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Intervalley excitonic hybridization, optical selection rules, and imperfect circular dichroism in monolayer hBN

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Abstract

We perform first-principles GW plus Bethe-Salpeter equation calculations to investigate the photophysics of monolayer hexagonal boron nitride (hBN), revealing excitons with novel **k**-space characteristics. The excitonic states forming the first and third peaks in its absorption spectrum are s-like, but those of the second peak is notably p-like, a first finding of strong co-occurrence of bright s-like and bright p-like states in an intrinsic 2D material. Moreover, even though the **k**-space wavefunction of these excitonic states are centered at the K- and K'-valleys like in monolayer transition metal dichalcogenides, the **k**-space envelope functions of the basis excitons at one valley have significant extents to the basin of the other valley. As a consequence, the optical response of monolayer hBN exhibits a lack of circular dichroism, as well as a coupling that induces an intervalley mixing between s- and p-like states.

Main text

Atomically thin two-dimensional (2D) semiconductors, such as gapped graphene systems [1-2] and monolayer transition-metal dichalcogenides (TMDs) [3-5], with honeycomb-like crystal structure and broken inversion symmetry, are of great interest due to their novel physical properties. Their low-energy optical absorption is dominated by the excitation of bound electron-hole pairs that are highly localized in \mathbf{k} -space, namely, Wannier excitons. The excitons from different valleys are commonly viewed as independent or known to be extremely weakly interacting with each other, and the highly \mathbf{k} -space localized nature of them has led to a series of discoveries, such as new optical selection rules due to non-trivial band topology and valley exciton circular dichroism [6-7].

However, both gapped graphene systems and mono- or few-layer TMDs are semiconductors with relatively small quasiparticle (QP) bandgaps, *e.g.*, of a few hundred meVs in biased bilayer graphene [8] and in the range of 2.6 eV to 2.8 eV in monolayer MoS₂ [9-11]. For 2D wide bandgap *insulators*, dielectric screening is much weaker than that in 2D semiconductors [12]. A large bandgap also leads to less dispersive bands with larger effective masses, which together with the reduced screening result in coupling of free electron-hole pairs over a large area of the Brillouin zone (BZ) and a large increase in the binding energy of the low-lying bound excitons. Unlike the extensive investigation of Wannier excitons in 2D semiconductors, the excitonic properties of 2D insulators are less studied [13] although a number of dark *p*-like exciton features were presented [14]. Whereas to date, 2D insulators, such as 2D hexagonal boron nitride (hBN), play a pivotal role in the fabrication of moiré heterostructures [15-17] and in usages of ultra-violet photophysics [18] and quantum emission [19].

In this work, we have explored the excitonic properties of monolayer hBN employing the *ab initio GW* and *GW* plus Bethe-Salpeter equation (*GW*-BSE) approaches [12,20]. We find that monolayer hBN possesses strongly bound excitons with novel **k**-space characteristics, although they can still be identified by their dominant C_3 -rotational features. In particular, the first and third peaks in the optical absorption spectrum correspond to *s*-like excitons while the second peak originates from the excitation of *p*-like states (see Fig. 1). To our knowledge, this is the first known case of co-existence of both strongly bright *s*- and bright *p*-like excitons for an intrinsic monolayer 2D material. Moreover, we find that even though these bright excitons are still centered at the *K*- or K'-valley, their envelope functions are highly non-localized with arms extending far from the *K*- or K'-point in the BZ. The mixing of the interband electron-hole excitations away from the bottom of a specific valley results in: (1) the absence of perfect circular dichroism; and (2) interactions between *s*- and *p*-like excitons from different valleys. These effects, so far, have not been well identified in honeycomb-like structured 2D materials in the literature.

