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# Quantum critical point in the itinerant ferromagnet $\text{Ni}_{1-x}\text{Rh}_x$

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We report a chemical substitution-induced ferromagnetic quantum critical point in polycrystalline  $\text{Ni}_{1-x}\text{Rh}_x$  alloys. Through magnetization and muon spin relaxation measurements, we show that the ferromagnetic ordering temperature is suppressed continuously to zero at  $x_{crit} = 0.375$  while the magnetic volume fraction remains 100% up to  $x_{crit}$ , pointing to a second order transition. Non-Fermi liquid behavior is observed close to  $x_{crit}$ , where the electronic specific heat  $C_{el}/T$  diverges logarithmically, while immediately above  $x_{crit}$  the volume thermal expansion coefficient  $\alpha_V/T$  and the Grüneisen ratio  $\Gamma = \alpha_V/C_{el}$  both diverge logarithmically in the low temperature limit, further indication of a ferromagnetic quantum critical point in  $\text{Ni}_{1-x}\text{Rh}_x$ .

A quantum critical point (QCP) occurs when a phase transition is continuously suppressed to zero temperature. The intense quantum fluctuations in the vicinity of a QCP profoundly alter a material's electronic properties, resulting in non-Fermi liquid behavior and, in some cases, unconventional superconductivity [1, 2]. The most ubiquitous QCP separates an antiferromagnetically ordered state from one in which quantum fluctuations disrupt the order. Notable examples are found among heavy fermion systems [1, 3, 4]. QCPs in ferromagnetic (FM) metals have proven far more elusive [5]. It is now understood that a FM QCP is inherently unstable and can survive only in rare circumstances [6]. In this work, we report the discovery of a FM QCP in  $\text{Ni}_{1-x}\text{Rh}_x$ , as evidenced by (i) a second-order phase transition up to the critical concentration  $x_{crit}$ , and (ii) divergence of the electronic specific heat coefficient  $C_{el}/T$ , the volume thermal expansion  $\alpha_V/T$ , and the Grüneisen ratio  $\Gamma = \alpha_V/C_{el}$ . The dilution of the  $d$ -electron magnetic sublattice as the tuning parameter to induce a FM QCP opens a new route for exploring FM quantum criticality and possible new collective phases near the QCP, such as unconventional superconductivity [7].

FM QCPs are revealed via chemical substitution in  $\text{Zr}_{1-x}\text{Nb}_x\text{Zn}_2$  [8],  $\text{SrCo}_2(\text{Ge}_{1-x}\text{P}_x)_2$  [9],  $\text{YbNi}_4(\text{P}_{1-x}\text{As}_x)_2$  [10], and  $(\text{Sc}_{1-x}\text{Lu}_x)_{3.1}\text{In}$  [11]. The disorder effect is minimal or negligible in these systems. For  $\text{SrCo}_2(\text{Ge}_{1-x}\text{P}_x)_2$ , the QCP is induced by the breaking of dimers [9]. However, the exact mechanism responsible for the FM QCP in the other three systems remains unclear. In most other FM metals, the QCP is preempted when the continuous (second-order)

transition as a function of non-thermal control parameter either becomes discontinuous (first-order), or the ferromagnetism is replaced by a spatially-modulated ordered state [5, 12–15]. Theoretical work by Belitz, Kirkpatrick, and Vojta (BKV) has proposed a route towards a FM QCP by long-range effective spin interactions that occur in the presence of quenched disorder [6, 16, 17]. A handful of FM QCPs have been identified as candidates for this phenomenology, including  $\text{UCo}_{1-x}\text{Fe}_x\text{Ge}$  [18],  $(\text{Mn}_{1-x}\text{Fe}_x)\text{Si}$  [19],  $\text{NiCoCr}_x$  [20], and  $\text{Ce}(\text{Pd}_{1-x}\text{Ni}_x)_2\text{P}_2$  [21], where disorder is inherently introduced by the chemical substitution. In most of these systems, the proposed existence of a QCP is based on either divergence of some thermodynamic parameters [18, 20, 21] or the second order nature of the transition [19]. However, the unambiguous identification of a QCP requires that both these criteria be fulfilled. This point is exemplified by disordered  $\text{Sr}_{1-x}\text{Ca}_x\text{RuO}_3$ , for which a QCP can be ruled out because the transition at  $T = 0$  is first order [22], and yet, quantum critical scaling is still observed [23]. Thus, in order to unambiguously identify a FM QCP it is essential that both thermodynamic signatures of quantum fluctuations *and* second-order behavior be observed simultaneously. **Our observation of both these requisite signatures in a chemically simple material where the FM QCP is induced via direct dilution of its  $d$ -electrons elevate  $\text{Ni}_{1-x}\text{Rh}_x$  to a top tier of candidates.**

