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New Direct Limit on Neutrinoless Double Beta Decay Half-Life of math xmlns="http://www.w3.org/1998/Math/MathML" display="inline">mrow>mg/1998/Math/MathML" display="inline">mrow>mmultiscripts>mrow>mi>Te/mi>/ mrow>mprescripts>/mprescripts>none>/none>mrow>mn >128/mn>/mrow>/mmultiscripts>/mrow>/math> with CUORE D. Q. Adams et al. (CUORE Collaboration)

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¹ New direct limit on neutrinoless double beta decay half-life of ¹²⁸Te with CUORE

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	The Cryogenic Underground Observatory for Bare Events (CUORE) at Laboratori Nazionali del

The Cryogenic Underground Observatory for Rare Events (CUORE) at Laboratori Nazionali del Gran Sasso of INFN in Italy is an experiment searching for neutrinoless double beta $(0\nu\beta\beta)$ decay. Its main goal is to investigate this decay in ¹³⁰Te, but its ton-scale mass and low background make CUORE sensitive to other rare processes as well. In this work, we present our first results on the

search for $0\nu\beta\beta$ decay of ¹²⁸Te, the Te isotope with the second highest natural isotopic abundance. We find no evidence for this decay, and using a Bayesian analysis we set a lower limit on the 128 Te $0\nu\beta\beta$ decay half-life of $T_{1/2} > 3.6 \times 10^{24}$ yr (90% CI). This represents the most stringent limit on the half-life of this isotope, improving by over a factor 30 the previous direct search results, and exceeding those from geochemical experiments for the first time.

54 interaction in which a nucleus (A, Z) transforms into its 101 assessment of the parent/daughter nuclei ratio. 55 56 57 58 59 60 61 62 neutrinoless double beta $(0\nu\beta\beta)$ decay, has been hypoth- 109 for the first time – the indirect geochemical results. 63 esized but never observed. This process would consist of ¹¹⁰ Before reporting the details of our direct search for 64 65 67 68 69 71 73 74 would provide significant input for the explanation of the 121 decay half-lives from CUORE-0 [17] and CUORE [18]. 75 matter-antimatter asymmetry in the Universe via lepto- $_{\scriptscriptstyle 122}$ 76 77 78 proaches [3, 6]. 79

80 81 82 84 85 86 91 $T_{1/2}^{0\nu} > 1.1 \cdot 10^{23} \text{ yr}$, was set by MiDBD in 2003 [14]. ₁₄₂ TeO₂-based detectors [25]. ⁹⁷ More stringent limits than this have been set by indirect 143 We acquire data in day-long periods called runs, which

isobar (A, Z+2) by the simultaneous transmutation of $_{102}$ The geochemical studies are not sensitive to the $\beta\beta$ two neutrons into two protons. This Standard Model 103 decay mode but rather to the sum of all the possible process occurs with the emission of two electrons and 104 decays $(2\nu\beta\beta \text{ or } 0\nu\beta\beta$, to the ground or excited states), two electron antineutrinos in the final state $(2\nu\beta\beta$ decay), 105 although the dominant contribution is expected to be the such that lepton number (L) conservation holds; this pro- 106 two-neutrino mode. The direct search result reported in ess has been measured for 11 nuclei [1], with half-lives 107 this letter improves by more than 30-fold the previous in the range of 10^{18} - 10^{22} years. A second decay mode, 108 best direct search limit for this isotope and surpasses –

a nucleus $\beta\beta$ -decaying into its daughter with the emission 111 ¹²⁸Te $0\nu\beta\beta$ decay, we present an updated evaluation of two electrons and no antineutrinos in the final state, 112 of the half-life value for 128 Te $\beta\beta$ decay based the rathus violating L by two units. The experimental signa- ¹¹³ tio $T_{1/2}(^{130}\text{Te})/T_{1/2}(^{128}\text{Te}) = (3.52 \pm 0.11) \cdot 10^{-4}$ [16] ture of this process is a peak in the two-electron total 114 from ion-counting mass spectrometry of Xe in ancient energy spectrum at the Q-value $(Q_{\beta\beta})$ of the transition. ¹¹⁵ Te samples. Using the most recent ¹³⁰Te $2\nu\beta\beta$ decay The search for $0\nu\beta\beta$ decay addresses one of the most rel-evant open questions in neutrino physics: its observation $_{117}$ yr [9], we obtain $T_{1/2}^{2\nu}(^{128}\text{Te}) = (2.19 \pm 0.07) \cdot 10^{24}$ yr. would establish that L is not a symmetry of nature and ¹¹⁸ This result replaces and is in agreement with the previneutrinos are Majorana fermions, providing a clear sig-¹¹⁹ ously published value of $T_{1/2}^{2\nu}(^{128}\text{Te}) = (2.25 \pm 0.09) \cdot 10^{24}$ nature of physics beyond the Standard Model [2, 3]. This $_{120}$ yr [1], which used the weighted average of the 130 Te $2\nu\beta\beta$

