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 Decay of α

$$^3\text{O}$$
 via β

-Delayed Charged-Particle Spectroscopy

J. Bishop, G. V. Rogachev, S. Ahn, M. Barbui, S. M. Cha, E. Harris, C. Hunt, C. H. Kim, D. Kim, S. H. Kim, E. Koshchiy, Z. Luo, C. Park, C. E. Parker, E. C. Pollacco, B. T. Roeder, M.

Roosa, A. Saastamoinen, and D. P. Scriven

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1 First observation of the $\beta 3\alpha p$ decay of ^{13}O via β -delayed charged-particle spectroscopy

2 J. Bishop,¹ G.V. Rogachev,^{1,2,3} S. Ahn,⁴ M. Barbui,¹ S.M. Cha,⁴ E. Harris,^{1,2} C. Hunt,^{1,2}
3 C.H. Kim,⁵ D. Kim,⁴ S.H. Kim,⁶ E. Koshchiy,¹ Z. Luo,^{1,2} C. Park,⁴ C.E. Parker,¹
4 E.C. Pollacco,⁷ B.T. Roeder,¹ M. Roosa,^{1,2} A. Saastamoinen,¹ and D.P. Scriven^{1,2}

5 ¹*Cyclotron Institute, Texas A&M University, College Station, TX 77843, USA*

6 ²*Department of Physics & Astronomy, Texas A&M University, College Station, TX 77843, USA*

7 ³*Nuclear Solutions Institute, Texas A&M University, College Station, TX 77843, USA*

8 ⁴*Center for Exotic Nuclear Studies, Institute for Basic Science, 34126 Daejeon, Republic of Korea*

9 ⁵*Department of Physics, Sungkyunkwan University (SKKU), Republic of Korea*

10 ⁶*Department of Physics, Sungkyunkwan University, Suwon 16419, Republic of Korea*

11 ⁷*IRFU, CEA, Université Paris-Saclay, Gif-Sur-Yvette, France*

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Background: The β -delayed proton-decay of ^{13}O has previously been studied, but the direct observation of β -delayed $3\alpha p$ decay has not been reported.

Purpose: Rare $3\alpha p$ events from the decay of excited states in $^{13}\text{N}^*$ provide a sensitive probe of cluster configurations in ^{13}N .

Method: To measure the low-energy products following β -delayed $3\alpha p$ -decay, the TexAT Time Projection Chamber was employed using the one-at-a-time β -delayed charged-particle spectroscopy technique at the Cyclotron Institute, Texas A&M University.

Results: A total of 1.9×10^5 ^{13}O implantations were made inside the TexAT Time Projection Chamber. 149 $3\alpha p$ events were observed yielding a β -delayed $3\alpha p$ branching ratio of 0.078(6)%.

Conclusion: Four previously unknown α -decaying excited states were observed in ^{13}N at 11.3 MeV, 12.4 MeV, 13.1 MeV and 13.7 MeV decaying via the $3\alpha+p$ channel.

13 INTRODUCTION

14 Exotic neutron-deficient nuclei provide an excellent op-
15 portunity to explore new decay modes. Large β -decay Q-
16 values make it possible to populate proton- or α -unbound
17 states in daughter nuclei, paving the way for observa-
18 tion of β -delayed charged-particle emissions. Reviews of
19 advances in β -delayed charged-particle emission studies
20 can be found in Ref. [1, 2], where β -delayed one, two,
21 and three proton decays as well as $\alpha p/p\alpha$ decays are dis-
22 cussed. Here we report on a new decay mode that has not
23 been observed before, the $\beta 3\alpha p$. Not only do we identify
24 these exotic decays of ^{13}O , but we were also able to use
25 it to obtain information on cluster structure in excited
26 states of the daughter nucleus, ^{13}N .

