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Carrier density induced ferromagnetism in EuTiO_3 bulk and heterostructures

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EuTiO_3 is an antiferromagnetic material showing strong spin-lattice interactions, large magnetoelectric response, and quantum paraelectric behavior at low temperatures. Using electronic-structure calculations, we show that adding electrons to the conduction band leads to ferromagnetism. The transition from antiferromagnetism to ferromagnetism is predicted to occur at ~ 0.08 electrons/Eu ($\sim 1.4 \times 10^{21} \text{ cm}^{-3}$). This effect is also predicted to occur in heterostructures such as $\text{LaAlO}_3/\text{EuTiO}_3$, where ferromagnetism is triggered by the formation of a high-density two-dimensional electron gas (2DEG) in the EuTiO_3 . Our analysis indicates that the coupling between Ti $3d$ and Eu $5d$ plays a crucial role in lowering the Ti $3d$ conduction band in the FM phase, leading to an almost linear dependence of the energy difference between the FM and AFM ordering on the carrier concentration. These findings open up possibilities in designing field-effect transistors using EuTiO_3 -based heterointerfaces to probe fundamental interactions between highly localized spins and itinerant, polarized charge carriers.

The coupling between spin, lattice, and charge in complex oxides gives rise to extremely rich phase diagrams including magnetism, ferroelectricity, magnetoelectricity, superconductivity, and colossal magnetoresistance [1, 2]. The combination of these three degrees of freedom is found in rare-earth titanates where itinerant Ti $3d$ electrons couple with localized rare-earth $4f$ electrons, in the presence of TiO_6 octahedral tilt and rotations [3]. Advances in epitaxial growth of oxide-based heterostructures, with meticulous control of thickness down to a monatomic layer, have enabled the study of the cross coupling of these interactions. Recently, an electric-field-tunable spin-polarized and superconducting quasi-2D electron system was created by inserting a few unit-cell thick layer of EuTiO_3 at the $\text{LaAlO}_3/\text{SrTiO}_3$ interface [4]. The $\text{LaAlO}_3/\text{EuTiO}_3/\text{SrTiO}_3$ δ -doped heterostructure was found to display different ground states depending on the carrier density, from Kondo-like transport at low carrier concentrations, to superconductivity and itinerant ferromagnetism as the 2D carrier density increases, with an intriguing transition from ferromagnetic to superconducting as a function of temperature. It is unclear whether a 2D superconducting state with unconventional order parameter is established as a result of the spin polarization of the itinerant Ti $3d$ electrons, or ferromagnetism and superconductivity coexist but at different depths inside the quasi-2D electron system [4]. Unraveling the interactions between the itinerant Ti- $3d$ and the localized Eu- $4f$ electrons is key to understanding these observations.

Electronic structure calculations are employed to investigate how excess electrons in the bulk of EuTiO_3 and at the $\text{LaAlO}_3/\text{EuTiO}_3$ interface affect the ordering of the Eu- $4f$ spins. As shown in Figure 1, we find that a transition from G -type antiferromagnetic (AFM) to ferromagnetic (FM) ordering occurs as the carrier concentration increases. The fundamental interactions underlying

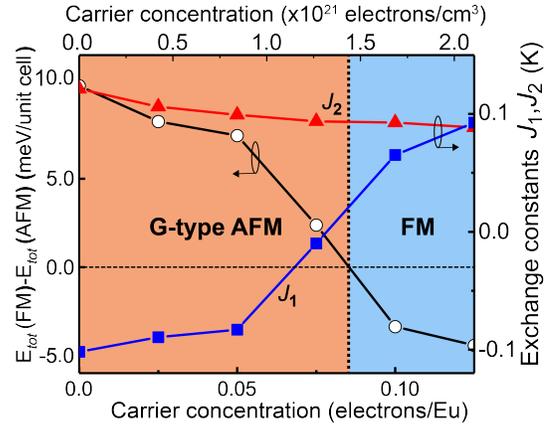


FIG. 1. Total-energy difference between the FM and G -AFM orderings, and first and second nearest-neighbor exchange constants, J_1 and J_2 , as a function of carrier concentration in EuTiO_3 .

the FM ordering are explained in terms of orbital couplings. We also show that the 2DEG in $\text{EuTiO}_3/\text{LaAlO}_3$ heterostructures also makes the EuTiO_3 ferromagnetic, which we attribute to the favored band alignment and charge transfer across the LaO-TiO_2 interface.

