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Bicircular Light Floquet Engineering of Magnetic Symmetry and Topology and Its Application to the Dirac Semimetal math xmlns="http://www.w3.org/1998/Math/MathML" display="inline">mrow>mrow>msub>Math/MathML" display="inline">mrow>mrow>msub>mrow>mi>Cd/mi>/ mrow>mrow>mn>3/mn>/mrow>/msub>/mrow>mi>Cd/mi>/ sub>mrow>mi>As/mi>/mrow>/msub>/mrow>mrow>m sub>mrow>mi>As/mi>/mrow>mrow>mn>2/mn>/mrow>/ msub>/mrow>/mrow>/math> Thaís V. Trevisan, Pablo Villar Arribi, Olle Heinonen, Robert-Jan Slager, and Peter P. Orth Phys. Rev. Lett. **128**, 066602 — Published 8 February 2022

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## Bicircular light Floquet engineering of magnetic symmetry and topolgy: application to Dirac semimetal Cd<sub>3</sub>As<sub>2</sub>

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We show that bicircular light (BCL) is a versatile way to control magnetic symmetries and topology in materials. The electric field of BCL, which is a superposition of two circularly polarized light waves with frequencies that are integer multiples of each other, traces out a rose pattern in the polarization plane that can be chosen to break selective symmetries, including spatial inversion. Using a realistic low-energy model, we theoretically demonstrate that the three-dimensional Dirac semimetal  $Cd_3As_2$  is a promising platform for BCL Floquet engineering. Without strain, BCL irradiation induces a transition to a non-centrosymmetric magnetic Weyl semimetal phase with tunable energy separation between the Weyl nodes. In the presence of strain, we predict the emergence of a magnetic topological crystalline insulator with exotic unpinned surface Dirac states that are protected by a combination of twofold rotation and time-reversal (2') and can be controlled by light.

Introduction.- Recent years have seen a surge of interest in symmetry-protected topological phases with unique properties arising from a nontrivial topology of the bulk band structure. Examples are topological (crystalline) insulators [1–4] with dissipationless metallic surface states, magnetic axion insulators with large magnetoelectric couplings [5-7], and three-dimensional (3D) Dirac and Weyl semimetals (SM) with exotic Fermi arc surface states [8]. Topological states also emerge in artificial systems such as cold atomic gases [9] and photonic waveguides [10]. The connection between symmetry and band topology is made explicit in classification schemes based on topological invariants like Chern and winding numbers [11], and in the more refined classification of crystalline materials using band compatibility relations [12–15], effectively generalize the parity indicator of Fu and Kane [16]. A particularly rich set of symmetry-protected topological phases arises from magnetic symmetries, which combine time-reversal (TR) with spatial symmetries, leading to a classification of phases in the 1651 magnetic space groups (MSGs) [17–19].

The relation between symmetry and topology not only facilitates the search for new realizations of symmetryprotected topological phases, but can also be employed to actively tune between different topological states by applying symmetry-breaking perturbations. Among them, periodic Floquet perturbations such as caused by irradiation with strong coherent light are particularly attractive since they allow for a *dynamic manipulation* on ultrafast time scales [20–25]. Floquet engineering of topological band structures has also been experimentally realized in artifical lattice systems [9, 26–29] and photonic systems [10, 30]. In real materials, light-control of symmetry has been achieved via a direct Floquet-dressing of electronic states using circularly polarized light (CL) [31, 32], but also via exciting resonant lattice modes [33–37], and via photocurrent generation [38]. It was experimentally shown that TR breaking via CL irradiation can induce a quantum anomalous Hall state in topological insulator (TI) surface states [31] and in graphene [32, 39].

Here, we show that Floquet engineering with bicircular light (BCL), which consists of a superposition of two CL waves with integer frequency ratio, offers an even greater tunability. The key idea is to use the polarization state of BCL to selectively break spatial symmetries, including inversion  $(\mathcal{I})$ , with direct consequences on band topology. This opens the possibility to realize non-centrosymmetric magnetic topological phases with unique, e.g., chiral and polar, properties. In two dimensions, the effect of BCL on graphene was recently discussed theoretically in Ref. 40. We here propose to use BCL to tune 3D topological semimetallic and insulating parent phases, where the presence of a nodal point in the bulk or surface spectrum is protected by symmetries. Application of BCL can lift these symmetries and induce a desired topological phase transition by imposing a particular magnetic symmetry group from one the subgroups of the crystal MSG.