27 Clustering phenomena are prevalent in light nuclei
28 and are an excellent testing ground for understand-
29 ing few-body systems that are theoretically accessible.
30 These clustering phenomena have been well-studied in
31 α -conjugate nuclei. Much less experimental information
32 is available for $N \neq Z$ nuclei. Yet, theoretical studies (e.g.
33 [3–5]) indicate that cluster configurations may be even
34 richer in non-self-conjugate nuclei, opening a window of
35 opportunity to confront the highly-non-trivial theoretical
36 predictions with experimental data. Recent experimental
37 studies of clustering in non-self-conjugate nuclei already
38 produced exciting results, such as hints for linear chain
39 structures stabilized by “extra” nucleons (e.g. [6–8]) and
40 indications for super-radiance [9, 10].

41 Of particular interest is the nucleus ^{13}N where three α

42 particles and an “extra” proton can form exotic cluster
43 configurations. Resonant $^9\text{B}+\alpha$ scattering or α -transfer
44 reactions are not possible because ^9B is proton unbound
45 with a half life of the order of 10^{-18} s. Instead, one may
46 use β -delayed charged-particle spectroscopy to populate
47 states in ^{13}N via ^{13}O and observe the decays to a final
48 state of $3\alpha p$. The β -delayed proton channel has previ-
49 ously been studied for ^{13}O [11] where limited statistics
50 showed only a very small sensitivity to populating the
51 $p+^{12}\text{C}(0_2^+)$ (Hoyle state) which results in a $3\alpha+p$ final
52 state. Utilizing the Texas Active Target (TexAT) Time
53 Projection Chamber to perform one-at-a-time β -delayed
54 charged-particle spectroscopy, α -decays from the near α -
55 threshold excited states in ^{13}N have been observed for
56 the first time, providing insights into the $\alpha+^9\text{B}$ clus-
57 tering. Capitalizing on the advantages of TPCs for β -
58 delayed charged-particle emission studies, unambiguous
59 and background-free identifications of the $\beta 3\alpha p$ events
60 were made. Reconstruction of complete kinematics for
61 these exotic decays allowed for robust decay channel as-
62 signments, providing insights into the cluster structure of
63 the ^{13}N excited states. Evidence for the $\frac{1}{2}^+$ first excited
64 state in ^9B , mirror of the well-known $\frac{1}{2}^+$ in ^9Be , was an
65 unexpected byproduct of these measurements, demon-
66 strating the sensitivity of the technique.

EXPERIMENTAL SETUP

67

68 The β -delayed charged-particle spectroscopy technique
 69 with the TexAT TPC has previously been applied for β -
 70 delayed 3α decay studies of ^{12}N via $^{12}\text{C}^*$ [12]. A detailed
 71 description of the technique is provided in [13]. Here,
 72 we utilize the same experimental approach to observe
 73 the β -delayed 3α p decays of ^{13}O via $^{13}\text{N}^*$. We implant
 74 β -decaying ^{13}O ($t_{1/2} = 8.58$ ms) one-at-a-time into the
 75 TexAT TPC by providing a phase shift signal to the K500
 76 Cyclotron at Texas A&M University when a successful
 77 implantation has taken place to halt the primary beam.
 78 This phase shift then lasts for three half-lives or until the
 79 observation of a β -delayed charged particle in TexAT,
 80 with the DAQ ready to accept the trigger. The phase
 81 shift is then reset to allow for the next implantation. A
 82 beam of ^{13}O was produced via the $^3\text{He}(^{14}\text{N}, ^{13}\text{O})$ reaction
 83 at the MARS (Momentum Achromat Recoil Separator)
 84 [14] with a typical intensity of 5 pps with an energy of
 85 15.1 MeV/u, degraded by an aluminum foil to 2 MeV/u,
 86 to stop inside of the TexAT sensitive area, filled with
 87 50 Torr of CO_2 gas. To measure the correlated implan-
 88 tation/decay events, the 2p trigger mode of GET elec-
 89 tronics [15] was employed where the occurrence of two
 90 triggers within a 30 ms time window was required for a
 91 full event. The first trigger, the L1A (implantation), is
 92 generated if the Micromegas pad multiplicity exceeds 10.
 93 If, during the 30 ms following the L1A trigger, another
 94 trigger occurs with Micromegas pad multiplicity above
 95 two, the second L1B (decay) trigger event and the time
 96 between the L1A and L1B are recorded. For normaliza-
 97 tion and beam characterization, all events were recorded,
 98 even if L1B trigger never came.