The CUORE detector comprises 19 towers of 52 crysgenesis [4, 5], as well as constraints on the absolute mass $_{123}$ tals each. The basic unit is a $5 \times 5 \times 5 \text{ cm}^3$ TeO₂ crystal scale and ordering of neutrinos complementing other ap- 124 operated as an individual cryogenic calorimeter. Each 125 crystal is equipped with a Neutron Transmutation Doped CUORE is a ton-scale array of 988 TeO₂ crystals de- 126 (NTD) Ge thermistor [19], used as a temperature sensigned to search for $0\nu\beta\beta$ decay of ¹³⁰Te. Besides having ₁₂₇ sor, and a Si resistor to inject controlled heat pulses the world leading sensitivity for this process [7, 8] due 128 for thermal gain stabilization. The crystal is coupled to its very large mass -742 kg of TeO₂- and low back- ₁₂₉ through PTFE and Cu supports to the coldest stage of a ground, CUORE is also a powerful detector for other rare $_{130}$ dilution refrigerator operating at a temperature of ~ 10 processes, in particular other Te decay channels [9–11]. 131 mK [20]. Any particle interaction in a TeO₂ absorber In this letter we report on a new direct search for ¹²⁸Te ₁₃₂ crystal produces an energy deposition that is converted $0\nu\beta\beta$ decay. The CUORE array is grown from material 133 into heat (phonons) and measured via the temperature with natural isotopic composition, which given the nat- 134 sensor. A large and novel cryogenic infrastructure has ⁸⁹ ural abundance of 31.75% [12] contains 188 kg of ¹²⁸Te. ¹³⁵ been developed to provide the needed cooling power [8]. ⁹⁰ Despite this high abundance, the direct search is chal- 136 The CUORE cryostat is designed to meet the CUORE lenging due to the low $Q_{\beta\beta}$ value of (866.7 ± 0.7) keV [13] ₁₃₇ background specifications [21], and provide a low therwhich lies in a region of the energy spectrum domi- 138 mal noise environment, minimizing vibration and ther-⁹³ nated by $2\nu\beta\beta$ decay of ¹³⁰Te and γ backgrounds from ₁₃₉ mal dissipation on the cryogenic calorimeters [20, 22–24]. $_{94}$ other natural radioactivity. The most recent 128 Te $0\nu\beta\beta_{140}$ CUORE is the most advanced realization of the cryogenic 95 decay half-life limit from a direct search experiment, 141 calorimetric technology, developed over 30 years using

geochemical measurements (see [15] for a review), which $_{144}$ in turn are grouped into $\sim 40-60$ day collections called ⁹⁹ evaluate the presence of the $\beta\beta$ decay products accumu-¹⁴⁵ datasets. A typical dataset consists of 4 – 5 days of cali- $_{146}$ bration runs, followed by 30-50 days of so-called physics $_{147}$ runs, and finally another 4-5 days of final calibration ¹⁴⁸ to check the energy scale stability within a dataset. Cal-¹⁴⁹ ibration runs are performed using γ -ray sources of ²³²Th

Double beta ($\beta\beta$) decay is a rare second-order Fermi 100 lated in geological mineral samples of known age via the

^{*} Deceased

¹⁵⁰ and ⁶⁰Co to illuminate the detectors.

151 152 153 154 155 156 157 158 159 160 161 (every 570 s) via the Si heaters affixed to the crystals. For 218 of these efficiency terms. 162 crystals with non-functional heaters we use the 2615 keV_{219} 163 164 165 166 167 study and determine if signals in different crystals within $_{224}$ (820 - 890) keV. 168 a short time and spatial distance (typically of 10 ms and ¹⁷⁰ 150 mm) are attributed to the same physical interaction. We refer to these as coincident signals, to which we as-171 sign a multiplicity number, \mathcal{M}_n , where *n* corresponds 172 to the number of crystals simultaneously involved in the interaction (e.g., two events in different crystals due to 174 Compton scattering of the 2615 keV^{-208} Tl line are labeled as \mathcal{M}_2), with single-crystal interactions labeled as 176 \mathcal{M}_1 . We apply a pulse shape analysis (PSA) algorithm 177 to identify and discriminate pulses due to particle energy 178 depositions from non-physical signals (e.g., noise spikes, 179 abrupt baseline disturbances, pile up events). 180

The present analysis includes 5 datasets for a total 181 TeO₂ exposure of 309.33 kg·yr or 78.56 kg·yr of 128 Te. 182 These are the same data we used to measure the 130 Te 183 $2\nu\beta\beta$ decay half-life [9]. However, the latter exposure 184 is marginally lower $(300.72 \text{ kg} \cdot \text{yr})$ due to stricter selec-185 tion criteria on the energy scale calibration in both the 186 $\beta/\gamma(\langle 3 \text{ MeV} \rangle)$ and $\alpha(\langle 3 \text{ MeV} \rangle)$ regions for the $2\nu\beta\beta$ de-187 cay result. In contrast, this analysis requires only good 188 performance in the β/γ region. 189

In the following, we provide a detailed description of 225 190 the analysis technique used to search for 128 Te $0\nu\beta\beta$ de-191 cay, whose signature is a mono-energetic peak at $Q_{\beta\beta} = 227$ Multiple peaks populate this energy window: the clos-192 193 194 195 196 of (820 - 890) keV. 197

198 ¹⁹⁹ ment efficiency and the total analysis efficiency. We de-²³⁴ ²³²Th chain. In addition, we observe a continuous back-200 fine the containment efficiency ($\epsilon_{\rm MC}$) as the fraction of 235 ground contribution mainly induced by the $2\nu\beta\beta$ decay $_{203}$ ulating 10^8 events in the CUORE crystals [21], obtain- $_{238}$ radiation. The choice of the ROI is driven by the need $_{204}$ ing $\epsilon_{\rm MC} = 97.59 \pm 0.01\%$. The total analysis efficiency $_{239}$ for the energy window to fully contain the events of the $_{205}$ (exposure-weighted average $\epsilon_{cut} = 87.74 \pm 0.19\%$) is the $_{240}$ posited $0\nu\beta\beta$ peak, while being large enough to include

