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# Astrophysical Constraints on the Symmetry Energy and the Neutron Skin of $^{208}\text{Pb}$ with Minimal Modeling Assumptions

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The symmetry energy and its density dependence are crucial inputs for many nuclear physics and astrophysics applications, as they determine properties ranging from the neutron-skin thickness of nuclei to the crust thickness and the radius of neutron stars. Recently, PREX-II reported a value of  $0.283 \pm 0.071$  fm for the neutron-skin thickness of  $^{208}\text{Pb}$ , implying a slope parameter  $106 \pm 37$  MeV, larger than most ranges obtained from microscopic calculations and other nuclear experiments. We use a nonparametric equation of state representation based on Gaussian processes to constrain the symmetry energy  $S_0$ ,  $L$ , and  $R_{\text{skin}}^{^{208}\text{Pb}}$  directly from observations of neutron stars with minimal modeling assumptions. The resulting astrophysical constraints from heavy pulsar masses, LIGO/Virgo, and NICER clearly favor smaller values of the neutron skin and  $L$ , as well as negative symmetry incompressibilities. Combining astrophysical data with PREX-II and chiral effective field theory constraints yields  $S_0 = 33.0_{-1.8}^{+2.0}$  MeV,  $L = 53_{-15}^{+14}$  MeV, and  $R_{\text{skin}}^{^{208}\text{Pb}} = 0.17_{-0.04}^{+0.04}$  fm.

*Introduction*— The symmetry energy  $S(n)$  is a central quantity in nuclear physics and astrophysics. It characterizes the change in the nuclear-matter energy as the ratio of protons to neutrons is varied and thus impacts, e.g., the neutron-skin thickness of nuclei [1–3], their dipole polarizability [4, 5], and the radius of neutron stars (NSs) [6, 7]. This information is encoded in the nuclear equation of state (EOS), described by the nucleonic energy per particle,  $E_{\text{nuc}}/A$ , a function of total baryon density  $n$  and proton fraction  $x = n_p/n$  for proton density  $n_p$ . The energy per particle is connected to the bulk properties of atomic nuclei for proton fractions close to  $x = 1/2$ , i.e., symmetric nuclear matter (SNM) with  $E_{\text{SNM}}/A = (E_{\text{nuc}}/A)|_{x=1/2}$ . As the neutron-proton asymmetry increases (or the proton fraction  $x$  decreases) the energy per particle increases, reaching a maximum for  $x = 0$ , i.e., pure neutron matter (PNM) with  $E_{\text{PNM}}/A = (E_{\text{nuc}}/A)|_{x=0}$ . PNM is closely related to NS matter. The symmetry energy characterizes the difference between these two systems:

$$S(n) = \frac{E_{\text{PNM}}}{A}(n) - \frac{E_{\text{SNM}}}{A}(n). \quad (1)$$

Crucial information is encoded in the density dependence of  $S(n)$ , which is captured by the slope parameter  $L$  and the curvature  $K_{\text{sym}}$  defined at nuclear saturation density,  $n_0 \approx 0.16 \text{ fm}^{-3}$ ,

$$L = 3n \left. \frac{\partial S(n)}{\partial n} \right|_{n_0}, \quad K_{\text{sym}}(n) = 9n^2 \left. \frac{\partial^2 S(n)}{\partial n^2} \right|_{n_0}. \quad (2)$$

As  $d(E_{\text{SNM}}/A)/dn = 0$  at  $n_0$ ,  $L$  describes the pressure of PNM around  $n_0$ .  $S_0 = S(n_0)$  and  $L$  are of great interest

to nuclear physics [5, 8, 9] and astrophysics [10–12]. Experimental [4, 5, 13, 14] and theoretical [15–18] determinations consistently place  $S_0$  in the range of 30–35 MeV and  $L$  in the range of 30–70 MeV. Recently, however, the PREX-II experiment reported a new result for the neutron-skin thickness of  $^{208}\text{Pb}$  [19],  $R_{\text{skin}}^{^{208}\text{Pb}}$ , a quantity strongly correlated with  $L$  (see, e.g., [1–3]). The measurement of  $R_{\text{skin}}^{^{208}\text{Pb}} = 0.283 \pm 0.071$  fm (mean  $\pm$  standard deviation), including PREX-I and PREX-II data, led Ref. [20] to conclude that  $L = 106 \pm 37$  MeV. This value is larger than previous determinations, and thus presents a challenge to our understanding of nuclear matter, should a high  $L$  value be confirmed precisely.

