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Milky Way Satellite Census. III. Constraints on Dark Matter Properties from Observations of Milky Way Satellite Galaxies

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We perform a comprehensive study of Milky Way (MW) satellite galaxies to constrain the fundamental properties of dark matter (DM). This analysis fully incorporates inhomogeneities in the spatial distribution and detectability of MW satellites, and marginalizes over uncertainties in the mapping between galaxies and DM halos, the properties of the MW system, and the disruption of subhalos by the MW disk. Our results are consistent with the cold, collisionless DM paradigm and yield the strongest cosmological constraints to date on particle models of warm, interacting, and fuzzy dark matter. At 95% confidence, we report limits on (i) the mass of thermal relic warm DM, $m_{\text{WDM}} > 6.5 \text{ keV}$ (free-streaming length, $\lambda_{\text{fs}} \lesssim 10 h^{-1} \text{ kpc}$), (ii) the velocity-independent DM–proton scattering cross section, $\sigma_0 < 8.8 \times 10^{-29} \text{ cm}^2$ for a 100 MeV DM particle mass (DM–proton coupling, $c_p \lesssim (0.3 \text{ GeV})^{-2}$), and (iii) the mass of fuzzy DM, $m_\phi > 2.9 \times 10^{-21} \text{ eV}$ (de Broglie wavelength, $\lambda_{\text{dB}} \lesssim 0.5 \text{ kpc}$). These constraints are complementary to other observational and laboratory constraints on DM properties.

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Introduction.—In the concordance model of cosmology, collisionless cold dark matter (CDM) makes up $\sim 25\%$ of the matter–energy density of the Universe [1]. While dark matter (DM) has the potential to solve a number of outstanding challenges in the Standard Model (SM) of particle physics [2–4], the only positive empirical evidence for DM comes from cosmological and astrophysical observations. Furthermore, by studying the astrophysical distribution of DM, it is possible to probe its particle nature [5, 6]. Specifically, the formation, abundance, and structure of gravitationally bound DM structures, known as “halos,” provide valuable information about viable ranges of the DM particle mass, production mechanism, and couplings to the SM. In particular, the abundance and properties of the smallest DM halos have the potential to indicate a departure from the CDM paradigm [5, 6].

The smallest known DM halos host the ultra-faint dwarf satellite galaxies of the Milky Way (MW) [7]. In these systems, star formation is highly suppressed by reionization and stellar feedback, leading to mass-to-light ratios that are hundreds of times larger than the universal average [7, 8]. Ultra-faint satellite galaxies are thus pristine laboratories for studying DM; in particular, the abundance of these systems is a sensitive probe of *any* DM physics that suppresses the formation or present-day abundance of small halos [9–16].

Here, we study the following theoretical paradigms for DM that affect the properties of the MW satellite population:

(i) *Warm dark matter (WDM)* is produced in the early Universe with a temperature of $\mathcal{O}(1 \text{ keV})$, although its momentum distribution can be non-thermal. Any viable WDM candidate must be cold enough to reproduce the observed large-scale structure, but its non-negligible free-streaming length suppresses the formation of the low-mass halos that host MW satellite galaxies [9, 11–14, 17]. One of the most popular WDM candidates is a sterile neutrino [18, 19].

(ii) *Interacting dark matter (IDM)* couples strongly enough to the SM to be heated by interactions with the photon–baryon fluid before recombination. This collisional damping washes out small-scale structure, even if the DM is produced non-thermally [20–22]. DM–nucleon interactions arise in generalizations of the weakly-interacting-massive-particle (WIMP) scenario [23–25], and the impact of DM–radiation interactions on low-mass halos has also been studied [15, 26, 27]. Here, we consider a velocity- and spin-independent DM–proton coupling, c_p .

(iii) *Fuzzy dark matter (FDM)* consists of an ultra-light boson with a sufficiently small mass, $\mathcal{O}(10^{-22} \text{ eV})$, such

that its de Broglie wavelength is comparable to the sizes of dwarf galaxies, $\mathcal{O}(1 \text{ kpc})$; this inhibits the formation of low-mass halos due to the uncertainty principle [28–31]. Ultra-light axions constitute one popular class of FDM [32].

In this *Letter*, we use novel measurements and modeling of the MW satellite galaxy population to constrain each DM paradigm described above. Specifically, we combine a census of MW satellites [33] from the Dark Energy Survey (DES; [34]) and Pan-STARRS1 (PS1; [35]) with a rigorous forward-modeling framework [36] to fit the position-dependent MW satellite luminosity function in each of these DM paradigms. This procedure fully incorporates inhomogeneities in the observed MW satellite population and marginalizes over uncertainties in the mapping between MW satellite galaxies and DM halos, the efficiency of subhalo disruption due to the MW disk, and the properties of the MW system.

