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Thermal interferometry of anyons in spin liquids

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Aharonov-Bohm interferometry is the most direct probe of anyonic statistics in the quantum Hall effect. The technique involves oscillations of the electric current as a function of the magnetic field and is not applicable to Kitaev spin liquids and other systems without charged quasiparticles. Here, we establish a novel protocol, involving heat transport, for revealing fractional statistics even in the absence of charged excitations, as is the case in quantum spin liquids. Specifically, we demonstrate that heat transport in Kitaev spin liquids through two distinct interferometer's geometries, Fabry-Perot and Mach-Zehnder, exhibits drastically different behaviors. Therefore, we propose the use of heat transport interferometry as a probe of anyonic statistics in charge insulators.

The last three years have seen important developments in probing fractional statistics in the quantum Hall effect [1]. One development was a Fabry-Perot interferometry experiment [2] at the filling factor 1/3 (Fig. 1a). In the experiment, electric current flows through two constrictions (QPC1 and QPC2). The interference of the contributions from the two constrictions manifests itself in Aharonov-Bohm oscillations of the current in response to changing magnetic field. The period of the oscillations is determined by the charge of the interfering quasiparticles. At some values of the field, the oscillation phase jumps. This happens because new anyons enter between the constrictions. The phase jumps encode the statistics of those anyons. The physics is even more interesting for non-Abelian anyons in the second Landau level, where the even-odd effect is expected: as new anyons enter the device, an interference picture alternatively turns on and off [3-5].

Anyons are electrically charged in the quantum Hall effect. Fractional statistics has also been long predicted in systems without charged excitations. Examples include the Kalmeyer-Laughlin [6] and Kitaev [7] spin liquids. A recent thermal conductance experiment [8] supports the presence of non-Abelian anyons in α -RuCl₃, which is believed to host a Kitaev liquid [9]. The interpretation of that experiment is currently debated [10-12], and it is clear that new methods are needed to test quasiparticle statistics of neutral excitations. Interferometry is the most direct probe [13-15] of statistics since it involves running anyons around other anyons. However, the Aharonov-Bohm technique cannot work in the absence of charged quasiparticles. Thus, one can only implement it indirectly by conjugating a spin liquid with a system that can carry electric current [14].

In this paper we show that a direct version of interferometry does not require charged excitations. It involves heat current instead of electric current and can be implemented in any systems since energy can flow in any system. The magnetic field ceases being a convenient experimental knob. Instead, it becomes useful to compare transport in the Fabry-Perot [13] and Mach-Zehnder



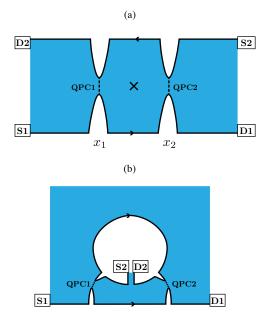


FIG. 1: Fabry-Perot (a) and Mach-Zehnder (b) interferometers. Heat travels from sources S1 and S2 to drains D1 and D2 along chiral edges and tunnels between the edges at the two point contacts shown with dashed lines. The cross shows a localized anyon.

Multiple experiments on quantized thermal conductance in topological matter have been published in recent years. This includes work on the integer quantum Hall effect [18], the fractional quantum Hall effect in GaAs [19, 20] and graphene [21, 22], and the high-magneticfield regime [8, 23] in α -RuCl₃. At low temperatures, the gapped bulk of a topological material does not participate in heat conduction and only the edges matter. At the same time, any material contains gapless phonons, which should be taken into account in the interpretation of the data [18–20]. Their interaction with the edges rapidly decreases as the temperature goes to zero [10, 11] and will be neglected below [24]. In the opposite limit of a strong interaction, interferometry cannot work due to the dominant dephasing of edge degrees of freedom by phonons [25].

