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Three-dimensional Vortex-induced Reaction Hotspots at Flow Intersections

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We show the emergence of reaction hotspots induced by three-dimensional (3D) vortices with a simple $A + B \rightarrow C$ reaction. We conduct microfluidics experiments to visualize the spatial map of the reaction rate with a chemiluminescence reaction and cross-validate the results with direct numerical simulations. 3D vortices form at spiral saddle type stagnation points, and the 3D vortex flow topology is essential for initiating reaction hotspots. The effect of vortices on mixing and reaction becomes more vigorous for rough-walled channels, and our findings are valid over wide ranges of channel dimensions and Damköhler numbers.

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7 ⁸ an axis line, commonly occurs in various channel flow systems such as rock fractures [1–4], porous media [5–8], pipe 9 flows [9, 10], micromixers [11], and blood vessels [12, 13]. 10 11 Specifically, vortices can have a distinctive flow topology [14– 16], and the topology of a flow field is known to control mix-12 ing processes, which in turn control reaction dynamics [17– 13 9]. Vortices at fluid flow intersections are particularly im-14 1 portant because fluids with different properties can mix and 15 react at flow intersections [20-22]. Notably, vortices may al-16 ter mixing dynamics and initiate local reaction hotspots where 17 reaction rates are locally maximum. Nevertheless, to the best 18 of our knowledge, there has been no study that elucidated the 19 ole of three-dimensional (3D) vortices on mixing and reac-20 tion at flow intersections. 21

In this study, we combined laboratory microfluidic exper-22 iments and direct numerical simulations to establish a pre-23 viously unrecognized link between the 3D flow topology of 24 ortices and reaction hotspots. A novel chemiluminescence 25 eaction was adopted to visualize the spatial map of reaction 26 ates in channel intersections across a wide range of Reynolds 27 umbers (Re). Further, flow and reactive transport simulations 28 rere experimentally cross-validated and used to demonstrate 29 the role of 3D vortex topology on the emergence of reaction 30 hotspots where reaction products are actively produced. To 31 demonstrate the ubiquitous nature of vortex-induced reaction 32 hotspots, we conducted experiments on rough-walled chan-33 nels and also performed simulations over wide ranges of chan-34 el dimensions and Damköhler numbers (Da). 35

Microfluidic experiment We conducted microfluidic ex-36 eriments with chemiluminescence reaction [23] to visualize 37 mixing and reaction at intersections. The mixing-induced re-38 action was performed by injecting two reactive solutions, la-39 beled A and B, into two separate inlets on a polydimethyl-40 siloxane (PDMS) microfluidic chip using a pulsation-free sy-41 ringe pump (neMESYS 290N, Cetoni, Korbussen, Germany). 42 The channels had a constant aperture of 100 μ m, a depth of 43

Vortex, a region in a fluid in which the flow revolves around 44 70 μ m, and a channel length of 2 cm. The two channels inaxis line, commonly occurs in various channel flow sysns such as rock fractures [1–4], porous media [5–8], pipe 46 at which the solutions mixed, and the chemiluminescence biws [9, 10], micromixers [11], and blood vessels [12, 13]. 47 molecular reaction (A + B \rightarrow C) occurred thereafter.

> 48 A reaction between A and B produces a photon, and the ⁴⁹ produced photons were detected by a scientific CMOS camera 50 (Orca-Flash4.0, Hamamatsu, Shizuoka, Japan) connected to a 51 motorized inverted microscope system (TI2-E Nikon). The ⁵² spatial map of reaction rate, $\frac{dc}{dt}$, was estimated by normalizing ⁵³ the accumulated light intensity values, which is proportional 54 to Δc , by the exposure time, Δt [24]. The composition of so-⁵⁵ lution A was 1.5 mM of 1,8-diazabicyclo-[5,4,0]-undec-7-ene 56 (DBU), 15 mM of 1,2,4-Triazole, 0.15 mM of 3- aminoflu- $_{57}$ oranthen (3 AFA), and 3 mM of H_2O_2 . The composition 58 of solution B was 3 mM of bis(2,4,6- trichlorophenyl)oxalate 59 (TCPO). The solutes were dissolved in acetonitrile, and 60 the experiments were performed at 25°C. All the chemicals 61 were purchased from Sigma-Aldrich (MO, USA). For passive 62 tracer experiments, plain solvent and a solution containing 3 63 mM of 3 - AFA, which is a fluorescently active species, were 64 separately injected into the two inlets, and the transport of the 65 tracer was monitored via a green fluorescent protein filter (EX: 66 470/40nm, EM: 525/50nm).

