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# Holographic Plasma Lenses

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A hologram fully encodes a three-dimensional light field by imprinting the interference between the field and a reference beam in a recording medium. Here we show that two collinear pump lasers with different foci overlapped in a gas jet produce a holographic plasma lens capable of focusing or collimating a probe laser at intensities several orders-of-magnitude higher than the limits of a non-ionized optic. We outline the theory of these diffractive plasma lenses and present simulations for two plasma mechanisms that allow their construction: spatially varying ionization and ponderomotively driven ion-density fluctuations. Damage-resistant plasma optics are necessary for manipulating high-intensity light, and divergence control of high-intensity pulses — provided by holographic plasma lenses — will be a critical component of high-power plasma-based lasers.

Holograms record both the phase and the amplitude of light, allowing the complete reconstruction of a light field at a later time [1]. A hologram is created by imprinting the interference between a signal beam and a reference beam in a light-sensitive medium, e.g. a photographic plate; a delayed second reference beam diffracts to reproduce the signal beam. The interference is commonly mapped to attenuation, but the pattern may also be embedded as a phase shift [2]: a variation of the refractive index's real component. Any medium where the index of refraction is modified by the intensity of light can be used, but current holograms rely on a limited collection of solid-state materials. The index of refraction ( $n$ ) of a plasma ( $n < 1$ ) differs from that of both vacuum ( $n = 1$ ) and neutral gas at similar density ( $n > 1$ ), and the formation and density evolution of plasma may be driven by light. We may therefore create a hologram using lasers to modulate plasma density.

The damage threshold of a plasma is orders-of-magnitude higher than that of a solid-state optic; plasma optics use this to manipulate light at extreme intensities [3]. Plasma-based versions of optical components include amplifiers [4–7], gratings [8–11], mirrors [12, 13], waveplates [14–16], and Pockels cells [17]. However, the only demonstrated solutions for focusing light with unfocused intensity above  $10^{12}$  W/cm<sup>2</sup> are the concave plasma mirror [18] and compound parabolic concentrator [19], neither of which is well-suited to high-repetition-rate experiments. A holographic plasma lens offers an alternative approach. Imprinting the interference between two co-propagating pump beams with different foci in a plasma (e.g. a collimated beam and a tightly focused one) results in a plasma-based zone plate, a diffractive lens which in non-plasma form is used to focus x rays [20]. An efficient holographic plasma lens could allow collimation of high-intensity light for high-order harmonic generation [21] and filamentation [22] experiments or improve the focusing of high-energy laser facilities (e.g. the Advanced

Radiographic Capability (ARC) laser [23]). Previous efforts to design plasma holograms have relied on reflective surface [24] and reflective volume [25] approaches, which require high-quality surfaces and high (near-solid) plasma density, restricting viability for high-repetition-rate systems, or electron plasma waves [26], which are short-lived and are destroyed when the probe intensity is comparable to that of the pump beams, a serious constraint for a plasma optic.

In this letter, we propose a new plasma lens concept based on transmission volume holograms constructed via two plausible plasma mechanisms: spatially varying ionization (SVI) or ponderomotively driven ion structures. Both schemes rely on two co-propagating pump beams whose interference pattern imprints a three-dimensional (3D) refractive index structure acting as a diffractive lens. SVI uses ionization of a background gas in the high-intensity fringes of the interference pattern while areas of destructive interference remain as neutral gas, leading to an index modulation  $n_{\text{gas}} - n_{\text{plasma}} \approx 10^{-2}$  [27–30]. For ponderomotively driven structures, electrons are ponderomotively forced out of high-intensity regions; the resultant space-charge force pulls ions down the intensity gradients as well. An index modulation is then formed by the plasma density difference between the high and low intensity regions [8–10, 31–33]. For both mechanisms, the diffractive lens structure remains after the pumps are turned off. The relaxation time is dictated by recombination and diffusion for SVI [29] and by ion motion for ponderomotive structures [10]. This enables the manipulation of a probe at a substantial delay or with a much longer duration than the pump lasers, and, as we show here, requires relatively small volumes of gas-density plasma to create efficient transmission holograms tolerating probe intensities from  $10^{14}$  to  $10^{17}$  W/cm<sup>2</sup>.

