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Weijian Chen, Maryam Abbasi, Yogesh N. Joglekar, and Kater W. Murch
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## Quantum jumps in the non-Hermitian dynamics of a superconducting qubit

Weijian Chen,<sup>1, 2, \*</sup> Maryam Abbasi,<sup>1</sup> Yogesh N. Joglekar,<sup>3</sup> and Kater W. Murch<sup>1, 2, †</sup>

<sup>1</sup>Department of Physics, Washington University, St. Louis, MO, USA

<sup>2</sup>Center for Quantum Sensors, Washington University, St. Louis, MO, USA

<sup>3</sup>Department of Physics, Indiana University-Purdue University Indianapolis, Indianapolis, IN, USA

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We study the dynamics of a driven non-Hermitian superconducting qubit which is perturbed by quantum jumps between energy levels, a purely quantum effect with no classical correspondence. The quantum jumps mix the qubit states leading to decoherence. We observe that this decoherence rate is enhanced near the exceptional point, owing to the cube-root topology of the non-Hermitian eigenenergies. Together with the effect of non-Hermitian gain/loss, quantum jumps can also lead to a breakdown of adiabatic evolution under the slow-driving limit. Our study shows the critical role of quantum jumps in generalizing the applications of classical non-Hermitian systems to open quantum systems for sensing and control.

Dissipation is ubiquitous in nature; as in radioactive decay of an atomic nucleus and wave propagation in absorptive media, dissipation results from the coupling of these systems to different environmental degrees of freedom. These dissipative systems can be phenomenologically described by effective non-Hermitian Hamiltonians, where the non-Hermitian terms are introduced to account for the dissipation. The non-Hermiticity leads to a complex energy spectrum with the imaginary part quantifying the loss of particles/energy from the system. The degeneracies of a non-Hermitian Hamiltonian are known as exceptional points (EPs), where both the eigenvalues and the associated eigenstates coalesce [1, 2]. The existence of EPs has been demonstrated in many classical systems [3–11] with applications in laser mode management [12–14], enhanced sensing [15–20], and topological mode transfer [21–24].

Though the effective Hamiltonian approach has been developed decades ago as part of quantum measurement theory, recent experiments with single electronic spins [25, 26], superconducting qubits [27], and photons [28– 30] have expanded interest in uniquely quantum effects in non-Hermitian dynamics. Two approaches have been taken to study non-Hermitian dynamics in the quantum regime. The first is to simulate these dynamics through a process known as Hamiltonian dilation—by embedding a non-Hermitian Hamiltonian into a larger Hermitian system [25, 26, 30]. A second approach is to directly isolate the non-Hermitian dynamics from a dissipative quantum system [27]. To understand this approach, recall that dissipative quantum systems are usually described by a Lindblad master equation that contains two dissipative terms: the first is a term that describes quantum jumps between the energy eigenstates of the system, and the second is a term that yields coherent non-unitary evolution [31–33]. By suppressing the former term, the resulting evolution is described by an effective non-Hermitian Hamiltonian. This can be achieved through post-selection to eliminate trajectories that contain quantum jumps (Fig. 1(a)) [27]. However, additional

sources of energy dissipation or pure dephasing can alter this non-Hermitian evolution [34, 35]. The combination of non-unitary dynamics and decoherence will lead to evolution that is starkly different than what is encountered with conventional open quantum systems. In this letter, we characterize these dynamics using experiments on a superconducting qutrit. We observe quantum dynamics that result from the competition of the nonunitary effect of complex energies and quantum jumps. This leads to decoherence enhancement near the EP, nonstationary evolution of system eigenstates, and a quantum jump-induced breakdown of adiabaticity when a system parameter is slowly varied.