In Fig. 1(a), we plot the band structure calculated using density-functional theory (DFT) with the Perdew-Burke-Ernzerhof (PBE) exchange-correlation functional [21] and that calculated with the full frequency eigenvalue-self-consistent GW approach. At the DFT-PBE level, monolayer hBN is predicted with a direct bandgap at the K-point in the BZ of 4.70 eV, which is much smaller than the GW direct bandgap at K of 8.03 eV, owing to strong self-energy effects. Moreover, at the GW level, monolayer hBN is an indirect gap insulator with a K-to- Γ indirect gap of 7.45 eV. The calculated absorption spectrum for linear polarized light is plotted in Fig. 1(b). There are three main peaks, labeled as A, B and C with excitation energies of 5.95 eV, 6.82 eV and 7.06 eV, respectively. The calculated position of the first peak is in excellent agreement with the measured absorption value of 6.03 eV [22]. These peaks are formed by degenerate excitons as monolayer hBN is a non-centrosymmetric crystal with minimum direct energy gaps of equal value at two valleys, K and K', which are related by time-reversal symmetry. The binding energy of the bright excitons contributing to peak A is calculated to be 2.08 eV, which is more than twice that of the lowest energy bright exciton in typical semiconducting monolayer TMDs (e.g., it is 0.65 eV for MoS₂ [9]). The huge binding energy in monolayer hBN is the combined effect of reduced dimensionality [9, 23-24] and large bandgap [12, 25] [see computational details, along with comparison with previous theoretical works in the Supplemental Material (SM) [26] Sec. I].

Now, we examine the characters of the excitons giving rise to the three peaks. The exciton wave functions are obtained by solving the BSE of the interacting two-particle Green's function [12, 30]

$$\left(E_{c,\mathbf{k}}^{QP} - E_{v,\mathbf{k}}^{QP}\right) A_{vc\mathbf{k}}^{S} + \sum_{v'c'\mathbf{k'}} \langle vc\mathbf{k} | K^{eh} | v'c'\mathbf{k'} \rangle A_{v'c'\mathbf{k'}}^{S} = \Omega_{S} A_{vc\mathbf{k}}^{S} \tag{1}$$

where $E_{c,k}^{QP}$ and $E_{v,k}^{QP}$ are QP energies of an electron in the conduction band and negative of the QP energy of a

hole in the valence band as reference to a common chemical potential that is set to zero. $|vck\rangle$ corresponds to a free electron-hole pair at the point k. K^{eh} is the electron-hole interaction kernel, containing a direct electron-hole attractive screened Coulomb term and a repulsive exchange bare Coulomb term [12]. Ω_S is the excitation energy of the exciton state $|S\rangle$, and A_{vck}^S describes the k-space exciton envelope function. In our study, we firstly solved Eq. (1) by zeroing out the BSE matrix elements outside of a radius of 1.13 Å-1 from the bottom point of the K-valley (we call the solutions at this stage single-valley excitons). By doing so, we only include mixing of interband transitions around the K-valley as the distance between K- and K'-points is 1.66 Å-1. For this calculation, we use a k-point sampling grid of $400 \times 400 \times 1$ for the full BZ, and the highest valence and lowest conduction bands only (band indices can thus be omitted in describing the exciton envelope function, i.e., with just A_k^S). In Fig. 2, we plot the amplitude and the phase of A_k^S for the first four lowest energy singlet excitons, with the K-point set as the origin. The gauge arbitrariness of the computed A_k^S is eliminated by introducing a gauge requiring the k-dependent

phase of the lowest-energy exciton to be smooth, resulting in a rotational quantum number of m=0 for this exciton [Fig. 2(e)]. For the lowest-energy exciton, which is optically bright with linear polarized light (peak A), the amplitude of A_k^S has deviations from azimuthal invariance and exhibits a strong trigonal warping, with long arms stretching along the K-to-M directions, consistent with a three-fold rotational symmetry of the system [Fig. 2(a)]. For the second lowest energy exciton which is also bright, giving rise to peak B, the phase of its A_k^S plotted in Fig. 2(f) has a phase winding pattern that corresponds to an angular quantum number of m=1, indicating that it is 2p-like. Also, its amplitude has lobed structures [Fig. 2(b)], the characteristic of hydrogen-like p-state wavefunction in a crystal field [31]. We find that the third lowest energy exciton with m=-1 is an optically inactive 2p-like state [Figs. 2(c) and 2(g)]. For the bright exciton forming peak C, a character of a 2s-like state is clearly seen in Figs. 2(d) and 2(e). For instance, it has a node in its amplitude that forms a dark circular ring with radius around 0.25 Å⁻¹ in Fig. 2(d), and the phase of A_k^S from the inside to the outside of the nodal circle changes by π with an angular momentum character of m=0. In summary, by restricting the solutions to basically only one valley, the bright singlet excitons forming peaks A, B and C are 1s-, 2p- and 2s-like states, respectively [46].