Our calculations are based on the density functional theory (DFT) [5, 6] and the HSE06 hybrid functional [7, 8] as implemented in the VASP code [9]. We use projected augmented wave potentials [10] with plane-wave basis set with a cutoff of 550 eV. For integrations over the Brillouin zone, we use a $7 \times 7 \times 5$ k -point mesh for bulk 20-atom cells and $3 \times 3 \times 1$ for the $\text{EuTiO}_3/\text{LaAlO}_3$ superlattices (composed of 7 unit-cell thick EuTiO_3 and 3 unit-cell thick LaAlO_3). The atomic positions are fully relaxed until the forces on each atom are less than 0.005 eV/\AA and total-energy differences between consecutive steps

are less than 10^{-6} eV. In the bulk calculations of the FM and AFM orderings, the lattice parameters and atomic positions are fully relaxed. For the $\text{EuTiO}_3/\text{LaAlO}_3$ superlattices, the in-plane lattice parameters were kept fixed during the structural relaxation to mimic the epitaxial growth on a SrTiO_3 substrate. Testing calculations based on DFT+ U [11–13] demonstrate robustness of our results and conclusions (Supplemental Material [14]).

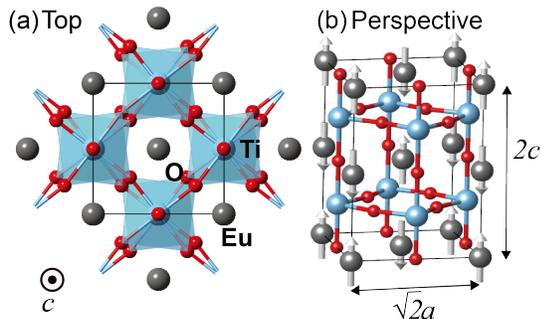


FIG. 2. Ball & stick model of the 20-atom unit cell of EuTiO_3 seen (a) from the $[001]$ direction with anti-phase rotations of oxygen octahedra around the c axis; (b) perspective view of the G -AFM ordering.

EuTiO_3 has a perovskite crystal structure with lattice parameters very close to those of SrTiO_3 . In contrast to SrTiO_3 , EuTiO_3 is magnetic, with a high spin $S = 7/2$ per Eu ($4f^7$). At temperatures lower than 5 K, EuTiO_3 displays G -type AFM ordering [15–17]. Above 5 K, EuTiO_3 becomes paramagnetic. DFT calculations and experiments have demonstrated that epitaxial EuTiO_3 thin films show FM ordering under tensile strain [13, 18–21], opening the door to higher-temperature implementations of strong ferromagnetic ferroelectrics and, potentially, to various device applications such as magnetic sensors, high-density multistate memory elements, tunable microwave filters, phase shifters and resonators. The use of epitaxial strain to stabilize the FM ordering has its limitations, relying on the speed of lattice response for switching between FM and AFM. Here, instead, we turn to doping as a way of controlling the magnetic ordering, i.e., we investigate how charge carriers affect the ordering of the Eu spin moments. Changing the doping level through a gated structure would allow for controlling the magnetization and exploring the fundamental interactions between itinerant electrons and highly localized spin moments.

For studying the effects of charge carriers in EuTiO_3 , we added electrons to the perfect bulk represented by a unit cell containing 20 atoms, which allows for the description of both FM and G -type AFM orderings, including the effects of octahedral tilt and rotations. The excess electrons are compensated by a homogeneous neutralizing background to ensure the system is charge neutral.