> ⁶⁷ We investigated the inertia effects on the flow and reactive ⁶⁸ transport by varying *Re* in the range of 1 – 300, which com-⁶⁹ monly occur in natural and engineering processes [4, 25–28]. ⁷⁰ *Re* was defined as $\frac{U_0h}{v}$ where U_0 is the average flow velocity ⁷¹ through a channel, *h* is the aperture of the channel, and *v* is ⁷² the kinematic viscosity of the fluid. *Da* is defined as $\frac{c_0h^2k}{D}$, ⁷³ where *D* is the diffusion coefficient of solutes, *k* is the reac-⁷⁴ tion constant, and c_0 is the initial solute concentration. The ⁷⁵ experiments were conducted under seven different Reynolds ⁷⁶ numbers: Re = [1, 10, 20, 50, 100, 150, 300]. For all studied ⁷⁷ cases, both flow and concentration fields reach steady state. ⁷⁸ The estimated *Da* in this study was 6.25, and this implies that ⁷⁹ the system was relatively diffusion-limited with respect to the ⁸⁰ reaction.

> Flow and reactive transport simulation We crossvalidated experimental results with direct numerical simulations. The fluid flow simulations were performed in COM-SOL Multiphysics (ver. 5.3). The density and kinematic vis-

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s cosity of acetonitrile are 787 kg/m³ and 1.6×10^{-6} m²/s, respectively. The fluid flow was induced by setting a fixed in-86 let flow rate which determines Re, and the flow fields were 87 obtained by solving the continuity equation and the Navier-88 Stokes equations with the finite element method. The flow 89 channel domain were discretized into 1.8×10^6 elements for 90 3D simulations and into 5×10^3 elements for 2D simulations, 91 and no slip boundary conditions were assigned at channel 92 walls. 2D simulations assume parallel plate flows and neglect 93 the boundary effects from the top and bottom boundaries. 94

The flow field solutions were then coupled with the 95 advection-diffusion-reaction equation [29]: 96

$$\frac{\partial c_i}{\partial t} = -\nabla \cdot (uc_i) + \nabla \cdot (D_i \nabla c_i) + R_i \tag{1}$$

where c_i is the concentration of solute *i*, t is the time, D_i 97 is the diffusion coefficient of solute i, and R_i is the reaction 98 rate of solute *i*. The subscript *i* represents species A, B, and C 99 involved in the reaction. The limiting agents H₂O₂ and TCPO were chosen as the representative species for solutions A and 101 B, respectively, and their initial concentrations of 3 mM were 102 introduced into the two separate inlets. The diffusion coeffi-103 cient of 3×10^{-9} m²/s was used for H₂O₂ [30], and 1.6×10^{-9} m²/s was used for TCPO [24] and product C. The temperature 105 was set to 25°C in the model. The reaction between A and B ¹⁰⁷ is irreversible and the rate of loss of each reactant is equal to ¹⁰⁸ the rate of production of the product C which is described by 109 a second-order reaction kinetics:

$$R_i = \frac{dc_C}{dt} = -\frac{dc_A}{dt} = -\frac{dc_B}{dt} = kc_A c_B \tag{2}$$

110 the initial solute concentration, and τ_r is the characteristic re-111 ction time which is obtained experimentally [23, 24, 31]. All 112 of the flow and reactive transport simulations were converged 113 to steady state. 114

115 *hotspots* The microfluidic experimental results from a ¹⁴⁰ the total reaction rate $\sum \frac{dc}{dt}$ at Re = 20. 116 straight orthogonal intersection are shown in Fig. 1, and the 141 117 118 119 eaction dynamics as *Re* increases from 1 to 300. Particularly, 120 121 greater than 200. 122

123 124 126 127 128 $_{130}$ observed at Re = 20, but the width of the reaction band and $_{154}$ leading to a relatively constant total reaction rate. ¹³¹ the total reaction rate, $\sum \frac{dc}{dt}$, which is obtained by integrat-¹⁵⁵ At Re = 200, the width of the secondary reaction streams



FIG. 1. The spatial maps of reaction rate obtained from the microfluidic reaction experiments at Re of (a) 1, (b) 20, (c) 100, (d) 200, and (e) 300, and (f) the plots of total $\frac{dc}{dt}$ (red solid line) and maximum $\frac{dc}{dt}$ (blue dashed line). The color scale represents the light intensity divided by the exposure time, which is proportional to the reaction rate, $\frac{dc}{dt}$. The channels have a constant aperture of 100 μ m and a depth of 70 μ m. Insets: streamlines obtained from flow simulations with the color scale showing a normalized velocity magnitude.