In this Letter, we address this question by constraining  $S_0$ , its density dependence  $L$ , and  $R_{\text{skin}}^{^{208}\text{Pb}}$  directly from astrophysical observations. We adopt a nonparametric representation for the EOS [22, 23] to minimize the model dependence of the analysis, in contrast to other astrophysical inferences, e.g., Refs. [24–27]. Nonparametric inference allows us to explore a multitude of EOSs that are informed *only* by a NS crust model at densities  $n < 0.3n_0$ , where the EOS uncertainty is small, combined with the requirements of causality and thermodynamic stability at higher densities. Following Ref. [28], the possible EOSs are weighed based on their compatibility with gravitational-wave (GW) and electromagnetic observations of NSs (massive pulsars and X-ray timing with NICER). By calculating  $S_0$ ,  $L$ ,  $K_{\text{sym}}$  and  $R_{\text{skin}}^{^{208}\text{Pb}}$  for each of these EOSs, we obtain astrophysically informed posterior distributions for these key nuclear properties. Furthermore, we study how  $L$  and  $R_{\text{skin}}^{^{208}\text{Pb}}$  change as constraints from nuclear theory are included up to progress-

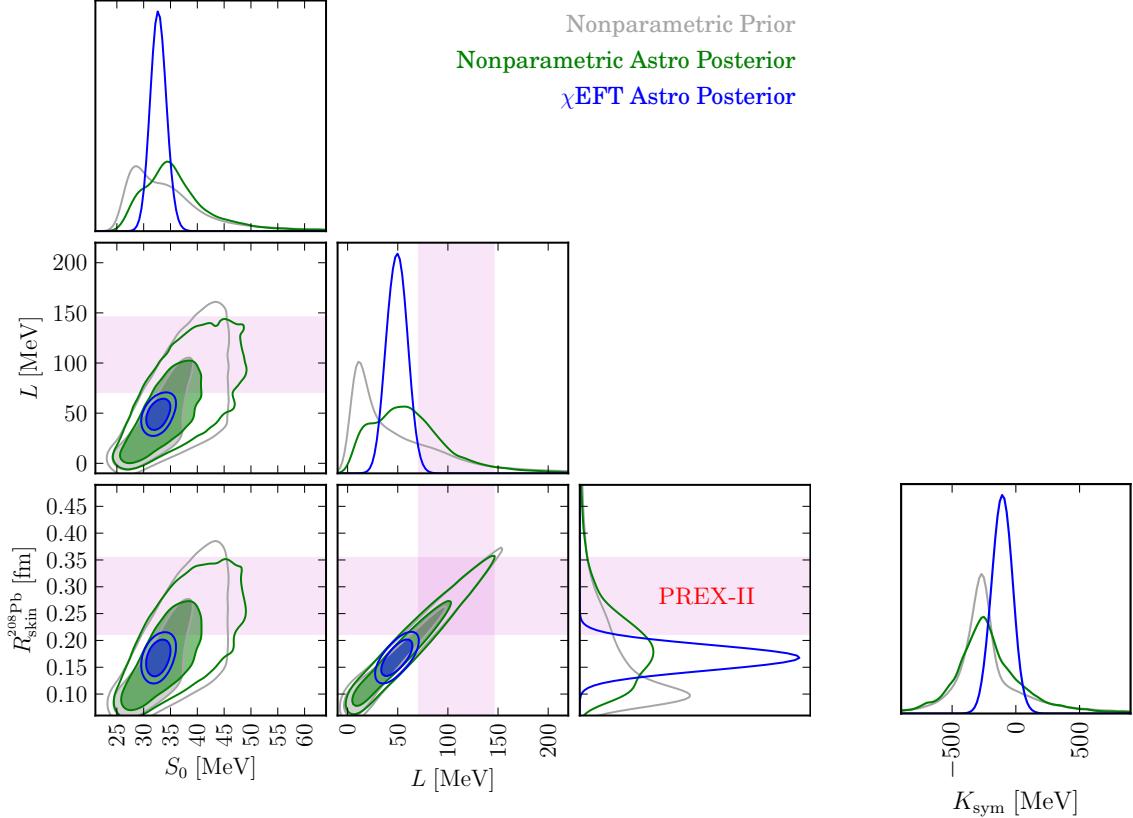


Figure 1. Correlations between the symmetry energy  $S_0$ , the slope parameter  $L$ , and the neutron skin thickness of  $^{208}\text{Pb}$   $R_{\text{skin}}^{^{208}\text{Pb}}$ . We show the nonparametric prior (grey), the nonparametric posterior conditioned on astrophysical observations (green), and the nonparametric posterior conditioned on an average over four  $\chi$ EFT calculations (up to  $\approx n_0$ ) and astrophysical observations (blue). Joint distributions show the 68% (shaded) and 90% (solid lines) credible regions. Shaded bands (pink) show the approximate 68% credible region for parameters constrained by PREX-II:  $R_{\text{skin}}^{^{208}\text{Pb}}$  [19] and the resulting constraints on  $L$  using the correlation from Ref. [21]. Note how the inclusion of the astrophysical observations shifts the peak in the marginal distributions for  $S_0$ ,  $L$ , and  $R_{\text{skin}}^{^{208}\text{Pb}}$ , a trend that is reinforced by the addition of  $\chi$ EFT information. We also show the one-dimensional marginal distributions for the symmetry incompressibility  $K_{\text{sym}}$  in a separate panel.