Our approach can be used with any fractional statistics. We will focus below on one particular anyon statistics predicted [7] in a non-Abelian Kitaev spin liquid. Three types of excitations exist in that liquid: trivial boson or vacuum 1, Majorana fermion ψ , and Ising anyon σ . Any combination of quasiparticles belongs to one of these sectors. Two quasiparticles can fuse in the following ways:

$$\psi \times \psi = 1; \ \psi \times \sigma = \sigma; \sigma \times \sigma = 1 + \psi,$$
 (1)

where the final equality expresses two possible fusion outcomes for Ising anyons. The outcome of an interferometry experiment can be expressed in terms of the anyonic topological spins [7] θ_x and depends on the phase $\exp(i\phi_{ab}^c) = \frac{\theta_c}{\theta_a \theta_b}$ accumulated by anyon *a* on a full counterclockwise circle around anyon *b* under the assumption that the two anyons fuse to *c*. We will need the following phases [26]:

$$\phi_{\sigma 1}^{\sigma} = 0; \ \phi_{\sigma \psi}^{\sigma} = \pi; \ \phi_{\sigma \sigma}^{1} = -\pi/4; \ \phi_{\sigma \sigma}^{\psi} = 3\pi/4.$$
 (2)

Such phases are accumulated when one anyon $a = \sigma$ tunnels consecutively through the two point contacts in Fig. 1 while another anyon $b = 1, \psi, \sigma$ is trapped between the two contacts.

Quantized thermal conductance is expected [27–29] when the two edges of a sample are far from each other. In interferometry, the edges are brought close in two points, and heat tunnels between the edges. This results in a non-universal correction to the thermal conductance. The correction depends on the tunneling amplitudes at the two contacts.

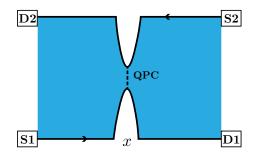


FIG. 2: A single tunneling contact is shown with a dashed line.

We start with a brief discussion of a single contact (Fig. 2). The Lagrangian of the system in Fig. 2

$$L_1 = L_{\rm edge,1} + L_{\rm edge,2} - T,$$
 (3)

where $L_{\text{edge},n}$ are the Lagrangians of the two edges and T describes tunneling. In the simplest model, the edges host free Majorana fermions [7]:

$$L_{\text{edge},n} = i \int dx \psi_n (\partial_t \pm v \partial_x) \psi_n, \qquad (4)$$

where v is the edge velocity and the sign shows the propagation direction. The tunneling operator creates two excitations that fuse to vacuum on the opposite sides of the contact. In the Ising order each particle is its own antiparticle and hence T creates two quasiparticles of the same type. In principle, T describes tunneling of multiple quasiparticle types and includes an infinite number of perturbations to the sum of the edge actions (4). At low temperatures and weak tunneling, the only perturbations that matter are relevant in the renormalization group sense. Our theory allows only one such perturbation

$$T = \exp(-i\pi/16)\Gamma\sigma_2(x)\sigma_1(x), \tag{5}$$

where σ_2 and σ_1 create Ising anyons in point x on the upper and lower edges respectively, $\Gamma > 0$ is the tunneling amplitude [30], and the exponential factor [14, 31] ensures hermiticity and equals $1/\sqrt{\text{topological spin.}}$

We are interested in the deviation of the thermal current between the terminals in Fig. 2 from the quantized value. The deviation equals the tunneling thermal current I_T through the point contact between the two edges. The current depends on the temperature difference between two sources S1 and S2 and hence the two edges that emanate from the source terminals. It also depends on the tunneling amplitude Γ and scales as Γ^2 in the lowest order of the perturbation theory at small Γ , $I_T = r(T_1, T_2)\Gamma^2$, where T_1 and T_2 are the temperatures of the two edges, and the factor $r(T_1, T_2)$ depends on details of the edge physics and can be computed with Fermi's golden rule:

$$r = \frac{2\pi}{\hbar} \sum_{mn} \Delta E |\langle m|T/\Gamma|n\rangle|^2 \delta(E_m - E_n) P_n(T_1, T_2), \quad (6)$$

where $|n\rangle, |m\rangle$ are eigenstates of the edge Hamiltonian, $E_{n,m}$ are the combined energies of the two edges in those states, P_n is the Gibbs distribution, and ΔE is the energy change of the upper edge in the $|n\rangle \rightarrow |m\rangle$ process.