Consider two collinear equal-power pump lasers ( $\alpha = A, B$ ) focused at distinct points  $f_\alpha$  along  $z$  with the f-number of each beam ( $F_\alpha$ ) chosen such that they have

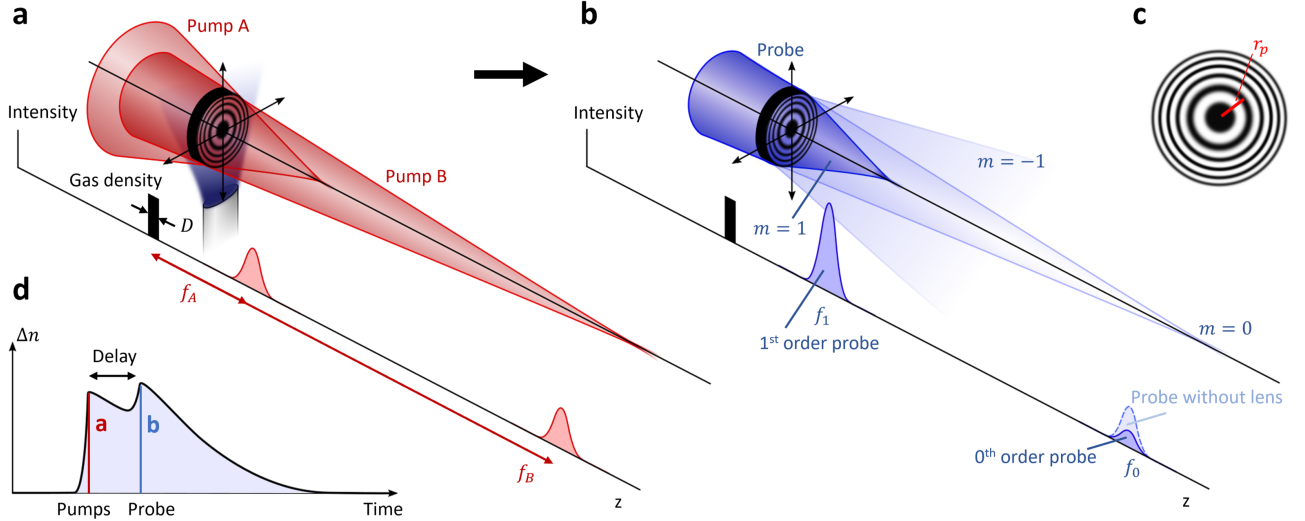


FIG. 1. Schematic of a holographic plasma lens. (a) Two pump lasers overlap in a gas (extent along  $z$  is  $D$ ), arranged so that their interference pattern is a sinusoidal zone plate. (b) At a delayed time, a probe laser passes through the resulting structure and is diffracted into one or more orders. (c) The intensity profile of the overlapped pumps and the resultant index modulation. (d) The peak index of refraction modulation as a function of time, showing the formation of the structure with the arrival of the pumps, followed by a decay and possible modification by the probe. The amplitude and timescale both depend on the chosen nonlinear mechanism.

the same beam diameter at  $z = 0$  ( $|f_A/F_A| = |f_B/F_B|$ ), as shown in Fig. 1a. The beams propagate in vacuum outside a region with extent  $D$  centered at  $z = 0$  where the index of refraction is intensity-dependent, a configuration that can, for example, be realized with a gas jet. For ease of analysis, we will restrict  $f_\alpha$  to be larger than the Rayleigh range. The two pumps interfere everywhere they overlap, but inside the gas that interference is encoded as a variation of the refractive index by the dependence of  $n$  on intensity ( $I$ ), creating the index modulation of a zone plate (Fig. 1c). At a delayed time (Fig. 1d), a probe crossing the index modulation can be focused (Fig. 1b), with the plasma density potentially evolving due to both the pumps and the probe.