Elemental Ni, which has a simple face-centered cubic structure, is known to order ferromagnetically below its Curie temperature  $T_C = 627$  K [24]. Upon alloying with Rh, the  $T_C$  of  $\text{Ni}_{1-x}\text{Rh}_x$  is quickly suppressed [25].

$\text{Ni}_{1-x}\text{Rh}_x$  has more configuration entropy than pure Ni [26]. Also, the metallic radii of Ni (124 pm) and Rh (134 pm) differ by  $\sim 8\%$ . Naturally, one would expect that, compared to pure Ni, there is more disorder in  $\text{Ni}_{1-x}\text{Rh}_x$  alloy, making it a good candidate to test for the existence of a disorder-driven FM QCP. Polycrystalline  $\text{Ni}_{1-x}\text{Rh}_x$  samples with  $0.3 \leq x \leq 0.42$  were prepared by arc-melting the constituents Ni and Rh and annealed at 1000° C. Magnetization measurements were carried out using a Quantum Design (QD) magnetic property measurement system. Zero-field muon spin relaxation measurements were performed at the M20 surface muon channel at TRIUMF. Specific heat was measured using a QD Dynacool physical property measurement system equipped with a dilution refrigerator. Thermal expansion was measured with a homemade capacitance dilatometer. More details about the sample characterizations and experimental methods are provided in the Supplemental Material [27–34].

Figure 1(a) shows the  $\mu_0 H = 0.01$  T magnetic susceptibility  $\Delta M(T)/H$  of  $\text{Ni}_{1-x}\text{Rh}_x$ , after a temperature-independent contribution  $M_0$  was subtracted from the measured  $M(T)$  ( $\Delta M = M - M_0$ ).  $\Delta M/H$  sharply increases as  $T$  is lowered through  $T_C$  for  $x = 0.32 - 0.36$  where  $T_C$  is determined both through a linear fit, as shown in Fig. 1(a), and the Arrott-Noakes analysis as discussed below. For  $x_{crit} = 0.375$  (where  $T_C \rightarrow 0$ ),  $\Delta M/H$  shows only a small increase down to the lowest measured temperature of 2 K, consistent with the complete suppression of FM order. Isothermal magnetization measurements at  $T = 2$  K confirm that  $\text{Ni}_{1-x}\text{Rh}_x$  is a soft ferromagnet without a measurable hysteresis (Fig 1(b)). We cannot rule out a very small antiferromagnetic component or canting close to  $x_{crit}$ , although magnetization suggests that FM correlations dominate, as evidenced by an abrupt increase of  $M(H)$  at the lowest field (Fig. 1(b)) and adherence to Arrott-Noakes scaling all the way up to  $x_{crit}$ . Future neutron scattering and nuclear magnetic resonance measurements will shed light on this issue. For the  $x = 0.32$  sample, which orders near 100 K, the inverse magnetic susceptibility  $H/\Delta M$  exhibits Curie-Weiss-like behavior between 150 and 300 K, from which we derive a paramagnetic (PM) effective moment  $\mu_{PM} = 1.97\mu_B/\text{f.u.}$  (see SM). For the same sample,  $\Delta M$  is small at 7 T ( $\sim 0.22\mu_B/\text{f.u.}$ ), and the Rhodes-Wohlfarth ratio,  $\mu_{PM}/\mu_{sat} = 9$ , much larger than unity, is indicative of itinerant moment behavior in  $\text{Ni}_{1-x}\text{Rh}_x$  [35]. An earlier study indicated spin glass behavior in  $\text{Ni}_{1-x}\text{Rh}_x$  [36]. However, our AC magnetic susceptibility measurements, presented in the SM, show no evidence for spin glass behavior near  $T_C$ . Such a discrepancy may be due to different purity of starting materials or sample homogeneity.