where k is the reaction constant defined as $k = \frac{1}{c_0 \tau_r}$: c_0 is $\frac{1}{c_0 \tau_r}$: c_0 is $\frac{1}{c_0 \tau_r}$: c_0 is the solute concentration and τ is the solute residence to the solute residence to the solute concentration and τ is the solute concentration of the solute concentration and τ is the solute concentration and τ is the solute concentration of the solute concentration and τ is the solute concentration of the solute concentration and τ is the solute concentration of 135 time, thereby reducing the amount of diffusive mixing. Con-136 sequently, the concentration gradient of solutes at the solu-137 tion interface increased thereby elevating the local reaction 138 rate (i.e., light intensity). On the other hand, the reduced reac-Experimental observation of vortex-induced reaction 139 tion area and the solute residence time, collectively, lowered

At Re = 100, a parabolic secondary reaction stream streamlines obtained from flow simulations are shown in the 142 emerges from the interface (indicated by an arrow in insets. The spatial map of $\frac{dc}{dt}$ shows notable changes in the 143 Fig. 1(c)). The streamlines in the inset show the emergence 144 of twisting secondary flows around the corner. Such 3D hevortices seem to be strongly involved in the reaction at Re 145 lical streamlines in the direction of flow characterize a dean 146 flow [32], and the path of secondary reaction stream from At Re = 1 (Fig. 1(a)), the reaction occurs through a diffusive ¹⁴⁷ the experiment was consistent with the dean flow streamlines mixing of A and B along the dividing streamline and contin- 148 obtained from the flow simulation. The secondary reaction ues downstream. The analysis of streamlines confirmed that, 149 stream increases the total reaction area and decreases the maxacross all Re, no streamlines enter the opposite stream, and 150 imum reaction rate by disturbing the high concentration grahe two inlet flows are separated along the dividing stream- 151 dient along the dividing streamline. The decrease in the solute line. This implies that tracers can travel across the dividing $_{152}$ residence time and the maximum reaction rate from Re = 20streamline only by diffusion. Similar reaction dynamics are 153 to 150 is balanced by the increase in the total reaction area

¹³² ing the light intensity values in the field of view, decreased ¹⁵⁶ broadens significantly and they enter the vortices (Fig. 1(d)).

¹⁵⁷ This is more evident at Re = 300 at which the circular flow pattern in the vortex zone is more pronounced and reflected 158 in the $\frac{dc}{dt}$ map (Fig. 1(e)). In this regime, the secondary re-159 action streams carrying reactive species are connected to vor-160 tices where the reactants are further mixed and reacted. Be-161 ause flow velocities in the vortices are significantly smaller 162 han those in the main flow as shown in the insets, the local 163 Da number is higher in the vortex-zone causing the vortex-164 one to become a local reaction hotspot. The vortex-induced 165 eaction significantly increases the total reaction rate near the 166 167 intersection (Fig. 1(f)). The vortices also exist at Re = 100 but not strong enough to bring the secondary reactive streams into 168 ortices. This highlights the importance of the connected flow 169 paths between the secondary reactive streams and vortices in 170 the formation of vortex-induced reaction hotspots. One can 171 conjecture that only a 3D flow effect can realize the connected 172 flow paths, and this will be highlighted in the next section. 173

To summarize, there are three distinctive regimes for reac-174 tion dynamics as a function of Re (shown by dashed verti-175 cal lines in Fig. 1(f)). At Re < 20, the reaction is controlled 176 by the diffusive mixing along the dividing streamline. At 177 < Re < 150, the secondary reaction streams control the 178 20 reaction dynamics. At Re > 150, the vortex-induced reac-179 ion hotspots control the reaction dynamics. Based on our ob-180 servations, we hypothesize that the connected 3D flow paths 181 from the secondary reaction streams to vortices induce reac-182 tion hotspots, which significantly raise the reaction rates in 183 the third reaction regime. We validate our hypothesis by per-184 forming flow topology analysis and comparing experimental 185 esults with 2D and 3D simulations. 186

3D vortex flow topology We studied transport characteris-187 cs by injecting a fluorescent passive tracer from the bottom 188 inlet. Figure 2(a) shows the projected spatial map of tracer ²¹⁸ 189 190 191 192 193 194 195 196 197 set). 198

199 200 201 202 stagnation points and spiral saddle type stagnation points, re-203 spectively [16]. From the trajectories, we confirm that 3D vor-204 205 206 207 dvectively transport solutes from the solution interface to the ²³⁷ reaction products will also actively occur in vortices. 208 ortex, but this is not possible in 2D vortices that do not have 238 209 210 211 212 to center stagnation points in 2D is a fundamental difference 241 least one point along their paths are defined as reactive stream-



FIG. 2. The projected spatial maps of tracer concentration at Re =300 obtained from (a) microfluidics experiment, (b) 3D simulation, and (c) 2D simulation. (d) The selected streamlines associated with vortex-connected streamlines. The yellow cross-surface shows the dividing stream surface (solution interface). The color bar indicates z-directional locations and highlights the z-directional motion of the spiral flow paths. Inset (a) Normalized projected concentration profiles along the cross-line AB. Inset (c) Streamlines obtained from the 2D simulation with red lines showing closed circular streamlines around the center type stagnation point.

