

## CHCRUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

## Magnetic Interactions of the Centrosymmetric Skyrmion Material math xmlns="http://www.w3.org/1998/Math/MathML" display="inline">mrow>msub>mrow>mi>Gd/mi>/mrow> mrow>mn>2/mn>/mrow>/msub>msub>mrow>mi>PdSi/ mi>/mrow>mrow>mn>3/mn>/mrow>/msub>/mrow>/mat h>

Joseph A. M. Paddison, Binod K. Rai, Andrew F. May, Stuart Calder, Matthew B. Stone, Matthias D. Frontzek, and Andrew D. Christianson Phys. Rev. Lett. **129**, 137202 — Published 23 September 2022 DOI: 10.1103/PhysRevLett.129.137202

## Magnetic Interactions of the Centrosymmetric Skyrmion Material Gd<sub>2</sub>PdSi<sub>3</sub>

Joseph A. M. Paddison,<sup>1,\*</sup> Binod K. Rai,<sup>1,2</sup> Andrew F. May,<sup>1</sup> Stuart A. Calder,<sup>3</sup> Matthew B. Stone,<sup>3</sup> Matthias D. Frontzek,<sup>3</sup> and Andrew D. Christianson<sup>1,†</sup>

<sup>1</sup>Materials Science and Technology Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA

<sup>2</sup>Savannah River National Laboratory, Aiken, South Carolina, 29808, USA

<sup>3</sup>Neutron Scattering Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA

The experimental realization of magnetic skyrmion crystals in centrosymmetric materials has been driven by theoretical understanding of how a delicate balance of anisotropy and frustration can stabilize topological spin structures in applied magnetic fields. Recently, the centrosymmetric material Gd<sub>2</sub>PdSi<sub>3</sub> was shown to host a field-induced skyrmion crystal, but the skyrmion stabilization mechanism remains unclear. Here, we employ neutron-scattering measurements on an isotopically-enriched polycrystalline Gd<sub>2</sub>PdSi<sub>3</sub> sample to quantify the interactions that drive skyrmion formation. Our analysis reveals spatially-extended interactions in triangular planes, and large ferromagnetic inter-planar magnetic interactions that are modulated by the Pd/Si superstructure. The skyrmion crystal emerges from a zero-field helical magnetic order with magnetic moments perpendicular to the magnetic propagation vector, indicating that the magnetic dipolar interaction plays a significant role. Our experimental results establish an interaction space that can promote skyrmion formation, facilitating identification and design of centrosymmetric skyrmion materials.

Magnetic skyrmions are topologically-nontrivial spin textures with potentially transformative applications in quantum computing and information storage [1–3]. Skyrmion crystals usually occur in noncentrosymmetric magnets, in which they can be stabilized by antisymmetric exchange interactions [4, 5]. However, it was recently shown that skyrmion crystals can be stabilized in centrosymmetric systems by frustrated (competing) interactions [6, 7], presenting the exciting prospects of higher skyrmion densities and manipulation of chiral degrees of freedom by external fields [8, 9]. While a small number of candidate centrosymmetric skyrmion materials have been identified [10–13], experimentally determining the magnetic interactions driving this behavior remains a key challenge. Addressing this challenge is a prerequisite for designing and manipulating skyrmion-based devices.

The hexagonal material Gd<sub>2</sub>PdSi<sub>3</sub> provides a rare example of a skyrmion crystal in a centrosymmetric system [10]. In Gd<sub>2</sub>PdSi<sub>3</sub>, triangular layers of magnetic Gd<sup>3+</sup> ions are separated by honeycomb PdSi<sub>3</sub> layers [Fig. 1(a)] [14]. A transition from the paramagnetic state occurs at  $T_{\rm N} = 21 \,{\rm K}$  to an incommensurate magnetic order with propagation vector  $\mathbf{q} = [q00]^*$  with  $q \approx 0.14$  [10]. The observed  $\mathbf{q}$  may be stabilized by competition between ferromagnetic nearest-neighbor interactions and antiferromagnetic further-neighbor interactions [Fig. 1(a,b)] [6,7]. Application of a magnetic field below  $T_{\rm N}$  yields a giant topological Hall effect, signifying a transition to a topologically-nontrivial skyrmion crystal, which is a triple-q structure formed by superposing magnetic helices with  $\mathbf{q} = [q00]^*$ ,  $[0q0]^*$ , and  $[\bar{q}q0]^*$  [10]. The bulk magnetic susceptibility follows a Curie-Weiss law with spin S = 7/2, g = 2, and a ferromagnetic Weiss temperature  $\theta \approx 30$  K, suggesting that Gd<sup>3+</sup> ions possess spin-only local moments [15– 17]. However, coupled electronic and spin correlations develop well above  $T_N$ , as indicated by a minimum in the resistivity at  $\sim 2T_{\rm N}$  and a large negative magnetoresistance that persists up to  $\sim 3T_N$  [16–18].