Our experiment uses the lowest three energy levels  $(|q\rangle)$ .  $|e\rangle$  and  $|f\rangle$ ) of a transmon superconducting circuit [36] that consists of a pair of Josephson junctions in a SQUID geometry shunted by a capacitor. The transmon circuit is placed within a three-dimensional copper microwave cavity that serves two purposes in the experiment. First, it mediates the interaction between the circuit and a nonuniform density of states of the electromagnetic field, allowing us to tune the dissipation rates of the transmon energy levels such that  $\gamma_e$  (the decay rate of the  $|e\rangle$ ) level) is much larger than  $\gamma_f$  (the decay rate of the  $|f\rangle$ level). Second, the dispersive interaction between cavity mode and the circuit results in a state-dependent cavity resonance frequency [37]. We achieve high-fidelity, single-shot readout of the transmon state by probing the cavity with a weak microwave signal and detecting its phase shift.

The dynamics of this three-level quantum system (Fig. 1(b)) is described by a Lindblad master equation

$$\frac{\partial \rho_{\text{tot}}}{\partial t} = -i[H_{\text{c}}, \rho_{\text{tot}}] + \sum_{k=e,f} [L_k \rho_{\text{tot}} L_k^{\dagger} - \frac{1}{2} \{L_k^{\dagger} L_k, \rho_{\text{tot}}\}],$$
(1)

where  $\rho_{\text{tot}}$  denotes a 3 × 3 density operator. The jump operators  $L_e = \sqrt{\gamma_e} |g\rangle \langle e|$  and  $L_f = \sqrt{\gamma_f} |e\rangle \langle f|$  describe the energy decay from  $|e\rangle$  to  $|g\rangle$  and from  $|f\rangle$ to  $|e\rangle$ , respectively. Here we only consider a drive at



FIG. 1. (a) Formation of a non-Hermitian qubit through a dissipative three-level system. The ground level  $|g\rangle$  acts as a continuum and can be used to monitor the quantum jumps from the  $\{|e\rangle, |f\rangle\}$  submanifold. When postselection is used to eliminate this dynamics, the evolution in the  $\{|e\rangle, |f\rangle\}$  submanifold is governed by a non-Hermitian Hamiltonian. J denotes the coupling rate from an applied drive with frequency detuning  $\Delta$  relative to the  $|e\rangle - |f\rangle$  transition, and  $\gamma_e$  denotes the dissipation rate of the  $|e\rangle$  level. (b) The quantum jumps from the  $|f\rangle$  level at rate  $\gamma_f$  are only recorded by the environment, and this missing information necessitates a hybrid-Liouvillian formalism (see main text).

the  $\{|e\rangle, |f\rangle\}$  submanifold, and in the rotating frame  $H_c = J(|e\rangle\langle f| + |f\rangle\langle e|) + \Delta/2(|e\rangle\langle e| - |f\rangle\langle f|)$ , where  $\Delta$  is the frequency detuning (relative to the  $|e\rangle - |f\rangle$  transition) of the microwave drive that couples the states at rate J. The dissipative dynamics of the qutrit to its steady state can be captured by a Liouvillian superoperator defined by Eq. (1), exhibiting the so-called Liouvillian EPs [34, 38, 39]. A classical analogy of this EP transition is a damped harmonic oscillator, where an EP (corresponding to the critical damping) marks the transition from overdamped to underdamped regime [34, 38, 39].

We utilize the high fidelity single shot readout to isolate dynamics in the  $\{|e\rangle, |f\rangle\}$  submanifold by eliminating any experimental trials where the qubit undergoes a jump to the state  $|g\rangle$  [27]. The resulting dynamics in the submanifold is governed by

$$\frac{\partial \rho}{\partial t} = -i(H_{\text{eff}}\rho - \rho H_{\text{eff}}^{\dagger}) + L_f \rho L_f^{\dagger}$$
(2)

where  $\rho$  denotes a 2 × 2 density operator. The effective non-Hermitian Hamiltonian  $H_{\text{eff}} = H_c - iL_e^{\dagger}L_e/2 - iL_f^{\dagger}L_f/2$  takes into account the coherent nonunitary dissipations of both levels and possesses a second-order EP at  $J_{\text{EP}} = (\gamma_e - \gamma_f)/4$  and  $\Delta = 0$ . This EP separates "broken" and "unbroken" regions of effective parity-time  $(\mathcal{PT})$  symmetry, where the difference between eigenvalues is either purely imaginary, or purely real. As shown in Eq. (2), if there are no quantum jumps from the  $|f\rangle$ level ( $L_f = 0$ ), or these jumps can be removed from the dynamics using post-selection, the system would evolve coherently under  $H_{\text{eff}}$ .

