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A linear magneto-electric phase in ultrathin MnPS_3 probed by optical second harmonic generation

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The transition metal thiophosphates MPS_3 ($M = \text{Mn, Fe, Ni}$) are a class of van der Waals stacked insulating antiferromagnets that can be exfoliated down to the ultrathin limit. MnPS_3 is particularly interesting because its Néel ordered state breaks both spatial-inversion and time-reversal symmetries, allowing for a linear magneto-electric phase that is rare among van der Waals materials. However, it is unknown whether this unique magnetic structure of bulk MnPS_3 remains stable in the ultrathin limit. Using optical second harmonic generation rotational anisotropy, we show that long-range linear magneto-electric type Néel order in MnPS_3 persists down to at least 5.3 nm thickness. However an unusual mirror symmetry breaking develops in ultrathin samples on SiO_2 substrates that is absent in bulk materials, which is likely related to substrate induced strain.

Thin film materials that exhibit the magneto-electric (ME) effect - a coupling between magnetic (electric) polarization and external electric (magnetic) fields - have potentially broad applications in spintronics, sensing and energy harvesting technologies [1, 2]. Although ME effects in single-phase bulk crystals have been continuously pursued since their discovery in Cr_2O_3 in 1960 [3, 4], advances in thin film deposition techniques over the past two decades have opened new pathways to stabilize and to control high quality materials with large ME coupling strengths via epitaxial strain and heterostructure engineering, allowing the possibility of integration into functional nanoscale devices. At present, searching for both single-phase and composite thin film materials with stronger ME coupling, and developing methods to scale them down to the ultrathin few-unit-cell limit, remain active areas of research.

The recent discoveries of long-range magnetic ordering in exfoliated van der Waals (vdW) semiconductors [5–8] potentially offer a new route to realizing ME materials in the ultrathin limit. The simplest type of ME effect, which involves a linear coupling between the external field and induced polarization, is allowed in materials that lack both spatial-inversion and time-reversal symmetries. As most of the naturally occurring vdW crystals are structurally centrosymmetric, a convenient strategy is to rely on the magnetic ordering itself to break inversion symmetry. This suggests that one should focus on antiferromagnetic (AFM) rather than ferromagnetic (FM) materials because the latter generally do not break

the inversion symmetry of the underlying lattice. It was recently reported that upon exfoliating CrI_3 down to a single bilayer, its magnetic order transforms from being FM to AFM, breaking inversion symmetry and turning on a linear ME coupling in the process [5, 9–11]. However, so far there are no reports of an ultrathin material that directly inherits linear ME properties from its bulk precursor.

The transition metal thiophosphates MPS_3 ($M = \text{Mn, Fe, Ni}$) present an interesting family of AFM vdW materials for such a study [12–15]. While the AFM orders in FePS_3 and NiPS_3 preserve inversion symmetry [16, 17], neutron diffraction studies have shown that the AFM order in bulk MnPS_3 breaks inversion symmetry and allows a linear ME effect [18]. However, it is not clear if the linear ME-type AFM order persists down to the ultrathin limit. Because such order does not exhibit any net magnetization, a magneto-optical Kerr rotation experiment is not applicable. Although Raman spectroscopy has detected phonon anomalies in ultrathin MnPS_3 that are potentially associated with AFM ordering [20], and spin transport measurements have shown evidence of persistent magnons in few layer MnPS_3 devices [21], a technique that directly probes the AFM structure in nanoscopic exfoliated samples is still urgently anticipated. Leveraging the sensitivity of optical second harmonic generation (SHG) to AFM order [22], we demonstrate here that SHG rotational anisotropy (RA) can directly couple to the AFM order parameter in MnPS_3 nanoflakes, and use it to show that the linear ME-type AFM order found in bulk MnPS_3 persists down to the ultrathin limit.

