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## Large Collective Lamb Shift of Two Distant Superconducting Artificial Atoms

P. Y. Wen, K.-T. Lin, A. F. Kockum, B. Suri, H. Ian, J. C. Chen, S. Y. Mao, C. C. Chiu, P. Delsing, F. Nori, G.-D. Lin, and I.-C. Hoi

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## Large collective Lamb shift of two distant superconducting artificial atoms

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P. Y. Wen, <sup>1, 2, *</sup> K.-T. Lin, <sup>3, *</sup> A. F. Kockum, <sup>4, 5, *</sup> B. Suri, <sup>6, 4</sup> H. Ian, <sup>7, 8</sup> J. C. Chen, <sup>1, 2</sup>
                S. Y. Mao, 9 C. C. Chiu, 10 P. Delsing, 4 F. Nori, 5, 11 G.-D. Lin, 3 and I.-C. Hoi<sup>1,2,†</sup>
                     <sup>1</sup>Department of Physics, National Tsing Hua University, Hsinchu 30013, Taiwan
               <sup>2</sup>Center for Quantum Technology, National Tsing Hua University, Hsinchu 30013, Taiwan
                   <sup>3</sup>CQSE, Department of Physics, National Taiwan University, Taipei 10617, Taiwan
                                      <sup>4</sup>Department of Microtechnology and Nanoscience,
                              Chalmers University of Technology, 412 96 Gothenburg, Sweden
<sup>5</sup> Theoretical Quantum Physics Laboratory, RIKEN Cluster for Pioneering Research, Wako-shi, Saitama 351-0198, Japan
                                    <sup>6</sup>Department of Instrumentation and Applied Physics,
                                    Indian Institute of Science, Bengaluru 560012, India
                  <sup>7</sup>Institute of Applied Physics and Materials Engineering, University of Macau, Macau
                              <sup>8</sup> UMacau Zhuhai Research Institute, Zhuhai, Guangdong, China
           <sup>9</sup>Institute of Electro-Optical Engineering, National Chiao Tung University, Hsinchu 30013, Taiwan
             <sup>10</sup>Department of Electrical Engineering, National Tsing Hua University, Hsinchu 30013, Taiwan
               <sup>11</sup>Physics Department, The University of Michigan, Ann Arbor, Michigan 48109-1040, USA
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Virtual photons can mediate interaction between atoms, resulting in an energy shift known as a collective Lamb shift. Observing the collective Lamb shift is challenging, since it can be obscured by radiative decay and direct atom-atom interactions. Here, we place two superconducting qubits in a transmission line terminated by a mirror, which suppresses decay. We measure a collective Lamb shift reaching 0.8% of the qubit transition frequency and twice the transition linewidth. We also show that the qubits can interact via the transmission line even if one of them does not decay into it

Introduction. In 1947, when attempting to pinpoint the fine structure of the hydrogen atom, Lamb and Retherford [1] discovered a small energy difference between the levels  $2S_{1/2}$  and  $2P_{1/2}$ , which were thought to be degenerate according to Dirac's theory of electrons. This energy difference between the two levels can be understood when vacuum fluctuations are included in the picture, as was verified later by self-energy calculations in the framework of quantum field theory [2–4]. Briefly put, a hydrogen atom will emit photons which are instantaneously reabsorbed; while these "virtual" photons are not detectable by themselves, they leave their traces in the Lamb shift.

The hydrogen atoms that Lamb and Retherford used were obtained from a process with a very low conversion rate, so the  $2S_{1/2}$  level was only populated in a few atoms. Hence, the observable effects of virtual photon processes were limited to self-interaction; exchanges of virtual photons between atoms could not be detected. However, it was later realized that atom-atom interaction mediated by virtual photons also gives rise to an energy shift, referred to as a collective, or cooperative, Lamb shift (CLS) [5–9]. The atom-atom interaction also underpins the collective decay known as Dicke superradiance [10, 11].