A zone plate consists of concentric alternating regions of opaque or phase shifting material, spaced so that transmitted light interferes constructively at the desired focal point [2, 34, 35]. The radii of boundaries between zones ( $r_p$  for the  $p$ th boundary) are associated with  $\lambda/2$  phase shifts of light, from which follows  $r_p^2 = p\lambda(f + p\lambda/4)$ ,  $\lambda$  is the wavelength of the light of interest, and  $f$  is the focal length. For  $p\lambda \ll f$ ,  $r_p^2 \approx p\lambda f$ . If the pump and probe have different wavelengths ( $\lambda_p$  and  $\lambda_0$ , respectively), both must satisfy  $p\lambda \ll f$  for efficient diffraction. The size of the focal spot is governed by the total number of zones ( $P$ ) as  $w_0 = \sqrt{\lambda f/4P}$ , which follows from the dependence of spot size on numerical aperture. Zone plates are highly chromatic, restricting the focusable bandwidth ( $\Delta\lambda$ ); the probe must satisfy  $\Delta\lambda/\lambda_0 \leq 1/P$  for the focal position of its component wavelengths to differ by no more than a Rayleigh range.

A zone plate created by two pump lasers with focal spots at  $f_A$  and  $f_B$  will have focal length:

$$f = \frac{f_A f_B}{f_A - f_B} \cdot \frac{\lambda_p}{\lambda_0}. \quad (1)$$

A probe focused at the point  $f_0$  along the  $z$  axis, will, after passing through the plasma zone plate, have new  $m$ -order focal spots at:

$$f_m = \frac{f f_0}{f + m f_0}, \quad (2)$$

where  $f$  is given by Eq. 1 and the energy in each order is determined by the detailed spatial variation of the refractive index [36].

We can distinguish two regimes for diffractive lenses by the thickness of the optic relative to the light wavelength and zone size. For a thin lens ( $Q = D\lambda_0/\delta^2 \ll 1$ , where  $\delta$  is the width of the outer-most zone), the thickness of the optic is set by the condition that adjacent zones produce a relative phase shift of  $\pi$ :  $\Delta\phi \approx \pi = 2\pi(D/\lambda_0)\Delta n$ . For a volumetric (thick) plasma lens ( $Q \gg 1$ ), which can be described by coupled mode theory [47], the required thickness is [48]:

$$\frac{D}{\lambda_0} \approx \frac{1}{\Delta n}. \quad (3)$$

Taking SVI as a representative example, we will neglect absorption and note that the real part of the refractive index varies between that for plasma ( $n = \sqrt{1 - n_e/n_c}$  where  $n_e$  is the plasma density and  $n_c$  is the plasma

