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**Ramsey Spectroscopy with Displaced Frequency Jumps**


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Sophisticated Ramsey-based interrogation protocols using composite laser pulse sequences have been recently proposed to provide next-generation high-precision atomic clocks with a near perfect elimination of frequency shifts induced during the atom-probing field interaction. We propose here a simple alternative approach to the auto-balanced Ramsey (ABR) interrogation protocol and demonstrate its application to a cold-atom microwave clock based on coherent population trapping (CPT). The main originality of the method, based on two consecutive Ramsey sequences with different dark periods, is to sample the central Ramsey fringes with frequency-jumps finely-adjusted by an additional frequency-displacement concomitant parameter, scaling as the inverse of the dark-period. The advantage of this displaced frequency-jumps Ramsey (DFJR) method is that the local oscillator (LO) frequency is used as a single physical variable to control both servo loops of the sequence, simplifying its implementation and avoiding noise associated with controlling the LO phase. When tested using a CPT cold-atom clock, the DFJR scheme reduces the sensitivity of the clock frequency to variations of the light shifts by more than an order of magnitude compared with the standard Ramsey interrogation. This simple method can be applied in a wide variety of Ramsey-spectroscopy based applications including frequency metrology with CPT-based and optical atomic clocks, mass spectrometry, and precision spectroscopy.

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Ramsey’s method of separated oscillating fields [1] enables the measurement of atomic and molecular spectral lines with unrivaled precision and accuracy. This widely-used spectroscopy and interrogation technique has been successfully applied in a variety of quantum-based measurements and devices including atomic frequency standards [2–7], matter-wave interferometry and atomic inertial sensors [8, 9], Bose-Einstein condensates [10], quantum computing [11], memories [12] and information processing [13], cavity quantum electrodynamics [14], optomechanics [15], extreme-ultraviolet spectroscopy [16], mass spectrometry [17], as well as the experimental confirmation of fundamental quantum mechanics concepts [18].

In a typical Ramsey sequence, atoms are probed with two successive pulses separated by a dark period T. The first pulse creates a coherence between targeted quantum states whose initial phase is dictated by the external field. During the dark period, a phase shift develops between the atomic coherence and the excitation field determined by their frequency difference and T. Through an interference process, the second pulse leads to the modulation of the field absorption spectrum allowing for an effective measurement of the phase difference between the atomic precession and the local oscillator (LO). Scanning the frequency of the excitation field around the exact resonance and measuring the absorption of the second pulse leads to the detection of Ramsey fringes, whose line-width scales as 1/(2T).

For clock applications, Ramsey spectroscopy reduces the sensitivity of the clock frequency to variations of the interrogating field [1, 19]. However, the Ramsey interrogation exhibits residual frequency-shifts induced by the probe field during the interrogation pulses. These interrogation-related shifts originate from a phase shift Δϕ acquired by the atomic coherence during the interrogation pulses. Since the spacing between Ramsey fringes is equal to 1/T, this phase-shift is compensated by an opposite phase-shift created by a 1/T-dependent frequency-shift Δf = −Δϕ/(2πT) between the atomic frequency and the LO frequency during the dark-period. These light-shifts can be a key limiting factor to the accuracy and long-term frequency stability of atomic clocks based on coherent population trapping (CPT) [19–22] and optical clocks that probe ultra-narrow quadrupole [23], octupole [24] or two-photon optical transitions [25, 26].

CPT-based clocks, in which the hyperfine microwave clock-transition frequency is probed using a dual-frequency optical field, are known to suffer from substantial light shifts that depend on the parameters of the optical field. Therefore, a CPT clock can serve as a test device for the investigation of interrogation-related shifts and their mitigation. The light-shifts in CPT clocks originate from resonant interaction of the dual-frequency optical field with the 3-level atomic A-scheme [27, 28] and from off-resonant coupling of the light field components.
with neighboring detuned atomic energy levels \([29, 30]\). The resonant shift results from incomplete dark-state formation during the first Ramsey-CPT pulse, and can be canceled by increasing the duration or intensity of the first Ramsey pulse \([21, 27, 30, 31]\). The off-resonant shift, depending mostly on the relative intensity of the two optical frequencies (CPT intensity ratio) \([32]\), remains the dominant effect limiting the clock performance.

