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Twist Angle Dependent Interlayer Exciton Lifetimes in van der Waals Heterostructures

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In van der Waals (vdW) heterostructures formed by stacking two monolayers of transition metal dichalcogenides, multiple exciton resonances with highly tunable properties are formed and subject to both vertical and lateral confinement. We investigate how a unique control knob, the twist angle between the two monolayers, can be used to control the exciton dynamics. We observe that the interlayer exciton lifetimes in MoSe₂/WSe₂ twisted bilayers (TBLs) change by one order of magnitude when the twist angle is varied from 1° to 3.5°. Using a low-energy continuum model, we theoretically separate two leading mechanisms that influence interlayer exciton radiative lifetimes. The shift to indirect transitions in the momentum space with an increasing twist angle and the energy modulation from the moiré potential both have a significant impact on interlayer exciton lifetimes. We further predict distinct temperature dependence of interlayer exciton lifetimes in TBLs with different twist angles, which is partially validated by experiments. While many recent studies have highlighted how the twist angle in a vdW TBL can be used to engineer the ground states and quantum phases due to many-body interaction, our studies explore its role in controlling the dynamics of optically excited states, thus, expanding the conceptual applications of “twistronics”.

Van der Waals (vdW) heterostructures offer a unique material platform with rich electronic and optical properties highly tunable via a wide selection of layer composition, strain, electric gating, and doping [1]. Because the lattice matching restriction is lifted at the interface, the twist angle between two monolayers (MLs) has emerged as a unique control knob to engineer the moiré superlattice formed by periodic variations of atomic alignment between the two layers [2, 3]. Following exciting discoveries in graphene twisted bilayers (TBLs) [4–6], transition metal dichalcogenide (TMD) TBLs have also been found to exhibit rich correlated electronic phases [7–10]. In a different context, the lateral confinement introduced by the moiré potential may be used to realize a regular array of quantum emitters, a long-standing goal in the field of solid-state quantum information technology [11, 12].

A type-II band alignment is typically found in a TMD TBL (Fig. 1a), leading to the formation of both intralayer and interlayer excitons [13–17]. We focus on interlayer excitons (IXs) because they are most likely to experience a deep moiré potential confinement. Because of the similar lattice constants of MoSe₂ and WSe₂ MLs, the size of the moiré supercell is determined by the twist angle (Fig. 1b). The twist angle in real space translates into a rotation in the momentum space, causing the relative rotation of Brillouin zones associated with each monolayer (Fig. 1c). Consequently, valleys in each layer are shifted from each other, changing a direct optical transition near the K-valley to an indirect transition, introducing longer IX lifetimes [14, 18]. We illustrate the exciton center of mass wavefunction in its own reference frame (i.e., the Γ point) in

the excitation picture of Fig. 1d. In TBLs with small twist angles ($\Theta < 5^\circ$), the thermally broadened IX distribution is sufficient to satisfy the momentum conservation requirement of an indirect transition, allowing the radiative decay process. A wide range of IX lifetimes in TMD TBLs have been reported in time-resolved photoluminescence (TRPL) measurements previously [14, 15, 19–24]. However, no prior studies have explained the origin of such variations.

We perform TRPL measurements on a series of MoSe₂/WSe₂ TBLs with accurately controlled twist angles. And we observe that the IX lifetime changes by one order of magnitude when the twist angle is changed from 1° to 3.5°. Theoretically, we examine two mechanisms that influence the IX radiative lifetimes. We find that both the shift to indirect optical transition with an increasing twist angle and the moiré potential have a significant effect on the lifetime. Our theory further predicts that IX lifetimes exhibit different temperature dependence in TBLs with different twist angles. This prediction is partially validated by the experimental observations.

The hBN encapsulated TBLs are prepared using a standard exfoliation and stacking procedure described in the supplementary materials (SM) [25]. The twist angle is estimated from high-resolution optical microscopy images, and the stacking type of the TBLs is determined by second-harmonic generation (SHG) (see SM for details) [26–29]. All optical experiments are performed using an averaged excitation power of 1 μ W and a focused laser spot size of $\sim 1 \mu$ m in diameter. Our far-field experiment probes hundreds of moiré supercells simultaneously.