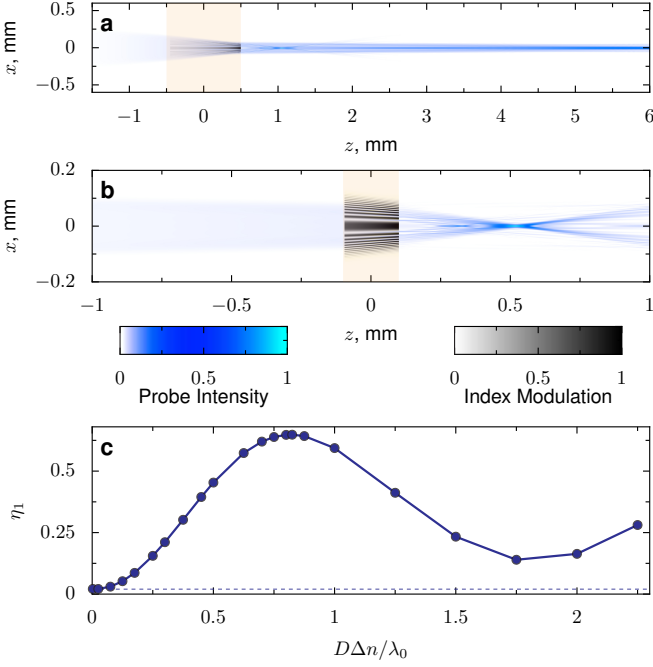


FIG. 2. Calculations (3D PPS) for a thick plasma lens, showing collimation (a) and focusing (b) depending on the initial probe focus position. (a) Probe (blue) near-collimated to focus at  $z = 6$  mm by lens formed in  $D = 1$  mm initial gas (orange), with  $\Delta n = 1.3 \times 10^{-4}$ ,  $\lambda_p = \lambda_0 = 400$  nm,  $f_A = 1$  mm, and  $f_B = 6$  mm; 81% of energy is within the focal spot at  $z = 6$  mm. (b) Focusing lens with  $D = 200$   $\mu$ m and  $\Delta n = 3.3 \times 10^{-3}$  for  $\lambda_0 = 800$  nm probe. Focal spot full-width-half-maximum is  $2.2$   $\mu$ m. Pumps have  $\lambda_p = 800$  nm,  $f_A = 0.5$  mm, and  $f_B = 3$  mm. (c) Efficiency ( $\eta_1$ ) for lens shown in (b), defined as probe energy within  $10$ - $\mu$ m radius at  $z = 0.5$  mm as  $\Delta n$  is varied between  $1 \times 10^{-5}$  and  $9 \times 10^{-3}$  for fixed  $D$ .

critical density  $n_c = \varepsilon_0 m_e \omega^2 / e^2$ ) and that for the non-ionized gas, where ordinarily  $|1 - n_{\text{plasma}}| \gg |1 - n_{\text{gas}}|$ . A reasonable approximation is then  $\Delta n \approx 1 - n_{\text{plasma}} =$

$1 - \sqrt{1 - n_e/n_c} \approx n_e/2n_c$  for  $n_e \ll n_c$ . From this and the above condition on  $\Delta\phi$ , the plasma density and thickness should satisfy:  $n_e D / 2n_c \approx \lambda_0$ .

Thin lenses support multiple diffraction orders, whereas a thick lens can produce a single well-defined spot [47]. This is analogous to the Raman-Nath and Bragg regimes for diffraction gratings. The loss of energy to higher orders for thin lenses makes them less attractive as focusing optics, and here we will focus on thick lens regime, using three types of simulation to study the interaction: a linear paraxial solver, a nonlinear paraxial solver, and particle-in-cell.

First, we use a linear 3D paraxial propagation solver (PPS) to numerically evaluate the formation and performance of diffractive lens shapes. The solver neglects the time dynamics of the pumps and probe and considers the interaction as three separate steps: (1) linear propagation of the pumps through a uniform medium, (2) change of the refractive index as a function of pump intensity, and (3) linear propagation of the probe through the new distribution of refractive index [36]. The arbitrary functional relationship between the pump intensity and the refractive index in step (2) allows both SVI and ponderomotive lenses to be approximated. Fig. 2a shows a probe beam with vacuum focus at  $z = 1$  mm being collimated by a thick plasma lens, with 80% of the energy within the (collimated)  $m = -1$  mode. In Fig. 2b, a similar plasma lens focuses a collimated incident probe, with more than 50% of the energy inside a  $2$   $\mu$ m spot. Figure 2c shows how the focusing efficiency of the optic in (b) decreases as the plasma density changes from its optimal value. The maximum efficiency occurs near where  $D/\lambda_0 = \Delta n$ , with smaller values of  $D\Delta n/\lambda_0$  producing minimal energy transfer to the  $m = 1$  order.

To capture the nonlinear dynamics of SVI, where high-intensity pulses propagate in an initially neutral gas, we use a 3D numerical envelope equation solver [49] with governing equation [40]:

$$\frac{\partial E}{\partial z} = \frac{i}{2k} \nabla_{\perp}^2 E - \frac{ik''}{2} \frac{\partial^2 E}{\partial t^2} - \frac{\sigma}{2} (1 + i\omega\tau) n_e E - W_{FI}(E) n_N \frac{U_i}{2|E|^2} + ik_0 n_2^T \left[ (1-f)|E|^2 + f \int_{-\infty}^{\infty} R(t-t') |E(t')|^2 dt' \right] \quad (4)$$