We emphasize that BCL Floquet engineering is a general approach that can be applied to a wide variety of systems including solid-state materials and artificial lattices. In the following, we consider a minimal model that describes general centrosymmetric 3D Dirac SM and TIs. For concreteness and to make quantitative predictions, we consider model parameters that describes the 3D SM Cd<sub>3</sub>As<sub>2</sub> [41] as an example. This material is a promising platform for BCL Floquet engineering, since high-mobility films are available [42] and the low-energy topological bands (arising from narrow As-4p states) are well separated in energy from other trivial bands by hundreds of meV [43]. This avoids heating of the topological states under a suitably chosen off-resonant Floquet drive in the mid to near infrared.

Theory of BCL Floquet engineering. – BCL corresponds to the superposition of two CL waves with opposite chirality and frequencies that are an integer ratio  $\eta$  of each other. It is described by the vector potential

$$\mathbf{A}(t) = \mathcal{A}_0 \sqrt{2} \operatorname{Re} \left[ e^{-i(\eta \omega t - \alpha)} \boldsymbol{\varepsilon}_R + e^{-i\omega t} \boldsymbol{\varepsilon}_L \right], \quad (1)$$

where  $\mathcal{A}_0$  is the amplitude and  $\boldsymbol{\varepsilon}_{L/R}$  are left (L) and right (R) CL polarization basis vectors (for details see Supplemental Material [44]). We assume uniform light illumination and neglect the photon momentum as it is typically much smaller than system momenta. This vector potential, and the corresponding electric field, traces out a  $(\eta + 1)$ -fold rose curve over a period  $T = 2\pi/\omega$ , as illustrated in Fig. 1(a). The spatial dependence of  $\mathbf{A}(t)$ is crucial for breaking crystal symmetries that cannot be broken by CL such as spatial inversion  $\mathcal{I}$ . Different magnetic symmetries can be broken by tuning the BCL frequency ratio  $\eta$ , which sets the rose pattern shape, the relative phase  $\alpha$ , which promotes a rotation of the pattern, and the light incidence direction. We note that experimentally changing  $\eta$  and  $\alpha$  is achieved by frequency selecting a particular higher-harmonic light mode with frequency  $\eta\omega$  and by modifying the phase shift  $\alpha$  between the fundamental and the higher-harmonic mode.

We consider BCL Floquet engineering in a generic 4band model describing centrosymmetric 3D Dirac SMs with two Dirac nodes near the Fermi level [43, 45],

$$\hat{h}(\mathbf{k}) = M_{\mathbf{k}}\sigma_0\tau_z + \varepsilon_{\mathbf{k}}\sigma_0\tau_0 + P_{\mathbf{k}}\sigma_z\tau_x - Q_{\mathbf{k}}\sigma_0\tau_y \,.$$
(2)

Here,  $\sigma_i$ ,  $\tau_i$  are Pauli matrices in spin and orbital space, respectively. The momentum-dependent coefficients  $M_{\mathbf{k}}$ and  $\varepsilon_{\mathbf{k}}$  describe spin-independent hopping processes and  $P_{\mathbf{k}}$  and  $Q_{\mathbf{k}}$  describe couplings between the orbital and the spin degrees of freedom. The underlying crystal symmetry enforces a certain form of the coefficients [44].

BCL couples to the system degrees of freedom via the standard Peierls' substitution,  $\hat{h}[\mathbf{k} + \mathbf{A}(t)]$ . Choosing an off-resonant light frequency  $\omega$  that is larger than the electronic transition energies allows for the use of a high-frequency approximation [46–49]. This results in a time-independent effective Floquet-Bloch Hamiltonian

$$\hat{h}_{\text{eff}}(\mathbf{k}) = \hat{h}_0(\mathbf{k}) + \hat{m}(\mathbf{k}) , \qquad (3)$$

$$\hat{m}(\mathbf{k}) = \frac{1}{\omega} \sum_{n=1}^{\infty} \frac{1}{n} \left[ \hat{h}_n(\mathbf{k}), \hat{h}_{-n}(\mathbf{k}) \right] + \mathcal{O}(\omega^{-2}) .$$
(4)

Here,  $\hat{h}_n(\mathbf{k}) = (1/T) \int_0^T dt \ e^{-in\omega t} \ \hat{h}[\mathbf{k} + \mathbf{A}(t)]$  is the *n*-th Fourier component of the time-dependent Hamiltonian. We discuss higher-order contributions and corrections to the high frequency regime in the Supplementary Material [44]. The two terms in Eq. (3) depend on the BCL