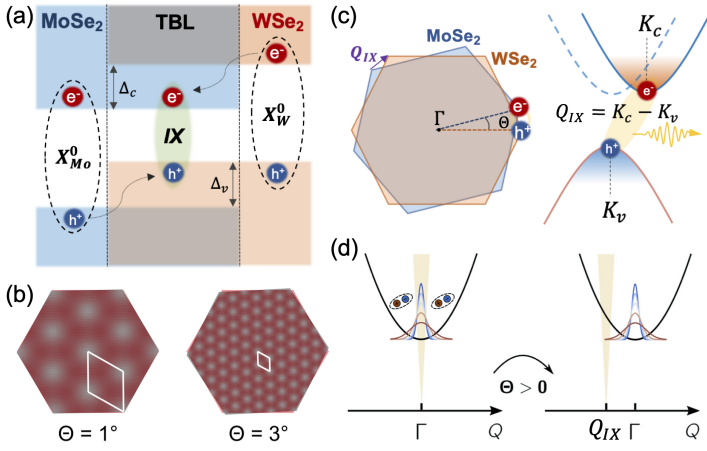


FIG. 1. Conceptual description of IXs in a TBL. (a) Schematic of type-II band alignment with band offsets (Δ_c and Δ_v) and inter-layer charge transfer lead to the formation of IXs. (b) Real-space representation of the moiré superlattice for twist angles of 1° and 3° with a moiré supercell marked in white. (c) Schematic of the Brillouin zone of MoSe₂ ML (blue) and WSe₂ ML (orange) twisted in the momentum space (left panel). $Q_{IX} = K_c - K_v$ denotes a finite momentum mismatch between the two layers and corresponds to the center of mass momentum of IXs. This twist leads to an indirect transition (right panel). (d) Thermal distribution of IXs with a near-zero (left) and a finite (right) twist angle plotted in the exciton's reference frame. Blue (red) curve illustrates the thermal distribution of IXs at a low (high) temperature. Yellow shaded region illustrates the light cone.

The data represent statistical averages of an ensemble of excitons. We present the low-temperature PL spectrum from the TBL with $\Theta = 1.0 \pm 0.3^\circ$ twist angle in Fig. 2a, in which both IXs and intra-layer exciton resonances with large binding energy of a few hundred meV are observed [14–16, 30–33]. We fit multiple IX resonances in the PL spectrum by Gaussian functions as shown in Fig. 2b. We present the PL spectra for the other two samples with different twist angles, and the analysis of the multiple IX resonances with consistent dielectric environments in the SM [34, 35]. Different possible interpretations for these resonances have been proposed, including phonon-mediated states, defect-bound states, and spin triplet states [36–39]. While we cannot rule out these alternative explanations definitively, we find that the interpretation of quantized exciton resonances confined within the moiré potential captures the essential features of our data as we further explain below [12, 15, 40].

The recombination dynamics of IXs in three TBLs are spectrally and temporally resolved at low temperatures as shown in Fig. 3a-c. The TRPL signals are fitted with a biexponential decay function. Such a biexponential decay indicates that a simple two-level model is not sufficient to explain the dynamics of IXs. This biexponential decay may originate from scattering between a bright and dark exciton [41–43]. Using a rate equation analysis for a three-level system (see SM for details, which includes Refs. [44–47]), we attribute the fast (slow) decay component to the lifetime of the bright (dark) exciton assuming the scattering rate between the bright and dark state is slower than the bright exciton lifetime. In all samples, we observe shorter IX lifetimes as the energy of the resonance increases as shown in the inset to each panel in Fig. 3a-c. This systematic change with energy is consistent with the interpretation that

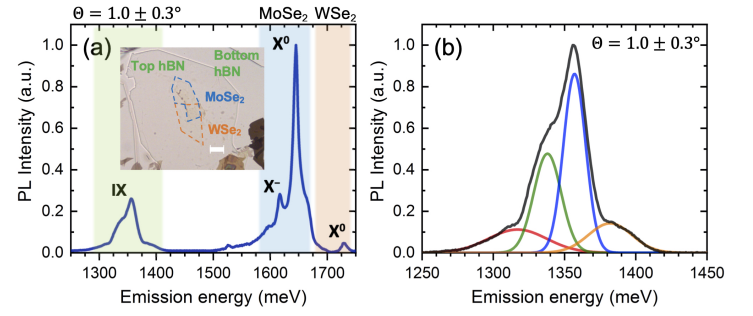


FIG. 2. (a) Low-temperature PL spectrum from a MoSe₂/WSe₂ TBL with $\Theta = 1.0 \pm 0.3^\circ$ twist angle, featuring both intralayer excitons (neutral exciton: X^0 , trion: X^-) and IXs. Inset shows the optical image of the hBN-encapsulated TBL. MoSe₂ and WSe₂ ML regions are indicated inside the blue and orange dashed lines, respectively. Scale bar: $20 \mu\text{m}$ (b) Gaussian fitting to multiple IXs. Black solid line is measured data.

the higher energy excitons are excited states in the moiré potential with additional relaxation channels [15]. The reduced exciton lifetimes associated with the excited states are often found in spatially localized excitons in other materials [48].

Most remarkably, the IX lifetime changes drastically as a function of the twist angle, as shown in Fig. 3d. Both the fast and slow components of the IX lifetime increase nearly by one order of magnitude when the twist angle increases from $\Theta = 1^\circ$ to 3.5° . For example, the fast (slow) decay time measured over the range of 1345 - 1355 meV increases from 1.3 (6.6) to 16.2 (217.5) ns. We focus on understanding this twist angle dependence of IX lifetimes in TBLs.