Our analysis yields stringent constraints on each DM paradigm based on the abundance of observed MW satellites. These limits are complementary to constraints from the Lyman- α forest [37–40], strongly-lensed systems [41, 42], and MW stellar streams [43]. Our results imply that CDM is consistent with astrophysical observations down to the smallest currently accessible scales ($k \sim 40 h \text{ Mpc}^{-1}$) and strongly reinforce previous work demonstrating that there is no [discrepancy between the number of MW satellites predicted by CDM and current observations](#) [44]. Throughout this work, we fix cosmological parameters at $h = 0.7$, $\Omega_m = 0.286$, $\Omega_\Lambda = 0.714$, $\sigma_8 = 0.82$, $n_s = 0.96$ [45].

Analysis Overview.—Before discussing our treatment of each DM paradigm in detail, we describe the main components of our analysis used to connect non-CDM scenarios to the observed MW satellite population. For each paradigm, we assume that the non-CDM component constitutes the entirety of the DM. [Fig. 1 illustrates how our analysis proceeds: non-CDM physics suppresses the linear matter power spectrum on small scales \(left panel\), which manifests as an underabundance of subhalos \(middle panel\) and faint MW satellite galaxies \(right panel\) relative to CDM predictions.](#)

Transfer function. The linear matter power spectrum, normalized to that of CDM, is used to generate initial conditions for simulations of structure formation. In particular, the transfer function is defined as

$$T^2(k) \equiv \frac{P_{\text{DM}}(k)}{P_{\text{CDM}}(k)}, \quad (1)$$

where k is the cosmological wavenumber, $P_{\text{CDM}}(k)$ is the CDM linear matter power spectrum, and $P_{\text{DM}}(k)$ is the linear matter power spectrum of a non-CDM model [46]. $P_{\text{DM}}(k)$ is obtained by integrating the relevant Boltzmann equation (which may include DM–SM

interactions) given the initial DM phase-space distribution. The left panel of Fig. 1 illustrates the transfer function for the three DM paradigms we consider.

It is convenient to define the *half-mode scale*, k_{hm} , as the wavenumber satisfying $T^2(k_{\text{hm}}) = 0.25$ [47]. The corresponding *half-mode mass*,

$$M_{\text{hm}} = \frac{4\pi}{3} \Omega_m \bar{\rho} \left(\frac{\pi}{k_{\text{hm}}} \right)^3, \quad (2)$$

is a characteristic mass scale below which the abundance of DM halos is significantly suppressed relative to CDM. Here, $\bar{\rho}$ is the critical density of the Universe today.

Subhalo mass function (SHMF). The abundance of subhalos within the virial radius of the MW is expressed as the cumulative number of subhalos as a function of subhalo mass, M . We follow [22] by using peak virial mass, defined according to the Bryan-Norman overdensity [48] with $\Delta_{\text{vir}} \simeq 99.2$ (consistent with our cosmological parameters). We define

$$\left(\frac{dN_{\text{sub}}}{dM} \right)_{\text{DM}} \equiv f_{\text{DM}}(M, \boldsymbol{\theta}_{\text{DM}}) \left(\frac{dN_{\text{sub}}}{dM} \right)_{\text{CDM}}, \quad (3)$$

where $f_{\text{DM}}(M, \boldsymbol{\theta}_{\text{DM}})$ is the suppression of the SHMF relative to CDM and $\boldsymbol{\theta}_{\text{DM}}$ are DM model parameters; both f_{DM} and $\boldsymbol{\theta}_{\text{DM}}$ depend on the DM model in question. The middle panel of Fig. 1 shows SHMF suppression for the three DM paradigms we consider.

MW satellite model. [Here, we describe the additions to our MW satellite model pertaining to the non-CDM paradigms described above. We comprehensively discuss the underlying galaxy–halo connection model in the Supplemental Material.](#) We combine the SHMF suppression in Eq. (3) with a state-of-the-art satellite modeling framework [36] to predict the abundance of observed MW satellites in each DM paradigm. Our modeling framework combines cosmological zoom-in simulations [of two halos from \[49\]—which are chosen to have masses, concentrations, and assembly histories similar to those inferred for the MW halo](#) and include realistic analogs of the Large Magellanic Cloud system—with a statistical model of the galaxy–halo connection in order to populate subhalos with satellite galaxies.