213 between 2D and 3D flow topologies [16]. The 3D topology 214 enables connectivity between main flow paths and vortices via ²¹⁵ 3D spiral flow paths, and this leads to the multi-peak behavior. 210

3D vortex-induced reaction hotspots We performed reacconcentration obtained from the microfluidic experiment at 219 tive transport simulations to confirm 3D vortex-induced reac-Re = 300. The active transport of tracer from the dividing ²²⁰ tion hotspots. The projected spatial map of reaction rate, $\frac{ac_c}{dt}$, reamline to the vortex is clearly observed. The 2D projected 221 obtained from the 3D simulation is consistent with the experacer concentration map from the 3D simulation shows a very 222 iment in which local reaction hotspots are formed at vortices similar pattern with the experiment while the vortex in the 2D 223 (Fig. 3(a)). On the other hand, the vortices in the 2D simulasimulation has zero concentration (Figs. 2(b) and (c)). Also, 224 tion are non-reactive (Fig. 3(b)). This discrepancy is caused the experimental and 3D simulation results show multi-peak 225 by the flow topology of 2D vortices that do not have flow conbehavior which is not captured in 2D simulation (Fig. 2(a) in- 226 nectivity with main flow paths (Fig. 2(c) inset). Notably, not ²²⁷ only is the reaction rate, $\frac{dc_C}{dt}$, high in the vortices, but the prod-The selected streamlines obtained from the 3D simulation 228 uct concentration, c_C , also increases significantly towards the (Fig. 2(d)) reveal 3D spiral flow paths from the solution inter- 229 3D vortices (Fig. 3(c)). The lowered local velocity in the vorface to the vortex. In this study, we define 2D and 3D vortices 230 tex zone allows the products to accumulate in the vortices. In as the regions with the local flow topology around center type 231 contrast, the product concentration is maximum along the di-²³² viding streamline in the 2D simulation (Fig. 3(c) inset). These ²³³ results suggest that the 3D connected flow paths turn vortices tices are formed at spiral saddle type stagnation points while 234 into reaction hotspots with not only high local reaction rates the vortices in the 2D simulation are formed at center type 235 but also high product concentrations. This implies that for stagnation points (Fig. 2(c) inset). The 3D spiral flow paths 236 multi-species reactive systems, successive reactions involving

We now directly quantify the link between reaction and vorflow connectivity with the main flow paths. The general oc- 239 tices. The streamlines that contain solutes from the opposite currence of spiral saddle stagnation points in 3D as opposed 240 solution at a concentration greater than 0.01 (i.e. $\frac{c_A}{c_0} > 0.01$) at



(a) $Da = 6.25 \times 10^2$ (b) $D_0 = 6.25$ $\frac{dc}{dt}$ $\frac{dc}{dt}$ normalized normalized 0 A dc/dt 1500 (c) Re 1 (d) Re 100 1000 500 100 un

FIG. 3. The projected spatial maps of local reaction rate, dc_C/dt at Re = 300 obtained from (a) 3D simulation, and (b) 2D simulation. Insets: the $\frac{dc_C}{dt}$ profile along the cross-line AB shown with the grey line. (c) The reaction product concentration, c_C , from 3D simulation. Inset: the c_C concentration profile along the cross-line AB for 3D and 2D simulations. (d) The illustration of reactive streamlines at Re = 300. The grey line shows a dividing streamline, and only a half of the intersection is shown because the system is symmetric. Inset: the plot of %vortex and normalized total reaction rates as a function of Re.

FIG. 4. (a) The normalized reaction rate profiles along the crossline AB as shown in the upper left inset. The red star in the inset shows the location of the maximum reaction rate. Upper right inset: the normalized maximum reaction rate in the vortex zone, $\frac{dc}{dt_{max}}$, obtained from 3D reactive transport simulations for a range of Da. (b) The normalized reaction rate profiles along the cross-line AB for a range of channel widths, h, from 100 μ m to 1 cm. (c) Reaction rate maps obtained from microfluidic experiments with rough-walled microchannel intersection at Re of 1, and (d) 100.