Over the last decade, sophisticated interrogation protocols based on Ramsey’s method have been proposed in order to eliminate probe-induced frequency shifts \([33, 34]\). Among them, the auto-balanced Ramsey (ABR) scheme \([35]\) is based on the extraction of two error signals derived from two successive Ramsey sequences with different dark periods. The first feedback loop uses the error signal generated by the short Ramsey sequence to apply a phase-step correction to the LO during the dark period that nulls the probe-field induced frequency shift. The second loop stabilizes the LO frequency using the error signal derived from the long Ramsey sequence. The ABR technique has been applied to different kinds of atomic clocks, demonstrating a significant reduction of the clock frequency sensitivity to light-shifts and improving the clock mid and long-term frequency stability \([35–37]\). In \([38]\) a theoretical generalization of the ABR method was presented, demonstrating the possibility to use various concomitant parameters including frequency steps during the Ramsey pulses.

In this letter, we propose and demonstrate a simple method to reduce interrogation-related frequency-shifts in Ramsey spectroscopy that we call Ramsey spectroscopy with displaced frequency jumps (DFJR). Similarly to the techniques presented previously \([35, 36, 38]\), two servo loops are used to control the clock frequency and a concomitant parameter that suppresses interrogation shifts. However, we propose a way to implement both control parameters with a single physical variable - the LO frequency. Aside from the requirement that the phase of the interrogation field is stable during the Ramsey cycle, no modulation or control of the LO phase is needed. This allows for simpler implementation and the elimination of the systematics associated with controlling and modulating the phase of the oscilator. We also note that the LO frequency remains constant throughout the Ramsey cycle and no rapid control of the LO frequency is required. This method can be applied to any Ramsey spectroscopy measurement, including for CPT atomic clocks and optical atomic clocks.

In a Ramsey clock, by sampling the half-height signal on both sides of the central Ramsey fringe with two consecutive Ramsey cycles, a zero-crossing error signal can be derived by subtraction of the two measurements and used to stabilize the frequency of the LO onto the fringe center. Two options are generally used for the generation of the error signal. One option, known as phase-jumps, is to abruptly change the phase of the LO between the first and second Ramsey pulse by \(\pi/2 (\pi/2)\) during the first (second) Ramsey cycle. Another option, known as frequency-jumps, is to jump the frequency of the LO to \(1/(4T)\) \((-1/(4T))\) from the estimated clock frequency during the first (second) Ramsey cycle.

The basic concept of the DFJR method is illustrated in Fig. 1. Figure 1A depicts a Ramsey-CPT fringe for \(T = 16\) ms, probed with standard \(\pm 1/(4T)\) frequency-jump interrogation, and assumed to be light-shifted by 3 Hz, which results in a similar shift of the stabilized clock frequency. This frequency shift can be eliminated by applying frequency-jumps of different magnitude to the right and left sides of the fringe such that the error signal steers the clock to the non-shifted frequency. The challenge is then to find the suitable frequency displacement \(\Delta f_T\). C. The DFJR method is used to find \(\Delta f_T\) and stabilize the clock frequency on the non-shifted resonance frequency \((f_C = 0\) Hz\). Using two different dark-periods, \(T_S = 4\) ms (lower part of the graph) and \(T_L = 16\) ms (upper part of the graph) and adding the frequency displacement \(\Delta f_T\) as a \(T\)-dependent control parameter, the clock frequency is free from light shifts.

\[
\Delta f_T = \frac{\alpha}{T}
\]

where \(\alpha\) is the concomitant control parameter in the
DFJR method. Without prior knowledge of the shifts in the system (which may also vary over time), the difficulty is then to find the correct $\Delta f_T$ value to apply.