We chose to add electrons to the conduction band, instead of explicitly adding shallow-donor impurities, to separate the effects of excess charge carriers from the chemical or size effects of the impurities. Possible ways of doping, such as incorporation of impurities and through polar/non-polar interfaces in heterostructures are discussed.

The spin configuration of the G -type AFM ordering in EuTiO_3 is shown in Figure 2. In both AFM and FM EuTiO_3 there is a small anti-phase octahedral rotation around the c axis. The calculated lattice parameters for the G -type AFM ground state are $a = 3.888$ Å, $c = 3.924$ Å, and $\alpha = 7.24^\circ$, in good agreement with the experimental values $a = 3.903$ Å, $c = 3.908$ Å, and $\alpha = 3.03^\circ$ [22, 23]. The lattice parameters for the FM ordering are $a = 3.888$ Å, $c = 3.926$ Å, and $\alpha = 7.23^\circ$, i.e., very close to those of the AFM ground state. Doping within the range considered in the present work, i.e., up to 0.125 electrons/Eu, leads to negligible changes in lattice parameters, of less than 0.68%.

To understand the effects of carriers on the magnetic ordering, we first analyze the electronic structure of undoped EuTiO_3 . The band structure of the G -AFM and FM orderings are shown in Figure 3. The AFM and FM configurations display a band gap, which is slightly smaller in the FM than in the AFM, and in both cases we find a magnetic moment of $S = 7/2/\text{Eu}$. The gap separates the occupied narrow Eu- $4f$ band from the unoccupied conduction band derived mostly from Ti- $3d$ orbitals. The O- $2p$ band is about 2 eV below the occupied Eu- $4f$ band. These results are in good agreement with previous HSE06 calculations and photoemission measurements [20], as well as diffusive reflectance [17] and absorption [24, 25] spectra. We also find a significant contribution from Eu $5d$ to the lowest-energy conduction bands, which suggests a coupling with Ti $3d$, as seen in the orbital-projected density of states in Figure 4. For the undoped case, we find the G -AFM to be lower in energy than the FM ordering by 10.3 meV per unit cell, consistent with previous studies [13, 15–21]. It is noteworthy that the conduction-band minimum (CBM) of the FM phase is lower than that of the AFM, i.e., $\Delta E_{CBM} = -0.10$ eV, which we determine following Ref. [26]

By inspecting the band structures in Figure 3, we note that the excess electrons will be occupying the Ti $3d$ conduction band. We also note that the exchange splitting at the CBM gives a net polarization to the excess electrons, which is aligned with the FM ordering of the Eu spins. As electrons are added to EuTiO_3 , the total-energy difference between the FM and AFM phases [$\Delta E_{FM-AFM} = E_{tot}(\text{FM}) - E_{tot}(\text{AFM})$] decreases (Figure 1). When the added electron concentration exceeds 0.08 electrons/Eu (1.4×10^{21} electrons/cm³), the FM becomes more energetically favorable than the AFM ordering ($\Delta E_{FM-AFM} < 0$). The monotonic decrease of ΔE_{FM-AFM} with the excess carriers and the nega-