To explain spin textures in centrosymmetric systems such



Figure 1. (a) Parent crystal structure of Gd<sub>2</sub>PdSi<sub>3</sub> (space group P6/mmm;  $a \approx 4.06$  Å,  $c \approx 4.09$  Å [19]). (b) Magnetic interactions within triangular Gd<sup>3+</sup> layers. (c) Proposed low-symmetry Pd/Si superstructure showing ...ABCDBADC... stacking of PdSi<sub>3</sub> layers (a' = b' = 2a, c' = 8c). The highest-symmetry space group compatible with the superlattice ordering is *Fddd* [19]. Black lines show inter-layer bonds with six Si neighbors.

as Gd<sub>2</sub>PdSi<sub>3</sub>, it is crucial to understand the system's underlying magnetic interactions. The experimental observation of Fermi surface nesting with a wavevector similar to **q** suggests the relevance of long-ranged RKKY interactions [26], while a theoretical study indicates that local exchange processes are also important [27]. However, quantifying the interactions experimentally is a complex problem, for three main reasons. First, the ordered magnetic structure in zero applied field is not conclusively solved [10, 17, 28]. Second, although the crystal structure may be approximately described with a statistical distribution of Pd and Si, these atoms actually form a superlattice that may affect exchange processes [Fig. 1(c)] [14]. Third, the large neutron-absorption cross-section of isotopically-natural Gd makes neutron-scattering experiments on large single crystals challenging. So far, this has prevented the use of neutron-scattering experiments to understand the magnetic interactions of  $Gd_2PdSi_3$ .

Here, we employ neutron-scattering experiments on <sup>160</sup>Gd<sub>2</sub>PdSi<sub>3</sub> to obtain a model of its zero-field magnetic structure and interactions that explains multiple experimental observations. We obtain the following key results. First, magnetic interactions within triangular layers are spatially extended and of competing sign. Second, ferromagnetic interactions between layers are dominant, and strongly modulated by the Pd/Si superlattice. Third, below  $T_N$ , a helix with the spin plane perpendicular to  $\mathbf{q}$  is the only structure consistent with our neutron data and physical constraints, suggesting the magnetic dipolar interaction plays a significant role below  $T_{\rm N}$ [29]. Finally, we confirm that our interaction model explains the skyrmion crystal at small applied magnetic fields below  $T_{\rm N}$  [10, 30]. Our results provide a foundation for theoretical modeling and experimental manipulation of spin textures in Gd<sub>2</sub>PdSi<sub>3</sub>.

We prepared a polycrystalline sample of  ${}^{160}$ Gd<sub>2</sub>PdSi<sub>3</sub> (mass ~0.8 g) by arc melting. Arc-melted samples were wrapped in Ta foil, sealed in a quartz tube under a vacuum, and annealed at 800 C for one week. The sample quality was confirmed by bulk magnetometry and by powder X-ray diffraction, which reveals broad superlattice peaks consistent with 126(6) Å domains of the superstructure shown in Fig. 1(c) [19]. To minimize neutron absorption, the sample was 98.1% enriched with <sup>160</sup>Gd, and an annular sample geometry was used for neutron diffraction and spectroscopy experiments, which were performed using the HB-2A and SE-QUOIA instruments at ORNL, respectively.