There are several obstacles impeding the experimental observation of the CLS. The shift can be enhanced by using many atoms, but, if these atoms are too close together, direct atom-atom interactions (not via virtual photons) can obscure the effect. Furthermore, the interaction giving rise to the CLS is relatively weak in

three dimensions, and the shift can also be hidden by the radiative linewidth (e.g., due to the collective decay). Despite these obstacles, there have been a few experimental demonstrations of CLSs: in xenon gas [12], iron nuclei [13], rubidium vapor [14], strontium ions [15], cold rubidium atoms [16], and potassium vapor [17]. Mostly, these experiments used developments in atomic trapping and cooling [18] that have enabled higher densities of atomic ensembles, leading to a strong coupling between atomic condensates and cavity fields [19, 20]. An improved theoretical understanding [21–23] of collective Dicke states also aided some of the experiments.

With the single exception of Ref. [15], these previous experiments all required a large number of atoms to demonstrate a CLS. The experiment of Ref. [15] only used two atoms, but the measured shift was small, 0.2% of the transition linewidth. In this Letter, we demonstrate a large CLS for two artificial atoms that exceeds the transition linewidth by a factor 2 and reaches 0.8% of the atomic transition frequency.

Our experimental setup, depicted in Fig. 1, is a superconducting quantum circuit [24, 25] with two transmon qubits [26] coupled to a one-dimensional (1D) waveguide. In such superconducting circuits, strong [25, 27, 28], and even ultrastrong [29–31], coupling can be engineered between the qubits and photons in the waveguide. Compared to three-dimensional setups, the 1D version strengthens the interaction between qubits and reduces the decay into unwanted modes. These features have enabled many important quantum-optical experiments in 1D waveguide QED in superconducting circuits in the

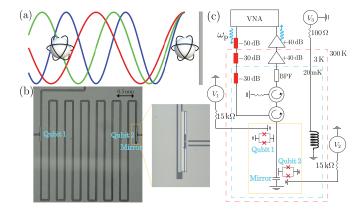


Figure 1. Experimental setup. (a) A conceptual sketch of the setup. Two atoms are placed in front of a mirror and interact via virtual photons of different frequencies. (b) A photo of the device. Qubit 1 is placed  $L \simeq 33 \,\mathrm{mm}$  from Qubit 2 (zoom-in on the right; the two bright parts form the qubit capacitance and the gap between them is bridged by two Josephson junctions forming a SQUID loop), which sits at the end of the transmission line (TL), i.e., at the mirror. The characteristic impedance of the TL is  $Z_0 \simeq 50 \Omega$ . The relatively long distance L makes it easier to tune Qubit 1 between nodes and anti-nodes of the electromagnetic (EM) field in the TL by tuning the qubit transition frequency. This tuning can be used to calibrate the velocity v of the EM field in the TL [72]. (c) Signal routing for the experiment. Each qubit frequency can be tuned by local magnetic fields via local voltage biases  $(V_1,$  $V_2$ ) and both frequencies can be tuned by a global magnetic field via  $V_3$ . For measurements, a coherent signal at frequency  $\omega_{\rm p}$  is generated by a vector network analyzer (VNA) at room temperature and fed through attenuators (red squares) to the sample, which sits in a cryostat cooled to 20 mK. At this low temperature, the number of thermal photons is negligible and the thermal excitation of the qubits should be less than a few percent [73]. The reflected signal passes a bandpass filter (BPF) and amplifiers, and is then measured with the VNA.

past decade [25, 27–29, 32–47] and inspired a wealth of theoretical studies for this platform [25, 32, 48–71].

As shown in Fig. 1, the transmission line (TL) to which the qubits couple is terminated in a capacitive coupling to ground, which is equivalent to placing a mirror in a waveguide. The presence of this mirror separates our experiment from that of Ref. [36], where two superconducting qubits were coupled to an open TL. In such an open waveguide, the connection between collective decay and the CLS entails that the shift always will be smaller than the linewidth [59], and the measurements of elastic scattering in Ref. [36] could thus not resolve the CLS. Although a splitting in the fluorescence spectrum (inelastic scattering) indicated the presence of the CLS, it is not straightforward to extract the size of the shift from the size of the splitting [36, 59]. In our setup, the presence of the mirror introduces interference effects that suppresses the collective decay more than the CLS [71, 72, 74], allowing us to clearly resolve the shift in simple reflection measurements of elastic scattering. Interestingly, it turns

out that these interference effects allow us to couple the two qubits via the TL even when one of the qubits is unable to relax into the TL.