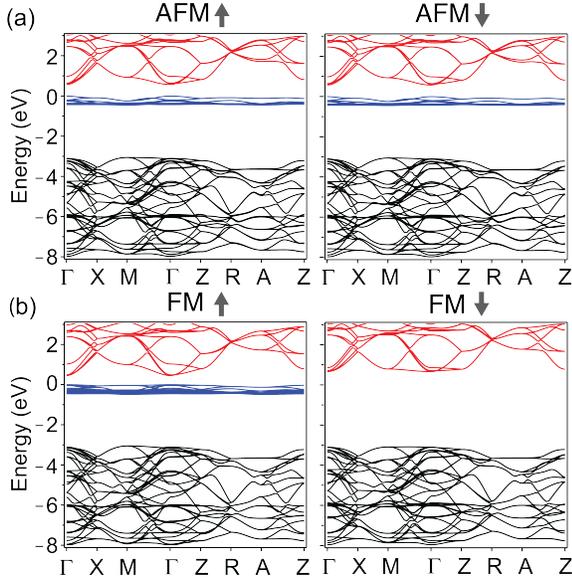


FIG. 3. Electronic band structures of EuTiO_3 for (a) G -type antiferromagnetic (AFM) ordering, and (b) ferromagnetic (FM) ordering. The zero in the energy axis was set to top of the occupied $\text{Eu-}4f$ band.

tive sign of ΔE_{CBM} suggest a simple rigid-band filling model: as electrons are added to the conduction band, the FM ordering will become more stable than the AFM when $n \times |\Delta E_{CBM}| > \Delta E_{FM-AFM}$, where n is the carrier concentration. From this simple picture, the estimated electron concentration that would make the FM more stable amounts to $n = 0.03$ electrons/Eu, in reasonable agreement with the direct calculated value of $n = 0.08$ electrons/Eu shown in Figure 1. A comparison of the electronic band structures of the undoped and doped EuTiO_3 (see Supplemental Material [14]) shows that the bands remain intact upon doping, corroborating the rigid-band filling picture.

Why is the CBM in the FM phase lower than that in AFM in EuTiO_3 , i.e., $\Delta E_{CBM} < 0$? We explain it based on the coupling between the $\text{Ti-}3d$ (t_{2g}) and the $\text{Eu-}5d$ (t_{2g}), $\text{Eu-}4f$, and $\text{O-}2p$ bands, of which the $\text{Eu } 5d$ - $\text{Ti } 3d$ and $\text{Eu } 4f$ - $\text{Ti } 3d$ are the most relevant because they act differently in the case of the AFM and FM orderings. From the orbital-projected DOS, we constructed the inter-band interaction diagrams shown in Figure 4, where we highlight the relevant couplings that affect the position of the $\text{Ti-}3d$ band. The energy shift of the $\text{Ti-}3d$ band due these couplings is denoted as $\Delta E_{5d-3d}^X(\uparrow;1,2)$, $\Delta E_{5d-3d}^X(\downarrow;1,2)$, $\Delta E_{4f-3d}^X(\uparrow;1,2)$, $\Delta E_{4f-3d}^X(\downarrow;1,2)$, where \uparrow or \downarrow indicate the spin channel, X refers to the AFM or FM ordering, and 1 or 2 represents the index of the two nearest Eu atoms to a given Ti atom. Thus, the spin-up

