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## Collective excitations in chiral Stoner magnets

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We argue that spin and valley-polarized metallic phases recently observed in graphene bilayers and trilayers support chiral edge modes that allow spin waves to propagate ballistically along system boundaries without backscattering. The chiral edge behavior in a gapless nontopological phase originates from the interaction between the orbital magnetization in a spin-polarized Dirac Fermi sea and the geometric magnetic field in a Stoner metal. The edge modes are weakly confined to the edge, featuring dispersion which is robust and insensitive to the detailed profile of magnetization at the edge. This unique character of edge modes reduces their overlap with edge disorder and enhances the mode lifetime. The mode propagation direction reverses upon reversing valley polarization, an effect that provides a clear testable signature of exotic geometric interactions in Dirac bands.

Stoner ferromagnetism in topological bands is a correlated electron phase prominent in 2D materials of current interest, including moiré graphene $[1-6]$  $[1-6]$ , and nontwisted graphene bilayers and trilayers [\[7–](#page-5-2)[11\]](#page-5-3). Yet, the fundamental properties of this state, especially those governed by the Berry curvature in  $k$  space, are presently poorly understood. Here we predict that this state hosts chiral spin excitations. These excitations are confined to system edge and propagate along it in a manner resembling Quantum Hall (QH) edge states, as illustrated in Fig[.1.](#page-1-0) The microscopic origin of this behavior is the geometric phase of carrier spins tracking magnetization along carrier trajectories. Carrier spin rotation by a positiondependent magnetization generates Berry phase in direct space that serves as a spin-dependent magnetic vector potential that couples to the orbital dynamics of carriers (see Eqs. $(4)$ , $(5)$ ) [\[12–](#page-5-4)[15\]](#page-5-5). Chiral edge behavior arises due to coupling between this geometric magnetic field and the orbital magnetization due to Berry curvature in k space. The geometric character of this interaction ensures robust chiral edge physics even in "vanilla" spin-polarized Fermi seas such as those seen in Refs.[\[7](#page-5-2)[–11\]](#page-5-3).

Needless to say, band magnetism of carriers with orbital magnetization is a broad framework relevant for a variety of different systems. This includes, in particular, the QH ferromagnets [\[16](#page-5-6)[–19\]](#page-5-7) and correlated excitonic phases in QH bilayers [\[20](#page-5-8)[–24\]](#page-5-9). Orbital magnetization in these systems is due to Landau levels rather than the kspace Berry curvature and in QH bilayers the layer index takes on the role of spin. While edge magnetoplasmons in QH systems have been widely investigated, the geometric interaction and associated chiral spin waves, to the best of our knowledge, have been overlooked in the literature [\[25–](#page-5-10)[28\]](#page-5-11). Here we focus on chiral edges in spin-polarized metals and, afterwards, comment on the QH systems.

In graphene multilayers [\[7–](#page-5-2)[11\]](#page-5-3), the predicted chiral edge behavior is sensitive to valley polarization. Since the band orbital magnetization is of opposite signs in valleys  $K$  and  $K'$ , in a valley-and-spin-polarized phase, identified as a quarter metal in Refs.[\[7](#page-5-2)[–11\]](#page-5-3), the edge mode chirality (propagation direction) reverses sign upon valley imbalance reversal. A very different behavior is expected in a



<span id="page-1-0"></span>FIG. 1. a) Schematic band structure of a fully spin-polarized Stoner phase in a valley-polarized graphene bilayer or trilayer band. Only the valley populated by carriers is shown. b) The spin-wave edge mode dispersion (red) positioned outside the bulk magnon continuum (blue). The group velocity  $v_q = d\omega/dq$  of a constant sign indicates the chiral character of the mode. The edge-to-bulk scattering (black arrow) is blocked by the energy and momentum conservation. c) Spatial dependence at the edge. The chiral mode is confined to the edge and propagates along it without backscattering.

valley-unpolarized but spin-polarized phase (half-metal in the nomenclature of Refs.[\[7–](#page-5-2)[11\]](#page-5-3)). In this case, the two valleys host Stoner metals with the band orbital magnetization of opposite signs. In this phase, the edges will host pairs of counter-propagating chiral edge modes, one for each valley. These two modes together respect the orbital time reversal symmetry, unbroken in the half-metal phase, i.e. the system is non-chiral.

