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Reply to Comment on "Is a Trineutron Resonance Lower in Energy than a Tetraneutron Resonance?" by A. Deltuva and R. Lazauskas

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In Ref. [1] we presented calculations for three- and fourneutron (3n and 4n) states in the presence of an external trapping potential. These calculations were extrapolated to the limit of zero trap depth, as in Ref. [2], and showed the remarkable feature that these extrapolations point to a common positive energy scale, independent of the trap geometries considered. Based on calculations for a twobody resonance, where the same extrapolation procedure correctly locates the resonance energy, we suggested that our results support the possible observation of a tetraneutron resonance [3], and provide indications that a 3nresonance might also exist at an energy below a possible 4n resonance. We did not claim that a 3n or 4n resonance definitely exists, nor did we quantify their widths.

The question of few-neutron resonances is an interesting and challenging problem with many conflicting theoretical results at present [1, 2, 4–10] including Ref. [11], which we regrettably missed in our Letter and the more recent Ref. [12], which already put forward the arguments raised in the Comment by Deltuva and Lazauskas [13].

The arguments presented in the Comment largely rely on ideas related to the Analytic Continuation in the Coupling Constant (ACCC) method, where the Hamiltonian of the system is written as $H(\lambda) = H_0 + \lambda H_{\text{att}}$, with $H_{\rm att}$ the attractive part of the ($\lambda = 1$) original Hamiltonian. However, we point out that ACCC is not the same as applying an external trap, which is the procedure we employ in our Letter. Therefore, while we agree that bound dineutrons emerge early on as the trap depth V_0 is nonzero, we do not agree with the authors' conclusion that "in the presumed $E_{4n} \approx 0$ region ... [t]he tetraneutron states ... are not true bound states." It is not clear what the authors mean by "true bound states." Bound states are states whose wave functions have compact support. This is the case for all of our calculated 3n and 4n states in the trap. In our Letter, we used the auxiliary field diffusion Monte Carlo method, which converges to the lowest energy eigenstate with the relevant quantum numbers of a given Hamiltonian. There are cases where diffusion Monte Carlo methods have been applied to states that decay. For example, the unbound nucleus ⁸Be was calculated using the Green's function Monte Carlo method in Ref. [14]. In this case, the states decay asymptotically to two α clusters, and this decay is observed clearly, e.g., in the evolution of the 4^+ energy even after a short imaginary time, as shown in the

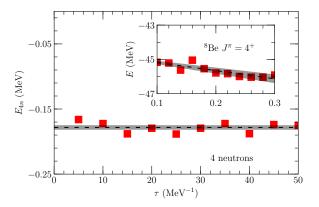


FIG. 1. The 4n energy in an external Woods-Saxon well with $V_0 = -1.25$ MeV and $R_{\rm WS} = 6.0$ fm as a function of imaginary time for the local chiral N²LO interactions used in Ref. [1]. The inset (extracted from Ref. [14]) shows that an unbound $J^{\pi} = 4^+$ state of ⁸Be decays very rapidly as a function imaginary time evolution (note the axes are in the same units).

inset of Fig. 1. As Fig. 1 also shows, for the 4n system in the region in question, where $E_{2n} < E_{4n}$ (e.g., $V_0 = -1.25$ MeV and $R_{\rm WS} = 6.0$ fm), we observe no such decay in the energy over a very long imaginary time evolution. This suggests that this 4n state is more complex than a pair of dineutrons, or a dineutron with a pair of neutrons. Moreover, we have checked that including in the extrapolation only the points where $E_{4n} < E_{2n}$ for $R_{\rm WS} = 7.5$ fm still identifies the potential 4n resonance at approximately 2.5 MeV.

Regarding the extrapolation procedure itself, we are aware that some care is needed, which is why we sought to establish that our extrapolation works well in the twobody S-wave (two-Gaussian) potential case as discussed in [1]. To reinforce this point, we have performed additional calculations for two two-body resonances shown in Fig. 2. As can be seen in Fig. 2, our extrapolation procedure correctly identifies the locations of the two resonances within the uncertainties of the fit. Furthermore, as our Letter notes, using the current extrapolation, we cannot make a comment about the width. It is entirely possible that the width is very broad (see also Ref. [9]) and therefore the resonance would have little or no effect on the observable scattering dynamics. In fact, we



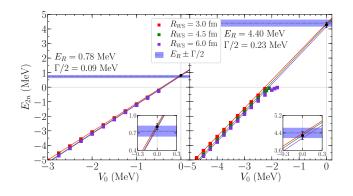


FIG. 2. The energy of two neutrons trapped in various Woods-Saxon wells interacting via an *S*-wave (two-Gaussian) potential as in Ref. [1] tuned to give two different resonances. The linear extrapolations to zero well depth correctly give the position of the resonance in both cases.

acknowledge that our current extrapolation cannot distinguish between a resonance and a virtual state.

In conclusion, the existence of few-neutron structures is ultimately a question that experiments have to decide. It remains an intriguing open question whether these systems exhibit resonances, virtual states, or other localized features of the cross section unrelated to S-matrix poles.

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