Bulk MnPS_3 crystallizes in a monoclinic structure with centrosymmetric $2/m$ point group symmetry [18]. It has

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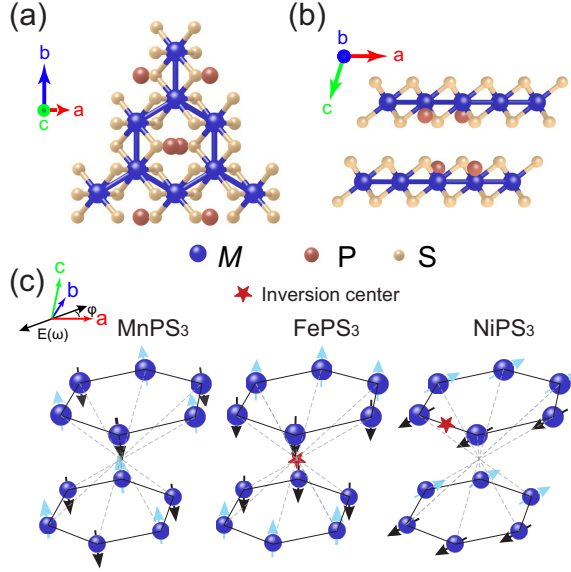


FIG. 1. Crystal and magnetic structure of MPS_3 . MPS_3 lattice viewed along the (a) c - and (b) b -axis. Adjacent ab planes are displaced by $a/3$ along the \hat{a} direction. (c) AFM structures of MPS_3 . Arrows denote spin orientation. Star denotes an inversion center of the AFM structure. The inset shows the in-plane orientation of the incident electric field.

a 2-fold rotation axis along the crystallographic b -axis and a mirror plane perpendicular to \hat{b} [Fig. 1(a) & (b)]. The Mn atoms are octahedrally coordinated by S atoms and form a honeycomb lattice in the ab plane, but the in-plane 6-fold rotational symmetry of the honeycomb lattice is absent in the bulk crystal due to the displacement of adjacent layers along \hat{a} . Despite the similar lattice structures of $MnPS_3$, $FePS_3$ and $NiPS_3$ [Fig. 1(c)], $MnPS_3$ hosts an inversion broken Néel-type AFM order [18] whereas $FePS_3$ and $NiPS_3$ exhibit inversion symmetric zigzag-type AFM order [16, 17]. The Néel-type AFM order preserves the size of the unit cell and exhibits no net moment, therefore it is challenging to detect via Raman spectroscopy and magneto-optical Kerr rotation respectively. However, because it breaks inversion symmetry, it should exhibit a finite second-order electric-dipole (ED) susceptibility that is responsible for SHG [19]. Therefore, we expect to see a finite SHG yield below the AFM ordering temperature T_{AF} from $MnPS_3$ and but not $FePS_3$ and $NiPS_3$.

The SHG-RA experiments were performed with a Ti:Sapph oscillator delivering laser pulses with a photon energy of $\hbar\omega = 1.5$ eV, a pulse width of 80 fs, and a repetition rate of 80 MHz. The SHG photons produced at 3 eV are resonant with the band gap of $MnPS_3$ [23]. A $5\times(50\times)$ microscope objective was used to focus light onto the bulk (exfoliated) samples at normal incidence with a spot size of approximately $30\ \mu\text{m}$ ($2\ \mu\text{m}$), and the intensity of the reflected SHG beam was measured using a photomultiplier tube. The pulse energy of the incoming beam was kept below 50 pJ. The SHG-RA patterns