99

ANALYSIS

100 The complete L1A (implant) + L1B (decay) events
 101 were selected with the time between the two triggers in
 102 the range of 1-30 ms. The short times (<1 ms) were
 103 omitted to remove double trigger events due to sudden
 104 beam-induced noise. To ensure the implanted ion is ^{13}O ,
 105 the energy deposited by the beam implant event in the
 106 Micromegas “Jr” (MM Jr) beam tracker [16] at the en-
 107 trance to the TexAT chamber was recorded. The beam
 108 contaminants were ^7Be and ^{10}C , dominated by ^7Be at \approx
 109 28% of the beam intensity.

110 Following an identification of ^{13}O implant, the stop-
 111 ping position was evaluated event-by-event using implant
 112 tracks, selecting only those which stopped inside the ac-
 113 tive area of the Micromegas and not closer than 31.5 mm
 114 from the edge. The spread of the ^{13}O stopping position
 115 inside TexAT was 67.5 mm due to straggling.

116 Further selection was performed by imposing tight cor-
 117 relation (<5 mm) between the ^{13}O stopping location and
 118 the vertex location of the respective decay event. Events

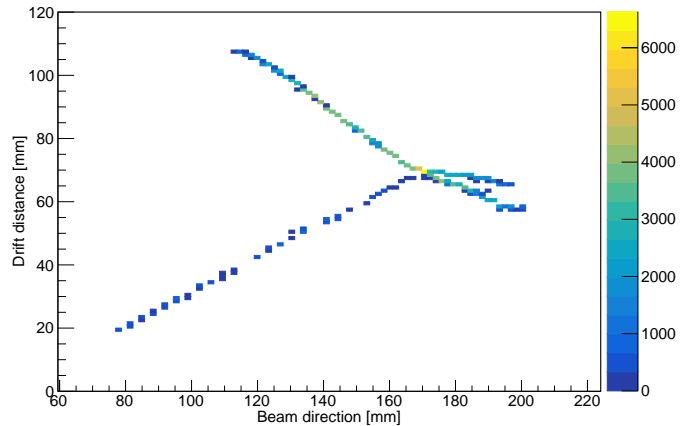


FIG. 1. Example $3\alpha+p$ event where the color (online) corre-
 sponds to the energy deposition within each voxel after pro-
 jection into 2D. The proton tracks extends from the vertex to
 the lower-left of the figure as evidenced by the lower energy de-
 position. Invariant mass reconstruction designated this event
 as decaying through the $^9\text{B}(\text{g.s.})+\alpha$ channel.

119 which passed this test were then fit with a single track
 120 segment using a randomly-sampled χ -squared minimiza-
 121 tion algorithm. If a good fit is achieved, these events
 122 were identified as single proton events. The β -delayed
 123 proton spectrum replicates the previous results [11] well,
 124 albeit with decreased resolution that will be covered in a
 125 subsequent publication with further experimental details.
 126 The remaining events were fit with four track segments
 127 as candidates for $\beta3\alpha$ p decay using randomly-sampled χ -
 128 squared minimization. They were then inspected visually
 129 to evaluate the fits' quality. Given the complexity of the
 130 fits, manual modifications of the fit algorithm parameters
 131 were required for some events.

$3\alpha+\text{PROTON}$ EVENTS

132 Overall, 149 $\beta3\alpha$ p events were identified, an example of
 133 which is shown in Fig. 1. Due to the size of the TPC and
 134 limitations on reconstruction in parts of the TexAT TPC,
 135 only 102 out of 149 of these events allow for complete
 136 reconstruction. The “incomplete” events are dominated
 137 by the $^9\text{B}(\text{g.s.})+\alpha$ decay as this produces a high-energy
 138 α -particle that may escape from the active volume of the
 139 TexAT TPC. The efficiency for the α_0 decay starts to
 140 deviate from 100% at $E_x = 10$ MeV, slowly drops to
 141 around 60% at $E_x = 14$ MeV (where α_i signifies $\alpha+^9\text{B}$
 142 decay with ^9B in the i^{th} excited state). The efficiency for
 143 α_1 and α_3 are less affected and only decrease to 70% at
 144 $E_x = 14$ MeV. In proton decays to the Hoyle state, most
 145 of the energy is taken by protons and the resulting three
 146 α -tracks of the pre-selected events are always confined to
 147 the active volume of the TPC. Proton tracks were not