sively higher densities.

*Nonparametric inference for the EOS*— We connect NS observables to  $S_0$ ,  $L$ , and  $K_{\text{sym}}$  using a nonparametric representation of the EOS based on Gaussian processes (GPs) [22, 23]. The GPs model the uncertainty in the correlations between the sound speed in  $\beta$ -equilibrium at different pressures, but do not specify the exact functional form of the EOS, unlike other parameterizations [29–37]. The nonparametric EOSs consequently exhibit a wider range of behavior than parametric EOSs, mitigating the impact of modeling assumptions. The nonparametric EOS inference proceeds through Monte-Carlo sampling from a prior constructed as a mixture of GPs to obtain a large set of EOS realizations. Each EOS is then compared to astrophysical observations via optimized kernel density estimates (KDEs) of the likelihoods, resulting in a discrete representation of the posterior EOS process as a list of weighted samples (see [23, 28] for more details). The posterior probability

of a given EOS realization, which we label by its energy density  $\varepsilon_\beta$ , is calculated as

$$P(\varepsilon_\beta | \{d\}) \propto P(\varepsilon_\beta) \prod_i P(d_i | \varepsilon_\beta), \quad (3)$$

where  $\{d\} = \{d_1, d_2, \dots\}$  is the set of observations,  $P(d_i | \varepsilon_\beta)$  are the corresponding likelihood models, and  $P(\varepsilon_\beta)$  is the EOS realization's prior probability. The specific likelihoods used in this work are as follows: (a) Pulsar timing measurements of masses for the two heaviest known NSs (PSR J0740+6620 [38, 39], PSR J0348+0432 [40]) modeled as Gaussian distributions with means and standard deviations  $2.08 \pm 0.07 M_\odot$  and  $2.01 \pm 0.04 M_\odot$ , respectively; (b) GW measurements of masses and tidal deformabilities in the binary NS merger GW170817 [41] from Advanced LIGO [42] and Virgo [43]; and (c) X-ray pulse-profile measurements of PSR J0030+0451's mass and radius assuming a three-hotspot configuration [44] (see also Ref. [45]), which yields