where  $k$  is the wavenumber,  $\sigma$  is the inverse Bremsstrahlung cross section,  $\tau$  is the collision time,  $W_{FI}$  is the field ionization rate,  $n_N$  is the neutral density,  $U_i$  is the ionization energy,  $n_2^T$  is the total Kerr nonlinearity with  $f$  the time delayed fraction, and  $R(t)$  is a damped harmonic oscillator model for the delayed response [36]. The terms on the right hand side describe diffraction, group velocity dispersion, plasma phase shift and absorption, ionization losses, and Kerr self-focusing, respectively. The evolution of the plasma due to field and

collisional ionization and recombination is separately calculated. Figure 3ab shows the results from a simulation of a  $170$   $\mu$ m diameter ionization lens formed in a  $2$  mm nitrogen gas column by two  $0.65$  mJ,  $10$  fs pumps. In Fig. 3a, the free electron density left by the pump lasers has the characteristic zone-plate shape. After a delay of  $0.8$  ps, a  $1$  ps  $60$  mJ probe passing through this lens is focused at  $z = 0.5$  mm. Slight distortion and a reduction in intensity at the tail end of the probe indicate that this pulse is near the maximum tolerance of the optic, which

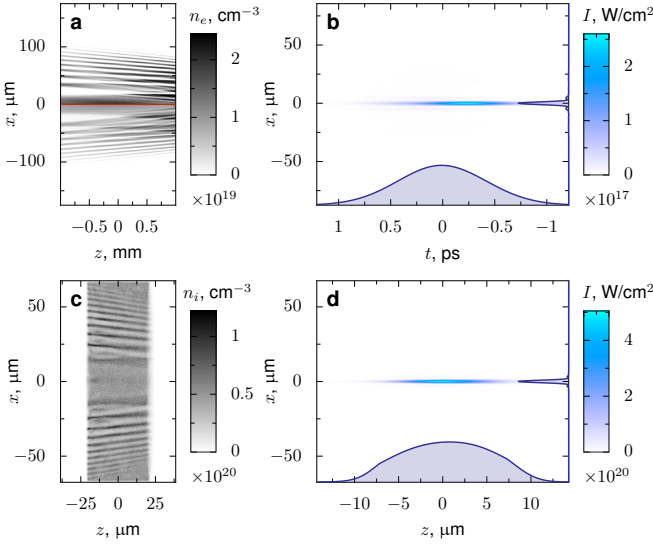


FIG. 3. Simulations of focusing by thick plasma lenses formed by SVI (a,b) and ion fluctuations (c,d) using a 3D nonlinear envelope equation solver (a,b) and 3D PIC simulations (c,d). (a) The density of plasma after passage of the pumps (upper half) and the probe (lower half) through a  $D = 200 \mu\text{m}$  column of molecular nitrogen. (b) The probe intensity at the  $z = 3 \text{ mm}$  focal spot. In (a,b), the pumps are 10 fs, 800 nm, 0.65 mJ pulses focused at  $z = 3 \text{ mm}$  and  $z = 0.5 \text{ mm}$ , and the probe is 1 ps, 800 nm, and 60 mJ. In (c,d), the pumps are 15 TW,  $1 \mu\text{m}$  pulses with 500 fs duration, the probe is a 100 TW,  $1 \mu\text{m}$  pulse with 40 fs duration, and the hydrogen plasma has  $D = 40 \mu\text{m}$  with an initial density  $n_e/n_c = 0.045$  and electron temperature  $T_e = 100 \text{ eV}$ . (c) The ion density after both the pump and the probe have passed, and (d) the probe intensity near the focal spot.

at  $2.4 \times 10^{14} \text{ W}/\text{cm}^2$  and  $230 \text{ J}/\text{cm}^2$  is well above the limits of glass.