For this purpose, the DFJR method consists of a composite Ramsey sequence involving two different dark-periods, and uses the measured error signals to find the suitable $\Delta f_T$ value and adapt it over time to compensate drifts in the light-shift. We take advantage of the fact that the interrogation-related frequency shifts depend inversely on the dark-period. By defining $\Delta f_T$ as a $T$-dependent parameter, the interrogation-related shifts can be distinguished and separated from the clock frequency $f_c$ (which is independent of $T$). We note that frequency-shifts that do not scale with $1/T$ (e.g. Zee-man shifts) will not be mitigated by the DFJR method. Figure 1.C illustrates the principle of the DFJR method.

Two Ramsey fringes obtained with a long dark period $T_L = 16$ ms and a short dark period $T_S = 4$ ms are assumed to be light-shifted by 3 Hz and 12 Hz respectively. The frequency jumps are displaced by $\Delta f_{T_L} = \frac{\alpha}{T_L}$ and $\Delta f_{T_S} = \frac{\alpha}{T_S}$ respectively. Two error signals are then generated (from the short and long cycles) and are used to stabilize the clock frequency $f_c$ and the concomitant control parameter $\alpha$. The only steady-state solution that nulls both error signals occurs when the clock frequency is on resonance, as depicted in Fig. 1.C. This results in a clock frequency free from the influence of interrogation related shifts.

Figure 2 shows the proposed DFJR sequence. It consists of two cycles with a long dark period $T_L$ and two cycles with a short dark period $T_S$. For each pair of cycles, the error signal is generated using frequency jumps from measurements of the half-height signal values on both sides of the central fringe (one value per cycle) and extracting their difference. In the long dark-period cycles, the sampling frequencies are $f_c - \left(\frac{1}{4T_L} - \frac{\alpha}{T_L}\right)$ and $f_c + \left(\frac{1}{4T_L} + \frac{\alpha}{T_L}\right)$, while for the short dark-period cycles the corresponding frequencies are $f_c - \left(\frac{1}{4T_S} - \frac{\alpha}{T_S}\right)$ and $f_c + \left(\frac{1}{4T_S} + \frac{\alpha}{T_S}\right)$. Thus in the DFJR method, one control parameter (the clock frequency, $f_c$) is the same for both dark-periods, while the other control parameter, $\alpha$, causes a frequency displacement that scales with the dark-period. This allows one to implement two control parameters combined in a single physical variable (the LO frequency). The error signal from the long dark-period cycle pair $\varepsilon_L$ is used to steer the clock frequency, while the error signal from the short dark-period cycle pair $\varepsilon_S$ is used to steer $\alpha$. In the presence of frequency shifts that depend inversely on the duration of the dark-period, the control system will stabilize such that the frequency displacement parameter adapts to compensate these shifts and the clock frequency is free from them. Note that the total DFJR sequence shown in Fig. 2 is symmetrized as reported in [37] for optimal efficiency of the light-shift rejection.

We implemented the DFJR protocol utilizing a cold-atom clock apparatus previously described in [21, 28]. A six-beam magneto-optical trap is applied for 20 ms followed by a 3 ms molasses, trapping and cooling $\sim 1 \times 10^6$ $^{87}$Rb atoms at a temperature of 10 $\mu$K. At this stage, the atoms are allowed to fall freely and are interrogated in a Ramsey-CPT cycle. A 3 ms CPT preparation pulse is followed by a dark-period $T = 4$-16 ms and a 50 $\mu$s reading CPT pulse. We use the lin || lin CPT interrogation scheme [39, 40] to enhance the CPT contrast and retro-reflect the CPT beam to minimize Doppler shifts [41]. A quantization magnetic field of $B_z = 4.4$ $\mu$T is applied in the direction of the CPT beam propagation. The CPT beam is generated from a laser modulated at 6.835 GHz (the Rb ground-state hyperfine splitting frequency) using an electro-optic modulator (EOM). The optical carrier and the $-1$-order sideband are used as the two CPT fields. The intensity ratio between the CPT fields is controlled using the EOM and measured by a Fabry-Perot interferometer. The intensity and frequency (one-photon detuning, OPD) of the CPT beam are controlled using an acousto-optic modulator. The Ramsey
The long cycle $\Delta f$ frequency to accommodate the changing light shift leaving the clock transition. The upper pane shows the clock frequency shifts. Figure 3 depicts a time trace of DFJR clock operation based on varying experimental parameters and interrogation CPT spectroscopy by running the cold-atom clock until the frequency shifts are measured. Error signals, an atomic clock is obtained and the absolute frequency shifts are measured.