The exceptional cleanness of graphene multilayers makes them an appealing system to probe this behavior. Spin lifetimes as long as 6 ns measurered in large bilayer graphene (BLG) systems by a nonlocal Hanle effect at 20 K [\[29\]](#page-5-12) are explained by residual magnetic disorder [\[30,](#page-5-13) [31\]](#page-5-14). In contrast, recently it was demonstrated that electrons isolated from edge disorder by gate confinement and trapped in gate-defined quantum dots acquire ultralong spin lifetimes, reaching values of 200  $\mu$ s [\[32\]](#page-5-15) and 50 ms [\[33\]](#page-5-16) measured in an applied magnetic field by pulsedgate spectroscopy. Therefore, probing spin excitations in gate-defined electron puddles presents a distinct advantage. Yet, spin lifetimes measured in large BLG systems [\[29\]](#page-5-12) also lie in a suitable range. Spin lifetimes can be further increased by applying nonquantizing magnetic fields that, apart from a constant offset, have little impact on the chiral spin-wave dispersion (see Eq.[\(18\)](#page-4-0)).

In a metallic state the chiral mode at the edge can, in principle, decay by scattering into the 2D spin-one particle-hole continuum and spin waves. The former process is blocked by energy conservation since the spin-one continuum is gapped at small momenta [see [\[34\]](#page-5-17) Fig. ?? a)]. The latter process, shown by the black arrow in Fig[.1](#page-1-0) b), is blocked by the energy and momentum conservation for a smooth edge but can be viable for a rough edge. However, as discussed in [\[34\]](#page-5-17), in the longwavelength limit the edge modes have vanishing overlaps with the edge disorder potential, a property that protects the modes from the edge-to-bulk scattering.

The chiral edge behavior in a Stoner metal phase discussed here is distinct from that predicted for magnetic phases with a nontrivial magnon band topology [\[35–](#page-6-0)[41\]](#page-6-1). In these systems, chiral edge excitations lie above the first magnon band and are therefore gapped. To the contrary, the chiral modes described here arise at the boundary of a uniformly spin-polarized Stoner Fermi sea—a metallic compressible state with a nontopological bulk magnon band. The edge excitations are gapless (in the absence of an externally applied magnetic field, see below) and have dispersion positioned beneath that of bulk spin waves (in our case these are nothing but the gapless magnons of a Heisenberg ferromagnet). Accordingly, here chiral modes arise in the absence of microscopic spindependent interactions such as Dzyaloshinskii-Moriya interaction (DMI) or dipolar interaction (as in Refs.[\[35](#page-6-0)[–39\]](#page-6-2) and Refs.[\[40,](#page-6-3) [41\]](#page-6-1), respectively). Instead, they originate from an interplay between the exchange interaction and orbital magnetization in bands with Berry curvature and broken time reversal symmetry. Our spin waves display an analogy to the chiral edge plasmons predicted for such bands [\[42\]](#page-6-4), yet they transport spin rather than charge and arise from a very different mechanism.