For ferromagnets, the equation of state at  $T_C$  is given by  $\Delta M \sim H^{1/\delta}$  [31]. From linear fits of  $\log(\Delta M)$  vs.  $\log(\mu_0 H)$ , as shown by the dashed line in Fig. 1(c), we

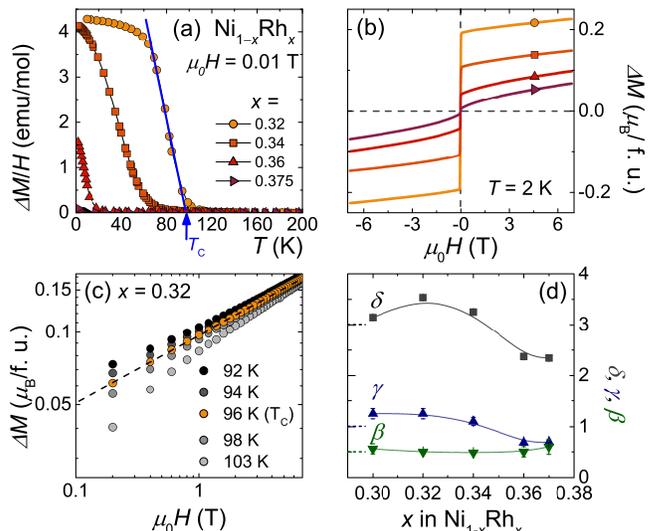


FIG. 1. (a) Magnetic susceptibility  $\Delta M/H = (M - M_0)/H$  for  $\mu_0 H = 0.01$  T and (b) isothermal magnetization  $\Delta M$  at  $T = 2$  K of  $\text{Ni}_{1-x}\text{Rh}_x$ . Solid line in (a) shows how  $T_C$  was determined. (c) Log-log magnetization isotherms for  $x = 0.32$ , with the dashed line showing  $T_C$ . (d) Critical exponents  $\beta$ ,  $\gamma$ , and  $\delta$  determined from the Arrott-Noakes scaling plots as a function of  $x$ . Solid lines are guides to the eye. Mean-field values  $\beta = 0.5$ ,  $\gamma = 1$ , and  $\delta = 3$  are indicated by horizontal dashed lines.

determine that  $T_C = 96$  K and  $\delta \sim 3.5$  for the  $x = 0.32$  sample. We applied the same analysis for all samples with  $x = 0.30 - 0.37$ . The critical exponents  $\beta$  and  $\gamma$  were determined by applying Arrott-Noakes scaling to the isotherms measured in the vicinity of  $T_C$  (see SM for details) [31]. The composition dependence of all three exponents,  $\delta$ ,  $\beta$ , and  $\gamma$ , is summarized in Fig. 1(d). The Widom relation  $\gamma/\beta = \delta - 1$  is obeyed over the entire range of Rh concentrations investigated here, a self-consistent check of the scaling analysis. At  $x = 0.30$ , which is well below  $x_{crit}$ , the exponents  $\beta = 0.5$ ,  $\gamma = 1.3$ , and  $\delta = 3.1$  are close to the expected mean-field values. With increasing  $x$ , the exponents deviate from the mean-field values and approach  $\beta = 0.6$ ,  $\gamma = 0.7$ , and  $\delta = 2.3$  at  $x = 0.37$ , just below  $x_{crit}$ . A similar evolution of the critical exponents with chemical substitution was observed in  $\text{Sr}_{1-x}\text{Ca}_x\text{RuO}_3$ , where it was proposed that disorder resulted in enhanced quantum fluctuations near  $x_{crit}$  [37].