To understand this drastic twist angle dependence, we calculate the radiative recombination rate of IXs in the TBLs (see the SM for details, which includes Refs. [23, 49–56]). We note that the lifetime measured is in fact the total lifetime, determined by both radiative and non-radiative processes. It is impractical to calculate all non-radiative processes, which may depend on many extrinsic properties. Thus, our calculations can only be compared to ideal emitters with unity quantum yield. Nevertheless, these calculations provide important understanding of IX dynamics controlled by the twist angle in a TBL and guide the search for more efficient emitters in a moiré crystal. Our calculations start with Fermi's golden rule [57]

$$\tau_{IX}^{-1} = \frac{2\pi}{\hbar} \sum_{if} |\langle f | H_{\text{rad}} | i \rangle|^2 \delta(\varepsilon_i - \varepsilon_f) N_i \quad (1)$$

where the optical matrix element describes transitions between the initial IX state $|i\rangle$ and the final photon state $|f\rangle = b_{\mathbf{q},\sigma}^\dagger |0\rangle$. Here, $b_{\mathbf{q},\sigma}^\dagger$ creates a photon with wave vector \mathbf{q} and polarization σ with respect to the vacuum state $|0\rangle$, and N_i is the occupation of the initial IX states. To describe the moiré exciton states we use a low energy continuum model that we derive along the lines of Ref. [11, 12, 18, 58]. As the basis of describing the hybridized IXs later, we have first written the wave function of IXs in the absence of interlayer coupling as:

$$|Q\rangle = \frac{1}{\sqrt{\mathcal{A}}} \sum_{\mathbf{k}} \phi_X(\mathbf{k}) a_{\mathbf{K}_c + \mathbf{k} + \frac{m_c}{M} \mathbf{Q}}^{\dagger,c} a_{\mathbf{K}_v + \mathbf{k} - \frac{m_v}{M} \mathbf{Q}}^v |0\rangle \quad (2)$$

with eigenenergies $E(Q) = \hbar^2 |Q|^2 / (2M) + E_{\text{gap}} - E_B$ that

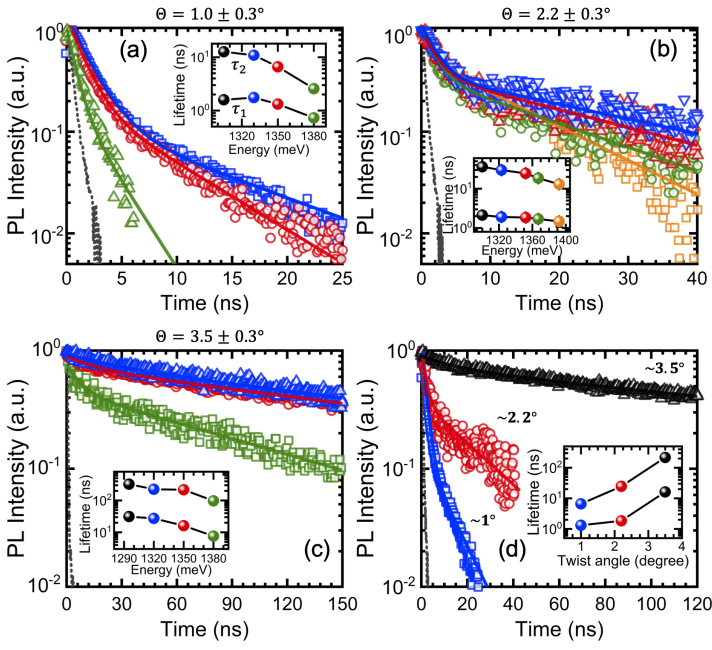


FIG. 3. Twist angle dependent lifetimes of all IX resonances measured from (a) $\Theta = 1.0 \pm 0.3^\circ$, (b) $2.2 \pm 0.3^\circ$, and (c) $3.5 \pm 0.3^\circ$ TBLs, respectively. Inset shows the energy dependence of the fast (τ_1) and slow (τ_2) decay components of IX lifetimes. Solid and black dotted lines represent fitting with a biexponential decay and instrumental response functions, respectively. (d) Twist angle dependence of IX lifetimes measured near 1345 - 1355 meV in the TBLs. Inset summarizes the extracted fast and slow decay components in the three TBLs.

are characterized by the center-of-mass momentum \mathbf{Q} . Here, $a_{\mathbf{K}_c+\mathbf{q}}^{\dagger,c}$ ($a_{\mathbf{K}_v+\mathbf{q}}^v$) creates (annihilates) an electron in the \mathbf{K}_c (\mathbf{K}_v)-valley of the conduction (valence) band, $M = m_e + m_h$ is the total exciton mass, and m_e (m_h) is the electron (hole) effective mass. \mathcal{A} is the crystal area. The electron-hole relative-motion wave function in momentum space $\phi_X(\mathbf{k})$ is determined by the Wannier equation. Its solution determines the IX energy $E_{\text{gap}} - E_B$, where E_B is the IX binding energy and E_{gap} is the band gap.