²⁰⁶ product of the total reconstruction efficiency, the anti-The procedure for the data acquisition and processing 207 coincidence efficiency and the PSA efficiency. The first described in [7]. We apply a digital optimum trigger 208 term is the probability that an event with a given energy algorithm [26, 27] to the acquired continuous data stream 209 is triggered, its energy is correctly reconstructed, and it and evaluate the amplitude of the triggered waveform by ²¹⁰ is not rejected as a pile-up event by the analysis cuts applying a frequency-based Optimum Filter (OF) that ²¹¹ applied during the data processing; the anti-coincidence weights the Fourier components of the signal, exploiting ²¹² efficiency is the probability that a single-hit event is not the noise power spectrum to reduce the impact of noisy 213 assigned the wrong multiplicity due to a random accifrequencies. We compensate for thermal gain variations 214 dental coincidence with an unrelated event; the PSA efin the crystals due to small fluctuations in their operating ²¹⁵ ficiency is the probability that events passing the base temperature with two independent methods. The first ²¹⁶ pile-up cuts also survive the PSA cut. We refer to [7] for utilizes heat pulses of fixed amplitude injected regularly 217 a more detailed description of the computation methods

To avoid introducing bias when choosing the fit model events from ²⁰⁸Tl in calibration data as a reference. We ₂₂₀ of the present analysis, we choose the ROI based on the se the data from calibration runs to convert the ther- 221 CUORE Background Model (BM) simulations, particumal amplitudes to units of energy. We exploit the gran- $_{222}$ larly taking into account backgrounds close to $Q_{\beta\beta}$ for ularity of the CUORE detector to perform a coincidence 223 ¹²⁸Te (Fig. 1). Based on this, we choose an ROI of



FIG. 1. \mathcal{M}_1 spectrum from the CUORE Background Model simulations in the proximity of the ¹²⁸Te $0\nu\beta\beta$ decay $Q_{\beta\beta}$. From left to right: ⁵⁴Mn γ (834.8 keV), ²⁰⁸Tl γ (860.6 keV) and 228 Ac γ (911.2 keV). The ROI for this analysis is denoted by the dashed green box, and includes the ${}^{54}Mn$ and ${}^{208}Tl$ lines.

 (866.7 ± 0.7) keV in the summed energy of the two emit-ted electrons. In the great majority of the cases the two ²²⁸/₂₂₉ from ²⁰⁸Tl, a ²³²Th chain element. A prominent peak electrons are absorbed by the same crystal: we therefore $_{230}$ at 834.8 keV due to a 54 Mn γ line is also identified: the select \mathcal{M}_1 events only, within a region of interest (ROI) 231 presence of ⁵⁴Mn stems from the cosmogenic activation ²³² of copper [17, 29]. The visible peak to the right of $Q_{\beta\beta}$ is The signal efficiency is the product of the contain- $_{233}$ the 911.2 keV γ line from 228 Ac, another element of the 128 Te $0\nu\beta\beta$ decay events that release their full energy, i.e. $_{236}$ of 130 Te and by multiple Compton scattering of the var- $Q_{\beta\beta}$, in a single crystal [28]. We evaluate ϵ_{MC} by sim- $_{237}$ ious γ rays from environmental radioactivity and cosmic

 $_{242}$ evaluate the signal rate correctly. The ROI contains the $_{289}$ is the dataset total analysis efficiency, and ϵ_{MC} is the $_{243}$ ⁵⁴Mn and ²⁰⁸Tl peaks, while the ²²⁸Ac line is excluded ₂₉₀ containment efficiency. The decay rate $\Gamma_{0\nu}$ in the model $_{244}$ as it is 45 keV (> 5 σ with FWHM energy resolution of $_{291}$ is a global parameter common to all the datasets. We $_{245} \sim 4.3 \,\text{keV}$ in the ROI) away from $Q_{\beta\beta}$.

We perform a simultaneous binned Bayesian fit on 293 246 247 248 249 $_{250}$ ing a Markov Chain Monte Carlo (MCMC) using the $_{297}$ alyzed data were taken over a period of ~ 2 years, thus $_{251}$ Metropolis-Hastings algorithm. We fit the CUORE \mathcal{M}_1 $_{298}$ we expect the number of events due to 54 Mn decay to 252 spectrum over the chosen ROI; the lower limit on the 299 decrease over time. To account for this reduction, we $_{253}$ $0\nu\beta\beta$ decay rate is taken as the rate corresponding to $_{300}$ include a multiplicative factor in the definition of the $_{254}$ 90% of the marginalized posterior.

255 256 ROI with a likelihood that includes the posited signal 303 the dataset duration: ²⁵⁷ peak plus the background structures present in the ROI, ²⁵⁸ namely the ⁵⁴Mn peak, the ²⁰⁸Tl peak, and a continuum 259 distribution. We model the latter with a linear function, 260 that describes the decreasing trend over the fit region. that describes the decreasing trend over the fit region. $_{304}$ where t_{ds}^{in} and t_{ds}^{fin} respectively refer to the start-time and This simpler effective model is consistent with the full $_{305}$ the end-time of the dataset with respect to the begin-261 CUORE background model [9]. The binned likelihood 262 for each dataset is the product of Poisson terms, and the 263 264 total likelihood is:

$$\mathscr{L} = \prod_{ds} \prod_{i}^{N_{bins}} \frac{\mu_i^{n_i} e^{-\mu_i}}{n_i!} \quad , \tag{1}$$

where ds indexes the dataset, and the index i runs over 265 $_{266}$ the 140 bins (0.5 keV/bin). In the approximation of small ₂₆₇ bin width, the number of expected counts μ_i in the *i*-th 268 bin can be taken as the value of the model function at 269 the center of the bin:

$$\mu_i = S f_S^{ds}(i) + C_{\rm Mn} f_{\rm Mn}^{ds}(i) + C_{\rm Tl} f_{\rm Tl}^{ds}(i) + f_{\rm linear}^{ds}(i) \ , \ (2)$$

²⁷⁰ where S, $C_{\rm Mn}$ and $C_{\rm Tl}$ are the number of counts at ²⁷¹ the signal, ⁵⁴Mn and ²⁰⁸Tl peaks, while $f_S^{ds}(i)$, $f_{\rm Mn}^{ds}(i)$, $_{272} f_{\text{Tl}}^{ds}(i)$, and $f_{\text{linear}}^{ds}(i)$ are the values at the *i*-th bin of the 273 probability density functions used to model the shape of each component. 274