Zero field  $\mu\text{SR}$  measurements were performed on six samples of  $\text{Ni}_{1-x}\text{Rh}_x$  with  $x = 0.30 - 0.39$ , in order to determine whether the magnetic order takes place via a first- or second-order process. Hallmarks of a first-order transition are phase separation or an abrupt change of ground state [22, 38]. Conversely, in the case of a second-order transition, the size of the ordered moment is expected to continuously decrease without phase separation.  $\mu\text{SR}$  allows an independent measure of both the

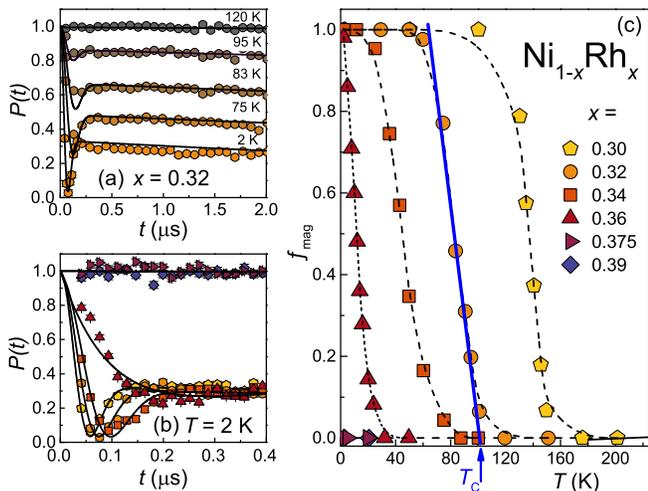


FIG. 2. (a) Temperature evolution of the normalized muon decay asymmetry  $P(t)$  for  $\text{Ni}_{1-x}\text{Rh}_x$  for  $x = 0.32$ . The solid lines are fits to Eqn. 1. (b)  $P(t)$  for all measured samples  $x = 0.30 - 0.39$ , at  $T = 2$  K. (c) The magnetic volume fraction  $f_{mag}$  as a function of temperature. Solid line shows how  $T_C$  was determined.

local order parameter and the magnetic volume fraction,  $f_{mag}$ , and can thus unambiguously distinguish between these scenarios. Representative muon decay asymmetry spectra,  $P(t)$ , are plotted in Fig. 2(a) for  $x = 0.32$  at various temperatures below and above  $T_C = 96$  K. Above  $T_C$ ,  $P(t)$  is essentially non-relaxing, as expected in a PM state. The onset of magnetic order is signaled by a fraction of the asymmetry undergoing rapid relaxation at early times. The compositional dependence of  $P(t)$  at  $T = 2$  K is presented in Fig. 2(b). This comparison reveals that the samples with the highest Rh concentrations,  $x = 0.375$  and  $0.39$  ( $\geq x_{crit}$ , blue and purple symbols), exhibit only weak relaxation down to the lowest measured temperatures, thus confirming the absence of magnetic order for these compositions. The samples with  $x < x_{crit}$  exhibit sharp relaxation associated with magnetic order. The  $P(t)$  data for all compositions and temperatures is well-described by the dynamic Kubo-Toyabe function [? ]:

$$P(t) = (1 - f_{mag}) \cdot e^{-\lambda t} + f_{mag} \cdot G_{DKT}(t, \sigma, \nu) \quad (1)$$

where  $\lambda$  and  $\sigma$  are the relaxation rates for the non-magnetic and magnetic fractions of the sample, respectively, and  $\nu$  is the hopping rate. The temperature dependence of  $f_{mag}$  is presented in Fig. 2(c), revealing no evidence for phase separation;  $f_{mag}$  remains 100% up to Rh concentrations of  $x = 0.36$  and drops to 0% at  $x_{crit} = 0.375$ . With increasing Rh concentration, the Kubo-Toyabe minimum moves to increasing times as can be seen in Fig. 2(b), consistent with a decreasing ordered moment. This suggests that the suppression of magnetic order in  $\text{Ni}_{1-x}\text{Rh}_x$  occurs via a continuous second-order