Figure 2(a) shows magnetic diffuse-scattering data I(Q)collected above  $T_N$  using HB-2A ( $\lambda = 2.4067$  Å). The data are background-subtracted and placed in absolute intensity units by normalization to the nuclear Bragg scattering. As the sample is cooled below 40 K, I(Q) increases at small wavevectors,  $Q \leq 0.3 \,\text{\AA}^{-1}$ , indicating the development of predominantly ferromagnetic short-range correlations. Figure 2(b) shows that the bulk magnetic susceptibility  $\chi T$  exhibits a large upturn over the same temperature range, as expected because  $\chi T \propto I(\mathbf{Q} = \mathbf{0})$  at high temperature [31]. For RKKY interactions with Fermi wave-vector  $k_{\rm F}$ , theory predicts an increase in  $I(Q \leq 2k_{\rm F})$  as  $T_{\rm N}$  is approached from above, with a simultaneous upturn in the resistivity [32]. To test this prediction, Fig. 2(c) compares  $I(Q \rightarrow 0)$ —obtained from  $\chi T$  and by averaging I(Q) over  $0.1 \le Q \le 0.3 \text{ Å}^{-1}$ —with published resistivity measurements [16]. Both  $I(Q \rightarrow 0)$  and the resistivity shown an upturn at the same temperature ( $\sim 40$  K), in qualitative agreement with the RKKY prediction [32]. This result suggests that RKKY interactions may play a significant role in Gd<sub>2</sub>PdSi<sub>3</sub>.

We quantify the magnetic interactions by analyzing I(Q)



Figure 2. (a) Magnetic diffuse scattering above  $T_N$ , showing experimental data (black circles), model fits (red lines), and data-fit (blue lines). Successive curves are shifted vertically by 50 bn sr<sup>-1</sup> Gd<sup>-1</sup>. Data collected and fitted at 35 K, 45 K, and 60 K follow the same trends and are omitted for clarity. The dotted green line shows the 22 K fit with five intra-layer couplings and  $J_c = 0$ . (b) Bulk magnetic susceptibility data and fit (colors as above). (c) Comparison of  $I(Q \rightarrow 0)$  from neutron data (green circles) and magnetic susceptibility data (solid green line) with published resistivity data from Ref. 16 (orange squares). (d) Dependence of goodness-of-fit metric  $R_{wp}$  for neutron data (green circles) and susceptibility data (orange squares) on the number of intra-layer neighbors, n. Solid symbols show results when inter-layer coupling  $J_c$  was fitted, and open symbols show results for  $J_c = 0$ . (e) Dependence of  $J(\mathbf{Q})$  along high-symmetry paths ( $\Gamma = (000)$ ; K =  $(\frac{1}{3}\frac{1}{3}0)$ ; M =  $(\frac{1}{2}00)$ ). Positions of global and local maxima in  $J(\mathbf{Q})$  are shown by long black and short gray arrows, respectively.

and  $\chi T$  data measured at  $T > T_N$  within a Heisenberg model,

$$H_{\rm ex} = -\frac{1}{2} \sum_{i,j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j, \qquad (1)$$

where  $\mathbf{S}_i$  denotes a classical spin vector with position  $\mathbf{R}_i$ and length  $\sqrt{S(S+1)}$ , and the interaction parameters  $J_{ij} \in \{J_1, J_2, J_3, J_4, J_c\}$  are shown in Fig. 1(a,b). We make two simplifying assumptions in this high-temperature analysis. First, we neglect non-Heisenberg terms such as the magnetic dipolar interaction and single-ion anisotropy, which have negligible effect above  $T_N$  because of their small energy scales [19]. Second, we assume the high-symmetry hexagonal structure,

$J_{\rm c}$ (K)	<i>J</i> <sub>1</sub> (K)	<i>J</i> <sub>2</sub> (K)	J <sub>3</sub> (K)	$J_4$ (K)
1.97(46)	0.31(9)	0.19(15)	0.27(18)	-0.21(5)

Table I. Fitted values of magnetic interaction parameters. Parameter uncertainties indicate  $3\sigma$  confidence intervals.

neglecting a possible variation in  $J_{ij}$  due to the Pd/Si superstructure. To calculate I(Q) from the  $J_{ij}$ , we apply reactionfield theory, a self-consistent mean-field theory that gives good agreement with classical Monte Carlo simulations [33– 35]. Within reaction-field theory, the wavevector-dependent susceptibility  $\chi(\mathbf{Q}) = \chi_0 / \{1 - \chi_0[J(\mathbf{Q}) - \lambda]\}$  [36], where  $J(\mathbf{Q}) = \sum_j J_{ij} \exp(i\mathbf{Q} \cdot \mathbf{R}_j), \ \chi_0 = S(S+1)/3, \ \lambda$  is obtained self-consistently by enforcing that  $\int_{\text{BZ}} \chi(\mathbf{Q}) d\mathbf{Q} = S(S+1)$ [36], and I(Q) is calculated by spherically averaging  $I(\mathbf{Q}) =$  $cT[f(Q)]^2 \chi(\mathbf{Q})$ , where c = 0.1937 bn [31] and f(Q) is the Gd<sup>3+</sup> magnetic form factor [37].