We model the shape of each peak as the sum of three 275 Gaussian distributions based on the CUORE detector re-276 sponse function, corrected for the energy dependence of 277 the detector response (energy-resolution scaling and en-278 ergy reconstruction bias) studied in Ref [7]. The defini-279 tion of each component of Eq. 2 is detailed in the fol-280 lowing. We implement all terms as parameters of the 281 fit. 282

The $0\nu\beta\beta$ decay rate $\Gamma_{0\nu}$ is connected to the expected 283 $_{284}$ number of signal counts S for a given dataset through ₂₈₅ the formula:

$$S = \Gamma_{0\nu} \cdot \frac{N_A}{A_{\text{TeO}_2}} \cdot \eta_{128} \cdot (M\Delta t)_{ds} \cdot \epsilon_{ds}^{cut} \cdot \epsilon_{\text{MC}} \quad , \qquad (3)$$

where N_A is Avogadro's constant, A_{TeO_2} is the TeO_{2 332} where BI_{ds} is the background index of dataset ds in units

 $_{241}$ and constrain the background structures, allowing us to $_{288}$ $(M\Delta t)_{ds}$ is the dataset exposure (in units of kg·yr), ϵ_{ds}^{cut} ²⁹² make a statistical inference on this parameter of interest.

The ⁵⁴Mn originates from cosmogenic activation of Cu, the five included datasets. The fit is performed with 294 which occurred before the CUORE cryostat and detecthe Bayesian Analysis Toolkit (BAT) [30], that sam- 295 tor structure components were moved underground at ples from the posterior probability density by perform- 296 LNGS. This element has a half-life of 312.2 days; the an-³⁰¹ number of expected ⁵⁴Mn events in each dataset, result-We fit the CUORE \mathcal{M}_1 spectrum over the chosen $_{302}$ ing from the integration of the exponential decay over

$$C_{\rm Mn} = \Gamma_{\rm Mn} \cdot \tau \cdot \left(e^{-\frac{t_{\rm Mn}^{\rm in}}{\tau_{\rm Mn}}} - e^{-\frac{t_{\rm Mn}^{\rm in}}{\tau_{\rm Mn}}}\right) \cdot \frac{(M\Delta t)_{ds}}{t_{ds}^{\rm fin} - t_{ds}^{\rm in}} \cdot \epsilon_{ds}^{cut} \quad , \quad (4)$$

 $\frac{\Delta t_{ds}}{t_{fa}^{in}-t_{a}^{in}}$ The livetime fraction $\frac{\Delta t_{ds}}{t_{fa}^{in}-t_{a}^{in}}$ 307 accounts for the dead times - few time intervals of data ³⁰⁸ taking that are removed from the analysis, for example ³⁰⁹ noisy periods due to short maintenance interruptions, ac-310 tivities in the local laboratory or earthquakes - over the ₃₁₁ integration time interval. The ⁵⁴Mn rate $\Gamma_{\rm Mn}$ (units of $_{312}$ counts/(kg·yr)) is a nuisance parameter of the fit common to all the datasets. 313

²⁰⁸Tl belongs to the naturally occurring ²³²Th chain. 314 Given that the amplitude of the observed higher intensity 315 208 Tl γ peaks are constant in time across the datasets, we ³¹⁷ assume the 860.6 keV rate to be stable. We then define ³¹⁸ the expected number of events at this ²⁰⁸Tl line in the 319 ROI for a given dataset as:

$$C_{\rm Tl} = \Gamma_{\rm Tl} \cdot (M\Delta t)_{ds} \cdot \epsilon_{ds}^{cut} \quad , \tag{5}$$

 $_{320}$ where the 208 Tl decay rate Γ_{Tl} is expressed in units of $_{321}$ counts/(kg·yr). As with the 54 Mn rate, this represents a 322 nuisance parameter of the fit.

We model the continuous background distribution as 323 ³²⁴ a linear function of energy according to the following ex-325 pression:

$$f_{\text{linear}}^{ds}(i) = C_b^{ds} + m_{ds}(E_i - E_{1/2}) \quad , \tag{6}$$

 $_{326}$ where C_b^{ds} and m_{ds} are the expected number of back-327 ground events and the background slope for a given $_{328}$ dataset, E_i is the energy at the center of the *i*-th bin, $_{329}$ and $E_{1/2}$ is the energy corresponding to center of the ₃₃₀ ROI. We define the expected number of events C_h^{ds} in 331 each dataset as:

$$C_b^{ds} = \mathrm{BI}_{ds} \cdot (M\Delta t)_{ds} \cdot w_i \quad , \tag{7}$$

²⁸⁷ molar mass, η_{128} is the ¹²⁸Te natural isotopic abundance, ³³³ of counts/(keV·kg·yr) and w_i is the bin width, which is

335 and are dataset-dependent quantities. 336

We adopt a uniform prior for each parameter of the 370 337 338 339 340 341 342 343 345 346 347 constructed through a fit on the same data that are used 348 349 350 351 nuisance parameters. The signal, ${}^{54}Mn$ and ${}^{208}Tl$ rates 352 $_{354}$ ues only, while for the background slope m both negative $_{387}$ is compatible with the 8.8% under-fluctuation obtained 355 and positive values are allowed. We run the Bayesian 388 from the sensitivity study.