FIG. 1. BCL control of Weyl node locations in Cd<sub>3</sub>As<sub>2</sub> and transport signature. (a) BCL vector potential  $\mathbf{A}(t)$  for  $\eta = 2$ and different  $\alpha$ , leading to a rotation of the rose pattern.  $A'_{\tau}, A'_{\mu}$  refer to two orthogonal directions in the polarization plane. Panels (b)-(d) show the location of Weyl nodes in  $Cd_3As_2$  as a function of  $\alpha$  for BCL direction normal to (112) surface. (b) Cut of the bulk bands of the effective Hamiltonian in Eq. (3) for fixed  $k_y = k_x$  and  $k_x$  as indicated. Here, we set  $\omega = 5E_{\text{Lif}} = 300 \text{ meV}, \ \mathcal{A}_0 = 2.6 \times 10^{-2} \text{ Å}^{-1} \text{ and } \alpha =$  $\pi/2$ . A narrow energy window is shown to emphasize the energy separation of two of the Weyl nodes (see [44] for the full spectrum). (c) Trajectory of the Weyl nodes in momentum space as  $\alpha$  evolves from 0 (black dots) to  $2\pi$ . The Weyl nodes move counterclockwise, as indicated by the gray arrow. The signs indicates the chirality of each node. Other parameters are identical to the ones in panel (b). Note the different scales on  $k_x, k_y$  and  $k_z$  axes. (d) Energy of Weyl nodes as a function of  $\alpha$ . (e) Gyrotropic magnetic effect induced electric current as a response to a low-frequency oscillating magnetic field in the  $\hat{z}$  direction as a function of  $\alpha$ . We set the amplitude of the field to 3T. Different colors refer to distinct values of  $0.02\text{\AA}^{-1} \leq \mathcal{A}_0 \leq 0.028\text{\AA}^{-1}$  with increasing steps of 0.002 Å<sup>-1</sup> in the direction of the arrows.

polarization state and incidence direction, and modify the bulk energy bands. While  $\hat{h}_0$ , which is the time average of  $\hat{h}[\mathbf{k} + \mathbf{A}(t)]$ , merely shifts the position of the Dirac nodes, the light-induced mass term

$$\hat{m}(\mathbf{k}) = m_{1,\mathbf{k}} \,\sigma_z \tau_y + m_{2,\mathbf{k}} \,\sigma_0 \tau_x + m_{3,\mathbf{k}} \,\sigma_z \tau_z \,\,, \quad (5)$$

lifts the band degeneracy and drives topological transitions. Note that  $\hat{m}(\mathbf{k})$  contains Pauli matrix products that are absent in the original model. The functions  $m_{j,\mathbf{k}}$ involve combinations of  $\hat{h}_n(\mathbf{k})$  (see [44] for their analytical form). Although CL and BCL generate the same set of terms in Eq.(5), the momentum dependence of  $m_{j,\mathbf{k}}$  is different in the two cases, leading to a distinct symmetry breaking as shown in Table I.

BCL Floquet engineering of  $Cd_3As_2$ . For concreteness, we focus in the following on a parameter set in model (2) that describes the tetragonal 3D Dirac SM

 $Cd_3As_2$  [43, 44, 50, 51]. This material exhibits two Dirac nodes located on the  $k_z$  axis, which are protected by fourfold rotation symmetry ( $C_{4z}$ ). The characteristic low energy scale describing the band inversion is given by the Lifshitz energy  $E_{\text{Lif}} = 60$  meV. Since trivial higher energy bands are well separated in energy, the low energy physics can be quantitatively described by a low-order expansion of the functions in Eq. (2) around  $\mathbf{k} = 0$  [43, 51].