	$E_{\text{PNM}}/A$ [MeV]	$S_0$ [MeV]	$L$ [MeV]	$K_{\text{sym}}$ [MeV]	$R_{\text{skin}}^{208\text{Pb}}$ [fm]
Nonparametric Prior	$17.5^{+14.6}_{-7.7}$	$33.3^{+14.7}_{-8.2}$	$38^{+109}_{-41}$	$-255^{+853}_{-566}$	$0.14^{+0.19}_{-0.09}$
Nonparametric Astro Posterior	$19.3^{+11.7}_{-8.5}$	$35.1^{+11.6}_{-8.9}$	$58^{+61}_{-56}$	$-240^{+559}_{-503}$	$0.19^{+0.12}_{-0.11}$
Nonparametric Astro+PREX-II Posterior	$21.5^{+10.8}_{-8.3}$	$37.3^{+11.8}_{-7.5}$	$80^{+51}_{-46}$	$-223^{+608}_{-565}$	$0.23^{+0.10}_{-0.10}$
$\chi$ EFT Astro Posterior	$16.9^{+1.5}_{-1.4}$	$32.7^{+1.9}_{-1.8}$	$49^{+14}_{-15}$	$-107^{+124}_{-128}$	$0.17^{+0.04}_{-0.04}$
$\chi$ EFT Astro+PREX-II Posterior	$17.1^{+1.5}_{-1.5}$	$33.0^{+2.0}_{-1.8}$	$53^{+14}_{-15}$	$-91^{+118}_{-130}$	$0.17^{+0.04}_{-0.04}$

Table I. Medians and 90% highest-probability-density credible regions for the studied nuclear properties. We compute  $R_{\text{skin}}^{208\text{Pb}}$  from  $L$  using the linear fit reported in Ref. [21], approximating the uncertainty in the fit as described in the text.

comparable results [28]).

Our basic nonparametric prior can also be conditioned self-consistently on theoretical calculations of the EOS at nuclear densities, while retaining complete model freedom at higher densities [46]. Here we marginalize over the uncertainty bands from four different chiral effective field theory ( $\chi$ EFT) calculations: quantum Monte Carlo calculations using local  $\chi$ EFT interactions up to next-to-next-to-leading order (N<sup>2</sup>LO) [47], many-body perturbation theory (MBPT) calculations using nonlocal  $\chi$ EFT interactions up to next-to-next-to-next-to-leading order (N<sup>3</sup>LO) of Refs. [16, 48], and MBPT calculations with two-nucleon interactions at N<sup>3</sup>LO and three-nucleon interactions at N<sup>2</sup>LO (based on a broader range of three-nucleon couplings) [32, 49]. The resulting marginalized  $\chi$ EFT band overlaps with results for other realistic Hamiltonians, particularly for Argonne- and Urbana-type interactions [50]. This allows us to account for different nuclear interactions and many-body approaches, increasing the robustness of our results.

To translate the EOS posterior process into distributions for the nuclear physics properties, we establish a probabilistic map from  $\varepsilon_\beta$  to  $E_{\text{PNM}}/A$ ,  $S_0$ ,  $L$ , and  $K_{\text{sym}}$  (described below). Marginalization over the EOS then yields a posterior

$$P(E_{\text{PNM}}/A, S_0, L, K_{\text{sym}} | \{d\}) = \int \mathcal{D}\varepsilon_\beta P(\varepsilon_\beta | \{d\}) P(E_{\text{PNM}}/A, S_0, L, K_{\text{sym}} | \varepsilon_\beta) \quad (4)$$

informed by the astrophysical observations. Constraints on  $R_{\text{skin}}^{208\text{Pb}}$  are obtained from empirical correlations with  $L$  [21] calculated from a broad range of nonrelativistic Skyrme and relativistic mean-field density functionals; see also Refs. [1, 3]. To account for the theoretical uncertainty in the fit of Ref. [2] and mitigate its model dependence (c.f. Refs. [13, 21, 51]), we adopt a probabilistic mapping:  $P(R_{\text{skin}}^{208\text{Pb}} | L) = \mathcal{N}(\mu_R(L) [\text{fm}] = 0.072 + 0.00194 \times (L [\text{MeV}]) \text{ and } \sigma_R = 0.0143 \text{ fm.}$