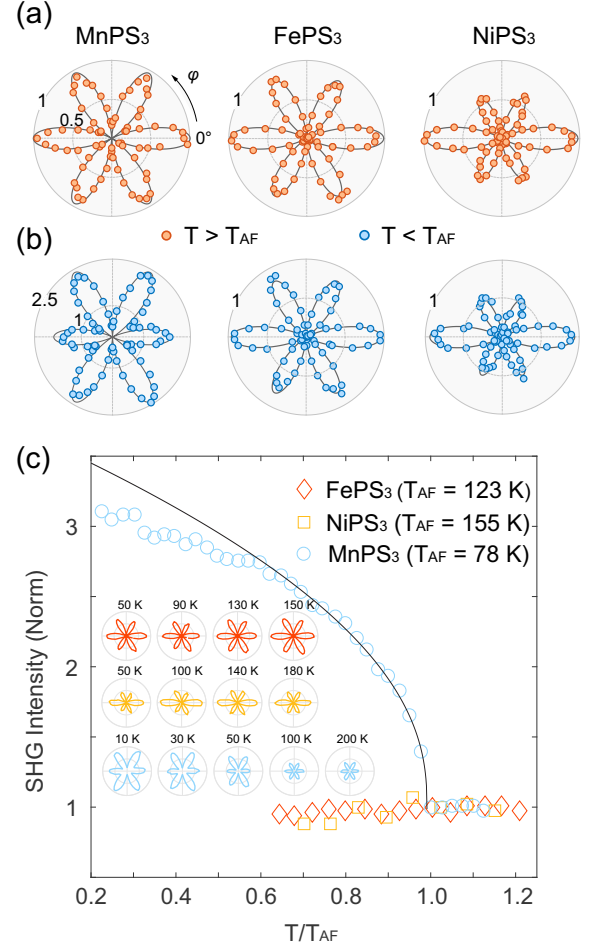


FIG. 2. SHG-RA patterns and long-range Néel order in $MnPS_3$. (a) SHG-RA patterns of MPS_3 above and (b) below their respective AFM ordering temperatures: $T_{AF} = 78$ K ($MnPS_3$), 123 K ($FePS_3$) and 155 K ($NiPS_3$). Filled circles are experimental data and the solid lines are best fits to the phenomenological model described in the main text. For $T > T_{AF}$, all data were fit using only an EQ term. For $T < T_{AF}$, the $FePS_3$ and $NiPS_3$ data were fit using only an EQ term, whereas the $MnPS_3$ data were fit using a coherent sum of an EQ and ED term. (c) Temperature dependence of the SHG intensity along the $\phi = 60^\circ$ direction. Solid line on the $MnPS_3$ data is a best fit to the power law function described in the main text, which accounts for a constant EQ term and a temperature dependent ED term.

were acquired by rotating the linear polarization of the incoming and outgoing beams (parameterized by the angle ϕ), which were maintained parallel to each other, in the ab -plane [Fig. 1(c)]. Bulk MPS_3 single crystals were grown by a self-flux method described elsewhere [24].

Despite having a centrosymmetric crystallographic point group, we observe weak but finite SHG-RA signals from all three bulk crystals even above T_{AF} [Fig. 2(a)]. This may arise from surface ED SHG or higher-rank bulk SHG processes such as electric-quadrupole (EQ) SHG [19], both of which are generally allowed in centrosym-

