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1	Ultrafast Dynamics of Intrinsic Anomalous Hall Effect in the
2	Topological Antiferromagnet Mn3Sn
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20	Abstract (600 Character)
21	We investigate ultrafast dynamics of the anomalous Hall effect (AHE) in the
22	topological antiferromagnet Mn ₃ Sn with sub-100 fs time resolution. Optical pulse
23	excitations largely elevate the electron temperature up to 700 K, and terahertz probe
24	pulses clearly resolves ultrafast suppression of the AHE before demagnetization.
25	The result is well reproduced by microscopic calculation of the intrinsic Berry-
26	curvature mechanism while the extrinsic contribution is clearly excluded. Our work
27	opens a new avenue for the study of nonequilibrium AHE to identify the microscopic
28	origin by drastic control of the electron temperature by light.

30 Main Text

The anomalous Hall effect (AHE), a deflection of current flow perpendicularly to the bias electric field as a consequence of the broken time-reversal (\mathcal{T}) symmetry in magnets, has been one of the central issues in modern condensed matter physics because of its topological nature [1]. The intrinsic anomalous Hall conductivity σ_{xy}^{int} in the DC limit is independent of scattering and solely determined by the band structure [2], as represented by

$$\sigma_{xy}^{\text{int}} = \frac{e^2}{\hbar} \sum_{n} \int \frac{\mathrm{d}\boldsymbol{k}}{(2\pi)^3} f(\epsilon_n(\boldsymbol{k})) B_{n,z}(\boldsymbol{k}), \qquad (1)$$

where *n* is a band index, $f(\epsilon_n(\mathbf{k}))$ is an electron distribution function, and $B_{n,z}(\mathbf{k})$ is 37 38 the Berry curvature in the momentum space. By contrast, the extrinsic AHE originating 39 from the skew scattering [3] or side-jump mechanism [4] is induced by impurity 40 scattering. To study the AHE, several approaches have been implemented to modulate a 41 parameter for the anomalous transport. Because of the distinct dependences on scattering for the intrinsic and extrinsic mechanisms, the universal scaling law between the Hall and 42 longitudinal conductivities can be used to discern the microscopic origins [5]. However, 43 44 certain materials can deviate from the scaling [6]. Tuning the Fermi level by the gate voltage is also highly informative to investigate the AHE [7-9]. However, this method 45 requires the gate electrode and is restricted for two-dimensional systems. In addition, the 46 tuning range is limited especially for conducting materials. The element substitution can 47 largely control the Fermi level [10], but concomitantly alters the magnetic properties and 48 49 the scattering rate. As a non-contact method without using electrodes nor dopants, optical spectroscopy using Faraday or Kerr rotation has been utilized to discuss the origin of 50 AHE [11] because the experimental result can be compared to the intrinsic Hall 51 conductivity spectrum calculated from the band structure. To obtain the spectrum close 52 to the DC transport, terahertz time-domain spectroscopy (THz-TDS) with the Faraday 53 54 rotation is important because the response functions are obtained as complex quantities without the Kramers-Kronig transformation [12-21]. However, the comparison between 55 the experiment and the first-principle calculation is difficult at the low energy scale of 56 millielectronvolts. 57

As an alternative approach, we employ ultrafast pump-probe spectroscopy. Photoexcited electrons are rapidly scattered to form quasi-thermalized distribution with an elevated electron temperature of several hundred kelvins, while the lattice degree of freedom remains intact until the excess energy is transferred via the electron-phonon interaction. By using the electron temperature as a largely controllable parameter, the transient AHE away from equilibrium can be probed by another short THz pulse. Although the static THz Faraday rotation spectroscopy has been performed in many magnets [12-21], to the best of our knowledge, ultrafast time-resolved spectroscopy has been reported only in a ferrimagnet [14], where sub-100 ps dynamics was discussed. The similar time resolution was also recently achieved in the electrical detection [22] and very recently used to study switching dynamics of Mn₃Sn [23]. However, ultrafast dynamics in the femtosecond regime has evaded experimental investigation thus far.

