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# Quasiparticle trapping at vortices producing Josephson supercurrent enhancement

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The Josephson junction of a strong spin-orbit material under a magnetic field is a promising Majorana fermion candidate. Supercurrent enhancement by a magnetic field has been observed in the InAs nanowire Josephson junctions and assigned to a topological transition. In this work we observe a similar phenomenon but discuss the non-topological origin by considering trapping of quasiparticles by vortices that penetrate the superconductor under a finite magnetic field. This assignment is supported by the observed hysteresis of the switching current when sweeping up and down the magnetic field. Our experiment shows the importance of quasiparticles in superconducting devices with a magnetic field, which can provide important insights for the design of quantum qubits using superconductors.

## Introduction

Combining an s-wave superconductor with a semiconductor nanowire (NW) made of strong spin-orbit interaction (SOI) materials, such as InAs and InSb, is of experimental interest, because it induces a topological transition to the topological superconductor (TSC) phase with suitable magnetic fields and chemical potential [1, 2]. The TSC phase of the NW coupled to the superconductor has Majorana fermions (MFs) at the edge. The MFs are expected to be applied to topologically protected quantum computing because of their non-abelian statistics, and recently, research on superconductor-semiconductor NW hybrid systems has been developed to find and control the MFs [3, 4]. In the literature, the zero-bias conductance peak [5–9], missing odd Shapiro steps [10], Josephson emission at half of the fundamental radiation frequency [11], and enhancement of supercurrent (SC) [12] have been presented as experimental evidence of MFs in the TSC phase. In these studies, the magnetic field is a crucial parameter that induces nontrivial topological states. However, there have been criticisms of the experimental evidence. Critics argue that the observed phenomena can arise from a trivial source unrelated to the MFs. For example, the zero-bias conductance peak can be attributed to the Andreev bound state (ABS) [13–17] or weak anti-localization [18]. In addition, 51

the missing odd integer Shapiro steps can be explained by non-adiabatic dynamics such as the Landau-Zener transition of the highly transparent Josephson junctions [19]. These recent criticisms indicate that thorough experimental study and careful data analysis to identify the origin of the novel superconducting transport phenomena are of great importance, significantly, for the establishment of not only TSC and MF physics but also the development of superconducting device physics.

In this report, we focus on the magnetic field-induced enhancement of SC in the Josephson junction of a single InAs NW [12]. This enhancement shows that the switching current almost doubles above a certain magnetic field  $B^*$  as the positive out-of-plane magnetic field is swept from 0 mT. In the first place, this previous report discusses that the most critical contribution to the enhancement is the existence of MFs induced by the magnetic field. In contrast, we have previously reported a similar experimental study [20] on the Josephson junction of an InAs single NW, where we found an enhancement of SC for the in-plane parallel magnetic field in the NW direction. We concluded that this enhancement can be interpreted as low-pass filter formation, which is not related to the presence of MFs. However, in this experimental report, we did not study the out-of-plane SC enhancement which is the most remarkable in the previous report [12]. Therefore, it is valuable to revisit the SC enhancement

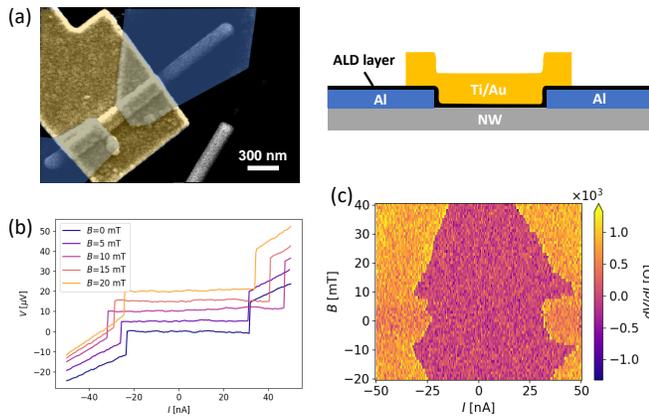


FIG. 1. (a) Left: SEM image of an InAs single NW Josephson junction device with a top gate electrode (yellow). The junction separation between the two Al (blue) electrodes was approximately 200 nm. The NW looks thicker than 80 nm because of the  $\text{Al}_2\text{O}_3$  layer. Right: Schematic view of cross section along NW. (b) Examples of  $V$  vs.  $I$  measured for various magnetic fields. Each curve was offset by  $5 \mu\text{V}$ . (c)  $dV/dI$  as a function of  $I$  and  $B$ .  $I_{\text{sw}}$  had a maximum at  $B = 10 \text{ mT}$ .

with the out-of-plane magnetic field.