Collective spin dynamics, both bulk and edge, are conveniently analyzed in the long-wavelength limit, at frequencies below the Stoner continuum [see [\[34\]](#page-5-17) Fig. ?? a)]:

<span id="page-2-4"></span>
$$
\Delta = U n_s > \omega(q),\tag{1}
$$

where  $\Delta$  is the Stoner gap, U is the exchange interaction,  $n_s$  is spin-polarized carrier density and  $\omega(q)$  is mode dispersion. We employ an effective action for spin variables obtained by integrating out fermion orbital degrees of freedom. In that, we assume the electron velocity is large compared to that of spin-waves,  $v_F \gg v_g = d\omega/dk$ . As found below, the long-wavelength spin-wave dispersion is

quadratic,  $\omega(k) \sim k^2$ , a behavior that confirms the separation of time scales for the orbital and spin degrees of freedom and justifies our analysis. The effective action for spin variables takes the form [see e.g. [\[43,](#page-6-5) [44\]](#page-6-6)]

<span id="page-2-2"></span>
$$
A = \int dt d^2 r \left( i n_s S_0 \langle \eta(\mathbf{r}, t) | \partial_t | \eta(\mathbf{r}, t) \rangle - \mathcal{H}[\mathbf{n}] \right), \quad (2)
$$

where the first term is the Wess-Zumino-Witten action, hereafter referred to as  $A_{\text{WZW}}$ , representing the singlespin Berry phase accumulated through time evolution. The second term is the Hamiltonian of a spin-polarized state discussed below. The quantity  $|\eta(\mathbf{r},t)\rangle$  represents a coherent spin state in  $(2+1)D$  space-time. Here  $n_s =$  $n_{\uparrow} - n_{\downarrow}$  is the density of spin-imbalanced carriers, the factor  $n_sS_0$  is the spin density, where  $S_0 = \hbar/2$ . In what follows spin polarization is described by a unit vector

$$
\boldsymbol{n}(\boldsymbol{r},t) = \langle \eta(\boldsymbol{r},t)|\boldsymbol{\sigma}|\eta(\boldsymbol{r},t)\rangle.
$$

The term  $\mathcal{H}[n]$  in Eq.[\(2\)](#page-2-2) is the effective spin Hamiltonian. Symmetry arguments and microscopic analysis predict [\[45\]](#page-6-7) the long-wavelength Hamiltonian

<span id="page-2-3"></span>
$$
\mathcal{H}[\boldsymbol{n}] = n_s \left[ \frac{J}{2} (\partial_{\mu} \boldsymbol{n})^2 - M(r) B(\boldsymbol{r}, t) - \boldsymbol{h}_0 \cdot \boldsymbol{n} \right]. \tag{3}
$$

Here  $J$  is spin stiffness, the second term is an interaction between the band orbital magnetization and the geometric magnetic field, the last term is the Zeeman energy per carrier, with the g-factor and Bohr magneton absorbed in the external magnetic field  $h_0$ .

As indicated above, the interaction  $-MB$  originates from the geometric Berry phase, arising due to electron spins tracking magnetization along electron trajectories. Spin rotation generates Berry phase in position space defined by a spin-dependent magnetic vector potential [\[12\]](#page-5-4)

<span id="page-2-0"></span>
$$
a_{\mu} = \frac{\hbar}{2e} \left( 1 - \cos \theta \right) \partial_{\mu} \phi, \quad \mu = x, y. \tag{4}
$$

Here  $\theta$  and  $\phi$  are the spherical polar and azimuthal angles measured with respect to the spin polarization axis in the ground state. The sign of  $a_{\mu}$  is chosen to describe the Berry phase accrued by the majority-spin carriers. For the minority-spin carriers the Berry phase is described by  $-a_{\mu}$ . The geometric magnetic field is simply the curl of  $a_{\mu}$ . In terms of **n**, it reads:

<span id="page-2-1"></span>
$$
B(\mathbf{r},t)=\nabla\times\mathbf{a}=\frac{\phi_0}{4\pi}\mathbf{n}\cdot(\partial_x\mathbf{n}\times\partial_y\mathbf{n}),\qquad(5)
$$

where  $\phi_0 = h/e$  is the flux quantum. This physics was first discussed in the early literature on high  $T_c$ superconductivity[\[46](#page-6-8)[–49\]](#page-6-9) and later in the literature on noncollinear magnetic systems [\[12–](#page-5-4)[15\]](#page-5-5). Importantly, unlike static spin textures in the latter systems, our spinwave dynamics generate a time-dependent vector potential, Eq.[\(4\)](#page-2-0). This leads to a geometric electric field