These bright singlet excitonic states here conform to the optical selection rules first derived in Ref. [6] by Cao, Wu and Louie (CWL), i.e., $m=-l_{\pm} \pmod n$, for a 2D insulator with n-fold rotational symmetry. Here, l_{\pm} denotes the winding number of the interband optical matrix element $e_{\pm} \cdot \langle v k | \hat{v} | c k \rangle$, corresponding to the coupling to σ_{\pm} polarized photon modes. The CWL selection rules make use of the topological invariants, l_{\pm} and l_{-} , that are characteristic of 2D insulating materials. For the lowest conduction band and highest valence band around the K-valley in monolayer hBN, $l_{+}=0$ and $l_{-}=-1$ (SM Sec. II), and the system has n=3 from the three-fold rotational symmetry. According to the CWL selections rules, for the K-valley, $l_+ = 0$ gives rise to optically active 1s- and 2s-like states (m = 0) in σ_+ polarized light, while $l_- = -1$ ensures the allowed excitation of one of the 2p-like states (m=1) by σ_{-} polarization. The time-reversed criteria apply for the K'-valley derived excitons. Note that while the CWL selection rules make clear which excitations are forbidden, they do not predict quantitively the oscillator strength of those allowed excitations. For monolayer TMDs, within a massive Dirac fermion model, the excitation of 2p-like exciton is also selection-allowed [47]. Nonetheless, it is not experimentally observed due to its extremely small oscillator strength [48]. The reason for the drastic difference between monolayer hBN and monolayer TMDs is that hBN has a larger trigonal warping effect than typical TMDs, and we find that the degree of trigonal warping is positively correlated to the oscillator strength of the 2p-like exciton (SM Sec. III). The strong trigonal warping of the 2p-like exciton (as well as the s-like excitons) in monolayer hBN is reflected in the distinct three-fold rotation symmetry seen in its envelope functions (Fig. 2).

Unlike excitons in common monolayer TMDs that are of Wannier type with k-space wavefunction localized at the bottoms of the two valleys, the single-valley excitons in hBN have k-space wavefunctions that are highly non-localized despite still being centered at K or K'. The blue dashed ring in Fig. 2(a) has a radius of 1/3 in units of $2\pi/a$ (a is the lattice constant of 2.509 Å), which is half the distance between K and K'. Outside of the blue dashed ring, the magnitude of A_k^S from the single-patch calculation is still considerably large outside of the K-valley, resulting in mixing of interband transitions from the two valleys once both valleys are taken into consideration. The true exciton envelope function is composed of coupling of transitions between the flat bands along fully in the K-M high-symmetry directions. This leads to the loss of distinct chirality associated with transitions restricted to an individual valley, resulting in the absence of perfect circular dichroism in the optical response of monolayer hBN. In typical monolayer TMDs, e.g. monolayer MoS₂, for most purposes, one can think of the excitons as being time-reversed pair of nearly independent excitonic states localized separately and isolated at either the bottom of the K-or K'-valley, with distinct chirality. As a result, polarization-resolved photoluminescence (PL) spectrum of MoS₂ exhibit circular dichroism (or valley polarization), namely when excited by σ_+ (σ_-) radiation, the polarization of

light from luminescence is basically purely σ_+ (σ_-). The helicity parameter ρ , as defined by $[I(\sigma_+) - I(\sigma_-)]/[I(\sigma_+) + I(\sigma_-)]$ where I denotes intensity, is virtually 1 (-1), as confirmed by experiment [49]. On the other hand, in monolayer hBN, a similar excitation by circularly polarized light will lead to excitation composed of interband electron-hole pairs from a large part of the BZ, including contributions from the other valley. Thus, our GW-BSE theory predicts that the luminescence exhibits both σ_+ and σ_- components. Our results give a value of $|\rho|$ equals to 0.78, 0.62 and 0.75 for photon energy corresponding to peak A, B and C, respectively (SM Sec. IV).