For this purpose, we fabricated a Josephson junction on an epitaxially grown InAs single NW and performed a DC measurement of the SC in a dilution refrigerator. Consequently, we observed the enhancement of the SC, as reported in a previous study [12, 20]. To determine the origin of the enhancement, we measured the switching current evolution with the gate voltage and magnetic field. Then, we found that  $B^*$  does not depend on the gate voltage, and the magnetic field dependence shows a clear hysteresis with respect to the magnetic field sweep direction. These results suggest that the magnetic-field-induced SC enhancement is related to the vortices penetrating the superconducting electrodes. Thus, we assign the enhancement origin to quasiparticles trapped in the vortex cores. We confirmed that the  $B^*$  dependence on the applied magnetic field angle supports the quasiparticle trapping scenario. Our results will contribute to the physics of superconducting devices and especially sort anomalous superconducting transport phenomena into trivial and nontrivial topological natures.

## Results

In this study, a Josephson junction was fabricated on an InAs single NW placed on a Si substrate. A scanning electron microscopy (SEM) image of the complete device and a schematic picture of cross section along the NW are shown in Fig. 1(a). We used two superconductor Al electrodes that were separated by approximately 200 nm. The carrier density of the NW was controlled using

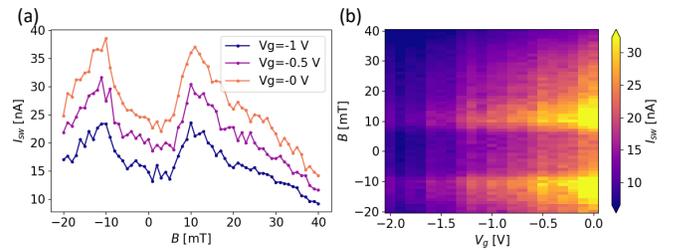


FIG. 2. (a)  $I_{\text{sw}}$  as a function of  $B$  at different  $V_g$ . (b)  $I_{\text{sw}}$  as a function of  $B$  and  $V_g$ .  $B^*$  is found to be independent of  $V_g$ .

top gate electrode. The voltage  $V$  across the junction as a function of the current  $I$  measured under various magnetic fields for a bath temperature of  $T = 37 \text{ mK}$  is shown in Fig. 1(b). Figure 1(c) shows the differential resistance  $dV/dI$  as a function of the bias current  $I$  and out-of-plane magnetic field  $B$  for the device at  $V_g = 0 \text{ V}$ .

The boundary identified by the color change gives the magnitude of the SC and switching current  $I_{\text{sw}}$ . The  $I_{\text{sw}}$  at  $B = 0 \text{ mT}$  was  $30 \text{ nA}$  and gradually increased as  $B$  increased to  $10 \text{ mT}$ , where it reached a maximum. We denoted this maximum point as  $B^*$ .  $I_{\text{sw}}$  then decreased and vanished at  $B = 60 \text{ mT}$ . This result is similar to the previous report [12], including in terms of the magnitude of the enhancement. It should be noted that  $dV/dI$  in the SC region remains zero at all measured  $B$ . This is a significant difference from the in-plane magnetic field case in Ref. [20], because the enhancement with the in-plane field is derived from partial breakdown of SC due to difference in thickness, which ends up as the formation of low-pass filters, causing the finite  $dV/dI$  at  $|B| > |B^*|$ .

To investigate whether the enhancement originated from the NW or superconducting metals, we varied the electron density of the NW by  $V_g$ . Figures 2(a) and (b) show  $I_{\text{sw}}$  as a function of  $B$  and  $V_g$ . Note that the junction can be completely depleted at  $V_g = -5.1 \text{ V}$  (See S.M. §1). The maximum point  $B^*$  remained constant, whereas  $I_{\text{sw}}$  changed with varying the electron density of the NW with  $V_g$ . This result indicates that the enhancement did not originate from the NW between the two superconducting electrodes but the superconducting metals or NW beneath the superconducting metals. If the enhancement originated from the MF contributions,  $B^*$  would change as  $V_g$  changes because the  $B$  corresponding to the topological transition depends on the Fermi energy of the NW. Therefore, the observed enhancement of the SC cannot be attributed to the appearance of the TSC phase. Because  $B^*$  did not depend on  $V_g$ , the enhancement must have been caused by magnetic field-induced phenomena generated in the superconducting electrodes rather than in the NW.