*Reconstructing the symmetry energy*—Because our nonparametric EOS realizations are not formulated in terms of  $S_0$ ,  $L$ , or  $K_{\text{sym}}$ , we discuss how to extract the nuclear parameters near  $n_0$  directly from the EOS, see the Supplemental Material for more details. The nonparametric

inference provides the individual EOSs in terms of the baryon density  $n$  as well as the pressure  $p_\beta$  and energy density  $\varepsilon_\beta$  in  $\beta$ -equilibrium. Each realization is matched to the BPS crust [52] around  $0.3n_0$ . The choice of a single crust at low densities does not affect our conclusions; see Sec. V of [53]. The EOS quantities are related to  $E_{\text{nuc}}/A$  through  $\varepsilon = n(E_{\text{nuc}}/A + m_N)$  with the average nucleon mass  $m_N$ . To reconstruct  $E_{\text{nuc}}/A$ , we correct  $\varepsilon_\beta$  by the electron contribution  $\varepsilon_e$ ,

$$\frac{E_{\text{nuc}}}{A}(n, x) = \frac{\varepsilon_\beta(n) - \varepsilon_e(n, x)}{n} - m_N. \quad (5)$$

The proton fraction  $x(n)$  is unknown and needs to be determined self-consistently for each EOS by enforcing  $\beta$ -equilibrium,  $\mu_n(n, x) = \mu_p(n, x) + \mu_e(n, x)$ , where  $\mu_i(n, x)$  is the chemical potential for particle species  $i$ . This leads to the condition for  $\beta$ -equilibrium (see [32] and the Supplemental Material for details),

$$0 = m_n - m_p - \frac{\partial (E_{\text{nuc}}/A)}{\partial x} - \mu_e(n, x). \quad (6)$$

To extract the symmetry energy from each EOS realization, we need to know the dependence of  $E_{\text{nuc}}/A$  with proton fraction. Here, we approximate the  $x$  dependence using the standard quadratic expansion,

$$\frac{E_{\text{nuc}}}{A}(n, x) = \frac{E_{\text{SNM}}}{A}(n) + S(n)(1 - 2x)^2. \quad (7)$$

Non-quadratic terms are small at  $n_0$  and can be neglected given current EOS uncertainties [54, 55]. Because we only work around  $n_0$ , we can characterize the SNM energy using the standard expansion,

$$\frac{E_{\text{SNM}}}{A}(n) = E_0 + \frac{1}{2}K_0 \left( \frac{n - n_0}{3n_0} \right)^2 + \dots, \quad (8)$$

where uncertainty in the saturation energy  $E_0$ ,  $n_0$ , and the incompressibility  $K_0$  is based on the empirical ranges from Ref. [9]. Combining Eqs. (1) and (5)–(8), we find that  $\beta$ -equilibrium must satisfy

$$\begin{aligned} & \frac{1 - 2x_\beta}{4} (m_p - m_n + \mu_e(n, x_\beta)) \\ &= \left( \frac{\varepsilon_\beta - \varepsilon_e(n, x_\beta)}{n} - m_N - \frac{E_{\text{SNM}}}{A}(n) \right). \end{aligned} \quad (9)$$