70 As a target material, we choose a topological antiferromagnet Mn_3Sn . Despite the absence of net magnetization, Mn₃Sn shows large AHE near room temperature 71 comparable with that in ferromagnets [24]. As shown in Fig. 1(a), the antiferromagnetic 72 phase is characterized by the cluster-octupole moment on the *a-b* plane which explicitly 73 breaks the \mathcal{T} symmetry [25], resulting in the topologically nontrivial band structure [26]. 74 75 The large AHE has opened a new avenue for novel antiferromagnetic spintronics [27,28]. 76 Ultrafast dynamics of AHE in Mn₃Sn is to be clarified for realization of high-speed readout spintronic information. Furthermore, Mn₃Sn thin films show a peculiar spin-77 reorientation phase transition as shown in Fig. 1(b). While the cluster-octupole phase 78 79 develops below $T_N \sim 430$ K, the Hall resistivity ρ_{xy} starts to decrease below 220 K due 80 to the transition into the helical phase [29] where the cluster-octupole moment rotates 81 along the c-axis with mitigating a degree of the broken \mathcal{T} symmetry. Consequently, the AHE near 150 K increases with increasing temperature, a trend that is opposite to that in 82 83 usual magnets. Therefore, photoinduced change of the AHE at the cluster-octupole and helical phases is highly intriguing to discuss what happens after photoinduced increase in 84 the electron temperature. 85

In this Letter, we report the first study of ultrafast time-resolved AHE in a Mn₃Sn thin film by using optical pump-THz Faraday rotation probe spectroscopy with a sub-100 fs time resolution, a few orders of magnitude faster than the earlier works. We observe a peculiar time trace of AHE, which clearly resolves that AHE is drastically suppressed by photoexcited electrons before demagnetization. The result agrees well with a microscopic view with the intrinsic mechanism, providing unprecedented insights into the nonequilibrium nature of AHE.

The sample is a polycrystalline Mn₃Sn thin film deposited on SiO₂ substrates by DC magnetron sputtering [30]. The film thickness of 20 nm is less than the penetration depth (22 nm) of the optical pump so that inhomogeneous excitation is avoided. The characterization of the sample is described in the Supplementary Material [31]. By using polarization-resolved THz-TDS [37], we evaluated the longitudinal and anomalous Hall conductivity spectra $\tilde{\sigma}_{xx}(\omega)$ and $\tilde{\sigma}_{xy}(\omega)$ at 280 K, as respectively shown in Figs. 1(d) and 1(e). $\tilde{\sigma}_{xx}(\omega)$ exhibits a typical Drude response with a scattering rate of ~10 fs [15,38]. Re $\tilde{\sigma}_{xy}(\omega)$ is flat and as large as 10 Ω^{-1} cm⁻¹ and Im $\tilde{\sigma}_{xy}(\omega)$ is negligibly small, showing that the THz AHE is also within the DC limit [15]. The circles on the left axes are the data obtained in the DC transport with values lower than the THz conductivity. This can be attributed to the effects of grain boundaries or surface roughness in the DC transport in such a very thin sample [39].

105 Figure 1(c) shows a schematic of the pump-probe setup. The THz pulse was linearly polarized along the x-direction before entering the sample and detected by the THz-TDS 106 with the transmission geometry. By changing the configuration of a wire-grid polarizer 107 (WGP2), the x- and y-components of the THz field after transmittance by the sample 108 can be obtained separately. By scanning the THz pulse delay time t_{probe} , the THz pulse 109 waveform was evaluated and converted to the frequency domain. The optical pump pulses 110 111 with 1.55-eV photon energy and 40-fs pulse duration irradiate the sample with a controllable pump delay t_{pump} . We performed the experiments under the magnetic field 112 of +2 and -2 T and obtained E_x and E_y of the THz field as even and odd components 113 114 for the magnetic field, respectively, and evaluated the longitudinal and Hall conductivity 115 spectra $\tilde{\sigma}_{xx}(\omega)$ and $\tilde{\sigma}_{xy}(\omega)$ [31].