We first tested a two-dimensional model by setting  $J_{\rm c} = 0$ and refining the intra-layer couplings  $\{J_1, ..., J_n\}$  to our I(Q)and  $\chi T$  data shown in Fig. 2(a) and (b). This model does not represent the data well. By contrast, also refining the interlayer coupling  $J_c$  substantially improves the refinement quality metric  $R_{wp}$  [Fig. 2(d)], demonstrating that the interactions are three-dimensional. To estimate the spatial extent of the interactions, Fig. 2(d) shows the dependence of  $R_{wp}$  on the number of  $J_n$  fitted in addition to  $J_c$ . No significant improvement is obtained for n > 4; hence, our minimal model contains  $\{J_1, J_2, J_3, J_4, J_c\}$ . The optimal parameter values from a global fit to I(Q) and  $\chi T$  data are given in Table I. Including dipolar interactions does not significantly affect the refined  $J_{ii}$  [19]. Ferromagnetic  $J_c$  is dominant, while intralayer interactions compete between antiferromagnetic  $J_4$  and shorter-range ferromagnetic couplings, resembling an RKKY interaction [38, 39]. Figure 2(e) shows the corresponding  $J(\mathbf{Q})$ , which is maximal at the calculated propagation vector,  $\mathbf{q}_{calc} \approx [0.12, 0, 0]^*$ . Notably, the energy scale  $S(S+1)J(\mathbf{q}_{calc})$ is similar to first-principles results [27, 40]. While  $q_{calc}$  is smaller than the measured low-temperature  $\mathbf{q} \approx [0.14, 0, 0]^*$ , the difference is plausible because  $\mathbf{q}$  decreases with increasing temperature below  $T_N$  [10]. Interestingly, a local  $J(\mathbf{Q})$ maximum occurs along the  $[110]^*$  direction with < 0.2% energy difference from  $J(\mathbf{q}_{calc})$ . Fermi-surface measurements of Gd<sub>2</sub>PdSi<sub>3</sub> show a nesting wavevector  $\sim \left[\frac{1}{6}\frac{1}{6}0\right]^*$  [26], while Tb<sub>2</sub>PdSi<sub>3</sub> exhibits short-range magnetic ordering with this periodicity [41], suggesting quasi-degeneracy may be generic to these materials. Finally, we considered an alternative fiveparameter model containing two inter-layer and three intralayer couplings. While this model yields a comparable refinement of I(Q) and  $\chi T$  measurements, it does not agree well with inelastic neutron-scattering data [19].

We now investigate the zero-field magnetic structure for  $T < T_{\rm N}$ . Taking the hexagonal structure as the parent phase, there are three magnetic irreducible representations (irreps) that correspond, respectively, to sinusoidal modulations of the Gd ordered magnetic moment  $\mu_{\rm ord}$  along orthogonal direc-



Figure 3. (a) Sinusoidal spin-density wave with spin axis perpendicular to **q**. (b) "Proper screw" helix with spin plane perpendicular to **q**. (c) Magnetic diffraction data at 1.5 K (black circles), model fits (red lines), and data-fit (blue lines). (d) Magnetic diffraction data, fits and data-fit (colors as above) on an expanded *Q*-axis scale for models (vi) and (vii), showing broadening of peaks with  $l \neq 0$  and improved fit for the elliptical helix (vii) compared to the circular helix (vi). (e) Goodness-of-fit metric  $R_{wp}$  for each model. (f) Maximum refined value of the ordered magnetic moment  $\mu_{ord}$  per Gd<sup>3+</sup> for each model. Parameter uncertainties represent 1 $\sigma$  confidence intervals. For model (vii),  $\mu_{ord} \parallel \mathbf{b}$  is shown as a gray bar.