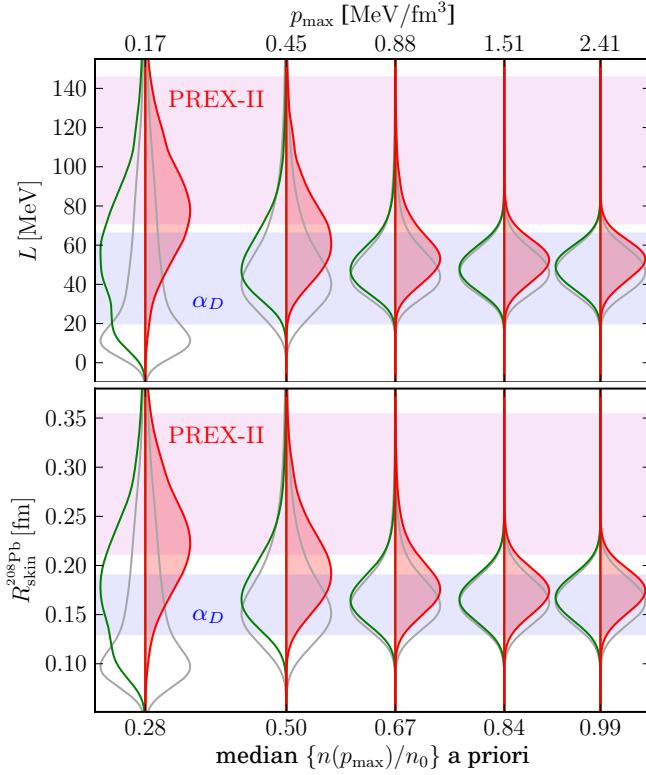


Figure 2. Prior (gray, unshaded), Astro posterior (green, left/unshaded), and Astro+PREX-II posterior (red, right/shaded) distributions for  $L$  (top) and  $R_{\text{skin}}^{208\text{Pb}}$  (bottom) as a function of the maximum pressure (top axis) or density (bottom axis) up to which we trust theoretical nuclear-physics predictions from  $\chi$ EFT (see text for details). Shaded bands show the approximate 68% credible region from PREX-II [19] (pink) and from Ref. [13] based on the electric dipole polarizability  $\alpha_D$  (light blue).

We use the relations for a relativistic Fermi gas for the electron energy density and chemical potential [56].

To summarize, given a nonparametric EOS realization and a sample from the empirical distribution for each of the parameters  $E_0$ ,  $K_0$ , and  $n_0$ , we reconstruct the proton fraction in  $\beta$ -equilibrium  $x_\beta$  self-consistently at each density around nuclear saturation. We then calculate  $E_{\text{PNM}}/A$ ,  $S_0$ ,  $L$ , and  $K_{\text{sym}}$  as a function of  $n$  and report their values at the reference density  $n_0^{(\text{ref})} = 0.16 \text{ fm}^{-3}$ . The neutron-skin thickness is estimated via the empirical fit between  $R_{\text{skin}}^{208\text{Pb}}$  and  $L$ , as discussed above.

*Results and discussion—* The constraints on  $S_0$ ,  $L$ ,  $K_{\text{sym}}$ , and  $R_{\text{skin}}^{208\text{Pb}}$  are shown in Fig. 1. We plot the nonparametric prior, the posterior constrained by astrophysical data, and the posterior additionally constrained by the  $\chi$ EFT calculations up to  $n \approx n_0$ . As our GPs are conditioned on  $\chi$ EFT up to a maximum pressure ( $p_{\text{max}}$ ), we report the median density at that pressure (the exact density at  $p_{\text{max}}$  varies due to uncertainty in the EOS from