Irradiation with BCL breaks both TR and  $\mathcal{I}$  symmetries and thus results in a splitting of the two Dirac nodes into four Weyl nodes. Generically, they reside at different momenta and energies [see Fig. 1(b,c)], unless the presence of additional symmetries, which relate partner Weyl nodes with opposite chirality, forces these two to lie at the same energy. For example, for BCL incident normal to (112) and  $\alpha = 0$  or  $\pi$ , one of the arms of the rose pattern aligns with the  $[1\overline{10}]$ -axis [see x-axis in Fig. 1(a)] and  $m'_{[1\bar{1}0]}$  symmetry is preserved. Thus, two partner nodes connected by  $m'_{[1\bar{1}0]}$  have the same energy. For all other values of  $\alpha$ , the four nodes are separated both in energy and momentum. The energy separation between partner Weyl cones is quadratic in BCL amplitude  $\mathcal{A}_0$  and scales as  $1/\omega^2$ . Thus, as  $\alpha$  is varied between 0 and  $2\pi$ , the Weyl nodes trace out closed loops in energy-momentum space [see Fig. 1(c)]. The size of the loop increases with the light amplitude  $\mathcal{A}_0$ , which opens the possibility of lightinduced braiding of the Weyl nodes. While in  $Cd_3As_2$ we found that Weyl nodes of opposite chirality annihilate before braiding occurs, such a scenario may be possible in other models with larger Lifshitz energy or with Weyl nodes in different bulk gaps. Interestingly, braiding Weyl nodes in different gaps can change their frame charge, leading to the situation that nodes with equal net frame charge reside in a given gap [52-56]. As a consequence of the emergent obstruction to the annihilation of Weyl nodes, a new invariant emerges, known as the Euler class, which is yet to be fully explored.

The dynamical manipulation of the energy separation between the Weyl nodes has another interesting consequence if one applies an additional slowly oscillating magnetic field  $\mathbf{B}(t)$ . According to the gyrotropic magnetic effect [57, 58], a non-centrosymmetry Weyl SM develops an electric current  $J \propto B$  as a response, whose amplitude is also proportional to the energy difference  $\Delta E$  of partner Weyl nodes:  $J = \frac{e^2}{3h^2}B\Delta E$ . Importantly,  $\Delta E$  can be controlled by the  $B\check{CL}$  amplitude  $\mathcal{A}_0$  and the relative phase parameter  $\alpha$ . We note that this effect requires the frequency of  $\mathbf{B}$  to be smaller than the scale of interband transitions, which is given by  $\Delta E$  and lies in the 100 MHz range for the parameters of Fig. 1, and ultraclean samples, since the gyrotropic current is suppressed by disorder [44, 57]. In the clean limit, we predict the gyrotropic current in BCL driven  $Cd_3As_2$  to lie within an experimentally accessible  $nA/\mu m^2$  range for realistic electric field amplitudes  $E_0 = \omega \mathcal{A}_0 \approx 10^7 \text{ V/m}$  and a magnetic



FIG. 2. Effect of CL and BCL on Fermi arc surface states at energy  $E = -E_{\rm Lif}/2 = -30$  meV, the location of Dirac nodes in the absence of light, on the (112) surface of Cd<sub>3</sub>As<sub>2</sub> (shown in blue in the insets).  $k'_x$  and  $k'_y$  are components of the surface momentum along directions [110] and [111], respectively. The gray regions correspond to the projection of bulk states onto the surface. Different panels show surface states: (a) in the absence of light, (b) for CL with light direction normal to (112), (c) for BCL with light direction normal to (112). In (b) and (c) we set  $\omega = 5E_{\rm Lif} = 300$  meV,  $A_0 = 2 \times 10^{-2}$ Å<sup>-1</sup> and  $\alpha = 0$ . The condition det M = 0 reflects our choice of boundary condition, and can be interpreted as finite overlap to bulk states [44]. Note that the results in panel (c) depend only weakly on the value of  $\alpha$ .

field  $B \approx 3$  T, which is modulated at less than MHz frequencies [59]. Due to the linear dispersion around the Weyl nodes, the gyrotropic magnetic effect exhibits only a weak temperature dependence, and we predict it to be robust up to 10 K [44]. As shown in Fig. 1(e), the current J is modulated as a function of  $\alpha$  and vanishes for  $\alpha = 0, \pi$ , where  $\Delta E = 0$ . To compute J, we have set the chemical potential equal to the energy of the pair of Weyl nodes in Fig. 1(b) at  $\alpha = 0$ . To reveal a unique signature of bulk Weyl nodes, we propose dynamically modulating  $\alpha(t)$  on a frequency scale different from that of the magnetic field (e.g., in the GHz range) in order to change the gyrotropic current at the same frequency. Importantly, even in the unavoidable presence of interband transitions and heating in real materials, which is an inherent challenge in Floquet engeneering, the coherent modulation of the gyromagnetic current can still be detected in a lock-in type experiment, since incoherent effects and heating are independent of  $\alpha$ .