tions **a**<sup>\*</sup>, **b**, and **c** [Fig. 3(a)] [42]. Alternatively, combining pairs of irreps yields helices with  $\mu_{ord}$  in the *ab*, *a*<sup>\*</sup>*c*, or *bc* plane [Fig. 3(b)]. Helical and sinusoidal models have been proposed for the zero-field structure of Gd<sub>2</sub>PdSi<sub>3</sub> [27, 28]. A triple-**q** meron-antimeron structure was also proposed [10]. In Fig. 3(c), we compare the Rietveld refinement for each model with the magnetic diffraction pattern, obtained as the difference between the 1.5 K and 25 K data. All magnetic Bragg peaks are explained by Gd magnetic ordering, indicating that any Pd magnetic polarization is below the detection limit of our data. For each model, Fig. 3(e) shows  $R_{wp}$ , and Fig. 3(f)



Figure 4. (a) Inelastic neutron-scattering data measured at T = 5.8 K with  $E_i = 11$  meV. Data are corrected for detailed balance and diffuse scattering is subtracted. (b) Linear spin-wave theory (LSWT) calculation for the interaction parameters given in Table I. (c) LSWT calculation with  $J_c$  split by  $\Delta = 0.8$  (defined in the text) for Pd/Si superlattice ordering with periodicity (2a, 2a, c). (d) LSWT calculation with  $J_c$  split by  $\Delta = 0.8$  for Pd/Si superlattice ordering with periodicity (2a, 2a, c). (d) LSWT calculation with  $J_c$  split by  $\Delta = 0.8$  for Pd/Si superlattice ordering with periodicity (2a, 2a, 8c). Each panel contains a color plot (left) of  $\sqrt{I(Q, E)}$ , and line cuts of intensity  $I_{avg}$  averaged over 0.5 < Q < 0.7 Å<sup>-1</sup> (black circles) and 0.5 < Q < 2.0 Å<sup>-1</sup> (blue squares).

shows the refined maximum value of  $\mu_{ord}$ . The **a**<sup>\*</sup>-sine model (i), with spins  $\mathbf{S} \parallel \mathbf{q}$ , would give zero intensity for the strong (q00) magnetic peak, and so is ruled out. Of the remaining models, b-sine (ii), bc-helix (vi), and bc-ellipse (vii) structures yield similarly high-quality refinements. The meronantimeron structure has an identical diffraction pattern to its single-q analog, the *bc*-helix, and is not shown separately. The refined  $\mu_{ord}$  is a key discriminating factor, as any physical model must satisfy the constraint that  $\max(\mu_{ord}) \leq 2S\mu_{B}$  $(=7.0\mu_{\rm B} \text{ for } {\rm Gd}^{3+})$  to ensure consistency with magnetic susceptibility and saturation magnetization measurements. This constraint rules out the **b**-sine model with  $max(\mu_{ord}) = 8.7\mu_{B}$ [Fig. 3(f)]. It also disfavors the meron-antimeron structure, for which  $\max(\mu_{ord}) = \frac{3}{2}\mu_{ord}^{helix}$ , where  $\mu_{ord}^{helix} = 6.14(7)\,\mu_{B}$  is the refined ordered moment of the bc-helix. Thus, the key result of our Rietveld analysis is that only "proper screw" helices with  $\mathbf{S} \perp \mathbf{q}$ , models (vi) and (vii), yield good fits and reasonable  $\mu_{ord}$  values. The best such refinement is for an elliptical helix with  $\mu_{\parallel c} = 5.13(7) \,\mu_{\rm B}$ , and  $\mu_{\parallel b}$  fixed to 7.0  $\mu_{\rm B}$ . Notably, the ordered moment is not fully polarized as  $\mu_{ord}^{helix} < 2S\mu_{B}$ at 1.5 K. Magnetic peaks are also selectively broadened compared to nuclear peaks [Fig. 3(d)]. Refinement of a quadraticin-l size-broadening term yields magnetic domain dimensions of 332(8) Å in the *ab*-plane vs. 27(2) Å along **c**, which may be a consequence of the disordered stacking of PdSi<sub>3</sub> layers indicated by our X-ray diffraction data [14, 19].