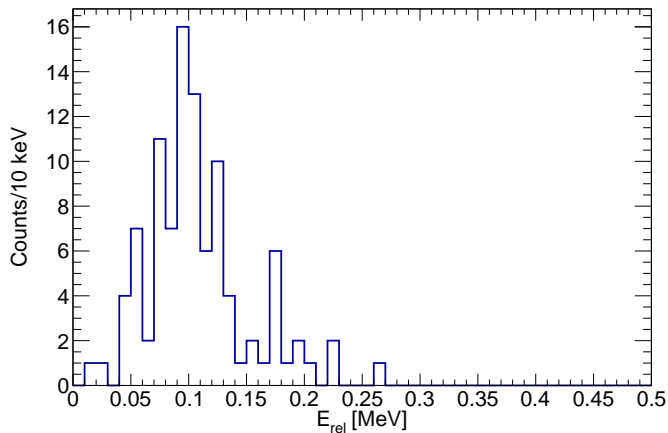


FIG. 2. Relative energy spectrum for pairs of α -particles with the smallest relative energy of the three α -tracks. The ${}^8\text{Be}(\text{g.s.})$ at 92 keV is well-reproduced.

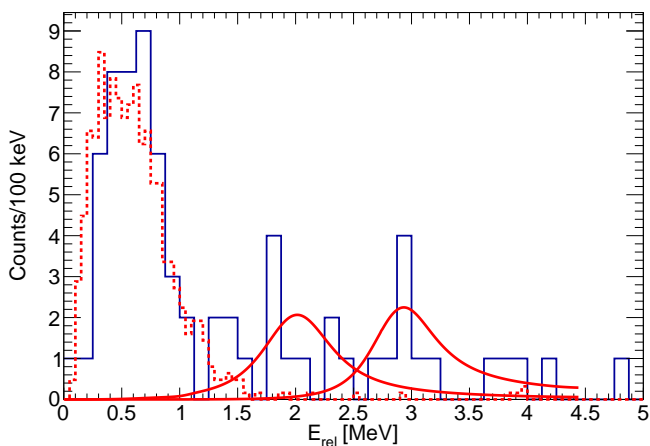


FIG. 3. For events that do not decay via the Hoyle state, the relative energy spectrum is shown here which is generated by selecting the two α -particles that produce the ${}^8\text{Be}(\text{g.s.})$ and then reconstructing the ${}^9\text{B}$ relative energy with the proton. Overlaid in dashed red are simulated data for the ground state contribution and in solid red are the $\frac{1}{2}^+$ and $\frac{5}{2}^+$ states from single channel R-Matrix calculations convoluted with a Gaussian with $\sigma = 0.23$ MeV. The $\frac{1}{2}^+$ parameters are those obtained by Wheldon [17] which show excellent agreement.

149 required in reconstruction as complete kinematics can be
150 recovered from the remaining three α -tracks. Therefore,
151 there was no efficiency reduction for the $p+{}^{12}\text{C}(\text{Hoyle})$
152 decays.

153 In order to identify the parent state in ${}^{13}\text{N}^*$, the low-
154 est energy deposition arm was identified as the proton
155 track and the momentum of the 3 α -particles was de-
156 termined by the length and direction of α -tracks in the
157 gas. Protons almost always escape the sensitive volume,
158 and the proton momentum is reconstructed from momen-
159 tum conservation. The decay energy is then the sum of