First, we conducted the pump-probe experiment at 220 K at which the AHE is 116 maximized. Figure 2(a) shows E_x and E_y of the THz pulse waveform after 117 transmittance by the sample without the pump. To detect the ultrafast dynamics, we set 118 t_{probe} equal to the peak ($t_{\text{probe}} = t_0$ in Fig. 2(a)) and scan t_{pump} to detect the change 119 in E_y induced by the pump, δE_y . Figure 2(b) shows the results of δE_y as a function of 120 $t_{\rm pump}$ with pump fluences $I_{\rm p}$ =300 and 500 µJ cm⁻². Immediately after the pump, $E_{\rm p}$ 121 rapidly decreased, and subsequently relaxed within a few picoseconds. We fitted the data 122 and evaluated the rising times of δE_{ν} as 50 and 120 fs for $I_{\rm p}$ =300 and 500 µJ cm⁻², 123 124 respectively, which are comparable to the time resolution limited by the pulse duration of 40 fs. To obtain the spectral information, we set t_{pump} to 0.52 ps and scanned t_{probe} . 125 Figure 2(c) shows $\operatorname{Re}\tilde{\sigma}_{xy}(\omega)$ for different pump fluences. Averaging the data between 126 2.0 and 5.2 meV, we found that $\text{Re}\tilde{\sigma}_{xv}(\omega)$ decreases by 40% for $I_p=500 \text{ }\mu\text{J} \text{ cm}^{-2}$. 127 Moreover, we also investigated the change in E_x and compared $\operatorname{Re} \tilde{\sigma}_{xx}(\omega)$ with and 128 129 without the pump in Fig. 2(d). We found that the change in $\tilde{\sigma}_{xx}(\omega)$ is negligibly small. A fitting with the Drude model suggested that the change in the scattering time by the 130 131 pump is only 3% at most [31].

Previously photoexcited dynamics of magnets has been studied by using time-132 resolved magneto-optical Kerr effect (TR-MOKE) or magnetic circular dichroism, etc 133 [40]. The polarization rotation of light $\theta(\omega)$ by the Faraday or Kerr effect is 134 proportional to $\sigma_{xy}(\omega)$ as far as $\theta(\omega)$ is small. According to the Onsager's theorem, 135 $\sigma_{xy}(\omega)$ is expressed as $\sigma_{xy}(\omega) = \alpha(\omega) \times M$, where M is the magnetization and 136 137 $\alpha(\omega)$ is a coefficient determined by the electron and lattice systems. Since the discovery of ultrafast TR-MOKE signal within 100-300 fs in ferromagnets [41,42], many efforts 138 139 have been devoted to clarifying ultrafast demagnetization with possible spin-flip scattering mechanisms [43,44] and superdiffusive transport [45]. In this work we exclude 140 141 the superdiffusive transport because the sample is thinner than the pump penetration depth 142 and the probe size is as large as 6 mm so that the spin diffusion away from the probe spot is unlikely. In addition, it is to be noted that an ultrafast change of $\sigma_{xy}(\omega)$ does not 143 necessarily indicate a change in the magnetization because of the relation: 144

$$\Delta \sigma_{xv} = \Delta \alpha \times M + \alpha \times \Delta M. \tag{2}$$

Equation (2) means that even if the magnetization is unchanged ($\Delta M = 0$), the $\Delta \sigma_{xy}$ 145 146 signal can be observed when the electron system largely changes ($\Delta \alpha \neq 0$) in magnets $(M \neq 0)$. Because the electron system largely changes right after the photoexcitation, the 147 first term $\Delta \alpha \times M$ can be dominant in the ultrafast regime [46-49]. However, the 148 existence of the first term has been often neglected in many literatures. For thorough 149 understanding of ultrafast dynamics, the electron contribution must be distinguished from 150 151 the change of spins. Note that M is a parameter that breaks the \mathcal{T} symmetry and corresponds to the cluster-octupole moment in the case of Mn₃Sn. 152

To elucidate the nonequilibrium dynamics, we cooled the sample down to 150 K. 153 154 Figure 3(a) shows the temperature dependence of the THz Hall conductivity, showing that the AHE near 150 K increases with increasing temperature in the helical phase in Fig. 155 3(b). Therefore, if the photoexcitation at 150 K heats the spin system, photoinduced 156 "enhancement" of the cluster-octupole phase is expected to occur with an increase in σ_{xy} . 157 The result of the pump-probe experiment at 150 K with δE_y as a function of t_{pump} is 158 shown in Fig. 3(c). Interestingly, we observed that δE_{ν} first became *negative* with the 159 timescale of ~100 fs similarly to the result at 220 K. A few picoseconds later, the signal 160 in turn became *positive* by flipping its sign. By fixing t_{pump} to 0.52 and 12 ps and by 161 scanning t_{probe} , we obtained Re $\Delta \tilde{\sigma}_{xy}(\omega)$ in Figs. 3(d) and 3(e), respectively. The 162 results clearly showed that the AHE is first suppressed and subsequently enhanced. By 163 averaging the data between 2.0 and 5.2 meV at $t_{pump}=12$ ps, the AHE was increased by 164 ~6 Ω^{-1} cm⁻¹ for I_p =500 µJ cm⁻², corresponding to an increase in the temperature by ~40 165 K in thermal equilibrium. 166