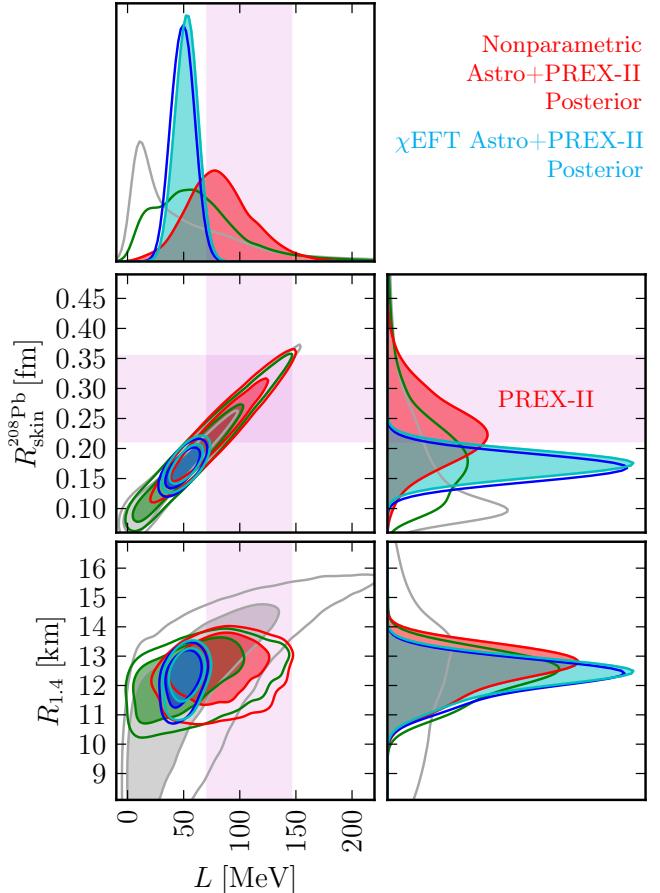


Figure 3. Correlations between  $R_{\text{skin}}^{208\text{Pb}}$ ,  $L$ , and the radius of a  $1.4M_\odot$  NS,  $R_{1.4}$ . In addition to the priors and posteriors shown in Fig. 1, we show the nonparametric (red) and  $\chi$ EFT (trusted up to  $n_0$ ; light blue) posteriors conditioned on both astrophysical observations and PREX-II. Astro+PREX-II posteriors are shaded in the one-dimensional distributions to distinguish them from the Astro-only posteriors. Joint distributions show the 68% (shaded) and 90% (solid lines) credible regions. Shaded bands (pink) show the approximate 68% credible region from PREX-II.

$\chi$ EFT). Prior and posterior credible regions are provided in Tb. I. We find that the PREX-II result for  $R_{\text{skin}}^{208\text{Pb}}$  and the extracted range for  $L$  of Ref. [20], 73–147 MeV at  $1\sigma$ , are in mild tension with the GP conditioned on  $\chi$ EFT calculations up to  $n_0$ , while the GP conditioned only on astrophysical observations is consistent with both results and cannot resolve any tension due to its large uncertainties. However, the Astro-only and  $\chi$ EFT posteriors peak at similar values for  $L$  (55–65 MeV), below the PREX-II result. The astrophysical data does not strongly constrain  $K_{\text{sym}}$ , but suggests it is negative.

In Fig. 2, we show the evolution of our constraints on  $L$  and  $R_{\text{skin}}^{208\text{Pb}}$  as a function of the maximum density up to which we condition on  $\chi$ EFT, from no conditioning

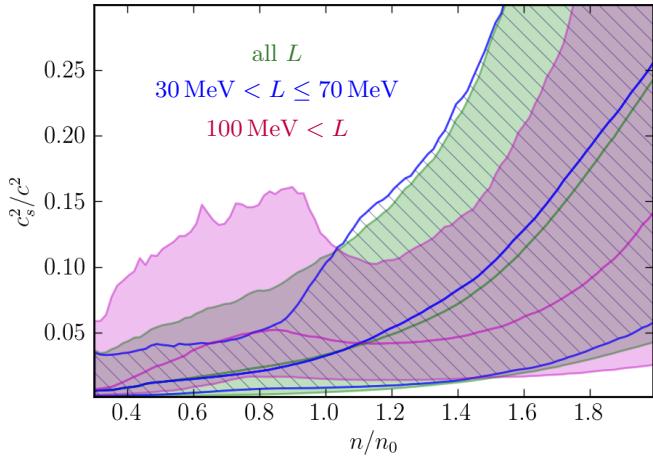


Figure 4. Median and 90% one-dimensional symmetric posterior credible regions for  $c_s^2$  at each density  $n$  with astrophysical observations for all  $L$  (shaded green),  $30 \text{ MeV} < L \leq 70 \text{ MeV}$  (unshaded blue hatches), and  $100 \text{ MeV} < L$  (shaded purple).

on  $\chi$ EFT to conditioning on  $\chi$ EFT up to  $n_0$ . The more we trust  $\chi$ EFT constraints, the larger the tension with PREX-II results becomes. We estimate a 12.3% probability ( $p$ -value) that the true  $R_{\text{skin}}^{208\text{Pb}}$  differs from the PREX-II mean at least as much as the Astro+ $\chi$ EFT posterior suggests, given the uncertainty in PREX-II's measurement. However, if a hypothetical experiment confirmed the PREX-II mean with half the uncertainty, this  $p$ -value would be reduced to 0.6%. We also show the estimate for  $R_{\text{skin}}^{208\text{Pb}}$  obtained from an analysis of dipole polarizability data ( $\alpha_D^{208\text{Pb}}$ , [13]), which finds  $R_{\text{skin}}^{208\text{Pb}} = 0.13\text{--}0.19 \text{ fm}$ . The latter agrees very well with both the  $\chi$ EFT results and the nonparametric GP. See [53] for more comparisons, including joint constraints with both  $R_{\text{skin}}^{208\text{Pb}}$  and  $\alpha_D^{208\text{Pb}}$ .