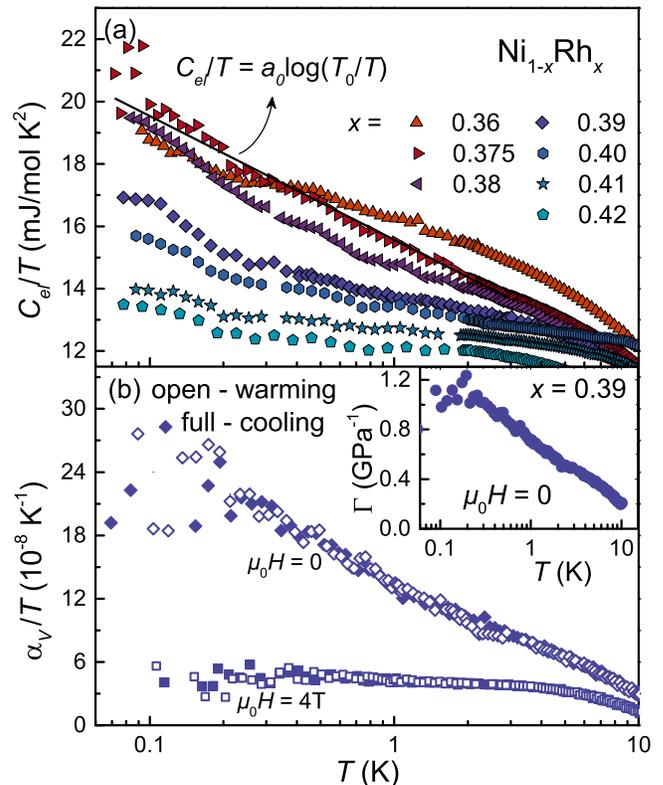


FIG. 3. (a) Temperature dependence of the electronic specific heat  $C_{el}/T$  for  $\text{Ni}_{1-x}\text{Rh}_x$  with  $x = 0.36 - 0.42$ . The solid line represents a fit to  $C_{el}/T = a_0 \log(T_0/T)$  at  $x_{crit} = 0.375$ . (b) The volume thermal expansion coefficient  $\alpha_V/T$  at  $\mu_0 H = 0$  (diamonds) and 4 T (squares) for  $\text{Ni}_{1-x}\text{Rh}_x$  with  $x = 0.39$ . The inset shows the Grüneisen ratio  $\Gamma$  vs.  $T$  at  $\mu_0 H = 0$ .

process.

Next we show evidence for divergent thermodynamic parameters in  $\text{Ni}_{1-x}\text{Rh}_x$ . Figure 3(a) shows the electronic specific heat  $C_{el}/T$  around  $x_{crit} = 0.375$ , where the phonon contribution has been subtracted from the measured specific heat. For concentrations that are both far above and far below  $x_{crit}$  ( $x \leq 0.15$  and  $x \geq 0.6$ ),  $C_{el}/T$  is nearly temperature-independent at low temperatures, as expected for a Fermi liquid (FL) [27]. Close to  $x_{crit}$ ,  $C_{el}/T$  diverges logarithmically on cooling. The fastest divergence occurs at  $x_{crit} = 0.375$ , where  $C_{el}/T = a_0 \log(T_0/T)$  between 0.1 and 3 K (solid line in Fig. 3(a)), such that  $a_0$  is maximum at the QCP (red diamonds in Fig. 4). This logarithmic divergence was previously reported in  $\text{Ni}_{0.62}\text{Rh}_{0.38}$  [39] and has also been observed in other QCP systems [9–11, 40]. For  $x > x_{crit}$ ,  $C_{el}/T$  levels off at the lowest temperatures, consistent with non-Fermi-liquid (NFL) to FL crossover. This is similar to other FM and antiferromagnetic quantum critical systems [1, 3–5].