We used the two-temperature model to evaluate photoinduced heating. Figure 4(a) 167 shows the simulation results at the original temperatures of 220 and 150 K and $I_p=500$ 168 μ J cm⁻² [31]. The optical pump excites electrons into higher energy bands, and these 169 electrons are expected to immediately form a quasi-thermalized distribution with an 170 171 electron temperature $T_{\rm e}$. The maximum $T_{\rm e}$ is as high as 700 and 630 K for the pump at 220 and 150 K, respectively. Subsequently, electron-phonon coupling elevates the lattice 172 temperature $T_{\rm L}$ such that the two systems are equilibrated within several picoseconds 173 with an increase in the temperature of ~40 K, which is in good agreement with the 174 increase in AHE observed in Fig. 3(e). Therefore, the positive sign of δE_{γ} around ~10 175 176 ps in Fig. 3(c) is attributed to pump-induced enhancement of the cluster-octupole phase 177 as a result of heating the sample from 150 K. In contrast, the ultrafast suppression of $\operatorname{Re}\tilde{\sigma}_{xy}(\omega)$ within 100 fs in Fig. 3(c) cannot be explained by the change in the spin 178 configuration. The same argument also holds at 220 K, at which the pump would heat the 179 sample at the timescale of ~10 ps and induce demagnetization. However, the temperature 180 181 increase by 40 K has a minor effect on the AHE at 220 K as shown in Fig. 3(a) and therefore the demagnetization at ~ 10 ps is not clearly identified in Fig. 2(b). Importantly, 182 the ultrafast reduction of $\operatorname{Re}\tilde{\sigma}_{xy}(\omega)$ within 100 fs is not explained by heating the sample 183 184 and therefore requires a more microscopic analysis.

185 Because the spin is a degree of freedom of electrons, an ultrafast change in the electron distribution itself may simultaneously alter the spin moment. To evaluate it, we 186 calculated the band structure of Mn₃Sn by using density functional theory (DFT), as 187 shown in Fig. 4(c). By considering finite electron temperatures, we calculated the local 188 spin moment which is proportional to the cluster-octupole moment [25], as shown in Fig. 189 190 4(b). Note that a previous angular-resolved photoemission spectroscopy in a comparison with the DFT calculation revealed that the band structure of Mn₃Sn in the vicinity of $E_{\rm F}$ 191 192 is renormalized by a factor of 5 owing to strong many-body correlation [26]. Therefore, $T_{\rm e}$ =700 K corresponds to $T_{\rm DFT}$ =3,500 K in the calculation. Figure 4(b) shows that the 193 increase from $T_e=220$ to 700 K ($T_{DFT}=1,100$ to 3,500 K) is accompanied by a decrease 194 195 in the local spin moment, although only by 6%. Such insensitivity of the local spin moment to $T_{\rm e}$ can be explained by the projected density of states for the cluster-octupole 196 moment as shown in the right panel of Fig. 4(c) [25], showing that the spin configuration 197 is determined mostly by the electrons of which the energy is a few eV below $E_{\rm F}$. 198 Therefore, the change in the electron distribution in the scale of T_{DFT} =3,500 K (~0.3 eV) 199 200 does not immediately alter the spin moment.

201 Based on the above arguments, we discuss the origin of the ultrafast reduction of the AHE within 100 fs, focusing on the well-defined cluster-octupole phase at 220 K because 202 calculating the band structure in the helical phase is difficult. We consider $T_{\rm e}$ to be 203 elevated to 700 K by the pump whereas the lattice and spin systems remain unperturbed 204 205 within 100 fs. This means that photoexcitation does not modify the band structure and 206 only broadens the electron distribution, which allows us to calculate the intrinsic AHE by using Eq. (1). The curves in Fig. 4(d) show the results of the calculated σ_{xy}^{int} normalized 207 at the value of 220 K as a function of $T_e = T_{DFT}/5$. The different colors correspond to 208 different chemical potentials. The composition of Mn in our sample indicates that the 209 210 chemical potential is close to zero. The markers in Fig. 4(d) show the experimental results of σ_{xy} at 220 K for $I_p=160$, 300, and 500 µJ cm⁻², corresponding to $T_e=430$, 560, and 211 700 K, respectively. The result shows that the photoinduced ultrafast decrease of AHE is 212 reasonably accounted for by the calculated intrinsic AHE with the elevated T_{e} . The 213 sensitiveness of the intrinsic AHE to the rise of T_e can be understood from Eq. (1). 214 Nominally all the electron states below $E_{\rm F}$ can contribute to the intrinsic AHE. However, 215 216 the Berry curvature are mainly located at around the (anti)crossing points in the band structure and the upper and lower branches of each (anti)crossing point have Berry 217 curvatures with opposite signs as schematically shown in Fig. 4(e). The contribution of 218 219 the states much below $E_{\rm F}$ is mostly cancelled by the integration in Eq. (1), and the (anti)crossing points near $E_{\rm F}$ is dominant. Therefore, the rise in $T_{\rm e}$ to several hundred 220 221 K can largely modify the intrinsic AHE and dominates the ultrafast dynamics.