The perturbative calculation is applicable as long as the tunneling heat current is much smaller than the total heat current along the edges. In the simplest model (4), $r \sim T_1^{1/4}$ at a constant ratio T_1/T_2 since the scaling dimension [7] of σ is 1/16.

We turn to a Fabry-Perot interferometer (Fig. 1a) now. The Lagrangian differs from (3) only by the presence of two tunneling terms in T:

$$T = \exp(-i\pi/16)\Gamma_1 \sigma_2(x_1)\sigma_1(x_1) + \exp(-i\pi/16)\Gamma_2 \sigma_2(x_2)\sigma_1(x_2),$$
(7)

where x_1 and x_2 are the locations of the two point contacts. The tunneling amplitudes Γ_1 and Γ_2 can be determined experimentally up to the factor $r(T_1, T_2)$ from comparison with a single-point-contact geometry. For such a comparison, one needs to fabricate a single point contact in exactly the same way as one of the two contacts in the interferometer and measure the tunneling heat current.

We will assume that the thermal length is much longer than the distance between the two QPCs, $hv/k_BT \gg x_2 - x_1$. This will allow us to treat the interferometer as a single point contact in an effective low-energy theory for energies $E \sim T_{1,2}$. In the absence of trapped quasiparticles, the low-temperature physics of the interferometer then reduces to that of a tunneling contact with the tunneling amplitude $\Gamma = \Gamma_1 + \Gamma_2$. Thus, the thermal current through the interferometer that contains no trapped topological charge

$$I_{\rm FP,1} = r(T_1, T_2)(\Gamma_1 + \Gamma_2)^2, \tag{8}$$

where the factor $r(T_1, T_2)$ is the same as for a single point contact. The above expression can be understood as the result of constructive interference of the two paths from the lower edge to the upper edge via the two point contacts.

A trapped Majorana fermion contributes a phase of π to any trajectory that encircles it. Hence, when the interferometer contains the topological charge ψ , there is a phase difference of π for the trajectories via the two point contacts. Interference becomes destructive:

$$I_{\rm FP,\psi} = r(T_1, T_2)(\Gamma_1 - \Gamma_2)^2.$$
(9)

A particularly interesting situation presents itself if the trapped topological charge in the device is $b = \sigma$. We need to consider separately two possibilities for the fusion channel of the tunneling and trapped anyons, c = 1 and $c = \psi$. The processes in the two fusion channels do not interfere with each other just like interference is absent for electron transport in the two spin channels. The probabilities of the two channels are equal as follows from the general expression [32]

$$P_{ab}^c = N_{ab}^c \frac{d_c}{d_a d_b},\tag{10}$$

where the fusion multiplicities $N_{\sigma\sigma}^1 = N_{\sigma\sigma}^{\psi} = 1$ and the quantum dimensions $d_1 = d_{\psi} = 1$, $d_{\sigma} = \sqrt{2}$. According

to Eq. (2), the interference phases in the two channels differ by π . Thus,

$$I_{\rm FP,\sigma} = \frac{r(T_1, T_2)}{2} \times \left[|\Gamma_1 + \exp(-i\pi/4)\Gamma_2|^2 + |\Gamma_1 - \exp(-i\pi/4)\Gamma_2|^2 \right] \\ = r(T_1, T_2)[\Gamma_1^2 + \Gamma_2^2].$$
(11)

If one can control the topological charge of the interferometer, the observation of the three regimes (8,9,11)would prove the Ising anyonic statistics. At present it is unclear [14] how to control the trapped charge, so it may happen that every interferometer is always in the same regime. This can only happen [33] in the regime (8), in which case the experiment is not very informative: the behavior (8) can be observed for any statistics, if the trapped topological charge is trivial. We thus turn to Mach-Zehnder interferometry (Fig. 1b) that does not require control of the trapped topological charge.