[\[14,](#page-5-18) [50\]](#page-6-10)

<span id="page-3-2"></span>
$$
E_{\mu} = -\partial a_{\mu}/\partial t - \nabla a_0 = \frac{\hbar}{2e} \mathbf{n} \cdot (\partial_t \mathbf{n} \times \partial_{\mu} \mathbf{n}), \quad (6)
$$

which can enable electrical detection the spin waves.

The quantity  $M(r)$  in the second term in Eq.[\(3\)](#page-2-3) describes the orbital magnetization per carrier in a spinimbalanced band arising due to Berry curvature in k space. It is given by a sum of contributions of the filled states in the spin-valley-polarized Fermi sea. For a partially spin-polarized Fermi sea the contributions to M of the majority-spin and minority-spin carriers are of opposite signs, giving  $M = M_{\uparrow} - M_{\downarrow}$ , accounting for the opposite signs of  $a_{\mu}$  for the spin-up and spin-down carriers discussed beneath Eq.[\(4\)](#page-2-0). These opposite sign contributions cancel in a spin-unpolarized state but lead to  $M \neq 0$  in a fully or partially spin-polarized state. The position dependence  $M(r)$  reflects spatially varying spin or valley imbalance arising, e.g., due to gating.

The geometric fields  $a_{\mu}$ , B and  $E_{\mu}$  are derived in the adiabatic regime when an electron spin tracks spin texture along the electron trajectory. The adiabatic regime occurs when the spin texture is sufficiently longwavelength such that the Stoner spin gap  $\Delta = U n_s$  is much greater than  $\hbar v_F q$ , where q is the characteristic spin-wave wavenumber and  $U$  is the exchange interaction (see Eq. $(1)$ ).

The Hamiltonian, Eq.[\(3\)](#page-2-3), features different phases de-pending on the M and J values [\[45\]](#page-6-7). If  $M > 2J$  and  $h_0$  is small enough, the uniformly polarized state is predicted to become unstable towards twisting, giving rise to a skyrmion texture with a nonzero chiral density B. Here we consider excitations in a uniformly polarized state

<span id="page-3-0"></span>
$$
\boldsymbol{n}(r,t)=\boldsymbol{n}_0+\delta\boldsymbol{n}(r,t),\quad\delta\boldsymbol{n}\perp\boldsymbol{n}_0,\qquad\qquad(7)
$$

with  $n_0 \parallel h_0$ , occurring for not too large M values.

The spin wave dispersion can be obtained from the canonical equations of motion found from the saddlepoint condition  $\delta A/\delta n = 0$ , with A given in Eq.[\(2\)](#page-2-2). Indeed, the variation of the Wess-Zumino-Witten term  $A_{\text{WZW}}$  [the first term in Eq.[\(2\)](#page-2-2)] can be found by noting that this term equals to  $n_sS_0$  times the solid angle swept by  $n$ . As a result, its variation can be expressed as

$$
\delta A_{\rm WZW} = n_s S_0 \int dt d^2 r (\delta \mathbf{n} \times \partial_t \mathbf{n}) \cdot \mathbf{n}, \qquad (8)
$$

The variation of the action in Eq.[\(2\)](#page-2-2) gives  $\delta A$  =  $(n_sS_0\partial_t\mathbf{n}\times\mathbf{n}-\delta\mathcal{H}/\delta\mathbf{n})\cdot\delta\mathbf{n}$ , giving equations of motion:

$$
n_s S_0 \partial_t \mathbf{n}(r) = \mathbf{h}(r) \times \mathbf{n}(r), \quad \mathbf{h} = -\frac{\partial \mathcal{H}}{\partial \mathbf{n}} + \partial_\mu \frac{\partial \mathcal{H}}{\partial \partial_\mu \mathbf{n}}. \tag{9}
$$