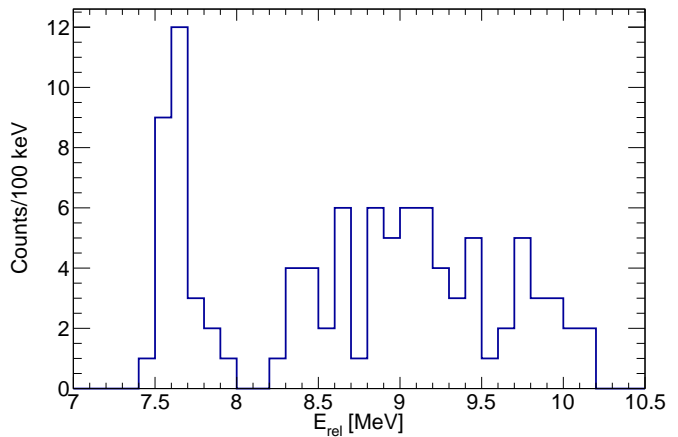


FIG. 4. Invariant mass spectrum from 3 α -particles assuming a ${}^{12}\text{C}$ origin. A peak at 7.65 MeV is seen, well reproducing the Hoyle state energy and a broad peak is seen at higher excitation energies which correspond to events that decay via ${}^9\text{B} + \alpha$. No peaks from higher excited states in ${}^{12}\text{C}$ can be seen.

160 the three α -particles' and proton energy. From here, the
161 ${}^8\text{Be}$ (Fig. 2), ${}^9\text{B}$ (Fig. 3) and ${}^{12}\text{C}$ (Fig. 4) excitation en-
162 ergies were determined from the invariant mass. This
163 allowed for a selection of events which proceeded to de-
164 cay via $p+{}^{12}\text{C}(0_2^+)$ [p_2], $\alpha+{}^9\text{B}(\text{g.s.})$ [α_0], $\alpha+{}^9\text{B}(\frac{1}{2}^+)$ [α_1]
165 and $\alpha+{}^9\text{B}(\frac{5}{2}^+)$ [α_3]. There is evidence of strength in ${}^9\text{B}$
166 between 1 and 2.4 MeV excitation energy (Fig. 3). It is
167 likely due to the $\frac{1}{2}^+$ state in ${}^9\text{B}$ [17] that is the mirror of
168 the well-known $\frac{1}{2}^+$ first excited state in ${}^9\text{Be}$. Attempts
169 to fit the spectrum without the $\frac{1}{2}^+$ in ${}^9\text{B}$ fail because it
170 is difficult to explain the excess of counts at excitation
171 energies between 1.4 and 2.4 MeV comparable to the 2.4
172 - 3.5 MeV region where there are known excited state in
173 ${}^9\text{B}$ states. Contributions from a broad $\frac{1}{2}^-$ state at 2.78
174 MeV may give a signature similar to that seen albeit at
175 lower energies (peaking at $E_{rel} = 1.3$ MeV for a ${}^{13}\text{N}(E_x)$
176 = 12.4 MeV) when considering the expected yield from a
177 $\frac{1}{2}^-$ state in ${}^{13}\text{N}$. The $L=0$ α -decay to the broad $\frac{1}{2}^-$ in ${}^9\text{B}$
178 will increase the yield at small excitation energies. While
179 this possibility is disfavored from the observed spectrum
180 due to the energy offset, it is mentioned here for com-
181 pleteness. The $\frac{1}{2}^+$ state in ${}^9\text{B}$ was selected by taking an
182 excitation energy of between 1.4 and 2.4 MeV in ${}^9\text{B}$ (fol-
183 lowing the centroid and width as observed via ${}^9\text{Be}({}^3\text{He}, t)$
184 [17] which is consistent with our current results) and the
185 $\frac{5}{2}^+$ was taken as having an excitation energy of above 2.4
186 MeV. Any contribution from the relatively-narrow 2.345
187 MeV $\frac{5}{2}^-$ (α_2) is not present in the presented plots as
188 this state decays almost exclusively via ${}^5\text{Li}$ and therefore
189 would not correspond to a peak in the ${}^8\text{Be}$ spectrum.
190 There were only 3 events associated with this decay to
191 ${}^5\text{Li}$ hence the statistics were insufficient to incorporate