An interlayer twist in real space generates a relative shift in momentum space ($\mathbf{K}_c - \mathbf{K}_v$, see Fig. 1c) as well as a spatial modulation of the exciton energy. In all three TBLs, the moiré periodicity can be assumed to be large compared to the IX Bohr radius. Thus, we neglect the variation of the binding energy in the moiré pattern and use a local approximation of the IX moiré potential $V^M(\mathbf{R})$ according to Ref. [12]. In this framework, the IX Hamiltonian reads

$$H = -\frac{\hbar^2}{2M}\Delta_{\mathbf{R}} + V^M(\mathbf{R}), \quad (3)$$

where $-\frac{\hbar^2}{2M}\Delta_{\mathbf{R}}$ is the exciton center-of-mass kinetic energy and can be diagonalized using a plane-wave expansion with eigenenergies $\varepsilon_{\mathbf{Q},\lambda}$ and eigenstates

$$|\mathbf{Q}, \lambda\rangle = \sum_{\mathbf{G}_M} c_{\mathbf{Q}-\mathbf{G}_M}^\lambda |\mathbf{Q} - \mathbf{G}_M\rangle. \quad (4)$$

The moiré reciprocal lattice vectors \mathbf{G}_M are derived as differences of top and bottom layer reciprocal lattice vectors. Therefore, the size of the moiré Brillouin zone (MBZ) scales with the interlayer twist angle. We represent its center and boundary

by γ and κ , respectively. We use the above plane-wave expansion, and solve the optical matrix element between the initial moiré exciton state $|\mathbf{Q}, \lambda\rangle$ and the final photon state $|\mathbf{q}, \sigma\rangle$. Moiré excitons can only recombine if the momentum conservation law $\mathbf{Q} - \mathbf{q}_{\parallel} = \mathbf{K}_c - \mathbf{K}_v := \mathbf{Q}_{IX}$ is fulfilled where \mathbf{q}_{\parallel} represents the in-plane component of the photon wavevector. We assume that the twist angle is sufficiently large so that typical photon momenta are still small compared to the MBZ, which in our case is well-justified for twist angles larger than 0.5° . In this case, we can discard umklapp processes.

In the numerical calculation shown in Fig. 4, we assume the exciton population is thermalized obeying a Boltzmann distribution. To clarify the twist angle dependence, we disentangle the influence of the valley shift in reciprocal space from the energy modulation of moiré potential. First of all, a drastic change in IX lifetimes with the twist angle is expected even in the absence of a moiré potential by just considering the shifted valleys illustrated in Fig. 1c and d. Only excitons within the light cone can decay radiatively. For a TBL with a small twist angle, low-temperatures are favorable to thermally keep as many excitons as possible within a narrow region around the Γ point in the excitation picture. On the other hand, in a TBL with a large twist angle, light-matter coupling benefits from long tails in the high-temperature exciton distribution to overcome the large momentum shift Q_{IX} . As a result, the temperature dependence of IX lifetimes exhibits opposite behavior in TBLs with small and large twist angles. We therefore predict a crossover between these two regimes around an intermediate twist angle of $\theta = 2^\circ$ as shown in Fig. 4a.

Figure 4c and d provide detailed insight for the cases of small and large twist angles at low-temperature, showing that at small twist angle the light cone overlaps with more occupied exciton states. Due to the absence of a moiré potential, the parabolic dispersion is simply folded back to the first MBZ without hybridization of bands. In Fig. 4b, the presence of a moiré potential does not change the general trends but leads to a softening of the twist angle dependence. This can be understood as the moiré potential introducing an interaction between the IXs with different center-of-mass momenta as represented by the matrix form of eq. (3). Thereby, the momentum conservation between the IX and photon in the light-matter coupling process is relaxed, opening additional channels for radiative recombination, as shown in Fig. 4e-f. Correspondingly, the IX bands become less dispersive due to the moiré potential. Nevertheless, the IX lifetimes are predicted to change by several orders of magnitude when the twist angle is tuned between 1° and 3.5° . Here, the symbol size quantifies the contribution of the moiré exciton states to the bright density-of-states as given by the coefficients $c_{\mathbf{Q}}^\lambda$ in eq. (4). Comparing panels e and f, we see that a small twist angle is particularly beneficial for light emission at low-temperatures due to the flattening of IX bands that leads to strong population of κ excitons. We further compare the moiré exciton distribution at 20 K (Fig. 4f) and 300 K (SM Fig. S5b), demonstrating how a thermally broadened IX distribution fosters exciton-photon coupling at a large twist angle. In all cases, we find that higher excitonic bands become occupied due to the moiré-induced mixture of bands represented by the relevant ($G_M = 0$)-contributions ($c_{\mathbf{Q}}^\lambda$ in eq. (4) as shown in Fig. 4e-f), in contrast to the cases when the moiré potential is not taken into account in Fig. 4c-d.