We study  $dV/dI$  dependence on  $I$  and  $B$  by changing the direction of the magnetic field, as shown in Fig. 3(a). The magnetic field was applied at an out-of-plane angle  $\phi$

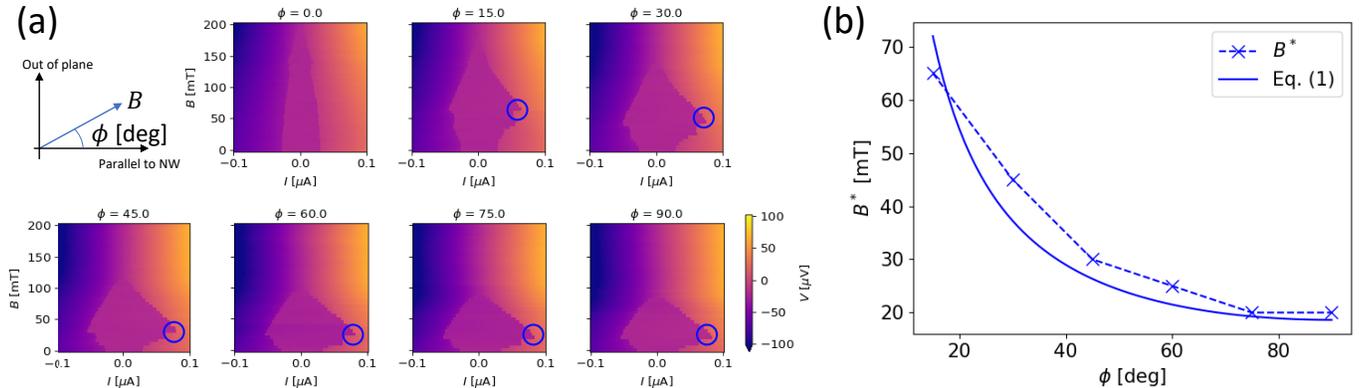


FIG. 3. (a) Bias voltage  $V$  as a function of  $B$  and  $I$ . The blue circles indicate  $B^*$ . (b) Magnetic field  $B^*$  vs.  $\phi$  (blue crosses). The blue solid line is the fitting result of the  $B^*$  vs.  $\phi$  data points to Eq. (1). The fitting parameter is given as  $A = 18.6(11)$  mT.

154 measured from the plane. We observed an increase in the 184  
 155 critical field as the applied  $B$  tilts from the out-of-plane 185  
 156 ( $\phi = 90^\circ$ ) to the in-plane ( $\phi = 0^\circ$ ) direction. In Fig. 3(a), 186  
 157 the enhancement peak points  $B^*$  are highlighted with 187  
 158 blue circles. 188

Here, we fit  $B^*$  (crosses in Fig. 3(b)) as a function of 189  
 the angle  $\phi$  using the following formula: 190

$$B^* = \frac{A}{\sin \phi}, \quad (1) \quad 191$$

192 where  $A$  corresponds to the out-of-plane component of 193  
 159  $B^*$ . The solid line in Fig. 3(b) shows the calculated 194  
 160 magnetic field of Eq. (1) compared to the experimentally 195  
 161 obtained  $B^*$ . The good agreement with the experiment 196  
 162 indicates that only the out-of-plane magnetic field com- 197  
 163 ponent determines  $B^*$ . 198