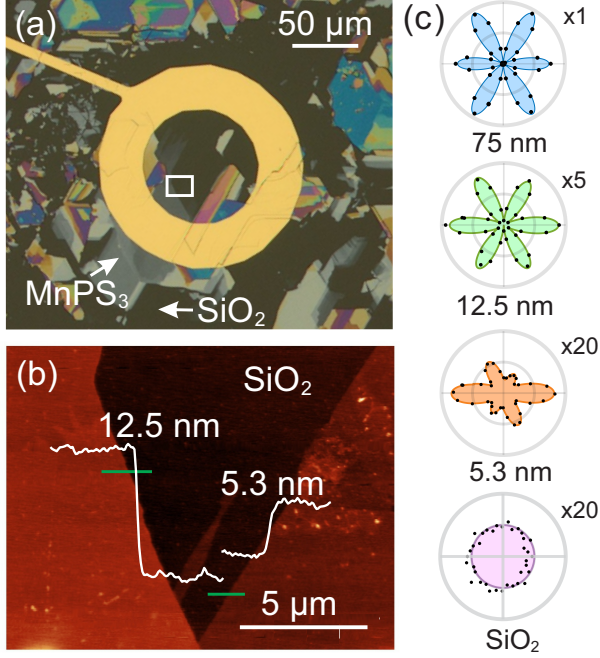


FIG. 3. MnPS₃ nanodevice for probing long-range Néel order. (a) Optical image of exfoliated MnPS₃ flakes on SiO₂ with gold ring and electrode on top to improve cooling efficiency. The 5.3 nm and 12.5 nm flakes are found within the white box. (b) Atomic force microscopy scan of the area bounded by the white box in (a). Green lines indicate the positions of line scans, with corresponding magnified line profiles shown in white. (c) SHG-RA patterns from various regions of the device at 10 K.

metric materials and were found to fit the data equally well [Fig. 2(a)] [25]. For simplicity, we therefore only consider the bulk EQ term in our later fitting. The loss of 6-fold rotational symmetry that arises from the stacking offset between adjacent honeycomb layers is apparent in the data, although the degree of departure from 6-fold symmetry varies across samples as well as across spots within a single sample. We speculate that this may be due to spatial variations in the strength of inter-layer coupling and/or variations in the concentration of 120° twins or stacking faults [26].

Below T_{AF} we observe no changes in the SHG intensity from both FePS₃ and NiPS₃, but an increase in the SHG intensity from MnPS₃ as anticipated. As shown in Fig. 2(b), the low temperature SHG-RA patterns from MnPS₃ can be well fit using the coherent sum of a non-magnetic EQ contribution and an AFM order induced time-noninvariant ED contribution described by the equation [25]:

$$P_i^{2\omega} = \chi_{ijkl}^{EQ} E_j^\omega \nabla_k E_l^\omega + \chi_{ijk}^{ED}(T) E_j^\omega E_k^\omega \quad (1)$$

where $P^{2\omega}$ is the induced electric polarization at the SHG frequency, E^ω is the magnitude of the incident electric field, χ_{ijkl}^{EQ} is the temperature independent EQ susceptibility from a $2/m$ crystallographic point group, and

$\chi_{ijk}^{ED}(T)$ is a temperature dependent ED susceptibility from the $2'/m$ magnetic point group describing the Néel phase [18]. As shown in Fig. 2(c), the SHG intensity from MnPS₃ shows an order parameter-like increase below T_{AF} . Since $\chi_{ijk}^{ED}(T)$ is directly proportional to the inversion broken Néel order parameter, we can extract the critical exponent of the order parameter (β) by fitting the temperature dependent SHG intensity to the phenomenological function $I^{2\omega} \propto [a + b(T_{AF} - T)^\beta]^2$, where a is fixed by the intensity of the EQ contribution above T_{AF} and both b and β are free parameters. Best fits to the region $60 \text{ K} \leq T \leq T_{AF}$ yield $\beta = 0.37(8)$ [Fig. 2(c)], which is close to the numerical calculation of ~ 0.369 for the 3D Heisenberg model [27].

To investigate whether the long-range Néel order in MnPS₃ survives in the ultrathin limit, we exfoliated bulk crystals onto an amorphous SiO₂ substrate in a nitrogen purged glove box. The choice of pure SiO₂ over SiO₂/Si as a substrate was made to reduce laser induced heating arising from optical absorption by Si at 800 nm and 400 nm. In contrast, SiO₂ is transparent to both 800 nm and 400 nm light. Due to the poor thermal conductivity of SiO₂ and the relatively high laser power needed for our SHG-RA measurements on MnPS₃ compared to other optical techniques for studying vdW magnets such as magneto-optical Kerr microscopy or Raman spectroscopy, we face more stringent sample cooling demands [25]. To increase cooling efficiency, we deposited gold rings around the MnPS₃ flakes, which are thermally anchored to the cryostat sample holder by gold electrodes. Fig. 3(a) shows an optical image of a typical device. Using atomic force microscopy, we identified ultrathin MnPS₃ nanoflakes with 5.3 nm and 12.5 nm step sizes above the substrate on this device [Fig. 3(b)]. Based on previously published atomic force microscopy data on MnPS₃ [24], these correspond to 7 and 16 single layers of MnPS₃ respectively. Figure 3(c) shows typical SHG-RA patterns obtained from these flakes at a temperature of 10 K, compared with both thicker (75 nm) flakes and the bare substrate. We find that the overall SHG intensity approximately scales with the sample thickness, consistent with a bulk dominated SHG signal. The SiO₂ substrate contributes an isotropic background and is thus easily distinguished from the MnPS₃ signal.