To examine the predicted temperature dependence of IX ra-

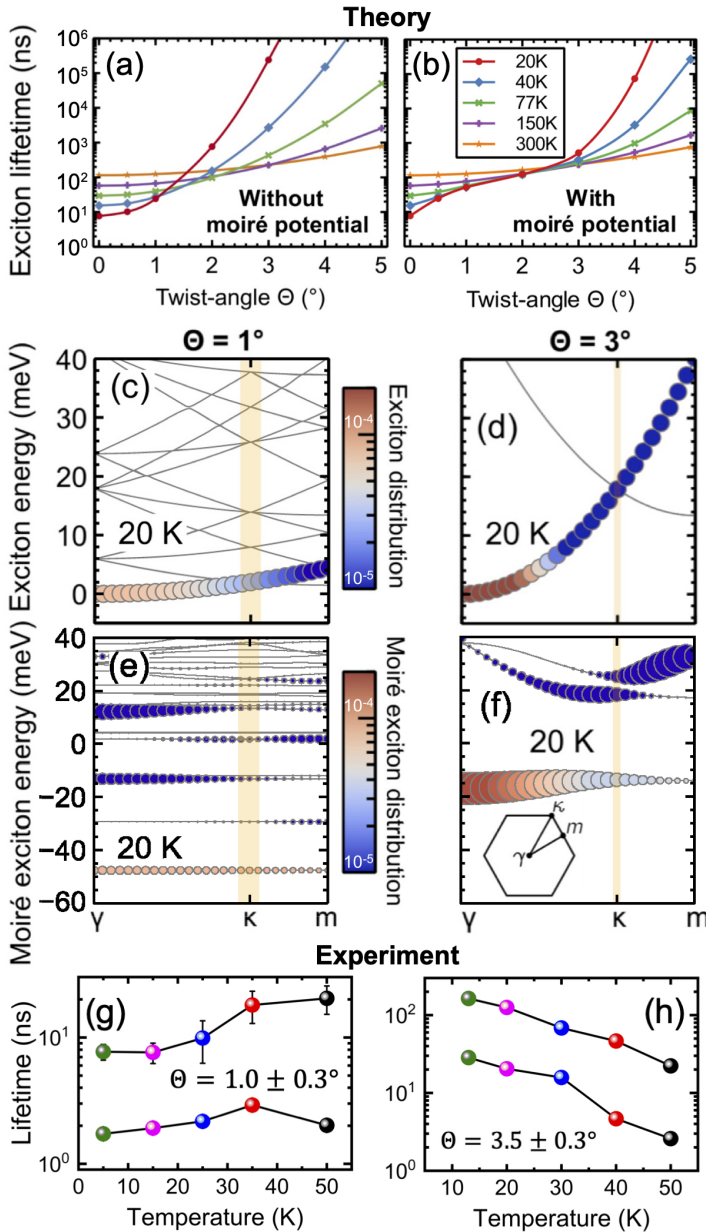


FIG. 4. Temperature and twist angle dependence of calculated IX radiative lifetimes in the absence/presence of a moiré potential and measured temperature dependent IX dynamics. Calculated twist angle dependence of the IX lifetimes shown for various temperatures in the (a) *absence* and (b) *presence* of a moiré potential. Panels (c) and (d) show the IX band structure in the *absence* of a moiré potential at twist angles of $\Theta = 1^{\circ}$ and $\Theta = 3^{\circ}$, respectively. Moiré exciton states are classified by momenta from the first MBZ shown in inset of (f). Light cone (orange shaded area) occupies a larger fraction of the MBZ for a TBL with a smaller twist angle. Panels (e)-(f) show the moiré exciton band structure, thermal distribution, and density-of-states contribution for different twist angles at low-temperature. Scale of the symbol size is the same for panel (c,d) and (e,f). Note that at small twist angle the IX bands become flat due to the moiré potential. (g, h) Measured temperature dependent fast and slow decay components of lifetimes near 1350 meV in the TBLs with $\Theta = 1.0 \pm 0.3^{\circ}$ ($3.5 \pm 0.3^{\circ}$) from 5 to 50 K (13 to 50 K). Error bars are smaller than the symbols for some data points.

diative lifetimes, we compare measurements performed on two TBLs with the caveat that the total lifetime is measured. Figure 4g and h show the temperature dependent two decay times extracted by fitting with a bi-exponential function for the two TBLs with $\Theta = 1^{\circ}$ and 3.5° , respectively. Indeed, we experimentally observed opposite trends in the temperature dependent IX lifetimes in two TBLs. The IX lifetime increased (decreased) at higher temperature in the small (large) twist angle sample. This trend is consistent with the calculation (Fig. 4b) although a much weaker temperature dependence was observed. The deviation of the fast lifetime component from the $\Theta = 1^{\circ}$ sample at ~ 50 K may originate from increased phonon-mediated non-radiative processes.

We discuss the scope and limitations of our studies. First, we focus on $\text{MoSe}_2/\text{WSe}_2$ TBLs with relatively small twist angles with an more accurate angle control than most previous experiments that have investigated the change of exciton resonances over a broader range of twist angle [59–62]. In TBLs with a small twist angle, the thermal distribution of the IX may be sufficient to satisfying the momentum conservation requirements of an indirect optical transition. In practice, phonon-assisted transitions do exist. Such transitions play an increasingly important roles in TBLs with larger twist angle ($\Theta > 5^{\circ}$). Second, the biexponential decay dynamics are not fully explained. We provide a rate equation analysis for a three-level system involving a dark state in the SM. Such a dark state may originate from an indirect transition involving electrons or holes in a different valley. Third, our calculations only address the radiative decay rate and our experiments measure the total decay rate. The calculation models an ideal situation where the IX dynamics is determined by the radiative process with unity quantum yield. It addresses the question of how radiative decay can be controlled by the twist angle with and without the presence of an moiré superlattice. The qualitative agreement between the experiments and calculations is noteworthy. This agreement may suggest that the non-radiative decay processes either do not depend on the twist angle strongly or depend on the twist angle in a similar way as the radiative decay.