199 Finally, we investigated the  $B$  dependence of  $I_{sw}$  when 200  
 166  $B$  was swept in different directions. Figures 4 (a), (b) and 201  
 167 (c) show  $I_{sw}$  as a function of  $B$  at  $T = 37$  mK, 375 mK, 202  
 168 and 425 mK, respectively. The blue (purple) lines rep- 203  
 169 resent the upward (downward) sweep. Here, we found a 204  
 170 clear hysteresis of  $I_{sw}$  depending on the  $B$  sweep direc- 205  
 171 tion, as shown in Fig. 4. The hysteresis was apparent for 206  
 172  $|B| < |B^*|$  while it did not appear for  $|B| > |B^*|$ . Fur- 207  
 173 thermore, in Fig. 4 (a),  $I_{sw}$  in  $-B^* < B < 0$  mT is larger 208  
 174 than that in  $0 < B < B^*$  in the sweep from negative 209  
 175 to positive and vice versa. In Figs. 4 (b) and (c), the 210  
 176 hysteresis appears between  $\pm B^*$  and dips around  $\pm 5$  mT 211  
 177 and has the same sweep direction dependence. Note that 212  
 178 the out-of-plane  $B$  dependence of  $I_{sw}$  in Ref. [12] is also 213  
 179 asymmetric for  $B^* > B > 0$  mT and  $-B^* < B < 0$  mT, 214  
 180 suggesting hysteresis. 215

## Discussion 216

182 We attribute the observed enhancement to quasipar- 220  
 183 ticle trapping by superconducting vortices. The vortices 221

penetrate a superconductor when a magnetic field ap-  
 184 plied to the superconductor exceeds the critical field  $B_{c1}$ .  
 185 Note that supercurrent enhancement has been observed  
 186 in similar nanowire systems [21, 22], but these results do  
 187 not show hysteresis of  $B$  field sweep, meaning the origins  
 188 of the enhancement are different from ours. The super-  
 189 conducting pair potential is broken at the vortex cores,  
 190 and they act as trapping potentials for quasiparticles.  
 191 These quasiparticles corresponds to the excited states in  
 192 the superconductors. Therefore, trapping at the vortex  
 193 cores makes the thermally excited quasiparticles relax to  
 194 the bound states in the cores whose energies are lower.  
 195 In the relaxation process, the thermally excited states  
 196 transfer their energies to the environment (heat bath)  
 197 as phonons (See S.M. §4). This type of quasiparticle  
 198 trapping can improve the superconducting device quality,  
 199 as observed in electron turnstile devices [23–25], because  
 200 the trapping effectively lowers the electron temperature.  
 201 This effect has been applied to the design of supercon-  
 202 ducting qubits, for example, forming vortices in the outer  
 203 region so that the system of interest is cooled down [26–  
 204 29]. The switching current  $I_{sw}$  is affected by thermally  
 205 excited quasiparticles, depending on the electron temper-  
 206 ature. Therefore, the observed SC enhancement can be  
 207 attributed to electron cooling due to quasiparticle trap-  
 208 ping.

In this scenario, the observed hysteresis is also reason-  
 216 able.  $B^*$  is the point that vortices enters the system, and  
 217 they always exist at higher  $B$  (where  $B < B_c$ ). The hys-  
 218 teresis appears, for example, when we sweep downward  
 219 from  $B > B^*$ . Here, some magnetic fluxes remain in the  
 220 system due to pinning effect by impurities or diffraction  
 221 and provide the cooling effect. This is consistent with the  
 result that  $I_{sw}$  of downward sweep is larger than one of  
 upward sweep where  $0 < B < B^*$ . When comparing the  
 results at several temperatures in Fig. 4, it is observed  
 that  $B^*$  (dashed lines) decreases with increasing  $T$ . This  
 indicates that  $B_{c1}$  becomes smaller as  $T$  increases, sup-