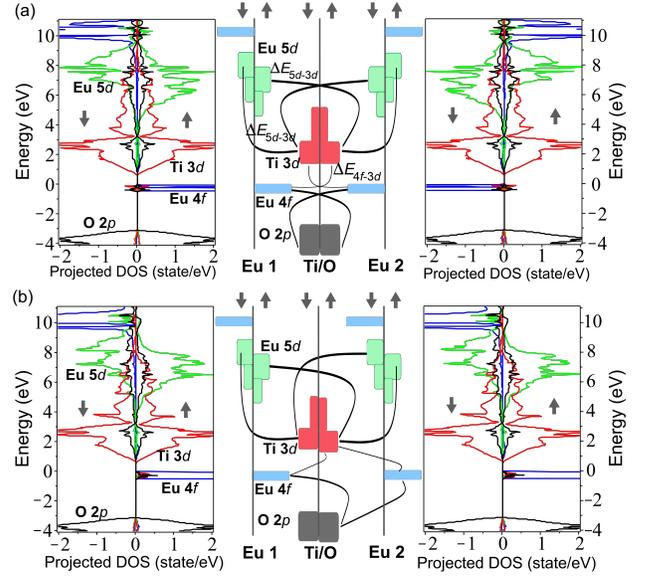


FIG. 4. Density of states projected on $\text{Eu-}4f$ orbitals (blue), $\text{Eu-}5d$ orbitals (green), $\text{Ti-}3d$ orbitals (red), and $\text{O-}2p$ orbitals (black), and the derived inter-band coupling diagrams for the (a) G -type antiferromagnetic (AFM) and (b) ferromagnetic (FM) ordering of undoped EuTiO_3 . In the inter-band coupling diagrams, the solid curly arrows indicate the most relevant couplings. The exchange splitting in the $\text{O-}2p$ bands and $\text{Ti-}3d$ bands are enlarged for ease of representation. The zero in the energy axis was set to the maximum of the occupied $\text{Eu-}4f$ band.

$\text{Ti-}3d$ band of the AFM ordering is shifted according to:

$$\begin{aligned} \Delta^{AFM} &= \Delta E_{4f-3d}^{AFM}(\uparrow;1) \\ &\quad - \Delta E_{5d-3d}^{AFM}(\uparrow;1) - \Delta E_{5d-3d}^{AFM}(\uparrow;2), \end{aligned} \quad (1)$$

where we neglected $\Delta E_{4f-3d}^{AFM}(\uparrow;2)$ due to the large energy separation between the $\text{Ti-}3d$ band and the empty $\text{Eu-}4f$ band, and the small overlap of the $\text{Ti-}3d$ and $\text{Eu-}4f$ orbitals due to the large distance between the Ti and Eu atoms. An equivalent expression can be written for the spin-down $\text{Ti-}3d$ band.

For the FM ordering, the spin-up $\text{Ti-}3d$ band is shifted according to:

$$\begin{aligned} \Delta^{FM} &= \Delta E_{4f-3d}^{FM}(\uparrow;1) + \Delta E_{4f-3d}^{FM}(\uparrow;2) \\ &\quad - \Delta E_{5d-3d}^{FM}(\uparrow;1) - \Delta E_{5d-3d}^{FM}(\uparrow;2). \end{aligned} \quad (2)$$

We note that $E_{5d-3d}^{FM}(\uparrow;1) = E_{5d-3d}^{FM}(\uparrow;2) \approx \Delta E_{5d-3d}^{AFM}(\uparrow;1) \gg \Delta E_{5d-3d}^{AFM}(\uparrow;2)$. Based on the DOS shown in Figure 4, and Eqs. 1 and 2, we conclude that the $\text{Eu } 5d$ - $\text{Ti } 3d$ coupling is responsible for lowering the $\text{Ti-}3d$ band in the FM compared to that in the AFM ordering.

In the case of undoped EuTiO_3 , it has been proposed that the competition between the antiferromagnetic superexchange and an indirect ferromagnetic exchange via

the Eu 5d states leads to a delicate balance between the AFM and FM phases [20]. Here we show how this competition between the AFM and FM orderings is altered by the presence of electrons in the Ti-3d conduction band. Basically, adding electrons to the conduction band favors the FM phase because its CBM is lower than that in the AFM phase.

It could also be argued that the stabilization of the FM ordering upon doping in EuTiO_3 follows the Stoner model [27]. As the doping concentration in the Ti-3d t_{2g} bands increases, the density of states at the Fermi level increases; at a certain doping concentration, the spin splitting of the Ti-3d bands becomes energetically favorable (since it reduces the electron-electron repulsion), which is consistent with the Stoner picture of magnetism [27]. However, it is important to note that the spin splitting of the Ti-3d bands is already present in the FM undoped EuTiO_3 . The polarized Eu-4f bands lead to the spin polarization of the Eu-5d bands, which are composed of orbitals that are quite delocalized in space and overlap with Ti-3d orbitals, thus leading to a spin-split conduction band. In the rigid-band filling model, adding electrons then lowers the energy of the FM with respect to the AFM ordering.