In conclusion, our studies represent a first step toward understanding how the twist angle of a vdW heterostructure can be used to control exciton dynamics. These results provide critical guidance to efforts on searching for exciton condensates where a long IX lifetime is preferred to reach an equilibrium temperature with the lattice. On the other hand, light-emitting devices should be built with TMD TBLs with a small twist angle. A faster radiative lifetime can compete favorably with other non-radiative processes and lead to higher quantum efficiency. Our work introduces new methods, “momentum-space band shift” and “periodic in-plane energy modulation” for controlling exciton lifetimes. These methods may be adapted by researchers investigating different classes of materials and be exploited by a wide variety of optoelectronic devices.

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- [1] K. S. Novoselov, A. Mishchenko, A. Carvalho, and A. H. Castro Neto, *Science* **353**, aac9439 (2016).
- [2] Y. Liu, N. O. Weiss, X. Duan, H.-C. Cheng, Y. Huang, and X. Duan, *Nature Reviews Materials* **1**, 16042 (2016).
- [3] J. Quan, L. Linhart, M.-L. Lin, D. Lee, J. Zhu, C.-Y. Wang, W.-T. Hsu, J. Choi, J. Embley, C. Young, T. Taniguchi, K. Watanabe, C.-K. Shih, K. Lai, A. H. MacDonald, P.-H. Tan, F. Libisch, and X. Li, "Phonon renormalization in reconstructed mos_2 moiré superlattices," (2020), arXiv:2009.10650 [cond-mat.mes-hall].
- [4] Y. Cao, V. Fatemi, A. Demir, S. Fang, S. L. Tomarken, J. Y. Luo, J. D. Sanchez-Yamagishi, K. Watanabe, T. Taniguchi, E. Kaxiras, R. C. Ashoori, and P. Jarillo-Herrero, *Nature* **556**, 80 (2018).
- [5] Y. Cao, V. Fatemi, S. Fang, K. Watanabe, T. Taniguchi, E. Kaxiras, and P. Jarillo-Herrero, *Nature* **556**, 43 (2018).
- [6] K. Kim, A. DaSilva, S. Huang, B. Fallahzad, S. Larentis, T. Taniguchi, K. Watanabe, B. J. LeRoy, A. H. MacDonald, and E. Tutuc, *Proceedings of the National Academy of Sciences* **114**, 3364 (2017).
- [7] Y. Tang, L. Li, T. Li, Y. Xu, S. Liu, K. Barmak, K. Watanabe, T. Taniguchi, A. H. MacDonald, J. Shan, and K. F. Mak, *Nature* **579**, 353 (2020).
- [8] E. C. Regan, D. Wang, C. Jin, M. I. Bakti Utama, B. Gao, X. Wei, S. Zhao, W. Zhao, Z. Zhang, K. Yumigeta, M. Blei, J. D. Carlström, K. Watanabe, T. Taniguchi, S. Tongay, M. Crommie, A. Zettl, and F. Wang, *Nature* **579**, 359 (2020).
- [9] Y. Shimazaki, I. Schwartz, K. Watanabe, T. Taniguchi, M. Kroner, and A. Imamoglu, *Nature* **580**, 472 (2020).
- [10] L. Wang, E.-M. Shih, A. Ghiotto, L. Xian, D. A. Rhodes, C. Tan, M. Claassen, D. M. Kennes, Y. Bai, B. Kim, K. Watanabe, T. Taniguchi, X. Zhu, J. Hone, A. Rubio, A. N. Pasupathy, and C. R. Dean, *Nature Materials* **19**, 861 (2020).
- [11] H. Yu, G.-B. Liu, J. Tang, X. Xu, and W. Yao, *Science Advances* **3**, e1701696 (2017).
- [12] F. C. Wu, T. Lovorn, and A. H. MacDonald, *Physical Review B* **97**, 035306 (2018).
- [13] J. Kang, S. Tongay, J. Zhou, J. Li, and J. Wu, *Applied Physics Letters* **102**, 012111 (2013).
- [14] P. Rivera, J. R. Schaibley, A. M. Jones, J. S. Ross, S. Wu, G. Aivazian, P. Klement, K. Seyler, G. Clark, N. J. Ghimire, J. Yan, D. G. Mandrus, W. Yao, and X. Xu, *Nature Communications* **6**, 6242 (2015).