Device and characterization. In our device, the interqubit separation L is fixed. However, we can vary the qubit transition frequencies  $\omega_{10}$  by applying a local magnetic flux [see Fig. 1(c)] and thus change the effective distance  $L/\lambda$ , where the wavelength  $\lambda = 2\pi v/\omega_{10}$ and v is the propagation velocity of the electromagnetic (EM) field in the waveguide [38]. Since Qubit 2 is placed next to the mirror, it will always be at an antinode of the voltage field in the waveguide [see Fig. 2(b)]. Qubit 1, on the other hand, can be tuned to a voltage node. In this case, Qubit 1 will not couple to the waveguide at its transition frequency, and thus will not contribute to any decay [38, 71]. However, the CLS arises due to emission and absorption of virtual photons in all other modes of the continuum in the waveguide, which results in an interaction of strength  $\Delta$  between the qubits. This interaction (CLS) leads to an avoided level crossing between the two qubits, which shows up as a frequency splitting of  $2\Delta$  in reflection measurements of the system using a weak coherent probe at frequency  $\omega_{\rm p}$ .

We first characterize each of the two transmon qubits through spectroscopy. We detune the transition frequency of one of the qubits far away and measure the amplitude reflection coefficient |r| of a weak coherent probe tone (i.e., the probe Rabi frequency  $\Omega_{\rm p}$  is much smaller than the decoherence rate  $\gamma$  of the qubit) as a function of the flux controlling the other qubit's transition frequency and of the probe frequency  $\omega_{\rm p}$ . The results are shown in Fig. 2 (Qubit 1 in the left column and Qubit 2 in the right column). For Qubit 1, which is placed at a distance L from the mirror, the spectroscopy data in Fig. 2(c) shows a linewidth narrowing [compare the linecuts A and B from Fig. 2(c), plotted in Fig. 2(e)] and a disappearing response around 4.75 GHz. At this frequency, the effective distance between Qubit 1 and the mirror is  $L = 7\lambda/4$ , which places the qubit at a node for the EM field in the TL, as illustrated in Fig. 2(a), and thus effectively decouples the qubit from the TL, reducing its relaxation rate into the TL below the lowest quantity we can measure [38]  $[\Gamma/2\pi = 0.3 \,\mathrm{MHz}$  for A in Fig. 2(e)]. Qubit 2, on the other hand, is always at an antinode of the EM field in the TL [Fig. 2(b)] and thus has an equally strong response at all frequencies [Fig. 2(d), (f)].

We perform further spectroscopy in the full range 4–8 GHz, which is the bandwidth of the cryogenic lownoise amplifier in our experimental setup. The maximum qubit frequency is outside this bandwidth. These data are presented in the supplementary material [72]. From these measurements, we extract [37] the qubit relaxation rate  $\Gamma$  into the TL, the pure dephasing rate  $\gamma_{\phi}$  (which also contains contributions from relaxation to other channels), and the speed of light in the TL. We further use two-tone spectroscopy, driving at the qubit frequency  $\omega_{10}$ 