How can electrons be added to the conduction band of EuTiO_3 and how to control their concentration? A conventional method of adding electrons to the conduction band of a semiconductor is to incorporate shallow-donor impurities. These are atoms that typically sit to the right of the host atoms in the periodic table. For EuTiO_3 , there are a few possibilities: trivalent impurities sitting on the Eu site, such as Gd and La, pentavalent impurities sitting on the Ti site, such as Nb, or F sitting on the O site. In addition, one could incorporate H, either as interstitial bonded to O, or substitutional replacing O atoms. Both forms have been reported to act as shallow donors in many oxides [28, 29].

Experimentally, it has been found that EuTiO_3 doped with either La, Gd, Dy, Nb, or H leads to ferromagnetism [30–34]. It has also been reported that by controlling oxygen partial pressure leads to conducting ferromagnetic films [35]. Specifically, $\text{EuTiO}_{3-x}\text{H}_x$, with x as low as 0.07, leads to ferromagnetic powders and thin films [34], and that ferromagnetism is observed in $\text{EuTi}_{1-x}\text{Nb}_x\text{O}_3$ for $x \geq 0.1$ [33]. These results are in good agreement with our predicted AFM-FM transition at ~ 0.08 electrons/Eu. In all these reports, the emergence of ferromagnetism in doped EuTiO_3 has been attributed to the Ruderman-Kittel-Kasuya-Yosida (RKKY) interaction, yet without any further justification. RKKY is often used to explain the exchange interaction between itinerant electrons and localized magnetic moments. Here, we find that the interaction between the Ti 3d and Eu 4f is of secondary importance, and that the Eu 5d-Ti 3d coupling (Figure 4) is key to stabilizing the FM ordering with increasing carrier concentration.

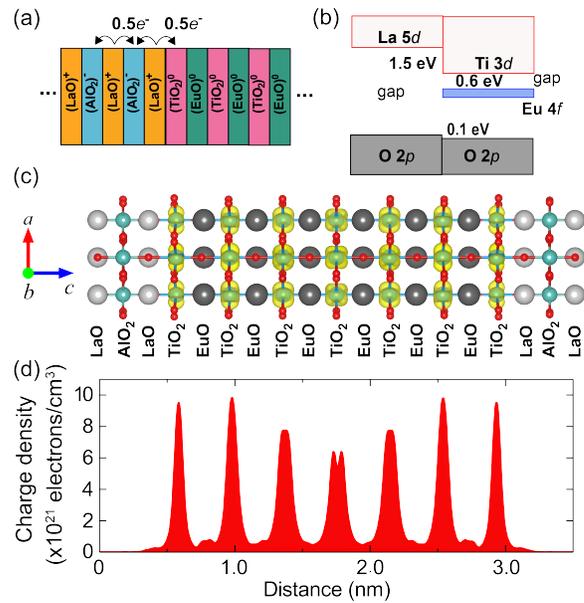


FIG. 5. (a) Formation of a 2DEG at the $\text{LaAlO}_3/\text{EuTiO}_3(001)$ interface with a LaO-TiO_2 termination. (b) Band alignment at the $\text{LaAlO}_3/\text{EuTiO}_3$. (c) Distribution of the charge carriers in the $\text{LaAlO}_3/\text{EuTiO}_3(001)$ superlattice with two equivalent LaO-TiO_2 interfaces, with isosurface set to 20% of the maximum value. (d) Planar-averaged excess charge as a function of the distance along the c axis of the superlattice in (c), showing excess charge accumulation in the EuTiO_3 .