To capture the effect of jumps from the  $|f\rangle$  level, we adopt a hybrid-Liouvillian formalism [35], which describes the non-Hermitian dynamics of an open quantum system under different post-selection efficiencies. The dissipative dynamics of the qubit is then written as,

$$\frac{\partial \rho}{\partial t} = (\mathcal{L}_0 + \mathcal{L}_1)\rho. \tag{3}$$

Here, the qubit dynamics is captured by two hybrid-Liouvillian superoperators  $\mathcal{L}_0 \rho \equiv -i(H_{\text{eff}}\rho - \rho H_{\text{eff}}^{\mathsf{T}})$  and  $\mathcal{L}_1 \rho \equiv L_f \rho L_f^{\dagger}$ . Compared to the Liouvillian superoperator defined by Eq. (1), the hybrid-Liouvillian superoperator does not lead to a completely positive and tracepreserving map [35]. In contrast to the non-Hermitian Hamiltonian approach based on a Hilbert space of dimension N = 2, this hybrid-Liouvillian formalism is based on a Liouville space of dimension  $N^2 = 4$ . In the Liouville space,  $\rho$  is represented as a  $4 \times 1$  vector, and  $\mathcal{L}_{i=0,1}$  is represented as a  $4 \times 4$  non-Hermitian matrix. Because  $\mathcal{L}_0$ encodes the evolution due to  $H_{\text{eff}}$ , it also exhibits an EP (denoted as 'hLEP') at  $J = (\gamma_e - \gamma_f)/4$  and  $\Delta = 0$ . One key difference is that three eigenvectors of  $\mathcal{L}_0$  coalesce at the EP, implying that a second-order Hamiltonian EP corresponds to a third-order hLEP [40].

In addition, the non-Hermitian qubit can also suffer from pure dephasing, described by a jump operator  $L_{\phi} = \sqrt{\gamma_{\phi}/2}\sigma_z$ . Its effect includes two aspects: on one hand, it modifies  $H_{\text{eff}}$  (and subsequently  $\mathcal{L}_0$ ) by adding a term  $-i\gamma_{\phi}I/4$  (*I* denotes an identity operator), which only shifts the overall loss and does not affect the position of EP in the parameter space; on the other hand, it provides another perturbation of quantum jumps, the effect of which can be included in  $\mathcal{L}_1$  [41].

Before proceeding to our experiments, we summarize the possible scenarios of non-Hermitian dynamics of an open quantum system. Depending on the post-selection efficiency  $\eta$  of quantum jumps through all possible channels, the resulting non-Hermitian dynamics is described by: (i) a Liouvillian superoperator with  $\eta = 0$ , i.e., no post-selection; (ii) a hybrid-Liouvillian superoperator with  $0 < \eta < 1$ , i.e., imperfect post-selection; (iii) an effective non-Hermitian Hamiltonian with  $\eta = 1$ , i.e., perfect post-selection [35]. In the semiclassical limit, the quantum jumps are neglected, that is, equivalent to  $\eta = 1$ ; subsequently, the dynamics of a dissipative classical system can be described by an effective non-Hermitian Hamiltonian [34].