Finally, light irradiation also impacts the shape, curvature and position of the Fermi arc surface states in  $Cd_3As_2$ , which allows to manipulate surface transport properties [60]. Figure 2 shows Fermi arc surface states on the experimentally accessible (112) surface [42] at fixed energy, both without light and in the presence of CL or BCL. The geometry of the Fermi arcs, which connect projections of the nodal points onto the (112) surface, is different for CL and BCL [44].

Floquet engineering of strained  $Cd_3As_2$ . – Under the influence of lattice strain that breaks  $C_{4z}$  symmetry,



FIG. 3. CL induced topological transition from topological to axion insulator gaps out the surface states in the (001) surface of Cd<sub>3</sub>As<sub>2</sub> under  $B_{1g}$  strain. Panel (a) is in the absence of light and (b) is in the presence of CL with  $\omega = 5E_{\text{Lif}} =$ 400 meV and  $\mathcal{A}_0 = 2.4 \times 10^{-2} \text{Å}^{-1}$ , incident normal to (112), as in the inset of Fig. 2(b). Here,  $k'_x$  ( $k'_y$ ) points along the [100] ([010]) direction. (c) Cut of the bulk bands of strained Cd<sub>3</sub>As<sub>2</sub> for fixed  $k_x = k_y = 0$  in absence (dashed) and presence (solid) of CL light with the same parameters as in panel (b).

Cd<sub>3</sub>As<sub>2</sub> becomes a strong TI with gapless Dirac surface states on every crystal surface. In the following, we consider experimentally realistic types of strain: first,  $B_{1q}$ symmetric strain that breaks  $C_{4z}$  and the two-fold rotations along the diagonals,  $C_{2,[110]}$  and  $C_{2,[1\overline{1}0]}$  [42, 51]. We also consider  $B_{2q}$ -symmetric strain that breaks  $C_{4z}$  and the two-fold rotations along the crystallographic axes,  $C_{2,[100]}$  and  $C_{2,[010]}$ . Within the generic 4-band model in Eq. (2),  $B_{1g}$  and  $B_{2g}$  strains correspond to terms of the form  $B_{\mathbf{k}}\sigma_x\tau_x$  and  $B_{\mathbf{k}}\sigma_y\tau_x$ , respectively, where  $B_{\mathbf{k}} \propto k_z$ . Additional terms that renormalize the parameters in Eq. (2) are allowed by symmetry, but vanish along  $k_z$  and thus do not contribute to the size of the bulk gap. Under irradiation these strain terms lead to additional light-induced mass terms beyond those listed in Eq. (5) that also contribute to magnetic symmetry breaking (see [44]). As we show next, this opens up an interesting possibility of inducing sought-after topological states protected by magnetic symmetries. Specifically, we predict a CL-induced axion insulator state [61] and a BCL-induced magnetic topological crystalline insulator protected by 2' symmetry [62, 63].

Table I shows that the combination of  $B_{1g}$  strain and CL irradiation along the (112) normal removes all symmetries except  $\mathcal{I}$ . Since the bulk gap remains open for not too large light intensities, we can conclude that CL induces a topological transition to an axion insulator state with quantized magnetoelectric coupling and halfquantized anomalous surface Hall conductivity [5]. As  $\mathcal{I}$  is naturally broken at the surface, the surface states acquire a gap as shown in Fig. 3 for the particular case of the (001) surface.

An even more intriguing situation arises in the presence of  $B_{2g}$  strain and BCL irradiation along (112) normal. Choosing  $\alpha$  as either  $\frac{\pi}{2}$  or  $\frac{3\pi}{2}$  removes all symmetries except the combination of a two-fold rotation around  $[1\bar{1}0]$ and time reversal:  $\Theta C_{2,[1\bar{1}0]} \equiv 2'_{[1\bar{1}0]}$ . Since a 2' operation