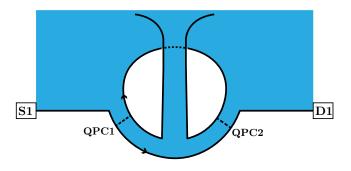


FIG. 3: The Mach-Zehnder setup is topologically equivalent to a setup with an infinite open inner edge.

In Mach-Zehnder interferometry, the topological charge inside the device changes after each tunneling event [1, 17]. Indeed, each anyon that tunnels into the inner edge of the device is eventually absorbed by a drain located inside the device. Fig. 3 depicts an alternative setting: a tunneling anyon ends up on a very long edge, which is inside the interference loop topologically. As a consequence, the tunneling probability changes for each tunneling event. We thus need to introduce a family of tunneling rates $p_{\sigma b}^c$, where b is the trapped topological charge and c is the fusion channel of b and the tunneling anyon σ . As before, we assume that the distance between the point contacts along each edge is much shorter than the thermal length. The tunneling Hamiltonian $\hat{T}=\Gamma_1\hat{T}_1+\Gamma_2\hat{T}_2e^{i\alpha}$ contains two real amplitudes $\Gamma_{1,2}$, two operators $\hat{T}_{1,2}$ that transfer an anyon from the outer edge to the inner edge, and a phase α , which ensures hermiticity. We will find α from the condition that the same tunneling rates obtain from \hat{T} and the tunneling Hamiltonian $\hat{T}^{\dagger} = \hat{T} = \Gamma_1 \hat{T}_1^{\dagger} + \Gamma_2 \hat{T}_2^{\dagger} e^{-i\alpha}$, where $\hat{T}_{1,2}^{\dagger}$ transfer anyons from the inner edge to the outer edge.

We first use \hat{T} . Only one fusion channel exists for $b = 1, \psi$, and one finds

$$p_{\sigma 1}^{\sigma} = p(T_1, T_2) |\Gamma_1 + \Gamma_2 e^{i\alpha}|^2;$$
(12)

$$p^{\sigma}_{\sigma\psi} = p(T_1, T_2) |\Gamma_1 - \Gamma_2 e^{i\alpha}|^2,$$
 (13)

where the expression for $p(T_1, T_2)$ follows from Fermi's golden rule and is similar to (6):

$$p = \frac{2\pi}{\hbar} \sum_{mn} |\langle m | \sigma_2(x) \sigma_1(x) | n \rangle|^2 \delta(E_m - E_n) P_n(T_1, T_2).$$
(14)

Two fusion outcomes are possible for $b = \sigma$. The probabilities of the fusion outcomes are identical, but the tunneling rates for the two outcomes are not:

$$p_{\sigma\sigma}^{1} = \frac{p(T_{1}, T_{2})}{2} \left| \Gamma_{1} + \Gamma_{2} \exp(i\alpha - i\pi/4) \right|^{2}; \qquad (15)$$

$$p_{\sigma\sigma}^{\psi} = \frac{p(T_1, T_2)}{2} \left| \Gamma_1 - \Gamma_2 \exp(i\alpha - i\pi/4) \right|^2.$$
(16)

The total tunneling rate

$$p_{\sigma\sigma} = p(T_1, T_2)[\Gamma_1^2 + \Gamma_2^2].$$
(17)

Repeating the same calculation [34] with T^{\dagger} gives the same set of answers for $\alpha = \pi/8$, which is thus the right choice in the above equations.

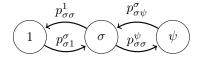


FIG. 4: The symbols in the circles show the trapped topological charge in a Mach-Zehnder interferometer. Arrows show possible transitions.