A holographic plasma lens can also be created via the ponderomotive force in a fully ionized plasma. As captured by the 3D particle-in-cell (PIC) simulation (using the code EPOCH [50]) shown in Fig. 3cd, the two pump lasers (15 TW, 500 fs duration) ponderomotively create an ion density perturbation in a fully-ionized hydrogen plasma (Fig. 3c). Although the pumps are only on for 500 fs, this modulation continues to evolve on a picosecond timescale due to the acquired ion momentum. Under these specific conditions, a 100 TW probe arriving 1.2 ps after the pumps is brought to a high-quality focal spot at  $z = 0.2 \text{ mm}$  (Fig. 3d). At this power, the probe closely follows the expected linear behavior based on the index modulation created in the plasma. In fact, as long as the probe is weak enough to not affect the lens, both SVI and ponderomotive optics are well-described by the linear PPS code, provided that we have an adequate model relating pump intensity to the index modulation. The agreement between PPS and PIC, in particular, suggests that a good understanding of the interaction can be achieved even without fully resolving all components of

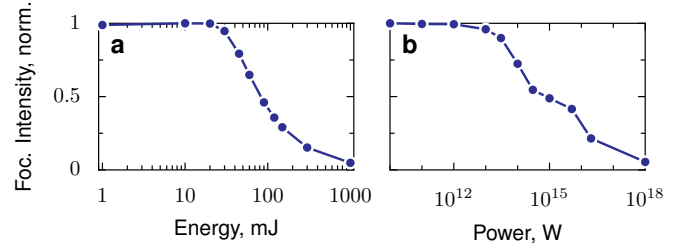


FIG. 4. Plasma lens efficacy (peak focal intensity normalized by incident probe power) at varied incident probe energy for (a) SVI calculated with the 3D nonlinear envelope equation and (b) the ponderomotive ion mechanism using 2D PIC. (a) Parameters apart from probe energy are the same as in Fig. 3ab. (b) Physical parameters are the same as in Fig. 3cd, although these simulations are 2D and the resolution is 20 cells/ $\lambda$  and 10 particles per cell.

the electromagnetic fields. However, inclusion of nonlinear effects is required to understand how performance changes as the probe energy increases.

Plasma optics are useful only if they support higher intensity or energy flux in the probe than is required in the pumps that create them, and to be practical, the damage tolerance must be much higher than solid-state equivalents. In Fig. 4a, 3D nonlinear envelope simulations measure the focusing efficacy, defined here as the peak intensity at focus divided by incident probe power and normalized to the low-power limit, for an SVI lens with the same parameters as in Fig. 3ab. As energy increases to 100 mJ, this efficacy drops, setting an effective damage threshold. At 60 mJ, where performance is above 65%, the probe energy is almost 100 times the energy in each pump and the flux seen by this lens is  $230 \text{ J}/\text{cm}^2$ , well above the energy flux limits for a solid-state optic exposed to a femtosecond pulse. In general, an SVI optic can take advantage of wavelength-dependent ionization or the differences between field and collisional ionization to support higher energy or intensity in the probe than required for the pumps.

A similar approach is used to find an effective damage threshold for a ponderomotive lens, as shown in Fig. 4b, where 2D PIC simulations at the same conditions as those in Fig. 3cd capture a gradual drop-off in lens efficacy above  $10^{14} \text{ W}$ . Near this threshold, the intensity within the lens is more than  $10^{17} \text{ W}/\text{cm}^2$ . A ponderomotive plasma optic relies on the relatively slow response of ions to intense light fields. Although the local electron density provides the index modulation, the plasma lens has an underlying ion density structure which changes shape slowly, helping maintain the overall structure even at high probe intensity. An ion structure can be formed over a several picoseconds by weak pumps, but requires far higher intensity to destroy during the 40 fs probe duration.

In conclusion, we have shown that plasma nonlineari-

ties can be used to create efficient high-damage-threshold diffractive plasma lenses. Simulations suggest that the intensity damage threshold of these lenses ranges from more than  $10^{14}$  W/cm<sup>2</sup> for the ionization mechanism to more than  $10^{17}$  W/cm<sup>2</sup> for the ponderomotive mechanism. The generality of holography means that holographic plasma optics can almost arbitrarily manipulate intense beams; these mechanisms are not limited to the creation of simple lenses.

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