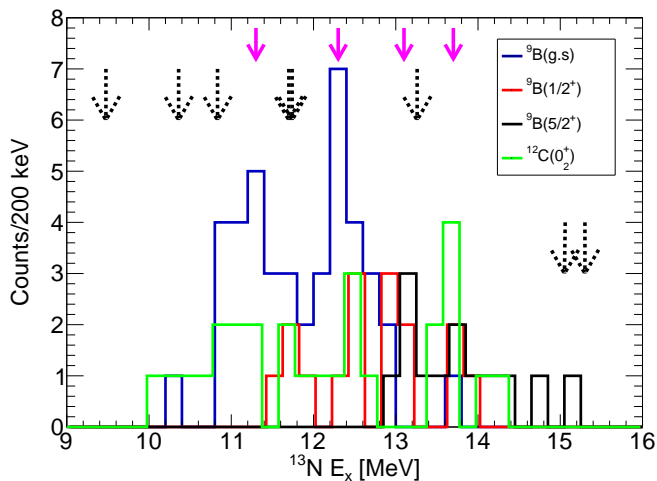


FIG. 5. Excitation spectrum in ^{13}N for $3\alpha + p$ separated by channels. Black dashed arrows show previously-known states populated by β -decay and new states observed are shown by solid magenta arrows.

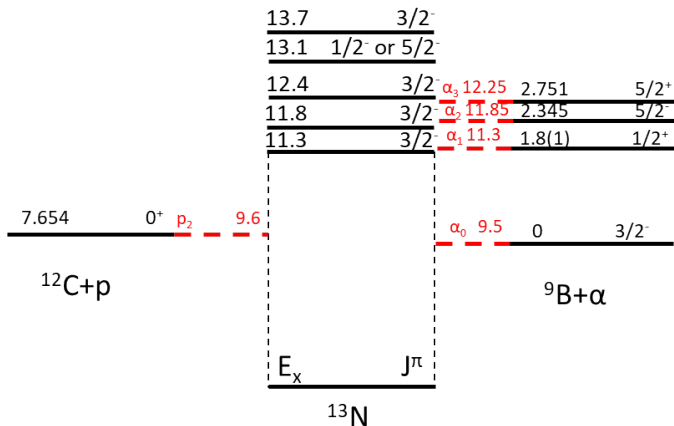


FIG. 6. Level scheme of measured $3\alpha+p$ states in ^{13}N in the central column with the proposed spin-parity assignments. The location of the thresholds for proton and α decay are shown in red with the equivalent excitation energy shown. The corresponding states in the daughter nuclei (^{12}C and ^9B) are also shown.

CONCLUSIONS

β -delayed $3\alpha p$ decay has been observed for the first time. While β -delayed αp has been previously observed in ^9C [18], ^{17}Ne [19], ^{21}Mg [20] and ^{23}Si [21], these states did not provide any structural insight and instead were mainly seen through isobaric analogue states that were well fed by β -decay. In this work, $\beta 3\alpha p$ decay was observed from the states below the isobaric analog in ^{13}N at $E_x = 15$ MeV, demonstrating this is not merely a phase-space effect. The β -delayed $3\alpha p$ decays observed here are in strong competition with β -delayed proton decay and therefore the states must have significant clustering. Evidence for the low-lying $\frac{1}{2}^+$ in ^9B in these background-free data, matching the parameters of previous observations [17], brings us closer to resolving the long-standing problem of searches for this elusive state. A paper will shortly be published that investigates the properties of the four new states observed here facilitated by this new technique and observed decay channel.

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into the analysis.

Following the channel selection, the excitation energy in ^{13}N was calculated and is shown in Fig. 5. Despite low statistics, a number of states can be seen at 11.3, 12.4, 13.1 and 13.7 MeV. The location of these states relative to the thresholds for $^9\text{B}+\alpha$ and $^{12}\text{C}(0_2^+)+p$ is shown in Fig. 6. The clear peak structures (particularly apparent for the $\alpha+^9\text{B}(\text{g.s.})$ channel) demonstrate the strength of this technique for studying cluster structures in ^{13}N . The nuclear structure implications of these states will be the topic of a follow-up paper that also includes more technical detail of the current work.

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