Strain	Light type	$\alpha$	MPG gen.	MSG
0	No light	×	$C_{2z}, C_{4z}, C_{2y}, \mathcal{I}, \Theta$	$I4_1/acd1'$
	$CL \perp (112)$	×	$\mathcal{I}, \Theta C_{2,[1\bar{1}0]}$	C2'/c'
	$BCL\perp$ (112)	$0, \pi$	$\Theta M_{[1\bar{1}0]}$	Cc'
		$\frac{\pi}{2}, \frac{3\pi}{2}$	$\Theta C_{2,[1\bar{1}0]}$	C2'
		N.A.	1	P1
$B_{1g}$	No light	×	$C_{2z}, C_{2y}, \mathcal{I}, \Theta$	Pcca1'
	$CL \perp (112)$	×	I	$P\bar{1}$
$B_{2g}$	No light	×	$C_{2z}, C_{2,[110]}, \mathcal{I}, \Theta$	Fddd1'
	$BCL \perp (112)$	$0, \pi$	$\Theta M_{[1\bar{1}0]}$	Cc'
		$\frac{\pi}{2}, \frac{3\pi}{2}$	$\Theta C_{2,[1\bar{1}0]}$	C2'
		N.A.	1	P1

TABLE I. Magnetic symmetries of Cd<sub>3</sub>As<sub>2</sub> with and without light and lattice strain. Light incidence direction is perpendicular to the (112) surface and BCL parameter  $\eta = 2$  (three-fold rose pattern). The table shows the generators of the magnetic point group (MPG) preserved by the light and the resulting MSG for Cd<sub>3</sub>As<sub>2</sub>.  $\Theta$  refers to TR symmetry and  $\mathcal{I}$  to spatial inversion. N.A. stands for none of the above. The parameter  $\alpha$  rotates the BCL rose pattern, which controls the MSG.

reverses an odd number of spacetime coordinates (like TR and  $\mathcal{I}$ ), the magnetoelectric coupling is still quantized [64]. Again, for light intensities that leave the bulk gap open, continuity ensures that BCL induces a topologically nontrivial axion insulator state. Here, however, not all surfaces are gapped. Instead, (110) surfaces (whose surface normal is parallel to the 2' axis) host exotic gapless Dirac states whose nodal position is unpinned from the surface TR invariant momenta. As shown in Fig. 4, the position of the nodal point is controlled by light parameters such as frequency and intensity [44]. All other surfaces are gapped and exhibit a half-quantized anomalous surface Hall conductivity.

*Conclusion.* – To conclude, we show that Floquet engineering using BCL offers wide tunability of the magnetic symmetries of a system beyond the capabilities of linear or circularly polarized light. This arises from the fact that the electric field of BCL follows a rose pattern that can be tailored to break desired spatial inversion and other symmetries, in addition to time-reversal, leading to a non-centrosymmetric effective Floquet-Bloch Hamiltonian. This general approach of BCL tuning of symmetries is applicable to a wide variety of materials and artificial lattice system and can have immediate impact on their band topology. As a concrete example, we predict effects of Floquet engineering in the Dirac SM  $Cd_3As_2$ , which is a suitable material platform that undergoes various light-induced topological phase transitions. In the absence of strain, BCL leads to a non-centrosymmetric magnetic Weyl SM phase with bulk nodes separated in both energy and momentum. We demonstrate that the position of the nodes can be controlled via light parameters, opening up the possibility of braiding. In the pres-



FIG. 4. BCL control of Dirac node position in light-induced 2' axion insulator state. Panel (a) shows the evolution of gapless surface states in the  $(1\overline{1}0)$  surface of Cd<sub>3</sub>As<sub>2</sub> (blue plane in the inset) in presence of  $B_{2g}$  strain when turning on BCL. Here,  $k'_x$   $(k'_y)$  are components along the [110] ([001]) directions. The ellipse centered around  $k'_x = k'_y = 0$  is a fixed-energy cut of the surface state at 37 meV close to the node in the absence of light. BCL irradiation along direction normal to (112) (red plane in the inset) induces a 2' magnetic topological crystalline insulator with unpinned Dirac surface states. The surface state moves in the direction indicated by the arrow when BCL is turned on, while the energy of the Dirac node changes only slightly to 36 meV. Color shows  $\det M$ , which has the same meaning as in Fig. 2. (b) Bulk energy bands of strained Cd<sub>3</sub>As<sub>2</sub> for fixed  $k_x = k_y = 0$  without light (dashed) and with BCL (solid). In both panels, we set  $\omega = 150 \text{ meV}$ ,  $\mathcal{A}_0 = 2.6 \times 10^{-2} \text{\AA}^{-1}$ ,  $\alpha = \pi/2$ .

ence of an additional slowly varying magnetic field, BCL leads to a tunable dissipationless current due to the gyrotropic magnetic effect, which is a unique signature of Weyl physics. Finally, combining lattice strain and BCL irradiation realizes a sought-after magnetic axion insulator phase with exotic unpinned surface states protected by 2' symmetry.

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