 $_{242}$ lines. In other words, the reactive streamlines describe stream- $_{272}$ simulations with different orders of channel aperture, h = 1 $_{243}$ lines containing both reactants with concentrations greater $_{273}$ mm and 1 cm, and Da numbers of 0.01 and 100 at Re = 300. 244 245 246 247 248 249 vortices is critical in the generation of reaction hotspots. 250

The connectedness of the reactive streamlines with vortices ²⁸¹ reaction hotspots. 251 is quantified by calculating the percentage of the red stream- 282 252 253 254 255 256 257 258 259 261 263 264 265 266 firms that both the 3D vortex flow topology and the decreased 297 in rough-walled channel flows. 267 velocity in vortices are critical for initiating reaction hotspots. 298 268 269 270 can vary widely depending on a system. To study the gen- 300 nature for the first time. 3D vortices occur at spiral saddle

271 erality of vortex-induced reaction hotspots, we conducted 3D than 0.01. Among reactive streamlines, red streamlines indi- 274 The depth of the channel was also changed to keep the same cate those that are drawn into a vortex while blue streamlines 275 aperture to depth aspect ratio (1:0.7), and the Da number denote those that do not enter a vortex (Fig. 3(d)). The pattern $_{276}$ was altered by changing the characteristic reaction time, τ_r . of red streamlines in Fig. 3(d) is consistent with the reaction 277 The normalized reaction rate along the cross-line AB, and the pattern obtained in the experiment (Fig. 1(e)). This indicates 278 maximum reaction rate in the vortex zone, $\frac{dc}{dt}$ max, are plotted that the flow connectivity between the reactive streams and 279 in Figs. 4(a) and (b). Regardless of channel dimension and re-280 action rates, we observe a ubiquitous nature of vortex-induced

The surfaces of flow channels are often rough, and the walllines with respect to the total reactive streamlines, i.e., %vortex. 283 roughness is known to promote the formation of vortices at This percentage, %vortex, and the normalized total reaction 284 lower Re, thereby impacting flow and transport [4]. We perrates obtained from the 3D and 2D simulations are plotted 285 formed experiments on a rough channel intersection to study as a function of Re (Fig. 3(d) inset). The increase in %vortex 286 the roughness effect on vortex-induced reaction hotspots. For from Re = 50 strongly correlates with the increase in the to- 287 generating rough surfaces, the Hurst exponent of 0.7 was tal reaction rates in the 3D simulation. In contrast, the 2D 288 used [29, 33, 34]. The channel had a constant aperture of simulation shows the opposite trend. This result indicates that $_{209}$ 100 μ m and a depth of 70 μ m. The experiments were per-3D description of flow and reaction at intersections is es- $_{290}$ formed at Re of 1 and 100. At Re = 1, the reaction occurred sential to capture reaction dynamics. Although the degree of 291 along the dividing streamline via diffusive mixing (Fig. 4(c)). the connectedness of the vortex dramatically increases from $_{292}$ At Re = 100, the reaction pattern changed significantly due Re = 200 to Re = 300, the total reaction rate does not exhibit 293 to the dean flow and 3D vortices formed at protruded areas similar behavior. This result is consistent with the experi- 294 (Fig. 4(d)). Note that such 3D flow characteristics emerged at ment (Fig. 1(f)), and it is due to the increased local velocity in $_{295}$ higher *Re* in the straight intersection. This result implies that the vortices which decrease Da inside of vortices. This con- 296 the vortex-induced reaction hotspots will more readily occur

In conclusion, we establish the mechanistic understanding Generality. The flow channel size and the reaction rate 299 of the vortex-induced reaction hotspots and their ubiquitous 301 type stagnation points, and this 3D flow topology is essential 338 [10] D. Oettinger, J. T. Ault, H. A. Stone, and G. Haller, Phys. Rev. in establishing the connected flow paths from the mainstream 339 302 to vortices through which the reactants enter the vortices 303 advectively. In addition, the increased solute residence time 304 inside the vortices due to the lower flow velocity, compared 305 to the main flow, facilitated the formation of a vortex-induced 344 [13] 306 reaction hotspot. Vortex-induced reaction hotspots are shown 345 307 occur over a wide range of channel dimensions and 346 [14] J. M. Délery, Annu. Rev. Fluid Mech. 33, 129 (2001). to 308 reaction rates, and they become more vigorous in rough 347 [15] G. Haller, Physica D 149, 248 (2001). 309 channels. These results have direct implications in many 310 engineering and natural processes involving mixing and 311 reaction in channel flows. 312

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