In summary, we presented ultrafast time-resolved study of AHE in Mn₃Sn. Isolating 222 the electron temperature from the lattice and spin subsystems, we clearly resolve ultrafast 223 suppression of AHE due to the rise of electron temperature before the photoexcited 224 demagnetization occurs, which is well explained by the intrinsic Berry-curvature 225 226 mechanism. Importantly, photoexcitation in Mn₃Sn largely suppressed the AHE whereas the scattering rate was almost unchanged, which also excludes the extrinsic mechanism. 227 228 Because our time-resolved study can observe $\sigma_{xx}(\omega)$, $\sigma_{xy}(\omega)$, and the scattering rate 229 with drastically elevating the electron temperature, this method can be utilized to distinguish the microscopic origin of AHE and is in principle applicable to other 230 conventional ferromagnets or topological magnets. This work opens a new avenue for the 231 study of AHE from the viewpoint of nonequilibrium. 232

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248 Figure captions

Fig. 1 (a) Schematics of the atom configuration (up) and the spin texture (down) in Mn₃Sn. (b) Temperature dependence of the anomalous Hall resistivity ρ_{xy} in DC transport. (c) A schematic of the optical pump and polarization-resolved THz probe setup. WGP: wire-grid polarizer. (d),(e) THz longitudinal and anomalous Hall conductivity spectra, $\tilde{\sigma}_{xx}(\omega)$ and $\tilde{\sigma}_{xy}(\omega)$, respectively, at 280 K.

Fig. 2 (a) *x*- and *y*-components of the THz pulse waveforms after transmittance by the sample at 220 K. The vertical line defines $t_{\text{probe}} = t_0$ at the peak. (b) Pump-induced change of E_y at $t_{\text{probe}} = t_0$ as a function of t_{pump} . The data for different pump fluences are shown with offset. The solid curves show results of fitting. (c) $\text{Re}\tilde{\sigma}_{xy}(\omega)$ at $t_{\text{pump}}=0.52$ ps for different pump fluences. (d) $\text{Re}\tilde{\sigma}_{xx}(\omega)$ at $t_{\text{pump}}=0.52$ ps for the maximum pump fluence of 500 µJ cm⁻².

Fig. 3 (a) Temperature dependence of $\operatorname{Re}\tilde{\sigma}_{xy}(\omega)$ in THz Faraday rotation. The open circles (ZFC) and closed ones (FC) are the results in zero-field cooling and at ± 2 T. (b) Schematics of the spin configurations. (c) Pump-induced change of E_y at $t_{\text{probe}} = t_0$ as a function of t_{pump} at 150 K. The data for different pump fluences are shown with offset. The solid curves show results of fitting. (d)(e) The change of $\operatorname{Re}\tilde{\sigma}_{xy}(\omega)$ at $t_{\text{pump}}=0.52$ and 12 ps, respectively, at 150 K.

Fig. 4 (a) The electron and lattice temperatures (T_e and T_L) in the two-temperature model at the original temperatures of 220 and 150 K and I_p =500 µJ cm⁻². (b) (left) The band structure of Mn₃Sn at the cluster-octupole phase calculated by DFT. (right) The projected 269 density of states for the spin configuration of the cluster octupole. (c) The local spin 270 moment in the DFT calculation with finite temperatures. (d) The circles show $\text{Re}\tilde{\sigma}_{xy}(\omega)$ 271 observed in the pump-probe experiment at $t_{\text{pump}}=0.52$ ps at 220 K as a function of the 272 maximum T_{e} . The curves show the calculated σ_{xy}^{int} in Eq. (1) with various chemical 273 potentials as a function of T_{DFT} . (e) (left) A schematic of the Berry curvature around 274 anticrossing points. (right) Occupation of electrons with low (blue) and high (red) 275 temperatures.

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Figure 1

















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