We implement SHMF suppression by multiplying the detection probability of each mock satellite, which includes terms that model tidal disruption due to the MW disk, the efficiency of galaxy formation, and observational detectability, by a factor of $f_{\text{DM}}(M, \boldsymbol{\theta}_{\text{DM}})$, following [22, 50]. This procedure assumes that the shape of the observed radial satellite distribution (which our model predicts reasonably well; [36]) is unchanged in alternative DM scenarios, which is consistent with results from cosmological WDM simulations of MW-mass halos [51, 52]. The validity of this assumption is less certain for FDM because dynamical friction operates differently

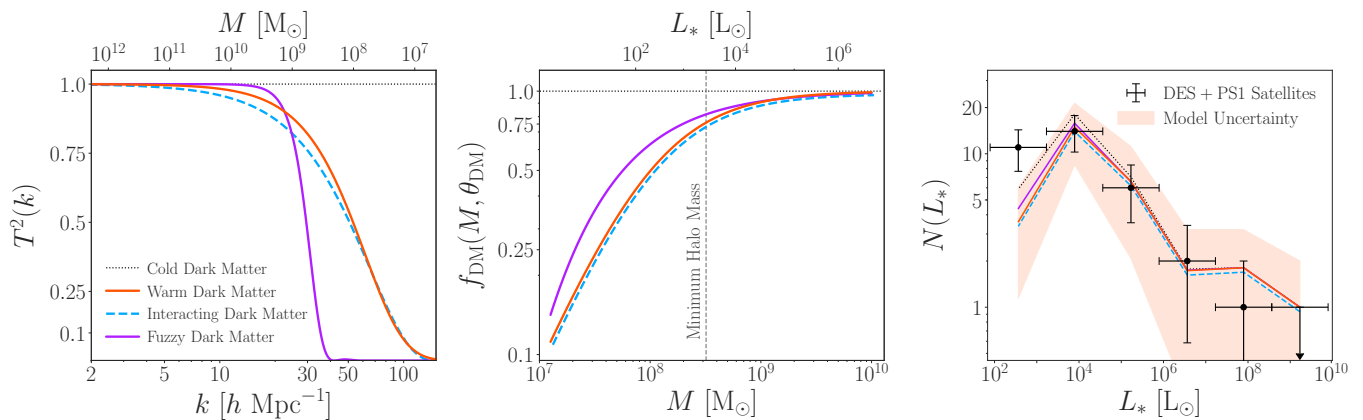


FIG. 1. *Left panel:* Transfer functions for the WDM (orange), IDM (blue), and FDM (magenta) models that are ruled out by our analysis at 95% confidence, corresponding to, $m_{\text{WDM}} = 6.5 \text{ keV}$, $\sigma_0 = 8.8 \times 10^{-29} \text{ cm}^2$ (for DM particle mass $m_\chi = 100 \text{ MeV}$), and $m_\phi = 2.9 \times 10^{-21} \text{ eV}$, respectively. These constraints are marginalized over our MW satellite model and the properties of the MW system. *Middle panel:* SHMF suppression relative to CDM for each ruled-out non-CDM model. The vertical dashed line indicates the 95% confidence upper limit on the lowest-mass halo inferred to host MW satellite galaxies [36]. Note that the IDM SHMF is assumed to be identical to the WDM SHMF in our analysis, and is offset slightly for visual clarity. *Right panel:* Predicted MW satellite galaxy luminosity functions for each ruled-out non-CDM model compared to DES and PS1 observations, evaluated at the best-fit MW satellite model parameters from [36]. The shaded band illustrates the uncertainty of our WDM prediction due to the stochasticity of our galaxy–halo connection model and the limited number of simulations used in our analysis; the size of this uncertainty is very similar to that in CDM and the other alternative DM models shown. This panel is a simple one-dimensional representation of our MW satellite and DM model fit to the luminosity, size, and spatial distribution of satellites in the DES and PS1 survey footprints. The comparison of our CDM model to data is described in [36], and full posterior distributions for our non-CDM analyses are provided in the Supplemental Material.

for wave-like versus particle DM [53], although this results in negligible differences in disruption timescales for the $\sim 10^8 M_\odot$ subhalos that drive our constraints [30]. The right panel of Fig. 1 shows the predicted satellite luminosity function for each non-CDM model under consideration evaluated with model parameters that are ruled out at 95% confidence.