Linearizing about a uniformly polarized state yields coupled linear equations for  $\delta n$  components, which are identical to those found for a nonchiral problem,

$$
S_0 \partial_t \delta \boldsymbol{n}(r,t) = \boldsymbol{h}_0 \times \delta \boldsymbol{n}(r,t) + J \partial_\mu^2 \delta \boldsymbol{n}(r,t) \times \boldsymbol{n}_0. \quad (10)
$$

Plane wave solutions to this equation yield a simple isotropic and non-chiral spin-wave dispersion

<span id="page-3-1"></span>
$$
\omega_{\pm}(q) = \pm (h_0 + Jq^2)/S_0, \tag{11}
$$

with values approaching  $\pm h_0/S_0$  in the limit  $q \to 0$ , universal and independent of the exchange interaction as required by the Larmor theorem.

For a spatially uniform M, the  $-MB$  term is a topological invariant. Therefore, a local twist of spin does not change the  $H$  value. As a result, this interaction neither affects the energy nor impacts the spin waves. A spatially varying  $M$ , to the contrary, has a profound effect on spin waves. In particular, system boundaries and interfaces between regions in which  $M$  takes different values support chiral spin-wave modes reminiscent of the QH edge states. To illustrate this behavior we consider a step

$$
M(y) = \begin{cases} M_1, & y > 0 \\ M_2, & y < 0. \end{cases}
$$
 (12)

In this case, after linearization, Eq.[\(7\)](#page-3-0), we find

$$
\boldsymbol{h} = n_s \left[ J \partial_\mu^2 \delta \boldsymbol{n} - \partial_y M(y) (\boldsymbol{n}_0 \times \partial_x \delta \boldsymbol{n}) + \boldsymbol{h}_0 \right]. \tag{13}
$$

Other terms vanish at first order in  $\delta n$ . As a result, the linearized equations of motion become

$$
S_0 \partial_t \delta n = \mathbf{h}_0 \times \delta \mathbf{n} + J \partial_\mu^2 \delta \mathbf{n} \times \mathbf{n}_0 + m \delta(y) (\mathbf{n}_0 \times \partial_x \delta \mathbf{n}) \times \mathbf{n}_0,
$$

where  $m = M_2 - M_1$  is the difference between M on two sides of the edge. These equations are solved by writing  $\delta n(x, y)$  as a superposition of left-handed and right-handed helical components:

$$
\delta \boldsymbol{n}(r,t) = \begin{pmatrix} \delta n_x(r,t) \\ \delta n_y(r,t) \end{pmatrix} = e^{iqx} \left[ e^{-i\omega_+ t} \psi_+(y) \begin{pmatrix} 1 \\ i \end{pmatrix} + e^{-i\omega_- t} \psi_-(y) \begin{pmatrix} 1 \\ -i \end{pmatrix} \right]
$$
(14)

where we carried out the Fourier transform in time and the translation-invariant  $x$  direction. Plugging this ansatz into the equations of motion for  $\delta n(r, t)$ , we obtain two decoupled 1D problems for a quantum particle in a delta-function potential:

$$
S_0 \omega_{\pm} \psi_{\pm}(y) = \pm \left[ h_0 + J(q^2 - \partial_y^2) \right] \psi_{\pm}(y) - m q \delta(y) \psi_{\pm}(y).
$$
\n(15)

These equations support bound states which are edge spin waves for the helical polarization of a plus (minus) sign for mq of a positive (negative) sign, respectively.