QCPs are characterized by an accumulation of magnetic entropy  $S_{mag}$  as a function of the control parameter at low, but finite temperatures. In  $\text{Ni}_{1-x}\text{Rh}_x$ , this is underscored by the dependence of the specific heat pa-

parameter  $a_0$  on  $x$  (red diamonds in Fig. 4), given that  $S_{mag}$  is commensurate to  $a_0$ , which, in turn, is maximum at the QCP. At the same time,  $S_{mag}$  is related to the volume thermal expansion  $\alpha_V$  through the Maxwell relation  $\alpha_V = -V^{-1}\partial S_{mag}/\partial p$  (where  $p$  is pressure), and the divergence of  $\alpha_V/T$  has been taken as proof of the QCP in heavy fermion systems, such as  $\text{CeCu}_{6-x}\text{Au}_x$  [41],  $\text{CeNi}_2\text{Ge}_2$ , and  $\text{YbRh}_2(\text{Si}_{0.95}\text{Ge}_{0.05})_2$  [42]. Our data shows that at  $x = 0.39$  (just above the QCP), zero-field  $\alpha_V/T$  diverges logarithmically between 10 and 0.1 K (diamonds in Fig. 3(b)). This is indicative of NFL behavior in proximity to the QCP [43]. The data show no hysteresis between heating (open) and cooling (full) measurements, ruling out any history-dependent spin glass effects. The length measurements on  $\text{Ni}_{1-x}\text{Rh}_x$  with  $x = 0.39$  reached the resolution limit of the dilatometer of  $\Delta L \geq 10^{-3}$  Å at the lowest measured temperatures, resulting in an enhanced scattering below  $\sim 0.2$  K. The application of a magnetic field of 4 T reduces  $\alpha_V/T$  to a nearly constant value below 4 K, indicating a recovery of the FL behavior (squares in Fig. 3(b)). This recovery of FL behavior is consistent with what has been observed in field-dependent specific heat measurements for  $\text{Ni}_{0.62}\text{Rh}_{0.38}$  [39].

An additional probe for a QCP is the Grüneisen ratio  $\Gamma = \alpha_V/C_{el} \sim 1/E^* \cdot \partial E^*/\partial p$ .  $\Gamma$  reveals the hydrostatic pressure dependence of the dominating, characteristic energy scale  $E^*$  (e.g., the energy related to the conduction band splitting at the Fermi energy, which is proportional to the spontaneous magnetization [44]). At a QCP,  $E^*$  vanishes, and  $\Gamma$  is expected to diverge with decreasing  $T$  [43]. In the low temperature range for the  $\alpha_V$  measurements, the phonon contribution is negligible. The calculated  $\Gamma$  is depicted in the inset of Fig. 3(b), showing logarithmic divergence over two decades in temperature from  $T = 10$  K to 0.1 K. **The fact that  $\Gamma \sim -\log T$  suggests either that the quantum critical behavior in  $\text{Ni}_{1-x}\text{Rh}_x$  extends to a finite pressure interval (rather than a point) [43], or that the system lies within a disordered quantum Griffiths phase [45].**

We summarize the  $T_C - x$  phase diagram of  $\text{Ni}_{1-x}\text{Rh}_x$  in Fig. 4. Magnetization  $M(T, H)$  and  $\mu\text{SR}$  measurements reveal the suppression of  $T_C$  with increasing Rh concentration up to  $x_{crit} = 0.375$  (black symbols). The magnetically-ordered volume fraction remains 100% up to  $x_{crit}$ , while the magnitude of the ordered moment per formula unit continuously decreases, as expected for a second order transition [19]. In addition, the FM QCP is also revealed by the divergence of  $C_{el}/T$ ,  $\alpha_V/T$ , and  $\Gamma$  in the low temperature limit, associated with NFL behavior that extends up to  $\sim 10$  K.