Fitting procedure. We fit predicted satellite populations to the observed satellite population from DES and PS1 using the observational selection functions derived in [33], assuming that satellite surface brightness is distributed according to a Poisson point process in each survey footprint [36, 54]. We use the Markov Chain Monte Carlo (MCMC) code `emcee` [55] to simultaneously fit for seven parameters governing the galaxy–halo connection, one parameter governing the impact of the MW disk on subhalo disruption, and one parameter governing the impact of the DM model in question, which we express as a subhalo mass scale. In particular, our thermal relic WDM constraint is derived by fitting for M_{hm} , and our FDM limit is derived by fitting for a characteristic mass scale M_0 . Further details on our fitting procedure are provided in the Supplemental Material.

Subhalo abundance is known to scale linearly with host halo mass [49], and we assume that satellite luminosity is a monotonic function of subhalo mass, modulo scatter [36]. We therefore expect a higher-mass MW host halo to yield weaker constraints on non-CDM models, because

observed satellites would inhabit correspondingly higher-mass subhalos. The average virial mass of the host halos in our two realistic MW-like simulations is $1.4 \times 10^{12} M_\odot$, which is consistent with the 95% confidence range for the virial mass of the MW halo inferred from *Gaia* measurements of satellite kinematics [56, 57]. To be conservative, we account for the uncertainty in MW halo mass on our DM constraints by assuming that the mass scale describing the suppression of the SHMF in each DM paradigm is linearly related to the virial mass of the MW halo, following the scaling for minimum halo mass derived in [36]. In particular, we multiply the upper limit on the characteristic mass scale in each of our non-CDM fits by the ratio of the largest allowed MW halo mass to the average host halo mass in our simulations. We validate this procedure by fitting the observed satellite population using each of our two MW-like simulations separately, which yields reasonable agreement with the linear scaling expectation. This conservative scaling mitigates the largest uncertainty associated with the limited statistics of our two realistic simulations.

In summary, our fit to the MW satellite population incorporates both intrinsic inhomogeneities in the spatial distribution of MW satellites and those introduced by the varying coverage and depth of current surveys. We assume that alternative DM physics only modifies the SHMF, via Eq. (3), and we report 95% confidence limits on DM model parameters that are marginalized over un-

certainties in our MW satellite model and the properties of the MW system.

WDM Analysis. Thermal relic WDM with particle mass, m_{WDM} , has been studied extensively in the literature (e.g., [17, 58]) and serves as a benchmark model for our analysis.

Transfer function. The transfer function for thermal relic WDM is given as a function of m_{WDM} by [58]. This transfer function is commonly assumed in cosmological studies of WDM and facilitates a well-defined comparison to other small-scale structure results [37, 38, 41–43]. However, the simple thermal relic transfer function is inadequate to describe specific particle models of WDM, such as resonantly-produced sterile neutrinos [59]. Thus, constraints on specific DM candidates must be inferred using transfer functions appropriate for the particle model in question, as we discuss below.

SHMF. Several authors have implemented the thermal relic WDM transfer function from [58] in cosmological zoom-in simulations to estimate the suppression of the SHMF in MW-mass host halos [17, 47, 52, 60]. These results depend on the algorithm used to remove spurious halos [60, 61], and therefore vary among studies. Following [62], SHMF suppression for thermal relic WDM can be expressed as

$$f_{\text{WDM}}(M, m_{\text{WDM}}) = \left[1 + \left(\frac{\alpha M_{\text{hm}}(m_{\text{WDM}})}{M} \right)^\beta \right]^\gamma, \quad (4)$$

where α , β , and γ are constants, and M_{hm} is related to m_{WDM} in our fiducial cosmology via

$$M_{\text{hm}}(m_{\text{WDM}}) = 5 \times 10^8 \left(\frac{m_{\text{WDM}}}{3 \text{ keV}} \right)^{-10/3} M_\odot. \quad (5)$$

To facilitate comparison with recent WDM constraints from analyses of the MW satellite population [22], strong gravitational lenses [41, 42], and stellar streams [43], we adopt the SHMF from [17], which corresponds to Eq. (4) with $\alpha = 2.7$, $\beta = 1.0$, and $\gamma = -0.99$. We note that the recent estimate of the SHMF from [62]—which specifically models resonantly-produced sterile neutrino WDM—is significantly *less* suppressed than the thermal relic SHMF from [17]. Thus, our fiducial WDM constraint only applies directly to thermal relic DM.