We first investigate the quantum-jump-induced decoherence in the  $\mathcal{PT}$ -symmetry unbroken regime. Figure 2(a) shows the complex eigenvalues  $\lambda$  of the hybrid-Liouvillian superoperator  $(\mathcal{L}_0 + \mathcal{L}_1)$  in the unbroken regime, with the real and imaginary parts indicated as projections. Note that the role of the imaginary/real parts of Hamiltonian and hybrid-Liouvillian spectra are reversed because the '-i' term in Eq. 2 is absorbed into the hybrid-Liouvillian superoperator. The perturbative effect of quantum jumps  $(\mathcal{L}_1)$  lifts the degeneracy of the third-order hLEP of  $\mathcal{L}_0$  and generates a new second-order hLEP (see [41] for further details). By lifting the degeneracy, this perturbation leads to decoherence, whose rate



FIG. 2. (a) Complex eigenvalues of the hybrid-Liouvillian superoperator  $\mathcal{L}_0 + \mathcal{L}_1$  in the unbroken regime (solid curves). The dashed curves are the projections of the eigenvalues on the J—Re[ $\lambda$ ] and J—Im[ $\lambda$ ] planes. The arrows mark the eigenvalue difference. J is normalized by the value at the second-order hybrid-Liouvillian EP ( $J_{hLEP2}$ ). Only three of the four Liouvillian eigenvalues involved in this study are shown. The blue dashed curve on the J—Re[ $\lambda$ ] plane has been slightly offset for clarity. (b) Population dynamics versus evolution time for three different values of J, marked by (i)-(iii) in (c). The red curves are experimental results, and the black curves are fits to decaying sine function. (c) The measured oscillation frequency (blue squares, left axis) and decay rate (red circles, right axis) for different drive amplitudes J. The solid lines are calculated from the Liouvillian spectra, where the dissipation rates  $\gamma_e = 4.5 \,\mu \text{s}^{-1}$ ,  $\gamma_f = 0.3 \,\mu \text{s}^{-1}$  and  $\gamma_{\phi} = 0.5 \,\mu \text{s}^{-1}$  are used.

is determined by the real part of the eigenvalue difference. The effect of the perturbation is enhanced by proximity to the EP due to the cube-root topology of the third-order degeneracy of  $\mathcal{L}_0$  [35, 41].

To experimentally measure the decoherence rates in the vicinity of the hLEP, we initialize the circuit in the  $|f\rangle$  state and then apply a microwave drive with amplitude J. We take  $10^4$  measurements per time point and



FIG. 3. (a) Left: Illustration of the eigenstates and Liouvillian eigenvectors on the Bloch sphere. With no quantum jumps, the two eigenstates  $|\pm\rangle$  of  $H_{\rm eff}$  represent the same states as two of the Liouvillian eigenvectors ( $\rho_{0,3}$ , dashed blue and red arrows). With quantum jumps, the two eigenvectors are perturbed: one corresponds to the steady state ( $\tilde{\rho}_0$ , solid red arrow); the other one is outside of the Bloch sphere and corresponds to an unphysical state ( $\tilde{\rho}_3$ , blue solid arrow). Right: Illustration of one quantum trajectory with the qubit prepared at  $|-\rangle$ , where the qubit first jumps to the  $|e\rangle$  level and then evolves to  $|+\rangle$  due to the non-Hermitian gain/loss effect. (b, c) Time evolution of the Bloch components (b) and the entropy (c) with the qubit initially prepared at the eigenstate of  $H_{\rm eff}$  with more loss.  $J = 0.85 \,\mathrm{rad} \,\mu \mathrm{s}^{-1}$  places the system in the  $\mathcal{PT}$ -symmetry broken regime. The symbols are experimental results, with shaded bands indicating the experimental uncertainty [41], and the curves are theoretical results from Eq. 3. Parameters used are:  $\gamma_e = 6.38 \,\mu \text{s}^{-1}, \, \gamma_f = 0.24 \,\mu \text{s}^{-1},$  $\gamma_{\phi} = 0.9 \,\mu \mathrm{s}^{-1}$ . Residual oscillations in the data are likely due to technical fluctuations of the tomography calibration.

only keep the results with the transmon remaining in the  $\{|e\rangle, |f\rangle\}$  submanifold for analysis. We record the final  $|f\rangle$  population as a function of time. These dynamics are characterized by damped oscillatory behavior of the population as shown in Fig. 2(b). We extract the decoherence rate and oscillation frequency for different values of J as shown in Fig. 2(c). The observed damping rates and oscillation frequencies are in good agreement with the real and imaginary parts of hybrid-Liouvillian spectra, respectively. In particular, we note that by proximity to the hLEP, the dissipation is dramatically enhanced over its background rate (i.e., the rate when far from the

hLEP).