Finally, we compare our results with other  $\text{Ni}_{1-y}\text{M}_y$  ( $M = \text{Al, Si, V, Cr, Mn, Cu, Zn, Pd, and Sb}$ ) alloys. Non-magnetic  $M$  metals dilute the Ni magnetic moment and therefore suppress the FM order. Magnetic susceptibility measurements on these alloys are sensitive to sample

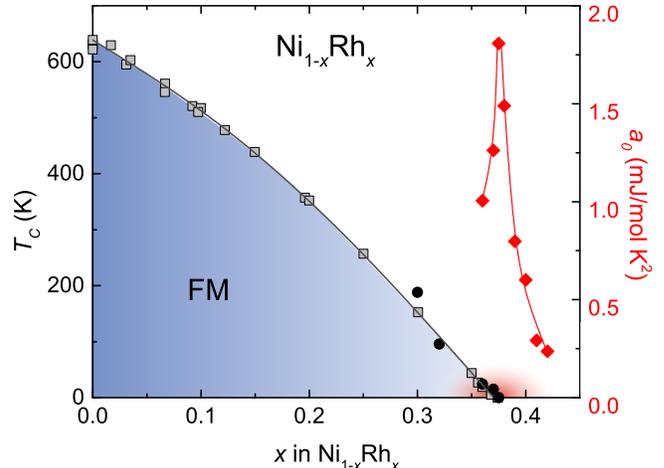


FIG. 4.  $T_C - x$  phase diagram of  $\text{Ni}_{1-x}\text{Rh}_x$ . The blue region corresponds to long-range FM order. The red area marks the NFL behavior around the QCP. Black circles:  $T_C$  and red diamonds: the coefficient  $a_0$  from the specific heat data (from current study). Gray squares: from Refs. [36, 46–49].

preparation [36, 50]. In the absence of a spin glass state or short range order, the enhancement of  $C_{el}/T$  has been observed for all  $M$  where  $T_C \rightarrow 0$  [50–52]. This commonality can be understood in terms of enhanced spin fluctuations and does not necessarily indicate quantum Griffiths effect that competes with critical behavior without reaching a QCP [53, 54]. By contrast,  $\text{Ni}_{1-x}\text{Rh}_x$  is the first member of the  $\text{Ni}_{1-y}\text{M}_y$  family where divergent  $\alpha_V/T$  and  $C_{el}/T$  result in divergent  $\Gamma$  [43], demonstrating the presence of a FM QCP. In fact, for most ferromagnets, when a dilution occurs in the magnetic sublattice, short-range order or spin glass behavior is observed [5]. The only exception is the  $5f$ -electron system  $\text{Th}_{1-x}\text{U}_x\text{Cu}_2\text{Si}_2$  that the FM transition remains continuous at the critical concentration, where NFL behavior is observed [55].

One plausible scenario to account for the FM QCP in  $\text{Ni}_{1-x}\text{Rh}_x$  is the aforementioned BKV theory [6, 16, 17]. The current study utilized polycrystalline samples and the residual resistivity ratio (not shown), which is often taken as a gauge of the amount of disorder, is small and comparable among the whole series of  $\text{Ni}_{1-x}\text{Rh}_x$ . To test if the FM quantum criticality in  $\text{Ni}_{1-x}\text{Rh}_x$  fulfills the universality class in the strong disorder regime of the BKV theory, the growth of single crystals is imperative and is the subject of an ongoing study.  $\text{Ni}_{1-x}\text{Rh}_x$  shows the first occurrence of a FM QCP with dilution of the  $d$ -electron magnetic sublattice. This is in contrast with chemical substitution on the non-magnetic sublattice in other FM QCP systems [9, 10, 18–21]. In particular, due

to its chemical simplicity,  $\text{Ni}_{1-x}\text{Rh}_x$  is an ideal platform for future studies and our work establishes a new approach to explore FM quantum criticality.

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