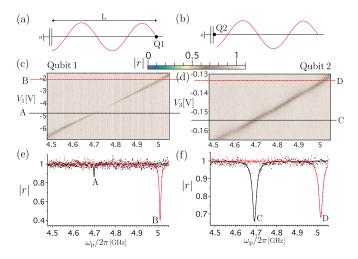


Figure 2. Single-tone spectroscopy of the individual qubits. (a), (b) Electromagnetic mode structure (red curve) in the TL seen by Qubit 1 (Q1) and Qubit 2 (Q2), respectively. (c), (d) Amplitude reflection coefficient |r| for a weak coherent probe as a function of probe frequency  $\omega_{\rm p}$  and qubit transition frequency (controlled by the voltages  $V_1$  and  $V_3$  for Qubit 1 and Qubit 2, respectively). Panel (c) shows how the response disappears when Qubit 1 ends up at a node for the EM field around 4.75 GHz. During these measurements, the frequency of the other qubit is tuned far from resonance with the probe. (e), (f) Linecuts from panels (c) and (d) as indicated. Dots are experimental data and solid curves are fits following Ref. [37]. The extracted parameters are given in Table S1 in the supplementary material [72]. The linewidth of the dip, which occurs at the resonance  $\omega_{\rm p} = \omega_{10}$ , is set by the qubit decoherence rate  $\gamma = \Gamma/2 + \gamma_{\phi}$ , where  $\Gamma$  is the relaxation rate and  $\gamma_{\phi}$  is the pure dephasing rate. Relaxation into other channels than the TL will affect the extracted value of  $\gamma_{\phi}$ . The depth of the dip is set by the ratio  $\Gamma/\gamma_{\phi}$ ; since  $\Gamma$  decreases close to the node of the field, the dip in linecut A is shallower than that

and probing around the transition frequency  $\omega_{21}$  from the first excited state to the second excited state, to determine the anharmonicity of the qubits. All extracted and derived parameters, for the qubits at antinodes, are summarized in Table I.

Collective Lamb shift. We now turn to experiments where both qubits are involved and the CLS is measured. We fix the transition frequency of Qubit 2 to  $\omega_{10}/2\pi = 4.75 \,\text{GHz}$ , the frequency at which Qubit 1 is at a node of the EM field [see Fig. 2(c)]. We then tune the frequency of Qubit 1 to values around this point and measure the reflection of a weak probe signal on the system for frequencies close to  $\omega_{10}$ . The results of these measurements are displayed in Fig. 3(a). We observe a clear anti-crossing between the vertical resonance, corresponding to Qubit 2, and the diagonal resonance, corresponding to Qubit 1. The observation of this anti-crossing indicates that the two qubits are coupled on resonance with strength  $\Delta$  through a coherent interaction, which must be mediated by the TL since the qubits are distant from

each other. The minimum size of the separation, shown in the lineaut in Fig. 3(c), is  $2\Delta \simeq 2\pi \times 38\,\mathrm{MHz}$ .

If the qubits were uncoupled, they would have eigenstates  $|00\rangle$ ,  $|01\rangle$ ,  $|10\rangle$ , and  $|11\rangle$ , with energies 0,  $\hbar\omega_{10}$ ,  $\hbar\omega_{10}$ , and  $2\hbar\omega_{10}$ , respectively. Here, 0 and 1 denote ground and excited states of a single qubit, respectively; the first number in the kets is for Qubit 1 and the second number is for Qubit 2. Due to the coupling, the eigenstates  $|01\rangle$  and  $|10\rangle$  are replaced by the symmetric and anti-symmetric eigenstates  $|s\rangle = \frac{1}{\sqrt{2}}(|01\rangle + |10\rangle)$  and  $|a\rangle = \frac{1}{\sqrt{2}}(|01\rangle - |10\rangle)$ , respectively, with eigenenergies  $\hbar(\omega_{10} \pm \Delta)$  [59]. When the coupling is due to virtual photons, as in our experiment, this thus gives a CLS of  $2\hbar\Delta$ , as illustrated in the inset in Fig. 3(c).

If the two qubits were placed in an open TL, it would not be possible to observe the CLS in this measurement, since each of the two resonances would have a linewidth set by a relaxation rate  $\Gamma=2\Delta$  [59]. This is not easily circumvented, since it is the coupling to the TL of the two qubits that determines both the relaxation into the TL and the strength of the interaction that is mediated via the TL. However, the presence of the mirror in our setup breaks this close connection between the linewidth and the CLS. In our setup, the CLS is given by [71, 72, 74]

$$2\Delta = \Gamma_0 \left\{ \sin \left[ \frac{\omega_{10}}{v} (x_1 + x_2) \right] + \sin \left[ \frac{\omega_{10}}{v} |x_1 - x_2| \right] \right\}, \tag{1}$$