Indeed, the bound state is described by an exponential solution for both helicities:

$$
\psi_{\pm}(y) = e^{-\lambda_q|y|}, \quad \lambda_q > 0,
$$
\n(16)

where the condition  $\lambda_q > 0$  is required for the mode to be normalizable. The value of  $\lambda_q$  and the dispersion are determined by the condition

$$
0 = \pm 2J\lambda_q \delta(y) - mq\delta(y),\tag{17}
$$

which gives  $\lambda_q = \pm \frac{mq}{2J}$ . Therefore, the right-helicity mode  $\psi_+$  exists only for  $mq > 0$ , whereas the left-helicity mode  $\psi$ <sub>-</sub> exists only for  $mq < 0$ .

<span id="page-4-0"></span>
$$
\omega_{\pm}(q) = \pm \frac{1}{S_0} \left[ h_0 + \left( J - \frac{m^2}{4J} \right) q^2 \right] \tag{18}
$$

The resulting dispersion is illustrated in Fig[.1](#page-1-0) b) for  $m >$ 0. The group velocity  $v_q = d\omega/dq$  is of the same sign for both helicities, as expected for a chiral edge mode.

Notably, the discrete chiral mode, Eq.[\(18\)](#page-4-0), appears in a robust manner regardless of magnetization values in the two halfplanes and the step size  $m = M_1 - M_2$ . At  $M_1$  approaching  $M_2$  the chiral mode, while remaining discrete, approaches the bulk magnon continuum and merges with it at  $M_1 = M_2$ . Another interesting aspect of the dispersion in Eq.[\(18\)](#page-4-0) is that the group velocity reverses when  $m$  exceeds 2J, upon which the mode propagation direction is reversed, with the left-moving excitations becoming right-moving and vice versa. In this regime the frequencies  $\omega_{\pm}(q)$  reverse their signs when the wavenumber reaches a certain critical value,  $q = q_* = \sqrt{4Jh_0/(4J^2 - m^2)}$ . Frequency sign reversal signals an instability towards a spatial modulation at the edge with spatial periodicity  $2\pi/q_*$ . Importantly, this instability can occur before skyrmions are nucleated in the bulk. This happens, in particular, when  $M_1$  and  $M_2$  are of opposite signs. In this case, the condition for skyrmion nucleation in the bulk,  $2J < |M_{1,2}|$ , is more stringent than that for the instability at the edge,  $2J < |M_1 - M_2|$ .

Next we consider polarization of chiral modes. As we found above, the modes of both helicities,  $\psi_+$  and  $\psi_-,$ propagate in the same direction. This gives rise to an interesting space-time picture that combines propagation with velocity  $v<sub>g</sub>$  and precession about  $h<sub>0</sub>$ . Indeed, a narrow wavepacket centered at  $q \approx q_0$  evolves as

$$
\delta \boldsymbol{n}(r,t) = \sum_{q>0} \phi_q^+(r,t) \begin{pmatrix} 1 \\ i \end{pmatrix} + \sum_{q<0} \phi_q^-(r,t) \begin{pmatrix} 1 \\ -i \end{pmatrix}
$$
 (19)  
 
$$
\sim e^{-\lambda_{q_0}|y|} \begin{pmatrix} \cos[\omega_0(t-x/v_g) + \theta_0] \\ \sin[\omega_0(t-x/v_g) + \theta_0] \end{pmatrix}.
$$

Here  $\phi_q^{\pm}(r,t) = e^{-i\omega_{\pm}(q)t + iqx - \lambda_q|y|} \psi_{q,\pm}, \ \omega_0 = \omega_+(q_0).$ This describes spin precession and propagation at the edge illustrated in Fig. [1](#page-1-0) c).