FIG. 2. Top: data spectrum in the ROI, together with the best-fit curve (red solid) and the best-fit curve with the signal rate set at the 90% CI limit (blue dashed). Bottom: residual plot with fit, compatible with 0 (intercept at -1.1 ± 2.6 counts/keV, $\chi^2/dof = 82/69.$)

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 $_{358}$ fit on the data, and find no evidence for $^{128}\mathrm{Te}~0\nu\beta\beta$ de-359 cay. From the marginalized posterior distribution of the ³⁶⁰ signal rate, we extract a 90% CI limit of

$$\Gamma_{0\nu} < 1.9 \cdot 10^{-25} \text{ yr}^{-1}$$
 . (8)

 $_{361}$ This lower limit corresponds to a 90% CI upper limit on $_{362}$ the $^{128}\text{Te}~0\nu\beta\beta$ decay half-life of

$$T_{1/2}^{0\nu} > 3.6 \cdot 10^{24} \text{ yr}$$
 . (9)

363 364 cay of ¹²⁸Te to date, representing a more than 30-fold 399 error. We thus repeat the Bayesian fit activating one ³⁶⁵ improvement over the previous limit [14] from direct ⁴⁰⁰ nuisance parameter at the time to allow its value to vary ₃₆₆ searches, and exceeds for the first time the combined ₄₀₁ according to the corresponding prior.

 $_{334}$ constant across the energy spectrum. The slope and the $_{367} 0\nu\beta\beta$ and $2\nu\beta\beta$ decay half life obtained by geochemical background index are also nuisance parameters in the fit 368 measurements. The fit result and the total ROI spectrum ³⁶⁹ are shown in Fig. 2.

We extract the median exclusion sensitivity to 128 Te fit for several reasons. Due to the 100-fold increase in $371 0\nu\beta\beta$ decay by repeating the statistical only Bayesian fit exposure, CUORE's sensitivity on $\Gamma_{0\nu}$ is expected to $_{372}$ on 10⁴ toy-MC simulations of the experiment. We probe factor of ~ 10 better with respect to the past direct $_{373}$ duce the toy-MCs using the global mode values of the limit. The absence of knowledge on $\Gamma_{0\nu}$ at the range $_{374}$ background parameters from a Bayesian fit without the that CUORE can probe justifies the choice of a uniform 375 signal component on the CUORE data. The median exprior for $\Gamma_{0\nu} \geq 0$ according to the Principle of Indiffer- $_{376}$ clusion sensitivity is the median of the distribution of ence, which assigns equal probabilities to all the possible $_{377}$ the 90% CI limits on $T_{1/2}^{0\nu}$, each resulting from a sigvalues up to a maximum that can be greater that the $_{378}$ nal plus background fit to one of the 10^4 backgroundpast limit. The CUORE Background Model can provide 379 only toy-MCs. This distribution is shown in Fig. 3, information on some nuisance parameters, however it is $_{380}$ and its median is $\hat{T}_{1/2}^{0\nu} = 2.2 \cdot 10^{24}$ yr. The probabil-³⁸¹ ity to obtain a more stringent limit than the one obfor the present analysis, and including such information 382 served with the CUORE data is 8.8%. We also repeat the would bias the result. Thus, in the absence the of in- 383 fit on the data, allowing the signal rate to assume nondependent measurements, we use a uniform prior for all 384 physical negative values. In this case, the global mode $_{385}$ of $\Gamma_{0\nu}$ is $(-2.4 \pm 1.8) \cdot 10^{-25}$ yr⁻¹, resulting in an underand the BI are constrained to non-negative physical val- $_{386}$ fluctuation with a statistical significance of $\sim 1.4\sigma$, which



FIG. 3. Distribution of the 90% CI limits on $T_{1/2}^{0\nu}$ extracted from repeating the analysis on the 10^4 backgroundonly pseudo-experiments. The solid line corresponds to the median exclusion sensitivity, while the dashed one shows the 90% CI limit from the analysis of the CUORE data.

We summarize in Table I a series of systematic uncer-389 ³⁹⁰ tainties affecting our limit. For this study, we run the fit ³⁹¹ without the constraint $\Gamma_{0\nu} \geq 0$, to access the full range $_{392}$ $\Gamma_{0\nu}$ marginalized posterior. We adopt a fully Bayesian ³⁹³ approach to evaluate the effect due to the uncertainties ³⁹⁴ on the containment efficiency, the analysis cut efficiency ³⁹⁵ and the ¹²⁸Te natural isotopic abundance. We imple-³⁹⁶ ment these as independent nuisance parameters in the ³⁹⁷ likelihood with a Gaussian prior, whose mean and sigma This result is the most stringent limit on the $0\nu\beta\beta$ de- 398 are equal to the respective central value and associated

TABLE I. Systematic effects on the ¹²⁸Te $0\nu\beta\beta$ decay signal rate 90% limit. The first row refers to the BAT intrinsic uncertainty, due to the stochastic nature of the MCMC. The efficiencies and the ¹²⁸Te isotopic abundance were treated as nuisance parameters in the fit, while an alternative approach was adopted for the uncertainties on the 128 Te $Q_{\beta\beta}$ and the detector response function parameters. The dominant systematic effect is the value on $Q_{\beta\beta}$.

Systematic	Prior	Effect on $\Gamma_{0\nu}^{90\%}$		
BAT Stat. Only fit	-	0.3%		
Bayesian Approach				
Containment Efficiency	Gaussian	0.4%		
¹²⁸ Te Isotopic Abundance	Gaussian	$< 0.3\% \ (0.05\%)$		
Analysis Cut Efficiency	Gaussian	$< 0.3\% \ (0.1\%)$		
Repeated Fit Approach				
¹²⁸ Te $Q_{\beta\beta}$	Gaussian	7.0%		
Energy Reconstruction Bias	Multivariate	$< 0.3\% \ (0.1\%)$		
Energy Resolution Scaling	Multivariate	$< 0.3\% \ (0.1\%)$		