Fitting procedure. We implement Eq. (4) in our fit to the MW satellite population to obtain a marginalized posterior distribution over M_{hm} . In particular, we fit for $\log_{10}(M_{\text{hm}})$ using a uniform prior on this logarithmic quantity, and we translate the resulting limit to m_{WDM} using Eq. (5). We translate our thermal relic WDM limit into constraints on resonantly-produced sterile neutrinos by following [63, 64]. Specifically, we analyze sterile neutrino transfer functions over a grid of mass and mixing angle values [65], and we constrain sterile neutrino models that produce transfer functions which are strictly

more suppressed than our 95% confidence ruled-out thermal relic WDM model. This procedure is described in detail in the Supplemental Material.

IDM Analysis. Our treatment of IDM follows the prescription of [22]. For concreteness, we focus on the case of velocity-independent DM–proton scattering.

Transfer function. Following [22], the transfer function in our fiducial IDM model is obtained using the modified version of the Boltzmann solver CLASS described in [23–25], which we use to evolve linear cosmological perturbations in the presence of velocity-independent DM–proton interactions. These interactions are described by the velocity-independent scattering cross section, σ_0 , and the DM particle mass, m_χ . As noted in [22], transfer functions for this model are very similar to those of thermal relic WDM, modulo dark acoustic oscillations that occur at very small scales and are significantly suppressed for our parameter space of interest.

SHMF. Because cosmological zoom-in simulations including DM–proton scattering have not been performed, we follow [22] by mapping the SHMF suppression of IDM to that of WDM based on the correspondence of the transfer functions. In particular, we match the half-mode scales in the transfer functions to construct a relation between m_{WDM} and (σ_0, m_χ) , and we assume that the IDM SHMF is identical to the corresponding thermal relic WDM SHMF from [17]. This procedure neglects late-time DM–proton scattering, [which has a negligible impact on subhalo abundances in our IDM model, even in regions with high baryon densities.](#)

Fitting procedure. Following [22], we use the mapping procedure described above to translate our 95% confidence limit on thermal relic WDM into limits on σ_0 for several values of m_χ in our fiducial IDM model.

FDM Analysis. Finally, we provide details on each step for the FDM paradigm. We focus on the case of ultra-light scalar field DM with negligible self-interactions and SM couplings.

Transfer function. The FDM transfer function is given as a function of the FDM mass, m_ϕ , by [28]. We note that this transfer function features steeper power suppression than thermal relic WDM for a fixed half-mode scale.

SHMF. We assume that the FDM SHMF suppression takes the form of Eq. (3), and we fit the results of the semi-analytic model in [30, 31] with a function of the form

$$f_{\text{FDM}}(M, m_\phi) = \left[1 + \left(\frac{M_0(m_\phi)}{M} \right)^{\tilde{\beta}(m_\phi)} \right]^{\tilde{\gamma}(m_\phi)}, \quad (6)$$

where $\tilde{\beta}(m_\phi)$ and $\tilde{\gamma}(m_\phi)$ are provided in the Supplemental Material. The characteristic subhalo mass scale M_0 is related to the FDM mass via [66]

$$M_0(m_\phi) = 1.6 \times 10^{10} \left(\frac{m_\phi}{10^{-22} \text{ eV}} \right)^{-4/3} M_\odot. \quad (7)$$

Dark Matter Paradigm	Parameter	Constraint	Derived Property	Constraint
Warm Dark Matter	Thermal Relic Mass	$m_{\text{WDM}} > 6.5 \text{ keV}$	Free-streaming Length	$\lambda_{\text{fs}} \lesssim 10 h^{-1} \text{ kpc}$
Interacting Dark Matter	Velocity-independent DM–Proton Cross Section	$\sigma_0 < 8.8 \times 10^{-29} \text{ cm}^2$	DM–Proton Coupling	$c_p \lesssim (0.3 \text{ GeV})^{-2}$
Fuzzy Dark Matter	Particle Mass	$m_\phi > 2.9 \times 10^{-21} \text{ eV}$	de Broglie Wavelength	$\lambda_{\text{dB}} \lesssim 0.5 \text{ kpc}$

TABLE I. Constraints on the WDM, IDM, and FDM paradigms from observations of MW satellite galaxies. Limits for each non-CDM model are derived by assuming that it constitutes the entirety of the DM. The first column lists the DM paradigm, the second column describes the particle physics parameters constrained by this analysis, the third column lists the corresponding constraints at 95% confidence, the fourth column describes the derived property constrained for each DM model, and the fifth column lists constraints on the derived parameters. Limits on the DM–proton scattering cross sections depend on the DM particle mass, m_χ (see Fig. 2); for simplicity, we present our constraint for $m_\chi = 100 \text{ MeV}$.