As shown in Fig. 2(c), the ED SHG signal from MnPS₃ below T_{AF} is of comparable magnitude to the high temperature EQ signal and is thus relatively weak overall. This is likely related to our incident 1.5 eV photon energy being well below the band gap ($\sim 3 \text{ eV}$) of MnPS₃. Consequently, when we attempted to protect the MnPS₃ flakes by encapsulation with a hexagonal boron nitride (hBN) thin flake, we found that the SHG signal was dominated by the hBN. Therefore we had to work with exposed MnPS₃ flakes, which are more prone to degradation. At cryogenic temperatures, we found that the SHG intensity from the few-layer regions starts to decrease over a time scale of several hours. This is likely due to surface adsorption of gas molecules and/or chem-

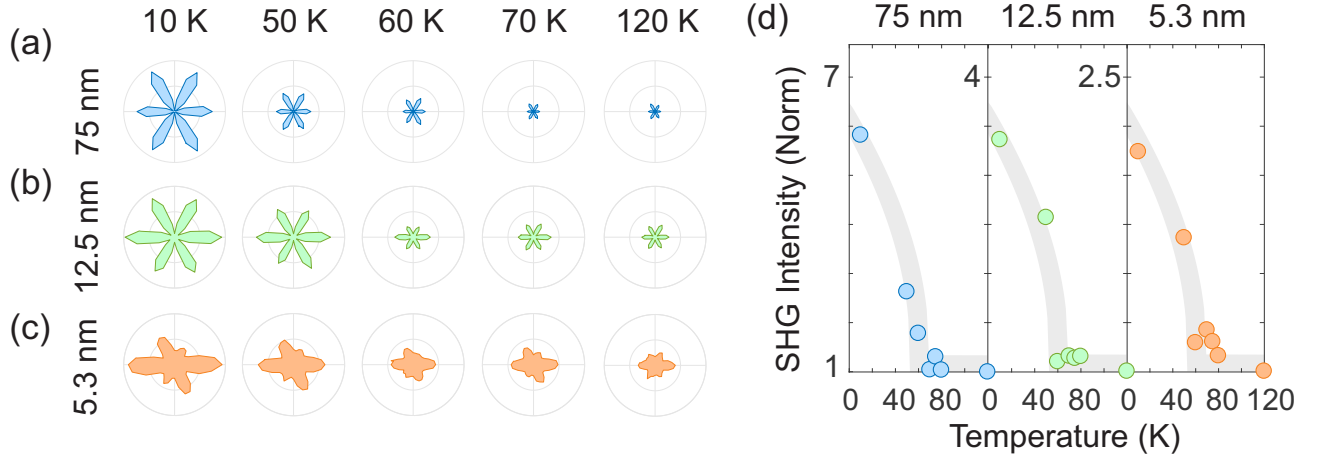


FIG. 4. Long-range Néel order in few-layer MnPS₃. (a)-(c) Temperature dependent SHG-RA patterns from MnPS₃ flakes of different thicknesses. (d) Normalized temperature dependence of SHG Intensity along the $\phi = 0^\circ$ direction.

ical reaction processes activated by laser exposure, as is observed in CrI₃ nanoflakes [28]. Therefore we were only able to acquire a limited number of SHG-RA scans at low temperatures before the onset of sample degradation. Nevertheless, our data clearly show an order parameter-like increase in the SHG intensity from the MnPS₃ nanoflakes below a temperature close to the bulk T_{AF} value (Fig. 4), which again saturates at only several times the high temperature value. This indicates that the linear ME-type Néel ordering observed in bulk crystals persists at least down to 7 layer thick samples. Measurements collected from 3 layer samples also show a markedly higher SHG intensity at 10 K compared to 100 K [25], but their faster degradation prevented a full temperature dependence measurement from being taken.