We can also add conduction electrons to EuTiO_3 through a heterointerface. In analogy to $\text{LaAlO}_3/\text{SrTiO}_3(001)$ [36–40], or $\text{GdTiO}_3/\text{SrTiO}_3(001)$ [41], we predict that a 2DEG will form at the $\text{LaAlO}_3/\text{EuTiO}_3$ with LaO-TiO_2 termination. In such systems, the charge transfer to the EuTiO_3 layer occurs due to the valence mismatch and the band alignment at the interface [38–40]. The conduction band in the band insulator LaAlO_3 or in the Mott insulator GdTiO_3 lie higher in energy than the conduction band in EuTiO_3 such that, at the LaO-TiO_2 termination the excess electrons from the LaO donor layer is accommodated in the conduction band of EuTiO_3 [26].

Basically, LaAlO_3 can be thought as composed of alternating charged planes $(\text{LaO})^+$ and $(\text{AlO}_2)^-$ along the $[001]$ direction, whereas EuTiO_3 is composed of charge-neutral planes $(\text{EuO})^0$ and $(\text{TiO}_2)^0$. In the LaAlO_3 , each $(\text{LaO})^+$ gives $0.5e^-$ per unit-cell area to the right and $0.5e^-$ to the left $(\text{AlO}_2)^-$, as indicated in Figure 5(a). Thus, at the LaO-TiO_2 interface, there will be an excess of $0.5e^-$ per unit-cell area, which due to the conduction-band offset, is accommodated on the EuTiO_3 side, forming a 2DEG near the interface. The excess electrons from the 2DEG is sufficient to turn the EuTiO_3 layer ferromagnetic.

To demonstrate this effect, we first calculated the band alignment between LaAlO_3 and EuTiO_3 , following the procedure described in [26]; the result is shown in Figure 5(b). Then we performed calculations for an $\text{LaAlO}_3/\text{EuTiO}_3(001)$ superlattice with two equivalent LaO-TiO_2 interfaces. The structure of the superlattice $\text{LaAlO}_3/\text{EuTiO}_3$ is given in Figure 5(c). The distribution of the excess charges in the EuTiO_3 layer is also shown in Figure 5(c) and the planar-averaged excess charge density along the c axis is shown in Figure 5(d).

We find that the FM is lower than the AFM ordering by 9.7 meV/(unit cell) in the heterostructure, and that each Eu atom in the heterostructure holds a magnetic spin moment of $S = 7/2/\text{Eu}$ ($4f^7$). Considering the thickness of the EuTiO_3 layer (23.5 Å), we obtain an excess electron concentration of $2.4 \times 10^{21} \text{ e}^-/\text{cm}^3$ since each interface gives 0.5 electron per unit cell area. The stability of the FM ordering is thus explained by the presence of the excess electrons in the conduction band of EuTiO_3 , consistent with the results for bulk shown in Figure 1. The excess electrons are uniformly distributed over the Ti-3d orbitals in EuTiO_3 , contributing with negligibly small moments to the total spin. Our results also explain the observed ferromagnetism in the $\text{LaAlO}_3/\text{EuTiO}_3/\text{SrTiO}_3$ δ -doped heterostructures [4], which arises from the charge transfer through the $\text{LaAlO}_3/\text{EuTiO}_3$ interface.

The results for the $\text{LaAlO}_3/\text{EuTiO}_3(001)$ in Figure 5 suggest that the ferromagnetism in the EuTiO_3 -based heterostructures could be controlled by an electric field. In a field-effect transistor design, and at low temperatures, an electric field applied through a gate electrode could be used to deplete/accumulate charge carriers in the EuTiO_3 layer near the interface, inducing FM/AFM transitions, thus enabling the control of the magnetic ordering through a gate voltage. Such FET has already been demonstrated in the case of $\text{LaAlO}_3/\text{SrTiO}_3$ [37, 42] and $\text{GdTiO}_3/\text{SrTiO}_3$ [43], although a complete depletion of the excess charge in the SrTiO_3 layer has been proved challenging. Such device could be used to manipulate and control the magnetic ordering in EuTiO_3 thin films, and also to investigate the fundamental interactions between the electrons in the 2DEG with the large Eu spin moments near the interface through the current between source and drain.

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