to giacalone@thphys.uni-heidelberg.de

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