We now turn to the  $\mathcal{PT}$ -symmetry broken regime, where the quantum jumps compete with the relative non-Hermitian gain/loss effect. In the absence of quantum jumps, the qubit has two stationary states, corresponding to the two eigenstates  $|\pm\rangle$  of  $H_{\rm eff}$  (Fig. 3(a)). The corresponding eigenvalues are purely imaginary. Recalling that imaginary eigenvalues correspond to gain or loss, here with  $0 \ge \text{Im}[\lambda_+] > \text{Im}[\lambda_-]$ , both states exhibit loss but the  $|+\rangle$  state has gain relative to  $|-\rangle$ . Therefore, the non-Hermitian dynamics favor the  $|+\rangle$  state. The eigenmatrices  $\rho_{0,3}$  of  $\mathcal{L}_0$  with the smallest and largest damping rates represent the same states, i.e.,  $\rho_0 \propto |+\rangle \langle +|$ ,  $\rho_3 \propto |-\rangle \langle -|$ . With the perturbation of quantum jumps  $(\mathcal{L}_1)$ , the eigenmatrix  $\rho_0$  becomes slightly mixed  $\rho_0 \to \tilde{\rho}_0$ and corresponds to the effective steady state of the non-Hermitian qubit, while the eigenmatrix  $\rho_3 \rightarrow \tilde{\rho}_3$ , a state that is not physically accessible (Fig. 3(a)).

The physical intuition can be understood at the quantum trajectory level. Given a trajectory with only a single quantum jump from the  $|f\rangle$  to  $|e\rangle$  level, the jump places the qubit in a superposition of  $|+\rangle$  and  $|-\rangle$ . After that, though no further quantum jumps occur, the non-Hermiticity (of  $H_{\text{eff}}$ ) selects the eigenstate with less loss, and the renormalization of the state subsequently leads to a non-exponential decay [31–33]. Hence, the eigenstate  $|-\rangle$  of  $H_{\text{eff}}$  is unstable and will decay to a steady state in a process that involves both quantum jumps and the non-Hermitian (gain/loss) evolution. Figure 3(a) displays an illustration of one possible trajectory. Since the trajectories contain unknown number of quantum jumps, the steady state is slightly mixed rather than at the eigenstate  $|+\rangle$ .

This prediction is experimentally confirmed through quantum state tomography. Here, we prepare the qubit at the eigenstate  $|-\rangle$  of  $H_{\text{eff}}$ , and measure the expectation values of the qubit Pauli operators;  $\{x, y, z\} \equiv$  $\{\langle \sigma_x \rangle, \langle \sigma_y \rangle, \langle \sigma_z \rangle\}$ . Figure 3(b) displays these expectation values for different evolution times. We highlight several features of the evolution that are different than the dissipative evolution of a Hermitian qubit, where we expect exponential decay to steady state. The non-Hermitian evolution, perturbed by quantum jumps exhibits i) nonexponential evolution, ii) occuring on a timescale much faster than the quantum jump rate  $\gamma_f$ . This occurs due to the non-zero overlap  $\langle -|f\rangle$ ; jumps from  $|f\rangle$  to  $|e\rangle$  create a mixed state. Thereafter the relative gain of the  $|+\rangle$ state causes its population to grow, leading to the nonexponential population evolution. This is further confirmed by examining the evolution of the entropy, defined as  $S \equiv -\sum p_i \log_2(p_i)$ , where  $p_i$  is the eigenvalue of the density matrix  $\rho$  of the qubit (Fig. 3(c)). The quantum jumps increase the entropy; this distinguishes the evolution from imperfect (pure) eigenstate preparation, which would also seed non-Hermitian evolution toward  $|+\rangle$ , but