The SHMF suppression in Eq. (6) encapsulates the effects of tidal stripping on subhalos with solitonic cores, which was explicitly included by [30, 31]. This SHMF suppression is significantly less severe than that estimated from the FDM simulations in [66]. As described in the Supplemental Material, using the SHMF from [66] in our fit yields a limit on the FDM mass that is roughly three times more stringent than our fiducial result. This confirms that the FDM SHMF is a key theoretical uncertainty that must be addressed [29].

Fitting procedure. We implement the SHMF in Eq. (6) in our fit to the MW satellite population to obtain a marginalized posterior distribution over M_0 . In particular, we fit for $\log_{10}(M_0)$ using a uniform prior on this logarithmic quantity, and we translate the resulting limit to m_ϕ using Eq. (7). We note that our procedure for constraining FDM uses the detailed *shape* of the SHMF suppression in this model, rather than mapping the half-mode scale of the FDM transfer function to that of thermal relic WDM as in [22] or bounding the FDM SHMF by ruled-out thermal relic WDM SHMFs as in [67]. This is necessary because both the shape of the FDM transfer function and the resulting suppression of the SHMF differ in detail from thermal relic WDM (see Fig. 1).

Results.—Table I presents our constraints on the WDM, IDM, and FDM paradigms. We describe these results below and translate the limits into constraints on specific models corresponding to each DM paradigm.

(i) *WDM.* Our fit using the thermal relic WDM SHMF suppression from [17] yields $M_{\text{hm}} < 3.0 \times 10^7 M_\odot$, or $m_{\text{WDM}} > 7.0 \text{ keV}$, at 95% confidence. Linear scaling with MW halo mass yields our fiducial constraint of $M_{\text{hm}} < 3.8 \times 10^7 M_\odot$, corresponding to $m_{\text{WDM}} > 6.5 \text{ keV}$. This translates to an upper limit on the free-streaming length of $\lambda_{\text{fs}} \lesssim 10 h^{-1} \text{ kpc}$, corresponding to the virial radii of the smallest halos that host MW satellite galaxies, and improves on previous m_{WDM} constraints from the MW satellite population by a factor of ~ 2 [22].

Our constraint on thermal relic WDM translates to

a lower limit of 50 keV on the mass of a non-resonant Dodelson–Widrow sterile neutrino [58, 77]. We also translate our thermal relic WDM limit into constraints on the mass and mixing angle of resonantly-produced sterile neutrinos assuming a Shi–Fuller production mechanism [78], following the conservative procedure described above. As shown by the red exclusion region in the left panel of Fig. 2, our analysis rules out nearly the entire remaining parameter space for resonantly produced sterile neutrinos in the Neutrino Minimal Standard Model [73] at greater than 95% confidence.¹ In addition, we robustly rule out the resonantly produced sterile neutrino interpretation of the 3.5 keV X-ray line [68].

(ii) *IDM.* Mapping our $m_{\text{WDM}} > 6.5 \text{ keV}$ constraint to the DM–proton scattering model following the procedure in [22] yields constraints on the velocity-independent interaction cross section of $(7.0 \times 10^{-30}, 2.6 \times 10^{-29}, 8.8 \times 10^{-29}, 1.7 \times 10^{-27}) \text{ cm}^2$ for DM particle masses of $(10^{-5}, 10^{-3}, 10^{-1}, 10) \text{ GeV}$ at 95% confidence. As shown by the red exclusion region in the right panel of Fig. 2, these constraints are highly complementary to direct detection limits, particularly at low DM masses [22].

We note that these constraints scale as $m_\chi^{1/4}$ (m_χ) for $m_\chi \ll 1 \text{ GeV}$ ($m_\chi \gg 1 \text{ GeV}$). At a DM mass of 100 MeV, our limit translates into an upper bound on the DM–proton coupling of $c_p \lesssim (0.3 \text{ GeV})^{-2}$ [23].

Despite our conservative marginalization over MW halo mass, these results improve upon those in [22] by a factor of ~ 3 at all DM masses. This is stronger than the improvement expected from the analytic prediction for cross section constraints derived in [22] due to a more precise determination of the SHMF, resulting from the sky coverage and sensitivity of DES and PS1.

Several complementary astrophysical and cosmological measurements probe the DM–proton scattering cross sec-

¹ A small region of parameter space is not excluded at the lowest viable mixing angles and $m_s \gtrsim 30 \text{ keV}$.