- [15] K. Tran, G. Moody, F. Wu, X. Lu, J. Choi, K. Kim, A. Rai, D. A. Sanchez, J. Quan, A. Singh, J. Embley, A. Zepeda, M. Campbell, T. Autry, T. Taniguchi, K. Watanabe, N. Lu, S. K. Banerjee, K. L. Silverman, S. Kim, E. Tutuc, L. Yang, A. H. MacDonald, and X. Li, *Nature* **567**, 71 (2019).
- [16] K. L. Seyler, P. Rivera, H. Yu, N. P. Wilson, E. L. Ray, D. G. Mandrus, J. Yan, W. Yao, and X. Xu, *Nature* **567**, 66 (2019).
- [17] E. M. Alexeev, D. A. Ruiz-Tijerina, M. Danovich, M. J. Hamer, D. J. Terry, P. K. Nayak, S. Ahn, S. Pak, J. Lee, J. I. Sohn, M. R. Molas, M. Koperski, K. Watanabe, T. Taniguchi, K. S. Novoselov, R. V. Gorbachev, H. S. Shin, V. I. Fal'ko, and A. I. Tartakovskii, *Nature* **567**, 81 (2019).
- [18] H. Yu, Y. Wang, Q. Tong, X. Xu, and W. Yao, *Physical Review Letters* **115**, 187002 (2015).
- [19] P. Rivera, K. L. Seyler, H. Y. Yu, J. R. Schaibley, J. Q. Yan, D. G. Mandrus, W. Yao, and X. D. Xu, *Science* **351**, 688 (2016).
- [20] B. Miller, A. Steinhoff, B. Pano, J. Klein, F. Jahnke, A. Holleitner, and U. Wurstbauer, *Nano Letters* **17**, 5229 (2017).
- [21] P. Nagler, M. V. Ballottin, A. A. Mitroglou, F. Mooshammer, N. Paradiso, C. Strunk, R. Huber, A. Chernikov, P. C. M. Christianen, C. Schuller, and T. Korn, *Nature Communications* **8**, 1551 (2017).
- [22] L. A. Jauregui, A. Y. Joe, K. Pistunova, D. S. Wild, A. A. High, Y. Zhou, G. Scuri, K. De Greve, A. Sushko, C.-H. Yu, T. Taniguchi, K. Watanabe, D. J. Needleman, M. D. Lukin, H. Park, and P. Kim, *Science* **366**, 870 (2019).
- [23] J. Wang, J. Ardelean, Y. Bai, A. Steinhoff, M. Florian, F. Jahnke, X. Xu, M. Kira, J. Hone, and X. Y. Zhu, *Science Advances* **5**, eaax0145 (2019).
- [24] J. Choi, W.-T. Hsu, L.-S. Lu, L. Sun, H.-Y. Cheng, M.-H. Lee, J. Quan, K. Tran, C.-Y. Wang, M. Staab, K. Jones, T. Taniguchi, K. Watanabe, M.-W. Chu, S. Gwo, S. Kim, C.-K. Shih, X. Li, and W.-H. Chang, *Science Advances* **6**, eaba8866 (2020).
- [25] A. Castellanos-Gomez, M. Buscema, R. Molenaar, V. Singh, L. Janssen, H. S. J. van der Zant, and G. A. Steele, *2D Materials* **1**, 011002 (2014).
- [26] N. Kumar, S. Najmaei, Q. Cui, F. Ceballos, P. M. Ajayan, J. Lou, and H. Zhao, *Physical Review B* **87**, 161403 (2013).
- [27] L. M. Malard, T. V. Alencar, A. P. M. Barboza, K. F. Mak, and A. M. de Paula, *Physical Review B* **87**, 201401 (2013).
- [28] Y. Li, Y. Rao, K. F. Mak, Y. You, S. Wang, C. R. Dean, and T. F. Heinz, *Nano Letters* **13**, 3329 (2013).
- [29] W. T. Hsu, Z. A. Zhao, L. J. Li, C. H. Chen, M. H. Chiu, P. S. Chang, Y. C. Chou, and W. H. Chang, *ACS Nano* **8**, 2951 (2014).
- [30] N. R. Wilson, P. V. Nguyen, K. Seyler, P. Rivera, A. J. Marsden, Z. P. L. Laker, G. C. Constantinescu, V. Kandyba, A. Barinov, N. D. M. Hine, X. Xu, and D. H. Cobden, *Science Advances* **3** (2017), 10.1126/sciadv.1601832.
- [31] M.-H. Chiu, M.-Y. Li, W. Zhang, W.-T. Hsu, W.-H. Chang, M. Terrones, H. Terrones, and L.-J. Li, *ACS Nano* **8**, 9649 (2014).
- [32] A. Chernikov, T. C. Berkelbach, H. M. Hill, A. Rigosi, Y. Li, O. B. Aslan, D. R. Reichman, M. S. Hybertsen, and T. F. Heinz, *Physical Review Letters* **113**, 076802 (2014).
- [33] M. M. Ugeda, A. J. Bradley, S.-F. Shi, F. H. da Jornada, Y. Zhang, D. Y. Qiu, W. Ruan, S.-K. Mo, Z. Hussain, Z.-X. Shen, F. Wang, S. G. Louie, and M. F. Crommie, *Nature Materials* **13**, 1091 (2014).
- [34] I. C. Gerber and X. Marie, *Physical Review B* **98**, 245126 (2018).
- [35] A. Raja, L. Waldecker, J. Zipfel, Y. Cho, S. Brem, J. D. Ziegler,