FIG. 4. (a) Illustration of the parameter path in the parameter space. (b) The real part of the Riemann surface, where the red (blue) surface represents the energy surface with relative gain (loss). The real part of the energy of the qubit  $(\text{Tr}[\rho H_{\text{eff}}])$  along the trajectory is plotted on the Riemann surface (black line) and also shown in the inset. The time evolution of the Bloch components (c) and the entropy of the corresponding density matrix (d) are displayed for the initial state  $|+x\rangle$  and the loop period  $T = 4\,\mu\text{s}$ . The solid curves are experimental results, with shaded bands indicating the experimental uncertainty [41], and the dashed curves are calculations from Eq. 3. For comparison, the evolution of the x component with no quantum jumps (due to  $\mathcal{L}_0$  only) is also shown (dashed green curve in (c)). Parameters used are:  $\gamma_e = 6.34\,\mu\text{s}^{-1}$ ,  $\gamma_f = 0.26\,\mu\text{s}^{-1}$ ,  $\gamma_{\phi} = 0.5\,\mu\text{s}^{-1}$ .

with fixed zero entropy [42].

Finally, we study the qubit dynamics under slow parameter variation to reveal the effects of quantum jumps on non-Hermitian adiabatic evolution. We choose a straight parameter path with  $J = 30 \text{ rad } \mu \text{s}^{-1}$  ( $\gg J_{\text{EP}} =$  $1.5 \text{ rad } \mu \text{s}^{-1}$ ) and  $\Delta = -30\pi \sin(2\pi t/T) \text{ rad } \mu \text{s}^{-1}$ , where  $T = 4 \mu \text{s}$  is the loop period (Fig. 4(a)). The initial state at t = 0 is chosen to be an eigenstate of  $H_{\text{eff}}$  (approximated as  $|+x\rangle$ ). Along this parameter path, the energy gap is large enough to satisfy the slow-driving condition  $T|\lambda_{+} - \lambda_{-}| \gg 1$ . For t < T/2, the initial state follows the instantaneous eigenstate  $|+\rangle$  with relative gain. At t = T/2, the parameter path crosses a branch cut for the imaginary Riemann surface at  $\Delta = 0$ . Here, the instantaneous eigenstates exhibit a loss-switch behavior; the eigenstate with relative gain becomes the eigenstate with more loss (Fig. 4(b)).

The results of quantum state tomography are shown in Fig. 4(c). At  $t = 2 \mu s$ , adiabatic evolution would return the qubit to the state  $|+x\rangle$ . The qubit returns close to this state, with slight mixing induced by the quantum jumps. For t > T/2 the qubit is now predominantly in the eigenstate with greater loss, seeding non-Hermitian evolution toward the eigenstate  $|-\rangle$ . At the end of the parameter sweep, the qubit has undergone a switch between eigenstates, induced by the small perturbation of quantum jumps. This transition is accompanied by a sharp increase in the entropy as shown in Fig. 4(d).

Similar nonadiabatic state/energy transfer has been observed when dynamically encircling an EP [21–24] as a result of nonadiabatic coupling between eigenstates and non-Hermitian gain-loss effects [43]. To verify that our parameter variation is sufficiently slow to prevent this nonadiabatic coupling, we plot the calculated dynamics in the absence of quantum jumps in Fig. 4(c), observing that there is no eigenstate switch. This reveals how quantum jumps effectively serve as a new source of nonadiabatic coupling, breaking adiabatic evolution even when parameter variation is sufficiently slow.

Quantum jumps, even when introduced at very modest rates, produce significant effects on non-Hermitian dynamics. The dissipation induced by these jumps is greatly enhanced by proximity to the EP, with dynamics driven by non-Hermitian evolution. In addition, quantum jumps introduce a new timescale relevant to adiabatic state transport in non-Hermitian systems. Our study elucidates the role and effect of dissipation on quantum non-Hermitian evolution, highlighting how controlling these dissipation mechanisms will be critical for harnessing non-Hermiticity and complex energies in quantum information processing and quantum sensing [40, 44–48].

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\* wchen34@wustl.edu

- <sup>†</sup> murch@physics.wustl.edu
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