where  $x_j$  denotes the distance of Qubit j from the mirror and  $\Gamma_0 = \sqrt{\Gamma_1(\omega_{10})\Gamma_2(\omega_{10})}$ , with  $\Gamma_j(\omega)$  the bare relaxation rate of Qubit j at frequency  $\omega$  into an open TL. This is calculated using the standard master-equation approach with the Born-Markov approximation and tracing out the photonic modes of the TL [72, 75]. When  $x_2 = 0$ and  $x_1$  corresponds to Qubit 1 being at a node of the field in the TL, as in Fig. 3, the CLS becomes  $2\Delta = 2\Gamma_0$ . However, since Qubit 1 is at a node, both the effective relaxation rate of Qubit 1 and the collective decay rate of the two qubits becomes zero. The only contribution from relaxation to the linewidths for the states  $|s\rangle$  and  $|a\rangle$  is half of  $2\Gamma_2$ , the effective relaxation rate of Qubit 2. In this experiment, we used  $\Gamma_1 \approx \Gamma_2$  (giving a shift  $2\Delta \approx 2\Gamma_2$ and a linewidth  $\gamma_c \approx \Gamma_2$ ), but we note that the CLS could be made many times larger than the linewidths by instead designing the qubits such that  $\Gamma_1 \gg \Gamma_2$ .

The fact that we can measure the CLS even though Qubit 1 ostensibly is decoupled from the TL confirms several predictions about how virtual photons influence relaxation and qubit-qubit interaction. The relaxation from Qubit 1 is stimulated by virtual photons in the TL at the transition frequency  $\omega_{10}$ . The relaxation is suppressed when Qubit 1 is placed at a node for the virtual photons at this frequency [38]. However, Qubit 1 is clearly coupled via virtual photons to Qubit 2. Thus, the virtual photons mediating this coupling, and causing the CLS, must have frequencies that are not equal to  $\omega_{10}$ .

Qubit	$E_C/h$ [MHz]	$\omega_{10}/2\pi \; [\mathrm{GHz}]$	$\Gamma/2\pi \; [\mathrm{MHz}]$	$\gamma_{\phi}/2\pi \; [\mathrm{MHz}]$	$\gamma/2\pi~[{ m MHz}]$	β	$v \ [10^8 \text{m/s}]$
Q1	$324 \pm 0.13$	(Antinode) $4.068 \pm 0.00005$	$27.18 \pm 0.24$	$2.15 \pm 0.2$	$15.74 \pm 0.08$	$0.285 \pm 0.001$	$0.8948 \pm 0.0131$
Q2	$406 \pm 0.65$	(Antinode) $4.746 \pm 0.00004$	$28.03 \pm 0.22$	$2.79 \pm 0.19$	$16.8 \pm 0.08$	$0.277 \pm 0.001$	

Table I. Extracted and derived qubit parameters. We extract  $\omega_{10}$ ,  $\Gamma$ , and  $\gamma$  from fitting the spectroscopic magnitude and phase data [37]. Note that the effective relaxation rate  $\Gamma$  at an antinode is twice what the relaxation rate would be in an open TL. The velocity v is extracted by finding multiple nodes of the field for Qubit 1 [72]. From the two-tone spectroscopy, we extract the anharmonicity, which approximately equals the charging energy  $E_C$  of the transmon qubits. We calculate  $\gamma_{\phi}$  from  $\Gamma$  and  $\gamma$ , and the ratio  $\beta = C_c/C_{\Sigma}$  between the coupling capacitance  $C_c$  to the TL and the qubit capacitance  $C_{\Sigma}$  from  $\Gamma$  and  $E_C$ .