The DFJR method was compared to standard Ramsey-CPT spectroscopy by running the cold-atom clock under varying experimental parameters and interrogation shifts. Figure 3 depicts a time trace of DFJR clock operation. The upper pane shows the clock frequency shift $f_c - f_{Rb}$, where $f_{Rb}$ is the generally accepted unperturbed $^{87}\text{Rb}$ hyperfine frequency [42], while the lower pane shows the frequency displacement for the long cycle $\Delta f_{T_c} = \frac{1}{T_c}$. During clock operation, the off-resonant light shift is altered by abruptly changing the CPT intensity ratio. Each time the CPT intensity ratio is changed, resulting in a different light shift, the frequency displacement control parameter $\alpha$ stabilizes to a new value, compensating for the light shift, and keeping the clock frequency $f_c$ unaffected. In essence, the two-loop control system keeps one of the control parameters (the clock frequency) protected from this particular kind of systematic.

Figure 4 shows the clock frequency shift $f_c - f_{Rb}$ versus the CPT intensity ratio in the standard Ramsey-CPT regime ($T = 16$ ms), compared to the DFJR scheme ($T_s = 4$ ms and $T_L = 16$ ms). In the standard Ramsey-CPT scheme (triangles) the clock frequency significantly changes with the CPT intensity ratio due to the off-resonant light shift [32]. With the DFJR scheme, the frequency displacement parameter $\alpha$ (squares) changes with the CPT intensity ratio in order to compensate for the light-shift, and the clock frequency (circles) variations are considerably reduced. The absolute clock frequency shift is then about 0.835 Hz, in good agreement with the expected second-order Zeeman shift in the linear configuration (which is $T$-independent and hence not canceled).

We also tested the ability of the DFJR method to mitigate light shifts that depend on the CPT laser OPD. For this purpose, we applied sinusoidal oscillations to the OPD with an amplitude of $\pm 1$ MHz and a period of about 2 hours ($\sim 1.4 \times 10^{-4}$ Hz frequency) during clock operation. Figure 5 shows the fast Fourier transform (FFT) spectrum of the clock frequency for the Ramsey-CPT and DFJR methods. In the Ramsey-CPT case, a strong peak is observed at the OPD oscillation frequency whereas the amplitude of this peak is reduced by an order-of-magnitude in the DFJR method. It is interesting to note that the FFT noise spectrum of the DFJR clock frequency shows an increased noise level. We attribute this
frequency displacement that scales with 1 ods. Using frequency-jumps, the first servo loop nulls the frequency shifts depend inversely on the dark-period and is scheme relies on the fact that interrogation-related fre-
displaced frequency jumps Ramsey (DFJR) spectroscopy and tested it using a cold-atom CPT clock. The so-called degradation to the longer clock sequence in the DFJR method.

In conclusion, we demonstrated a simple method to reduce interrogation-related shifts in Ramsey spectroscopy and tested it using a cold-atom CPT clock. The so-called displaced frequency jumps Ramsey (DFJR) spectroscopy scheme relies on the fact that interrogation-related frequency shifts depend inversely on the dark-period and is based on Ramsey interrogations with different dark periods. Using frequency-jumps, the first servo loop nulls the probing-field induced frequency shift by adding a slight frequency displacement that scales with 1/T while the second servo loop stabilizes the LO frequency. This approach presents the benefit of controlling only a single physical variable (the frequency of the LO), simplifying implementation and eliminating the noise associated with controlling the LO phase. A significant reduction by more than an order-of-magnitude of the clock frequency dependence to variations of the CPT intensity ratio and of the laser OPD has been observed with the DFJR scheme, in comparison with the standard Ramsey-CPT scheme.

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