Because of intervalley coupling, strictly speaking, one cannot classify the true excitons in hBN in terms of hydrogenic/Rydberg-like states, but as demonstrated below we can still approximately do so. To theoretical analysis, one can expand the true exciton states ψ_i of monolayer hBN in terms of some basis excitonic states ϕ_K^j and $\phi_{K'}^l$, that are derived from restricting the basis excitons being composed of transitions from either the K or K' region as in a "patch" calculation (which are the single-valley excitons). That is, $\psi_i = \sum_{j,l} (C^i_{K,j} \phi^j_K + C^i_{K',l} \phi^l_{K'})$ where jand l denote the quantum numbers of the K and K' basis excitons, respectively. Such a coupling between the basis excitons ϕ_K^J and $\phi_{K'}^l$ (derived from K- and K'-valleys) is naturally included in our complete theory when the full BSE Hamiltonian is solved. Given our finding of the non-localized nature of the true excitons ψ_i in kspace, this intervalley interaction (that is nonzero values for the off-diagonal coefficients C) may, in fact, be significant for some states. According to symmetry analysis [14], 1s-like basis exciton ϕ_K^{1s} with its time-reversal counterpart $\phi_{K'}^{1s}$ form two orthogonal basis functions of the two-dimensional irreducible representation E of the crystal symmetry: the basis exciton in the K- (K'-) valley belongs to E_+ (E_-) component with $e^{-i\frac{2\pi}{3}}$ ($e^{i\frac{2\pi}{3}}$) eigenvalue of C_3 -rotation. The 2s-like basis excitons ϕ_K^{2s} and $\phi_{K'}^{2s}$ from the two valleys have exactly the same symmetry properties as those of the 1s-like basis excitons. Although the bright 2p-like (m = 1 and m = -1 for K- and K'-valleys respectively) basis excitons, $\phi_K^{2p_+}$ and $\phi_{K'}^{2p_-}$, have the same representation E, the E_+ (E_-) component is in the K'- (K-) valley, which is opposite to the 1s- and 2s-like basis excitons. When intervalley interactions are taken into considerations, only basis excitonic states (ϕ_K^I and $\phi_{K'}^I$) with both same irreducible representation and the same representation component can be hybridized, as the full BSE Hamiltonian respects the crystal symmetries. Therefore, only 2p-like basis exciton in the K- (K'-) valley is allowed to be hybridized with 1s- and 2s-like excitons in the K'- (K-) valley. Since the energy difference between 1s- and 2p-like basis excitons is as large as 890 meV compared to a value of 240 meV between the 2s- and 2p-like states, we expect stronger intervalley coupling between the latter states from different valleys. Indeed, our calculations in the full BZ using a **k**-points sampling $400 \times 400 \times 1$ show that the inclusion of K and K' interactions causes a level repulsion between 2p- and 2s-like states, with the energy level of 2p- (2s-) like state decreased (increased) by 30 (28) meV (SM Sec. V) as compared to that in the absence of K and K' interactions, while the energy of the 1s-like states remains unchanged [50]. Thus, although intervalley coupling is there, its influence to the energy and character of the excitons is not dominant; we shall therefore continue to denote a true exciton state with the nomenclature of the Rydberg series associated with its corresponding primary basis exciton.

The intervalley 2p-2s excitonic hybridization can be further seen from Fig. 3, where the square root of the sum of the magnitude square of the envelope functions ($\sqrt{\sum_{S} |A_k^S|^2}$, here S denotes summation over degenerate states) contributing to peaks A [Fig. 3(a)], B [Fig. 3(b)] and C [Fig. 3(c)] from the calculation with inclusion of intervalley interaction are plotted. It is clear peak A is still 1s-like. While excitons forming peak B (C) are 2p-like (2s-like)

without including intervalley interaction (see Fig. 2), the peak now has characteristic of both 2p- and 2s-like states in the presence of K- and K'-valleys interaction. In particular, for excitons forming peak B, the non-zero magnitude of electron-hole pair excitations at exactly the K- or K'-point shown in Fig. 3(b) comes from admixture with the 2s-like states; For peak C, the nodal structure of 2s-state [Fig. 3(c)] disappears due to non-zero electron-hole pairs excitations of 2p-like states in the same k-points. The intervalley interaction induces hybridization of 2s- and 2p-like states located in different valleys, making the amplitude of the excitons envelope functions contributing to peak B and peak C similar as shown in Figs. 3(b) and 3(c), as well as resulting in novel excitonic s-p hybridization states which were not previously reported.