Lastly, we discuss the relation between the analysis above and the collective spin excitations in QH ferromagnets. The seminal prediction of skyrmions in QH ferromagnets by Sondhi et al.[\[51\]](#page-6-11) relies on the notion of an excess charge induced on a chiral spin texture,  $\delta \rho(r) = \sigma_{xy} B(r)$ , a value that follows from the topo-logical pumping argument [\[52,](#page-6-12) [53\]](#page-6-13) with  $\sigma_{xy}$  the Hall conductivity of a filled Landau level an  $B$  the quantity in Eq.[\(5\)](#page-2-1). This gives a contribution to the energy

<span id="page-4-1"></span>
$$
\delta E = \int d^2 r V_g \delta \rho(r),\tag{20}
$$

where  $V_g$  is the gate voltage. Since  $B(r) = \frac{\phi_0}{4\pi} n \cdot \partial_1 n \times$  $\partial_2$ n, the quantity in Eq.[\(20\)](#page-4-1) is identical in form to our  $-MB$  interaction (the second term in Eq.[\(3\)](#page-2-3)). Furthermore, it is straightforward to link the prefactor with the orbital magnetization of a fully filled Landau level

$$
M = eV_g \sigma_{xy}.
$$
 (21)

This relation follows from the thermodynamic relation  $dM/d\mu = dn/dB_{\text{ext}}$  and the Streda formula  $dn/dB_{\text{ext}} =$  $\frac{\sigma_{xy}}{e}$ . Having reproduced the  $-MB$  interaction we are led to conclude that the chiral spin waves derived above must also occur in QH ferromagnets. Yet, the existing theoretical approaches, such as those developed in Refs[.26](#page-5-19) and [27,](#page-5-20) do not include this interaction and, as a result, miss the chiral edge spin waves.

Lastly, we point out that extending the pulsed gate spectroscopy of Refs. [\[32,](#page-5-15) [33\]](#page-5-16) to probe the gate-confined electron puddles can allow to launch the chiral spin waves and detect them in a manner analogous to the timedomain detection of QH edge magnetoplasmons [\[54–](#page-6-14)[57\]](#page-6-15). Further, performing electron-spin resonance (ESR) measurements on such puddles by the technique recently used to probe ESR in graphene[\[58\]](#page-6-16) can provide direct information of the chiral mode dispersion. Indeed, for a puddle of circumference  $L$  the mode dispersion in Eq.[\(18\)](#page-4-0), will translate into sidebands of the ESR resonance with frequencies

$$
\omega_n = \omega(q_n), \quad q_n = 2\pi n/L, \tag{22}
$$

with integer *n*. Here  $n = 0$  is the fundamental ESR frequency and  $n = 1, 2, 3...$  describes a family of chiral mode excitations. The  $\omega = \omega_n$  resonances will occur over a continuous background due to the 2D spin-wave continuum, Eq.  $(11)$ . As an example, we consider a disk of circumference  $L = 10 \,\mu\text{m}$  for which the minimal wavenumber is  $q_1 = 2\pi/L$ . Estimating the stiffness as the e-e interaction at the Fermi wavelength scale,  $J \sim e^2/(\kappa \lambda_F)$ , for realistic parameter values we find the sideband frequency detuning of  $\omega_1 - \omega_0 \approx 50$  MHz. This value is greater than  $1/T_1$  found in Refs.[\[32,](#page-5-15) [33\]](#page-5-16) and lies in a convenient range for microwave measurements. We also note that, as discussed above, spin dynamics in our system is accompanied by a geometric electric field given in Eq.[\(6\)](#page-3-2). This field generates an oscillating electric dipole signal which can be used for a direct electrical detection of the chiral spin-wave dynamics.

Summing up, we predict a new type of chiral edge excitations arising in a metallic spin-polarized Fermi sea with a Berry band curvature. Despite occurring in a nontopological setting this mode is protected from backscattering by its chiral character. Correlated-electron phases that host chiral edge modes allowing excitations to propagate along system boundaries in a one-way manner are of keen interest for fundamental physics and are expected to harbor interesting applications. We describe the requirements for such modes to exist and argue that the

chiral behavior and associated exotic physics are generic and readily accessible in state-of-the-art systems.

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