In Fig. 3, we present the modeled correlation between  $L$  and  $R_{\text{skin}}^{208\text{Pb}}$  as well as the radius of a  $1.4M_\odot$  NS,  $R_{1.4}$ . Besides those shared with Fig. 1, we show posteriors that are also conditioned on the PREX-II result. Even though the results for  $L$  and  $R_{\text{skin}}^{208\text{Pb}}$  are very different for the various constraints,  $R_{1.4}$  does not significantly change. Indeed, the mapping from  $L$  to  $R_{1.4}$  is broader than often assumed [6], and we find that  $R_{1.4}$  is nearly independent of our range for  $L$ . Hence, the findings of Ref. [20], indicating that PREX-II requires large radii, include some model dependence.

Given the mild tension between the PREX-II value of  $R_{\text{skin}}^{208\text{Pb}}$  and that inferred from the astrophysical inference with  $\chi$ EFT information, we investigate what kind of EOS behavior is required to satisfy both the PREX-II and astrophysical constraints. In Fig. 4 we show the speed of sound  $c_s$  as a function of density for the nonparametric

GP conditioned only on astrophysical data for all values of  $L$ , for  $30 \text{ MeV} < L \leq 70 \text{ MeV}$ , and for  $L > 100 \text{ MeV}$ . We find that the speed of sound generally increases with density. However, if we assume  $L > 100 \text{ MeV}$ , we find a local maximum in the median  $c_s(n)$  just below  $n_0$ , although the uncertainties in  $c_s$  are large. The reason for this feature is that EOSs that are stiff at low densities (large  $L$ ) need to soften beyond  $n_0$  to remain consistent with astrophysical data from GW observations, in particular GW170817. Should the PREX-II constraints be confirmed with smaller uncertainty in the future, this might favor the existence of a phase transition between  $1\text{--}2n_0$ .

In summary, we have used nonparametric GP EOS inference to constrain the symmetry energy, its density dependence, and  $R_{\text{skin}}^{208\text{Pb}}$  directly from astrophysical data, leading to  $S_0 = 35.1^{+11.6}_{-8.9} \text{ MeV}$ ,  $L = 58^{+61}_{-56} \text{ MeV}$ , and  $R_{\text{skin}}^{208\text{Pb}} = 0.19^{+0.12}_{-0.11} \text{ fm}$ . Folding in  $\chi$ EFT constraints reduces these ranges to  $S_0 = 32.7^{+1.9}_{-1.8} \text{ MeV}$ ,  $L = 49^{+14}_{-15} \text{ MeV}$ , and  $R_{\text{skin}}^{208\text{Pb}} = 0.17^{+0.04}_{-0.04} \text{ fm}$ . While these results prefer values below the recent PREX-II values [19, 20], in good agreement with other nuclear physics information, the PREX-II uncertainties are still broad and any tension is mild. Our nonparametric analysis suggests that a  $R_{\text{skin}}^{208\text{Pb}}$  uncertainty of  $\pm 0.04 \text{ fm}$  could challenge astrophysical and  $\chi$ EFT constraints. Note that the formation of light clusters at the surface of heavy nuclei could affect the extracted  $L$  value [57]. Finally, our results demonstrate that the correlation between  $R_{1.4}$  and  $L$  (or  $R_{\text{skin}}^{208\text{Pb}}$ ) is looser than analyses based on a specific class of EOS models would suggest. Extrapolating neutron-skin thickness measurements to NS scales thus requires a careful treatment of systematic EOS model uncertainties. In particular, the PREX-II result does not require large NS radii. However, if the high  $L$  values of PREX-II persist, this may suggest a peak in the sound speed around saturation density.

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