In conclusion, we have performed first-principles calculations of the electronic and optical properties of monolayer hBN with many-electron interaction effects included, employing the *GW* and *GW*-BSE methods, respectively. We identify and analyze the characters of the exciton peaks in the optical spectrum. The first peak corresponds to 1s-like excitons at 5.95 eV with a large binding energy of 2.08 eV. Remarkably, we discovered that the second peak corresponds to bright p-like excitons with an excitation energy of 6.84 eV, which is consistent with the CWL optical selection rules [6] for excitons in 2D insulators, but has not previously been characterized correctly in experiment or theory. Also, due to the extended **k**-space envelope function of the excitons, the near perfect circular dichroism seen in monolayer TMDs is no longer present in monolayer hBN, and intervalley coupling of s-and p-like excitons further leads to symmetry-allowed intervalley s-p hybridization. We expect that the novel p-like excitons and s-p excitonic hybridization found here would help us to understand excitonic properties of defects in and heterostructures made by hBN layers, as well as open a new avenue for photoelectronics.

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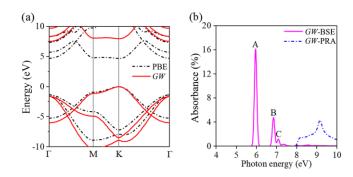


FIG. 1. (a) DFT-PBE (dash black) and full-frequency eigenvalue-self-consistent GW (solid red) band structures. The top of the valence band is set at 0 eV. (b) Calculated absorption spectrum with (GW-BSE, solid pink) and without (GW-RPA, dash blue) electron-hole interactions for linear-polarized light. The first three peaks are labeled as A, B and C, respectively. A gaussian broadening factor of 100 meV is included.

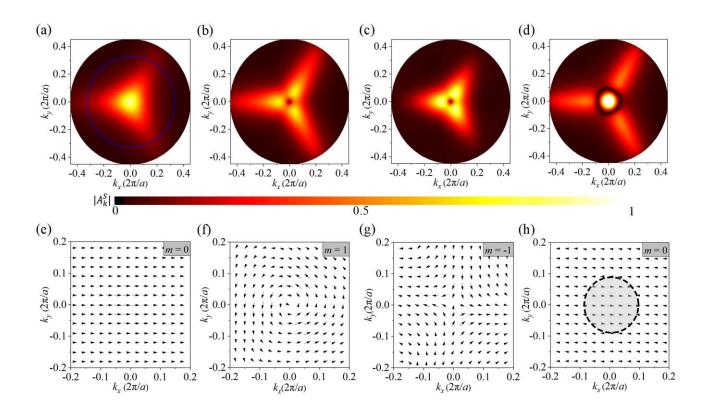


FIG. 2. Calculated amplitude and phase in **k**-space of the envelope function A_k^S for the first four lowest energy singlet excitons, from a calculation restricting coupling only of interband transitions within the K-valley region. The amplitude of A_k^S of the state corresponding to (a) peak A, (b) peak B, (c) a dark exciton near peak B, and (d) peak C, as labeled in Fig.1. The amplitude indicates the magnitude of the free electron-hole pair excitation at each **k**-point. The plotted value of each point has been normalized to its overall largest value in the BZ. The color scalebar is shown under panels (a)-(d). The phase of A_k^S is presented for states in (e) peak A, (f) peak B, (g) a dark exciton near peak B, and (h) peak C. The angle of the arrows with respect to the **k**_x-direction gives the phase of A_k^S . Length of arrows' tail represents the relative amplitude of A_k^S . The winding number about the K-point, M, denotes the angular quantum number of A_k^S . All plots use Cartesian coordinates where the origin is set at K-point. The blue dashed circle in (a) has radius $\frac{1}{3} \cdot \frac{2\pi}{a}$. The black dashed circle in (h) highlights the nodal structure as seen in (d). Note that the **k**-space regions in (a-d) are different from those in (e-h).

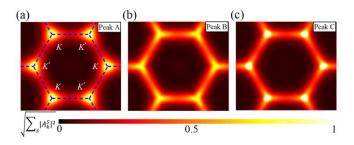


FIG. 3. Calculated amplitude of the envelope function A_k^S of bright excitons contributing to the first three peaks in the optical absorption spectrum of monolayer hBN, in the presence of K- and K'-valley interaction. The square root of the sum of amplitude square of excitons corresponding to (a) peak A, (b) peak B, and (c) peak C in the full BZ region, normalized to its overall largest value with the color scale-bar shown below the panels. The summation index S represents degenerate bright excitonic states.