The magnetic excitation spectrum at  $T \ll T_N$  provides a

sensitive test of our model. Our inelastic neutron-scattering data ( $E_i = 11 \text{ meV}$ ) show spin-wave excitations at T = 5 K, superimposed on a diffuse magnetic background that likely occurs because  $\mu_{\text{ord}}^{\text{helix}} < 2S\mu_{\text{B}}$ . In Fig. 4(a), we show  $I'_{5\text{K}} = I_{5\text{K}} - [1 - (\mu_{\text{ord}}^{\text{helix}}/2S\mu_{\text{B}})^2]I_{25\text{K}}$ , which isolates the spin-wave contribution. Our data show an overall bandwidth of approximately 4 meV. For E < 4 meV, the spectrum has a broad energy dependence with intensity minima for  $0 \leq E \leq 1 \text{ meV}$ and  $2 \lesssim E \lesssim 3 \,\mathrm{meV}$  that are most apparent at small  $Q \lesssim$  $0.7 \text{ Å}^{-1}$ . Figure 4(b) shows the calculated spectrum for the interaction parameters given in Table I and a single-q helical ground state, calculated within linear spin-wave theory [43] using the SpinW program [44]. Including the dipolar interaction has only a small effect on the spectrum [19]. This model reproduces the overall bandwidth, but fails to explain the intensity minimum for  $2 \le E \le 3$  meV. Attempts to refine  $\{J_1, J_2, J_3, J_4, J_c\}$  to the inelastic data also failed to reproduce this feature. To explain our data, it was necessary to consider the effect of the Pd/Si superstructure on  $J_c$ . All proposed models of the Pd/Si superstructure involve doubling the unit cell along **a** and **b**, such that 75% of  $J_c$  bonds (notated  $J_{c+}$ ) have four Si and two Pd neighbors, while the remaining  $J_{\rm c}$ bonds (notated  $J_{c-}$ ) have six Si neighbors [Fig. 1(c)]. We assume the superstructure splits  $J_c$  by an amount  $\Delta J_c$ , such that  $J_{c+} = J_c(1 + \Delta/4)$  and  $J_{c-} = J_c(1 - 3\Delta/4)$ , and neglect any splitting of the weaker interactions. For the (2a, 2a, 8c) superstructure shown in Fig. 1(c), the stacking of  $J_{c\pm}$  bonds is ...ABCDBADC... [14], whereas the (2a, 2a, c) superstructure considered in Ref. 27 has ...AAA... stacking. Taking  $\Delta = 0.8$ with the (2a, 2a, c) superstructure reproduces the intensity minimum for  $2 \leq E \leq 3$  meV and yields good overall agreement with our inelastic neutron-scattering data [Fig. 4(c)], without degrading the agreement with I(Q) data above  $T_N$ [19]. Taking  $\Delta = 0.8$  with the (2a, 2a, 8c) superstructure also generates intensity minima, but yields worse agreement with our data [Fig. 4(d)]. Our results show that the Pd/Si superstructure strongly enhances  $J_c$  for bonds with Pd neighbors, perhaps consistent with a superexchange contribution here.

We use extensive Monte Carlo simulations [45] to calculate the phase diagram of our model as a function of temperature T and applied magnetic field **B** || **c**. The spin Hamiltonian is given by

$$H = H_{\text{ex}} + g\mu_{\text{B}}B\sum_{i}S_{i}^{z} + D\sum_{i>j}\frac{\mathbf{S}_{i}\cdot\mathbf{S}_{j} - 3\left(\mathbf{S}_{i}\cdot\hat{\mathbf{r}}_{ij}\right)\left(\mathbf{S}_{j}\cdot\hat{\mathbf{r}}_{ij}\right)}{\left(r_{ij}/r_{1}\right)^{3}},$$
(2)

where, to stabilize helical ordering with  $\mathbf{S} \perp \mathbf{q}$ , we include the magnetic dipolar interaction with magnitude D = 0.037 K at the nearest-neighbor distance  $r_1$  [29, 46]. To minimize finite-size effects, we constrain the interactions to stabilize  $\mathbf{q}_{MC} = [q_{MC}00]^* \approx \mathbf{q}_{calc}$ , with commensurate  $q_{MC} = \frac{1}{8}$  or  $\frac{1}{9}$ . The calculated magnetic susceptibility  $\chi_{zz}^{calc}(B,T)$  is shown in Fig. 5(a), and reveals both similarities and differences with experiment [30, 47]. In agreement with experiment, we find  $T_N^{calc} \approx 20$  K, and below  $T_N$ , a transition from a helical to a skyrmion crystal at small *B* (calculated as 0.25 T; c.f. 0.38 T