Given that the low temperature SHG signal from MnPS₃ involves the interference between a time-noninvariant ED response and a time-invariant EQ response, the existence of two different 180° AFM domains related by time-reversal should produce different SHG intensities, analogous to what has previously been observed in Cr₂O₃ [29]. Assuming that the roughly 2-fold SHG intensity increase in our 5.3 nm flakes at low temperature [Fig. 4(d)] arises from a pure + domain where the ED and EQ contributions interfere constructively, the ratio of the ED to EQ SHG electric fields should be roughly $\frac{1}{2}$. By extension, the SHG intensity from a - domain is expected to be $\sim 25\%$ of the high temperature value, or $(1 + \frac{1}{2})^2 / (1 - \frac{1}{2})^2 = 9$ times lower in intensity compared to the + domain. By raster scanning our beam of spot size $\sim 2 \mu\text{m}$ over the roughly $4 \mu\text{m} \times 4 \mu\text{m}$ area of our 5.3 nm MnPS₃ flake at 10 K, we found the SHG intensity varies by only approximately $\pm 30\%$ about the mean intensity. These small variations may be due to sample inhomogeneity and/or slight changes in alignment and are inconsistent with 180° domains. Therefore we believe our flake to be a single AFM domain, which is comparable to the FM domain sizes observed in ultrathin vdW

materials like CrI₃ [5] and Cr₂Ge₂Te₆ [6].

We note that the low temperature SHG-RA patterns from the ultrathin 5.3 nm flakes exhibit an unusual symmetry. In particular, the *ac* mirror plane (reflection about the horizontal line in the SHG-RA patterns) that is preserved by both the $2/m$ and $2'/m$ point groups is absent [Fig. 3(c)]. This mirror symmetry breaking only becomes apparent as the material thickness is reduced and as the temperature is lowered below T_{AF} [Fig. 4(c)]. We believe that this is related to a substrate induced strain because for ultrathin MnPS₃ flakes that are exfoliated onto SiO₂/Si substrates, which are much smoother than pure SiO₂ substrates, there is no clear evidence of *ac* mirror breaking in the low temperature SHG-RA patterns [25]. Model Hamiltonian calculations [30] show that a spiral spin texture that breaks *ac* mirror symmetry is favored over the collinear Néel order only if the second nearest-neighbor Dzyaloshinskii-Moriya interaction D_2 is comparable to the nearest-neighbor exchange J_1 in MnPS₃, which is around 1.5 meV according to inelastic neutron diffraction experiments [31]. However spin Hall based measurements of D_2 in MnPS₃ put its value at merely 0.3 meV [32]. Since it is unlikely that D_2 is several times larger in ultrathin flakes compared to bulk crystals, especially given that Raman spectroscopy studies show no drastic changes in T_{AF} or the phonon spectrum as a function of thickness [20], we rule out a non-collinear spin texture as the cause for *ac* mirror breaking. Instead, it is possible that the substrate induced strain tilts the easy-axis, causing the Néel ordered moments to rigidly cant out of the *ac* plane. Further structural and magnetic characterization of thin MnPS₃ flakes will be necessary to confirm this hypothesis.

In conclusion, we have demonstrated SHG-RA to be a direct and effective probe of inversion breaking AFM order parameters in exfoliated vdW materials. A linear ME-type Néel order that features in bulk crystals of MnPS₃ was found to survive down to the few layer limit.

Future quantitative measurements of the ME coupling strength in ultrathin MnPS_3 samples will help to assess its potential for applications in nanoscale spintronics and optoelectronics devices.

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