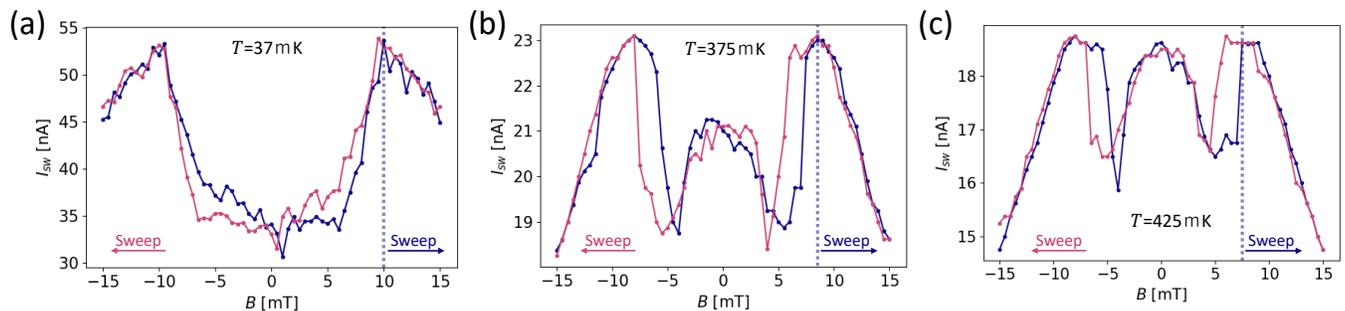


FIG. 4.  $I_{sw}$  vs.  $B$  at (a)  $T = 37$  mK, (b) 375 mK, (c) and 425 mK. The blue (purple) lines represent the results for the upward (downward) sweep. The hysteresis is visible for  $|B| < |B^*|$ .  $B^*$  determined in the upward sweep is shown as dashed lines.

porting the electron cooling scenario.

In addition, the enhancement at  $B = B^*$  gradually decreases as  $T$  increases. This behavior is consistent with the decrease in the electron cooling effect at higher temperatures, because the number of quasi-particles at higher temperatures increases. The order of the cooling effect can be estimated as 100 mK (See Fig. S5), which is comparable to a previous report on normal-metal/insulator/superconductor junction [27]. We note that the  $0-\pi$  transition of the junction and magnetic impurities in the NW cannot explain the hysteresis, even if they make  $B^*$  remain constant with  $V_g$ . For the same reason, the hysteresis cannot be attributed to the topological transition in the proximitized region.

Our results revealed that the enhancement of the switching current by an out-of-plane magnetic field is non-topological. However, to realize topological qubits using MFs [30, 31], it is important to reduce the quasi-particle density to protect the information of the qubits from quasiparticle poisoning. Even with a higher magnetic field, if the material is a type-II superconductor or thin film in which vortices can penetrate, the device can be designed to trap quasiparticles effectively so that the system of interest is cooled. Effectiveness of quasi-particle trapping is known to depend strongly on device structure [23], and therefore further studies for optimal design for cooling will be necessary. This report shows that quasiparticles in superconducting devices can be reduced by quasiparticle trapping under a finite perpendicular magnetic field, which provides important insights for the design of topological qubit devices in the near future.

## Methods

The InAs NW had a diameter of approximately 80 nm and was grown on an InAs(111)B substrate by chemical beam epitaxy [32]. A Josephson junction was fabricated on the NW after transferring it onto a 280 nm-thick  $\text{SiO}_2$  substrate by standard dry transfer technique with cotton buds. Ti/Au markers were fabricated on the

substrate in advance, so that we can determine positions of randomly spread NWs. We made a polymethyl methacrylate pattern for the contact areas using electron beam lithography and performed surface treatment using a  $(\text{NH}_4)_2\text{S}_x$  solution to remove the native surface oxidised layer. Then, the superconducting electrodes were fabricated by depositing Ti/Au (1 nm/60 nm) and lift-off. The top gate was fabricated by growth of 20 nm thick  $\text{Al}_2\text{O}_3$  by atomic layer deposition followed by depositing a gate electrodes of Ti/Au (50 nm/150 nm) [20, 32–35].

## Measurement setup

All measurements were done in a dilution fridge with a standard quasi-4-terminal method. The base temperature of the thermal bus was about 35 mK. The conductance was measured with lock-in amplifiers with an excitation voltage of 10  $\mu\text{V}$ . For the SC measurements, DC voltages across the device were measured with a constant current bias.

For the magnetic field dependent measurements, we swept the field at rate of 0.1 T/min and then wait 15 s before sweep of bias current.

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### Author contributions

K.U. and S.M. designed the device; Y.S., K.U., Y.T.,  
 H.K., S.M., S.T. joined discussions and their previous  
 results inspired the design; K.U. followed their fabrica-  
 tion process; K.L., L.S., H.Q.X. provided the nanowires  
 used in the experiment; Y.S. performed experiments with  
 input from K.U., S.M. and S.T.; Y.S. and K.U. wrote the  
 manuscript, with input from all authors; S.M. and S.T.  
 initiated the project.

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