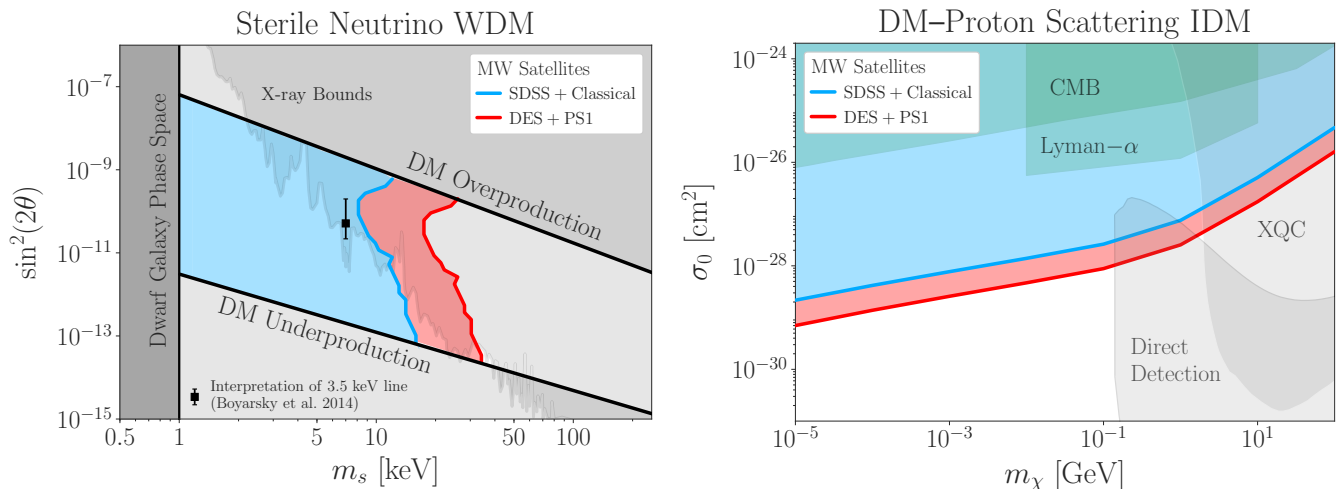


FIG. 2. **Exclusion regions for WDM and IDM models** from our analysis of MW satellites observed with DES and PS1 (red) compared to previous constraints from classical and SDSS satellites [22] (blue) and other experimental results. *Left panel:* Constraints on the mass and mixing angle of resonantly-produced sterile neutrino DM. These constraints are derived by finding mass and mixing angle combinations that suppress the linear matter power spectrum more strongly than the $m_{\text{WDM}} = 6.5 \text{ keV}$ thermal relic ruled out at 95% confidence by our analysis. The black point with error bars shows the sterile neutrino interpretation of the 3.5 keV X-ray line [68]. The dark gray region is ruled out by dwarf galaxy internal dynamics [69], and the gray contour shows X-ray constraints [70–72]. Solid black lines indicate regions of parameter space in which resonantly-produced sterile neutrinos cannot constitute all of the DM in the Neutrino Minimal Standard Model [63, 73]. *Right panel:* Constraints on the interaction cross section and DM mass for velocity-independent DM–proton scattering. Green contours show cosmological limits from the CMB [23, 25] and the Lyman- α forest [74]. Light gray contours show experimental limits from the X-ray Quantum Calorimeter [75] and direct detection results as interpreted by [76].

tion. Stringent limits have been derived by reinterpreting direct detection constraints in the context of cosmic ray upscattering [79]. We do not show these results in Fig. 2 because they constrain the DM–proton scattering at relativistic energies, which precludes a straightforward mapping to the velocity-independent cross section constrained here. The IDM model we consider contributes to the energy density of relativistic species at Big Bang Nucleosynthesis, which sets a lower on its mass that depends on the spin statistics of the DM particle [80–82]. Understanding the interplay of these results with our limits is an important area for future work.

(iii) *FDM.* We obtain $M_0 < 1.4 \times 10^8 M_\odot$ at 95% confidence from our fiducial FDM fit. Applying linear MW-host mass scaling yields $M_0 < 1.8 \times 10^8 M_\odot$ at 95% confidence, or $m_\phi > 2.9 \times 10^{-21} \text{ eV}$. This translates to an upper limit on the de Broglie wavelength of $\lambda_{\text{dB}} \lesssim 0.5 h^{-1} \text{ kpc}$, roughly corresponding to the sizes of the smallest MW satellite galaxies. Thus, the 10^{-22} eV FDM model invoked to reconcile the apparent mismatch between the predicted and observed inner dark matter density profiles of dwarf galaxies [29], and to fit the internal dynamics of low-surface-brightness [83, 84] and ultra-diffuse [85] galaxies, is strongly disfavored by MW satellite abundances.