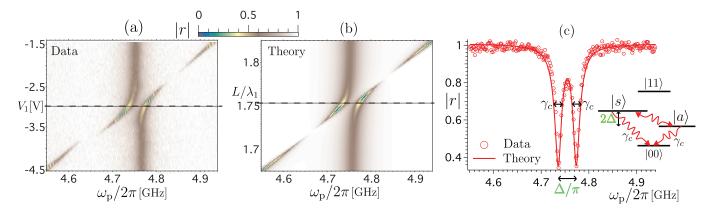


Figure 3. Collective Lamb shift. (a) The amplitude reflection coefficient for a weak probe as a function of the probe frequency  $\omega_{\rm p}$  and the transition frequency of Qubit 1 (controlled through  $V_1$ ). The frequency of Qubit 2 is fixed at  $\omega_{10}/2\pi=4.75\,{\rm GHz}$  and the frequency of Qubit 1 is tuned through resonance with this frequency. (b) Theory simulation [72] of the single-tone spectroscopy data in panel (a). The simulation is done with previously fitted parameters from Table I, with the exceptions of the free parameters  $\beta_1=0.323,\ \beta_2=0.306,\ {\rm and}\ \gamma_\phi/2\pi=2.3\,{\rm MHz}$  for Qubit 1, which all are close to the values in Table I. The agreement between the data in (a) and the simulation in (b) is excellent. We note that the extinction of the signal around  $\omega_{\rm p}/2\pi=4.65\,{\rm GHz}$  and  $\omega_{\rm p}/2\pi=4.85\,{\rm GHz}$  can be explained by an interplay between detuning and decoherence [72]. (c) A lineaut of the data and theory [dashed line in panels (a) and (b)], at the point where the two qubits are on resonance and the CLS  $2\Delta$  is most clearly visible. From this figure, we extract a CLS of  $2\Delta\simeq2\pi\times38\,{\rm MHz}$ . The inset shows the level structure of the eigenstates of the qubits that are coupled through the CLS. The two dips in the reflection correspond to the symmetric and anti-symmetric eigenstates  $|s\rangle$  and  $|a\rangle$ . Each of these two states have the same decay rate, giving a linewidth  $\gamma_c$  smaller than the CLS due to the presence of the mirror, as explained in the text.

In fact, the coupling is given by a sum over all virtual modes at frequencies separate from  $\omega_{10}$  [59].

Finally, we note that there are several processes, with real photons, where a strong drive shifts or dresses energy levels of qubits to create an effect that could look similar to what we have observed. To rule out such effects, e.g., the Mollow triplet [76] and Autler-Townes splitting [77], we measure  $\Delta$  as a function of the power P of the coherent probe. The results are shown in Fig. 4. Clearly, the energy shift  $\Delta$  is independent of P (before the power is high enough to saturate the qubits), indicating that the CLS we measure really is due to virtual photons.

Summary and outlook. In this Letter, we demonstrated a large collective Lamb shift with two distant superconducting qubits in front of an effective mirror in a 1D transmission-line waveguide. Using interference effects due to the mirror, we overcame previous limitations on the size of the shift compared to the linewidth, allowing us to observe a shift reaching 0.8% of the qubit transition frequency and exceeding the transition linewidth. We explained how future experiments could increase the

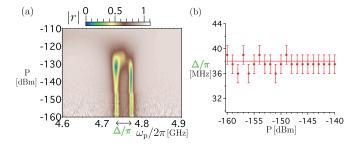


Figure 4. Energy shift as a function of input power. (a) Amplitude reflection coefficient |r| as a function of probe frequency  $\omega_{\rm p}$  and probe power P for both qubit frequencies fixed at  $\omega_{10}/2\pi=4.75\,{\rm GHz}$ . The data agree very well with theoretical simulations [72]. At high probe powers, the qubits are saturated and most photons are simply reflected from the mirror, resulting in  $|r|\approx 1$ . (b) The extracted splitting  $2\Delta$  (red points) from panel (a) as a function of P, and the splitting extracted from theoretical simulations (red curve) [72]. The splitting is clearly independent of the input power in this wide range.

shift relative to the linewidth even more. This experiment also demonstrated that a qubit can couple to, and become entangled with, another, spatially distant qubit via the transmission line even though the first qubit is prevented from decaying into the transmission line. These results give further insight into how virtual photons affect both atomic relaxation rates and inter-atomic coupling, which is of fundamental importance for quantum physics, and how these effects can be controlled using interference, which could have applications in quantum communication and quantum information processing.

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- \* These authors contributed equally † e-mail:ichoi@phys.nthu.edu.tw
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