The average energy transferred between the edges in each tunneling event is the same [35]: ΔE = $r(T_1,T_2)/p(T_1,T_2)$. Thus, to compute the heat current we need to find the average number of tunneling events per unit time. All possible tunneling events are represented by the diagram in Fig. 4. The states of the interferometer are labeled with the trapped topological charge b. If we assume that the initial trapped charge is $b = \sigma$, the average time until a tunneling event $t_{\sigma} = 1/p_{\sigma\sigma}$. The probabilities of tunneling into states with b = 1 and $b = \psi$ are $q_1 = p_{\sigma\sigma}^1 / p_{\sigma\sigma}$ and $q_{\psi} = p_{\sigma\sigma}^{\psi} / p_{\sigma\sigma}$ respectively. The average times until tunneling from the states with b = 1 and $b = \psi$ to $b = \sigma$ are $t_1 = 1/p_{\sigma 1}$ and $t_{\psi} = 1/p_{\sigma \psi}$. After two tunneling events the system always returns to $b = \sigma$. The average time of two tunneling events is given by

Hence, the thermal current becomes

$$I_T = \frac{2\overline{\Delta E}}{\overline{t}} = r(T_1, T_2)(\Gamma_1^2 + \Gamma_2^2).$$
(19)

For comparison, if the tunneling particles are bosons or fermions, the behavior is the same as in the Fabry-Perot setup, Eq. (8). Thus, the observation of the contrasting behavior (8) and (19) in the two setups is a signature of fractional statistics is a system without charged quasiparticles.

The results for a Mach-Zehnder interferometer do not change if topological charge can tunnel between the edges of the device and localized states in the bulk as long as the typical time between tunneling events exceeds the time between tunneling events at the point contacts. This is not the case in the Fabry-Perot setup, where the tunneling to localized states must be slow on the laboratory time-scale to have no effect on the current. Rare tunneling events into localized states in the Fabry-Perot geometry lead to strong telegraph noise [36] that serves as another signature of fractional statistics. In the absence of tunneling into localized states, telegraph noise can be induced by making a hole in the device as discussed in Supplemental Material [34].

To measure edge heat currents, one can transfer all or a fraction of the heat current to a quantum Hall (QH) edge. The transferred heat current can be extracted from the temperature of a piece of metal, connected to a QH edge [18, 19, 34]. One approach to heat transfer between a Kitaev magnet and a QH system relies on a superconductor as an intermediary [14]. Alternatively, one can transfer heat from the spin liquid to a conductor connected with a QH edge. Fig. 5 illustrates the setup for a quantum wire in the role of the conductor. A hole is created in the Kitaev liquid near the edge so that anyon tunneling is possible between the edge of the hole and the outer edge of the liquid in the constriction. The most relevant interaction of the wire and the Kitaev magnet is $W = \sigma_h \sigma_e \partial_x \phi$, where $\sigma_{h,e}$ create Ising anyons on the edge of the hole and the outer edge of the liquid; $\partial_x \phi$ is proportional to the charge density in the wire. Near a resonance, the Hamiltonian of the Kitaev liquid contains no tunneling term $\sigma_h \sigma_e$. The scaling dimension of W is 9/8 and W ensures significant energy exchange between the wire and the magnet.

In conclusion, interferometry allows probing fractional statistics with heat transport. Information about heat currents can be extracted from the temperatures of the source and drain reservoirs. The temperatures of electrically conducting reservoirs can be found from noise [18–20] or quantum dot [37–41] thermometry. The contrast-

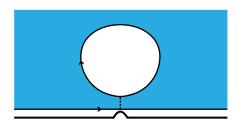


FIG. 5: A dashed line shows a constriction between the outer edge and the edge of the hole in a Kitaev magnet. The thick line at the bottom represents a conductor in contact with a magnet edge and a QH edge (not shown).

ing behavior of Mach-Zehnder and Fabry-Perot interferometers is a smoking gun evidence of fractional statistics.

Acknowledgments

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Note added: After the completion of this paper we became aware of Ref. [42] that overlaps with our work.

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phonons wipes out the universal behavior. Hence, here universal results are expected at low temperatures, where the Majorana-phonon interaction is suppressed.

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