To connect to particle models of FDM, we plot this limit in the well-motivated parameter space of ultra-light

axion mass versus axion–photon coupling in Fig. 3. For the range of axion–photon couplings that we consider, this mixing has a negligible effect on structure formation. We reiterate that our constraint was derived assuming a light scalar field without self-interactions; this assumption may be violated in specific ultra-light axion models. Although our analysis and Lyman- α forest studies exclude a similar region of parameter space [39, 40], our work probes structure on complementary physical scales with distinct theoretical and observational systematics.

Discussion.—In this *Letter*, we used a state-of-the-art model of the MW satellite galaxy population to place stringent and robust limits on three fundamental DM paradigms: WDM, IDM, and FDM. Although some of these alternative DM models gained popularity by solving apparent small-scale structure “challenges” facing CDM, recent observational and theoretical advances have reversed this scenario. In particular, astrophysical and cosmological observations of the smallest DM structures are now among the strongest constraints on the micro-physical properties of DM.

This analysis improves upon previous work by using MW satellite observations over nearly the entire sky and rigorously accounting for both satellite detectability and uncertainties in the galaxy–halo connection. Our constraints are comparable in sensitivity to Lyman- α forest, strong lensing, and stellar stream perturbation analyses.

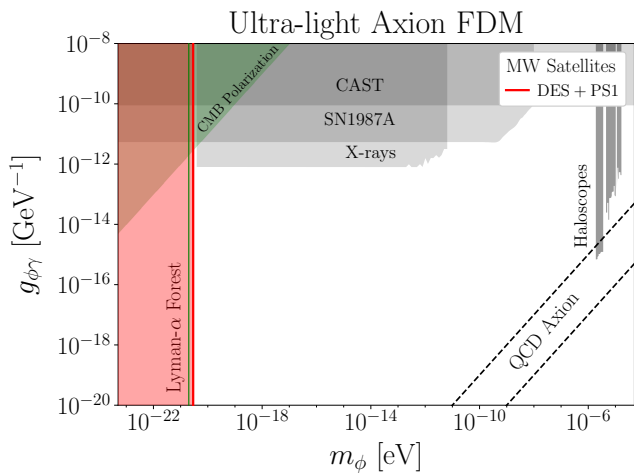


FIG. 3. Constraints on ultra-light axion particle mass versus axion–photon coupling from our analysis of the MW satellite population (red). Limits from CMB polarization washout [86] and the Lyman- α forest [39] are shown in green, and halo-scope limits are shown as gray vertical bands. Experimental constraints from the the CAST experiment [87], the lack of a γ -ray signal from SN1987A [88], and the X-ray transparency of the intracluster medium [89] are shown in gray and do not require that the ultra-light axion makes up all of the DM. The dashed lines indicate canonical QCD axion models [90, 91].

Future cosmic surveys promise to further improve these measurements and to enable a detailed comparisons to the internal dynamics of these galaxies [92, 93].

As the observational data improve, there are several uncertainties in the current modeling framework that are important to address. In particular, our use of only two realistic MW simulations limits the range of host halos and subhalo populations that enter our analysis; sampling a wider range of host halo masses, formation histories, and environments will improve the accuracy and precision of DM constraints derived from MW satellite galaxies. We describe other model uncertainties in the Supplemental Material.

The breadth of DM models constrained by observations of MW satellites is particularly important given the growing interest in a wide range of theoretical possibilities following non-detections in collider, direct, and indirect searches for canonical WIMPs. In addition to the three DM paradigms considered in this work, small-scale structure measurements are also sensitive to the initial DM velocity distribution in non-thermal production scenarios [94], the DM formation epoch [95, 96], the DM self-interaction cross section [97–100], and the DM particle lifetime [10, 101].

Future work could generalize our approach by measuring deviations in the small-scale linear matter power spectrum relative to a baseline CDM scenario, rather than setting constraints in the context of particular DM

models. Features in the power spectrum on extremely small scales are a hallmark of many inflationary models [102, 103], and it is conceivable that DM substructure measurements can be used to infer the nature of the corresponding primordial density fluctuations.

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² https://github.com/eonadler/subhalo_satellite_connection

Nottingham, Ohio State University, University of Pennsylvania, University of Portsmouth, SLAC, Stanford University, University of Sussex, Texas A&M University, and the OzDES Membership Consortium.

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