402 $_{403}$ the ¹²⁸Te $Q_{\beta\beta}$ and on the detector response function $_{459}$ tematic, affecting the result at the level of 7.0%, is due parameters (namely the energy reconstruction bias and $_{460}$ to the uncertainty on $Q_{\beta\beta}$. 404 resolution scaling) using an alternative approach, which 405 we refer to as the Repeated Fit Approach, because of 406 the excessive computation time required to treat them as nuisance parameters in the fit. This method consists 408 of repeating the fit for a series of discrete values of the 409 systematic parameter under study, covering a $\pm 3\sigma$ re-410 gion around its prior mean value. We then sum the $\Gamma_{0\nu}$ ⁴¹² marginalized posteriors obtained from each fit weighting by the prior probability of the parameter considered as $_{466}$ 414 systematic, and take the signal rate corresponding to the 467 staff of the Laboratori Nazionali del Gran Sasso and 415 90% quantile of the obtained distribution. We take addi-468 the technical staff of our laboratories. This work was 416 tional care when treating the detector response parame- 469 supported by the Istituto Nazionale di Fisica Nucle-417 418 419 420 421 422 parameters describes the energy bias and another set of 475 sity. This material is also based upon work supported 423 three exists for the resolution scaling. The correlations 476 by the US Department of Energy (DOE) Office of Sci-424 among these parameters are taken into account using 477 ence under Contract Nos. DE-AC02- 05CH11231 and 425 427 429 430 431 432 behavior (0.3%). 433

434 ⁴³⁶ takes place [31–33]. Among these models, the exchange ⁴³⁹ CUPID-0 Collaborations.

⁴³⁷ of a light Majorana neutrino is the most favored [34]. ⁴³⁸ However, a positive signal for the $0\nu\beta\beta$ decay of a single 439 isotope would not determine the mechanism of this pro-⁴⁴⁰ cess [2]. Discriminating among the existing models [35] ⁴⁴¹ and possibly testing the calculations of nuclear matrix el-⁴⁴² ements for double beta decay [36], would be possible via ⁴⁴³ the comparison of results from different isotopes. It has ⁴⁴⁴ been pointed out [35] that the study of the $0\nu\beta\beta$ decay of ⁴⁴⁵ ¹²⁸Te can be particularly useful for such model discrimi-446 nation. In this paper, we present the first results on the ⁴⁴⁷ ¹²⁸Te $0\nu\beta\beta$ decay search with the CUORE experiment. 448 With a binned Bayesian fit of the CUORE data with a total exposure of 309.33 kg·yr (78.6 kg·yr of ¹²⁸Te), we $_{450}$ find no evidence for $^{128}\text{Te}~0\nu\beta\beta$ decay, and we set a 90% ₄₅₁ CI limit on the half-life of this process at $T_{1/2}^{0\nu} > 3.6 \cdot 10^{24}$ ⁴⁵² yr. This represents the most stringent limit in literature, ⁴⁵³ improving by over a factor 30 the previous limit from a di-⁴⁵⁴ rect search experiment, and exceeding those from indirect 455 geochemical measurements for the first time. From the 456 analyzed exposure, the CUORE median exclusion sensi-457 tivity to this decay is $\hat{T}_{1/2}^{0\nu} = 2.2 \cdot 10^{24}$ yr, giving an 8.8% We treat the systematics due to the uncertainty on 458 probability to obtain a stronger limit. The dominant sys-

> The analysis presented in this paper has been carried ⁴⁶² out with about one-tenth of the final exposure scheduled 463 for CUORE, corresponding to ~ 3.7 ton y. We plan to ⁴⁶⁴ update these results with such unprecedented amount of $_{465}$ data collected with TeO₂ crystals.

The CUORE Collaboration thanks the directors and ter systematics. It was previously observed in CUORE [7] 470 are (INFN); the National Science Foundation under that both the bias on the energy reconstruction and the 471 Grant Nos. NSF-PHY-0605119, NSF-PHY- 0500337, resolution scaling exhibit an energy dependence which 472 NSF-PHY-0855314, NSF-PHY-0902171, NSF- PHYwe model with two independent second order polynomial 473 0969852, NSF-PHY-1307204, NSF-PHY-1314881, NSFfunctions. As a consequence, a set of three correlated 474 PHY-1401832, and NSF-PHY-1913374; and Yale Univermulti-dimensional priors. The dominant systematic is 478 DE-AC52-07NA27344; by the DOE Office of Science, Of- $Q_{\beta\beta}$, which has an effect of 7.0% on the limit. We ex- 479 fice of Nuclear Physics under Contract Nos. DE-FG02pect this due to the relatively large error on its literature 480 08ER41551, DE-FG03-00ER41138, DE- SC0012654, DEvalue, (866.7 ± 0.7) keV [13]. All the other systemat- $_{481}$ SC0020423, DE-SC0019316; and by the EU Horiics affect the limit by less than 1%; the 128 Te isotopic $_{482}$ zon2020 research and innovation program under the abundance, the analysis cut efficiency, and the detector 483 Marie Sklodowska-Curie Grant Agreement No. 754496. response function parameters result in values below the 484 This research used resources of the National Energy intrinsic BAT uncertainty due to the MCMC stochastic 485 Research Scientific Computing Center (NERSC). This ⁴⁸⁶ work makes use of both the DIANA data analysis and Several Standard Model extended theories include 487 APOLLO data acquisition software packages, which were mechanisms that try to explain how the $0\nu\beta\beta$ decay 488 developed by the CUORICINO, CUORE, LUCIFER and