Figure 5. (a) Calculated magnetic susceptibility  $\chi_{zz}^{calc}$  and estimated phase boundaries (green crosses) for our interaction model, obtained using Monte Carlo simulations. Results are shown for  $q_{MC} = \frac{1}{9}$  and a 9 × 9 × 9 supercell of the hexagonal unit cell. (b) Calculated  $\chi_{zz}^{calc}$  at T = 15 K for the distorted (2a, 2a, c) supercell with  $\Delta = 0.8$  and  $q_{MC} = \frac{1}{8}$  (green circles), and the undistorted structure with  $\Delta = 0$  and  $q_{MC} = \frac{1}{9}$  (orange squares). The calculated magnetic diffraction patterns are for each phase are shown above, for B = 0.11, 0.40, and 0.79 T (left to right). The values of *B* are scaled by the quantum correction factor  $\sqrt{(S+1)/S} \approx 1.134$ .

experimentally [30]). At larger *B*, a further transition occurs to a topologically-trivial triple-**q** phase previously identified using mean-field theory [29]. The single-**q** *vs*. triple-**q** nature of each phase is revealed by its calculated magnetic diffraction pattern [insets in Fig. 5(b)]. The behavior is not qualitatively affected by the splitting of  $J_c$ , or by the precise value of  $q_{MC}$  [Fig. 5(b)]. Given the simplicity of our model, its reasonable agreement with experiment at small *B* is satisfying; however, it does not explain the large increase in saturation field on cooling the sample ( $B_{sat} \approx 8 \text{ T}$  at 2 K [30]) or the presence of magnetic transitions for B > 1 T [47]. These differences motivate further theoretical work to understand the role of non-Heisenberg interactions.

Our neutron-scattering results provide an experimental understanding of the magnetic interactions in  $Gd_2PdSi_3$  and clarify its zero-field magnetic structure. This approach may provide insight into other centrosymmetric skyrmion materials, such as  $Gd_3Ru_4Al_{12}$  and  $GdRu_2Si_2$  [11, 13]. Notably, our interaction model explains key aspects of the experimental behavior without invoking biquadratic or multi-spin interactions [48]. However, the spin dynamics can only be understood by accounting for the Pd/Si superstructure, suggesting it is important to include this in models. We anticipate that this model of the skyrmion stabilization mechanism in  $Gd_2PdSi_3$  will facilitate design and identification of new centrosymmetric skyrmion hosts, including in materials where large single-crystal samples are unavailable or unsuitable for neutron-scattering measurements.

We are grateful to Cristian Batista, Matthew Cliffe, Randy Fishman, Shang Gao, and Stephen Nagler for valuable discussions. This work was supported by the U.S. Department of Energy, Office of Science, Basic Energy Sciences, Materials Sciences and Engineering Division. This research used resources at the High Flux Isotope Reactor and Spallation Neutron Source, DOE Office of Science User Facilities operated by the Oak Ridge National Laboratory. The isotope used in this research was supplied by the U.S. Department of Energy Isotope Program, managed by the Office of Isotope R&D and Production.