- M. Kulig, T. Taniguchi, K. Watanabe, E. Malic, T. F. Heinz, T. C. Berkelbach, and A. Chernikov, *Nature Nanotechnology* **14**, 832 (2019).
- [36] M. Danovich, D. A. Ruiz-Tijerina, R. J. Hunt, M. Szyniszewski, N. D. Drummond, and V. I. Fal'ko, *Physical Review B* **97**, 195452 (2018).
- [37] L. Zhang, R. Gogna, G. W. Burg, J. Horng, E. Paik, Y.-H. Chou, K. Kim, E. Tutuc, and H. Deng, *Physical Review B* **100**, 041402 (2019).
- [38] A. Ciarrocchi, D. Unuchek, A. Avsar, K. Watanabe, T. Taniguchi, and A. Kis, *Nature Photonics* **13**, 131 (2019).
- [39] W. Li, X. Lu, S. Dubey, L. Devenica, and A. Srivastava, *Nature Materials* (2020), 10.1038/s41563-020-0661-4.
- [40] S. Brem, C. Linderälv, P. Erhart, and E. Malic, *Nano Letters* (2020), 10.1021/acs.nanolett.0c03019.
- [41] G. Moody, J. Schaibley, and X. Xu, *Journal of the Optical Society of America B* **33**, C39 (2016).
- [42] M. Palumbo, M. Bernardi, and J. C. Grossman, *Nano Letters* **15**, 2794 (2015).
- [43] X.-X. Zhang, Y. You, S. Y. F. Zhao, and T. F. Heinz, *Physical Review Letters* **115**, 257403 (2015).
- [44] P. A. Dalgarno, J. M. Smith, B. D. Gerardot, A. O. Govorov, K. Karrai, P. M. Petroff, and R. J. Warburton, *physica status solidi (a)* **202**, 2591 (2005).
- [45] Y. Chen, J. Vela, H. Htoon, J. L. Casson, D. J. Werder, D. A. Bussian, V. I. Klimov, and J. A. Hollingsworth, *Journal of the American Chemical Society* **130**, 5026 (2008).
- [46] C. J. Hanson, M. R. Buck, K. Acharya, J. A. Torres, J. Kundu, X. Ma, S. Bouquin, C. E. Hamilton, H. Htoon, and J. A. Hollingsworth, *ACS Applied Materials & Interfaces* **7**, 13125 (2015).
- [47] N. J. Orfield, S. Majumder, J. R. McBride, F. Yik-Ching Koh, A. Singh, S. J. Bouquin, J. L. Casson, A. D. Johnson, L. Sun, X. Li, C.-K. Shih, S. J. Rosenthal, J. A. Hollingsworth, and H. Htoon, *ACS Nano* **12**, 4206 (2018).
- [48] A. Steinhoff, H. Kurtze, P. Gartner, M. Florian, D. Reuter, A. D. Wieck, M. Bayer, and F. Jahnke, *Physical Review B* **88**, 205309 (2013).
- [49] G.-B. Liu, W.-Y. Shan, Y. Yao, W. Yao, and D. Xiao, *Physical Review B* **88**, 085433 (2013).
- [50] M. Florian, M. Hartmann, A. Steinhoff, J. Klein, A. W. Holleitner, J. J. Finley, T. O. Wehling, M. Kaniber, and C. Gies, *Nano Letters* **18**, 2725 (2018).
- [51] N. A. Asriyan, I. L. Kurbakov, A. K. Fedorov, and Y. E. Lozovik, *Physical Review B* **99**, 085108 (2019), publisher: American Physical Society.
- [52] M. A. Semina, *Physics of the Solid State* **61**, 2218 (2019).
- [53] I. Kylänpää and H.-P. Komsa, *Physical Review B* **92**, 205418 (2015).
- [54] R. Geick, C. H. Perry, and G. Rupprecht, *Physical Review* **146**, 543 (1966).
- [55] N. S. Rytova, *Proc. MSU, Phys.* **3**, 30 (1967).
- [56] L. V. Keldysh, *Soviet Journal of Experimental and Theoretical Physics Letters* **29**, 658 (1979).
- [57] A. Esser, E. Runge, R. Zimmermann, and W. Langbein, *Physical Review B* **62**, 8232 (2000).
- [58] F. Wu, T. Lovorn, and A. MacDonald, *Physical Review Letters* **118**, 147401 (2017).
- [59] A. M. van der Zande, J. Kunstmann, A. Chernikov, D. A. Chenet, Y. You, X. Zhang, P. Y. Huang, T. C. Berkelbach, L. Wang, F. Zhang, M. S. Hybertsen, D. A. Muller, D. R. Reichman, T. F. Heinz, and J. C. Hone, *Nano Letters* **14**, 3869 (2014).
- [60] P. K. Nayak, Y. Horbatenko, S. Ahn, G. Kim, J.-U. Lee, K. Y. Ma, A. R. Jang, H. Lim, D. Kim, S. Ryu, H. Cheong, N. Park, and H. S. Shin, *ACS Nano* **11**, 4041 (2017).
- [61] J. Kunstmann, F. Mooshammer, P. Nagler, A. Chaves, F. Stein, N. Paradiso, G. Plechinger, C. Strunk, C. Schüller, G. Seifert, D. R. Reichman, and T. Korn, *Nature Physics* **14**, 801 (2018).
- [62] W.-T. Hsu, B.-H. Lin, L.-S. Lu, M.-H. Lee, M.-W. Chu, L.-J. Li, W. Yao, W.-H. Chang, and C.-K. Shih, *Science Advances* **5**, eaax7407 (2019).