- ⁴⁹⁰ [1] A. S. Barabash, Universe **6**, 159 (2020).
- [2] S. M. Bilenky and C. Giunti, Int. J. Mod. Phys. A 30,
 1530001 (2015).
- [3] M. J. Dolinski, A. W. P. Poon, and W. Rodejohann,
 Ann. Rev. Nucl. Part. Sci. 69, 219 (2019).
- ⁴⁹⁵ [4] L. Canetti, M. Drewes, and M. Shaposhnikov, New J.
 ⁴⁹⁶ Phys. 14, 095012 (2012).
- ⁴⁹⁷ [5] M. A. Luty, Phys. Rev. D **45**, 455 (1992).
- [6] S. Dell'Oro, S. Marcocci, and F. Vissani, Phys. Rev. D
 100, 073003 (2019).
- 500 [7] D. Q. Adams *et al.* (CUORE Collaboration), Phys. Rev.
 501 Lett. **124**, 122501 (2020).
- ⁵⁰² [8] D. Q. Adams *et al.* (CUORE), Nature **604**, 53 (2022).
- ⁵⁰³ [9] D. Q. Adams *et al.* (CUORE Collaboration), Phys. Rev.
 ⁵⁰⁴ Lett. **126**, 171801 (2021).
- ⁵⁰⁵ [10] D. Q. Adams *et al.* (CUORE), Eur. Phys. J. C **81**, 567
 (2021).
- 507 [11] D. Q. Adams et al., (2022), arXiv:2203.08684 [nucl-ex].
- ⁵⁰⁸ [12] M. A. Fehr, M. Rehkamper, and A. N. Halliday, Int. J.
 ⁵⁰⁹ Mass Spectrom. **232**, 83 (2004).
- 510 [13] M. Wang, W. J. Huang, F. G. Kondev, G. Audi, and
 511 S. Naimi, Chin. Phys. C 45, 030003 (2021).
- ⁵¹² [14] C. Arnaboldi *et al.*, Phys. Lett. B **557**, 167 (2003).
- 513 [15] A. Campani, V. Dompè, and G. Fantini, Universe 7, 212 514 (2021).
- ⁵¹⁵ [16] T. Bernatowicz, J. Brannon, R. Brazzle, R. Cowsik,
 ⁵¹⁶ C. Hohenberg, and F. Podosek, Phys. Rev. Lett. 69,
 ⁵¹⁷ 2341 (1992).
- ⁵¹⁸ [17] C. Alduino *et al.* (CUORE), Eur. Phys. J. C **77**, 13 ⁵¹⁹ (2017).
- ⁵²⁰ [18] I. Nutini et al., J. Low Temp. Phys. **199**, 519 (2020).
- ⁵²¹ [19] E. E. Haller, N. P. Palaio, M. Rodder, W. L. Hansen,
 ⁵²² and E. Kreysa, "NTD germanium: A novel material
 ⁵²³ for low temperature bolometers," in *Neutron Transmu-*⁵²⁴ tation Doping of Semiconductor Materials (Springer US,
 ⁵²⁵ Boston, MA, 1984) pp. 21–36.
- ⁵²⁶ [20] C. Alduino *et al.*, Cryogenics **102**, 9 (2019).
- ⁵²⁷ [21] C. Alduino *et al.* (CUORE Collaboration), Eur. Phys. J.
 ⁵²⁸ C 77, 543 (2017).
- ⁵²⁹ [22] A. D'Addabbo, C. Bucci, L. Canonica, S. Di Domizio,
 P. Gorla, L. Marini, A. Nucciotti, I. Nutini, C. Rusconi,
 ⁵³¹ and B. Welliver, Cryogenics **93**, 56 (2018).
- ⁵³² [23] V. Domp *et al.*, J. Low Temp. Phys. **200**, 286294 (2020).
- ⁵³³ [24] D. Adams *et al.*, Progress in Particle and Nuclear Physics
 ⁵³⁴ **122**, 103902 (2022).
- 535 [25] C. Brofferio and S. Dell'Oro, Rev. Sci. Instrum. 89, 536 121502 (2018).
- 537 [26] S. Di Domizio, F. Orio, and M. Vignati, JINST 6,
 538 P02007 (2011).
- 539 [27] A. Campani et al., J. Low Temp. Phys. 200, 321 (2020).
- 540 [28] C. Alduino *et al.* (CUORE), Phys. Rev. C 93, 045503
 541 (2016).
- 542 [29] M. Laubenstein and G. Heusser, Appl. Radiat. Isot. 67, 543 750 (2009).
- 544 [30] A. Caldwell, D. Kollar, and K. Kroninger, Comput.
 545 Phys. Commun. 180, 2197 (2009).
- 546 [31] B. Pontecorvo, Phys. Lett. B 26, 630 (1968).
- 547 [32] M. Mitra, G. Senjanovic, and F. Vissani, Nucl. Phys. B
 548 856, 26 (2012).
- 549 [33] V. Tello, M. Nemevsek, F. Nesti, G. Senjanovic, and
- ⁵⁵⁰ F. Vissani, Phys. Rev. Lett. **106**, 151801 (2011).

- 551 [34] S. Dell'Oro, S. Marcocci, M. Viel, and F. Vissani, Adv.
- ⁵⁵² High Energy Phys. **2016**, 2162659 (2016).

557

558

559

560

- ⁵⁵³ [35] F. Deppisch and H. Ps, Phys. Rev. Lett. 98, 232501
 ⁵⁵⁴ (2007).
- ⁵⁵⁵ [36] S. M. Bilenky and J. A. Grifols, Phys. Lett. B 550, 154
 (2002).
 - [37] V. Dompè, Search for neutrinoless double beta decay of ¹²⁸ Te with the CUORE experiment, Ph.D. thesis, Gran Sasso Science Institute (2021).