- \* paddisonja@ornl.gov
- <sup>†</sup> christiansad@ornl.gov
- [1] Y. Tokura, N. Kanazawa, Chem. Rev. 121, 2857 (2021).
- [2] A. Fert, N. Reyren, V. Cros, Nat. Rev. Mater. 2, 17031 (2017).
- [3] A. N. Bogdanov, C. Panagopoulos, *Nat. Rev. Phys.* 2, 492 (2020).
- [4] S. Mühlbauer, et al., Science 323, 915 (2009).
- [5] X. Z. Yu, et al., Nature 465, 901 (2010).
- [6] T. Okubo, S. Chung, H. Kawamura, *Phys. Rev. Lett.* 108, 017206 (2012).
- [7] A. O. Leonov, M. Mostovoy, Nat. Commun. 6, 8275 (2015).
- [8] X. Yu, et al., Proc. Nat. Acad. Sci. 109, 8856 (2012).
- [9] X. Yao, J. Chen, S. Dong, New J. Phys. 22, 083032 (2020).
- [10] T. Kurumaji, et al., Science **365**, 914 (2019).
- [11] M. Hirschberger, et al., Nat. Commun. 10, 5831 (2019).
- [12] S. Gao, et al., Nature 586, 37 (2020).
- [13] N. D. Khanh, et al., Nat. Nanotechnol. 15, 444 (2020).
- [14] F. Tang, et al., Phys. Rev. B 84, 104105 (2011).
- [15] P. Kotsanidis, J. Yakinthos, E. Gamari-Seale, J. Magn. Magn. Mater. 87, 199 (1990).
- [16] S. R. Saha, et al., Phys. Rev. B 60, 12162 (1999).
- [17] H. Zhang, et al., New J. Phys. 22, 083056 (2020).
- [18] R. Mallik, E. V. Sampathkumaran, M. Strecker, G. Wortmann, *Europhys. Lett. (EPL)* 41, 315 (1998).
- [19] See supplemental material for supplemental figures, tables of refinement results, experimental and computational methods, and Refs. 20-25.
- [20] F. James, M. Roos, Comp. Phys. Commun. 10, 343 (1975).
- [21] F. James, MINUIT Function Minimization and Error Analysis: Reference Manual Version 94.1, CERN (1994).
- [22] T. Proffen, T. R. Welberry, Acta Crystallogr. A 53, 202 (1997).
- [23] M. Enjalran, M. J. P. Gingras, Phys. Rev. B 70, 174426 (2004).
- [24] Z. Wang, C. Holm, J. Chem. Phys. 115, 6351 (2001).
- [25] I. A. Blech, B. L. Averbach, Physics 1, 31 (1964).
- [26] D. S. Inosov, et al., Phys. Rev. Lett. 102, 046401 (2009).
- [27] T. Nomoto, T. Koretsune, R. Arita, *Phys. Rev. Lett.* **125**, 117204 (2020).
- [28] S. H. Moody, et al., arXiv 2010.14326 (2021).
- [29] O. I. Utesov, Phys. Rev. B 105, 054435 (2022).
- [30] M. Hirschberger, et al., Phys. Rev. B 101, 220401 (2020).
- [31] S. W. Lovesey, Theory of Neutron Scattering from Condensed Matter: Polarization Effects and Magnetic Scattering, vol. 2 (Oxford University Press, Oxford, 1987).
- [32] Z. Wang, K. Barros, G.-W. Chern, D. L. Maslov, C. D. Batista, *Phys. Rev. Lett.* **117**, 206601 (2016).
- [33] D. Hohlwein, J.-U. Hoffmann, R. Schneider, *Phys. Rev. B* 68, 140408 (2003).
- [34] P. H. Conlon, J. T. Chalker, Phys. Rev. B 81, 224413 (2010).
- [35] G. Pokharel, et al., Phys. Rev. Lett. 125, 167201 (2020).
- [36] D. E. Logan, Y. H. Szczech, M. A. Tusch, *Europhys. Lett. (EPL)* 30, 307 (1995).
- [37] P. J. Brown, International Tables for Crystallography (Kluwer Academic Publishers, Dordrecht, 2004), vol. C, chap. Magnetic

Form Factors, pp. 454-460.

- [38] Z. Wang, Y. Su, S.-Z. Lin, C. D. Batista, Phys. Rev. Lett. 124, 207201 (2020).
- [39] Z. Wang, C. D. Batista, arXiv 2111.13976 (2021).
- [40] J. Bouaziz, E. Mendive-Tapia, S. Blügel, J. B. Staunton, *Phys. Rev. Lett.* **128**, 157206 (2022).
- [41] M. Frontzek, et al., J. Phys.: Condens. Matter 19, 145276 (2007).
- [42] A. Wills, J. Phys. IV France 11, 133 (2001).

- [43] R. S. Fishman, J. A. Fernandez-Baca, T. Rõõm, Spin-Wave Theory and its Applications to Neutron Scattering and THz Spectroscopy, 2053-2571 (Morgan and Claypool Publishers, 2018).
- [44] S. Toth, B. Lake, J. Phys.: Condens. Matter 27, 166002 (2015).
  [45] M. E. J. Newman, G. T. Barkema, Monte Carlo Methods in
- Statistical Physics (Oxford University Press, Oxford, 1999). [46] O. I. Utesov, Phys. Rev. B 103, 064414 (2021).
- [47] S. Spachmann, A. Elghandour, M. Frontzek, W. Löser, R. Klingeler, *Phys. Rev. B* 103, 184424 (2021).
- [48] S. Hayami, Y. Motome, Phys. Rev. B 103, 024439 (2021).