SUPPLEMENTAL MATERIAL

We develop and optimize the fit strategy on toy-MC 562 spectra. We generate the toy-MCs according to the ⁵⁶³ signal-plus-background model, extracting the values of $\Gamma_{\rm Mn}$, $\Gamma_{\rm Tl}$, BI and *m* from the CUORE Background 564 565 Model. We refer to Ref. [37] for a more detailed discus-⁵⁶⁶ sion of the method. We take advantage of the toy-MCs 567 to verify that the fit correctly reconstructs the simulated ⁵⁶⁸ background components and to inspect if a bias is in-⁵⁶⁹ troduced in the $0\nu\beta\beta$ decay rate reconstruction when a ⁵⁷⁰ signal contribution is added in the toy-MC. We generate $_{571}$ 10⁴ toy-MCs with no signal and run the fit independently ⁵⁷² on each of them. We then construct the distributions of ⁵⁷³ the best-fit values from all the toy-MCs for each parame-⁵⁷⁴ ter, in order to compare the extracted and simulated val-575 ues. As expected, these distributions are centered at the ⁵⁷⁶ values used to produce the toy-MC. Thanks to the large 577 number of toy-MCs, we are able to identify a small bias in the reconstruction of the BI and the slope corresponding to a <0.15% underestimation and a <1.6% overestima-579 tion, respectively. No correlations are seen between these 580 two parameters. The reconstructed values of the ${}^{54}Mn$ 581 ⁵⁸² and ²⁰⁸Tl rates are compatible with the injected values. 583 To test the signal rate reconstruction, we repeat the fit 584 on five sets of 2000 toy-MCs, injecting a different signal set amplitude in the range $(2 - 10) \cdot 10^{-25}$ yr⁻¹ in each set. This range includes the signal rate corresponding to the CUORE sensitivity of $3.2 \cdot 10^{-25}$ yr⁻¹ obtained from pure 587 toy-MC, i.e. without including real data. 588

Figure 4 shows the mean reconstructed signal rate as a function of the injected one. The relation between the son two is well described by a linear function: the intercept is compatible with 0 at a $\sim 1.3 \sigma$, and the slope is compatson ible with 1 within 1σ . These results allow us to conclude that no bias is introduced by the Bayesian fit in the signal rate reconstruction.

We also study the intrinsic stability of the BAT fit, by repeating it $2 \cdot 10^3$ times on the same toy-MC populated only with the background components, obtaining a 0.3% root mean square on the distribution of the $\Gamma_{0\nu}$ limits at components of the $\Gamma_{0\nu}$ limits at

⁶⁰¹ Table II reports the ranges for all fit parameters. All ⁶⁰² parameters proportional to a number of counts, namely ⁶⁰³ the signal, Mn and Tl rates, are allowed to assume only ⁶⁰⁴ non-negative values. The BI of each dataset is further



FIG. 4. Linear fit on the mean reconstructed signal rate as a function of the injected one. The intercept and slope are compatible with 0 and 1, respectively.

⁶⁰⁵ constrained according to a preliminary estimation of the ⁶⁰⁶ number of background counts. The background slopes ⁶⁰⁷ are allowed to assume also negative values.

Table III reports the value at the global mode for all parameters of the fit to the data.

Figure 5 shows the posterior distribution for $\Gamma_{0\nu}$ obfination from the reference fit, and from the alternative fit performed with the signal rate allowed to artificially fit assume non-physical negative values.

TABLE II. Parameter ranges for the fit parameters. All parameters are assigned a uniform prior; the signal, Mn and Tl rates and the BI are constrained to non-negative physical values only, while both positive and negative values are allowed for the background slope.

Parameter	Prior Range
$\Gamma_{0\nu}$	$[0, 1.74 \cdot 10^{-24}] \text{ yr}^{-1}$
BI_1	$[1.1634, 1.73] \text{ cts}/(\text{keV}\cdot\text{kg}\cdot\text{yr})$
BI_2	$[1.188, 1.6513] \text{ cts}/(\text{keV}\cdot\text{kg}\cdot\text{yr})$
BI_3	$[1.2453, 1.7374] \text{ cts}/(\text{keV}\cdot\text{kg}\cdot\text{yr})$
BI_4	$[1.2204, 1.7412] \text{ cts}/(\text{keV}\cdot\text{kg}\cdot\text{yr})$
BI_5	$[1.0221, 1.4536] \text{ cts}/(\text{keV}\cdot\text{kg}\cdot\text{yr})$
m_1	[-1, 1] 1/keV
m_2	[-1, 1] 1/keV
m_3	[-1, 1] 1/keV
m_4	[-1, 1] 1/keV
m_5	[-1, 1] 1/keV
Γ_{Mn}	[0, 44.58] cts/(kg·yr)
$\Gamma_{\rm Tl}$	[0, 6.16] cts/(kg·yr)

TABLE III. Best-fit values for all parameters of the fit on CUORE data. The signal rate is allowed to take non-negative values only.

Parameter	Fit Result	Units
$\Gamma_{0\nu}$	0	yr^{-1}
BI_1	1.48 ± 0.02	$\rm cts/(keV \cdot kg \cdot yr)$
BI_2	1.43 ± 0.02	$\rm cts/(keV \cdot kg \cdot yr)$
BI_3	1.49 ± 0.02	$\rm cts/(keV \cdot kg \cdot yr)$
BI_4	1.48 ± 0.02	$\rm cts/(keV\cdot kg\cdot yr)$
BI_5	1.26 ± 0.02	$\rm cts/(keV\cdot kg\cdot yr)$
m_1	-0.07 ± 0.03	keV^{-1}
m_2	-0.06 ± 0.03	keV^{-1}
m_3	-0.08 ± 0.03	keV^{-1}
m_4	-0.04 ± 0.03	keV^{-1}
m_5	-0.12 ± 0.03	keV^{-1}
Γ_{Mn}	15.9 ± 0.7	$\rm cts/(kg\cdot yr)$
Γ_{Tl}	0.5 ± 0.2	$\rm cts/(kg\cdot yr)$



FIG. 5. Top: marginalized posterior of the signal rate obtained from the official fit, which allows only physical values. Bottom: marginalized posterior of the signal rate obtained from the alternative fit, which allows also non-physical values of $\Gamma_{0\nu}$. A ~ 1.4 σ significance under-fluctuation, compatible with the results of the sensitivity studies, is observed. Both distributions are normalized to one.