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Phys. Rev. Lett. **122**, 040405 — Published 1 February 2019

DOI: [10.1103/PhysRevLett.122.040405](https://doi.org/10.1103/PhysRevLett.122.040405)

# Designer Spatial Control of Interactions in Ultracold Gases

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(Dated: January 10, 2019)

Designer optical control of interactions in ultracold atomic gases has wide applications, from creating new quantum phases to modeling the physics of black holes. We demonstrate wide tunability and spatial control of interactions in a two-component cloud of  ${}^6\text{Li}$  fermions, using electromagnetically induced transparency (EIT). With two control fields detuned  $\simeq 1.5$  THz from atomic resonance, MHz changes in the frequency of one optical beam tune the measured scattering length over the full range achieved by magnetic control, with negligible ( $10^{-6}$ ) effect on the net optical confining potential. A 1D “sandwich” of resonantly and weakly interacting regions is imprinted on the trapped cloud and broadly manipulated with sub-MHz frequency changes. All of the data are in excellent agreement with our continuum-dressed state theoretical model of optical control, which includes both the spatial and momentum dependence of the scattering amplitude.

Tunability of interactions in ultracold atomic gases has been achieved by exploiting magnetically controlled collisional (Feshbach) resonances [1], where the total energy of two colliding atoms in an energetically open channel is tuned into resonance with a bound dimer state in a closed channel. Optical field control offers a much richer palette, by creating designer interactions with high resolution in position, energy, momentum, and time. These techniques enable new paradigms. For example, energy resolution will provide better models of neutron matter by controlling the effective range [2, 3], while momentum resolution will create pairs with a nonzero center of mass momentum in two-component Fermi gases [4, 5]. The increased temporal resolution enables studies of non-equilibrium thermodynamics of strongly interacting gases on time scales faster than the Fermi time [6]. Spatial manipulation of interactions can be utilized to study controllable soliton emission [7], exotic quantum phases [8], long-living Bloch oscillations of matter waves [9], the physics of Hawking radiation from black holes [10], and scale-invariant dimer pairing [11]. Optical control methods are therefore of great interest [12–19], but generally suffer from atom loss and heating due to spontaneous scattering, which severely limits their applicability.

In a major breakthrough for suppressing spontaneous scattering, Bauer et al., [16] used a bound-to-bound transition in the closed channel, which is far away from the atomic resonance. To further suppress atom loss, large detunings from the bound-bound transition were employed, but this limited the tunability of the scattering length  $a$  to  $\Delta a \simeq 2 a_{bg}$ , where  $a_{bg}$  is the background scattering length. In addition, the interaction strength was tuned by changing the intensity of the laser light, which changes the net external potential experienced by the atoms. Cetina et al., [17] avoided this problem by changing the spot size synchronously with the intensity to maintain a constant potential. Clark and coworkers [18] employed a “magic” wavelength approach for  ${}^{133}\text{Cs}$  atoms, by tuning the control beam between the  $D1$

and  $D2$  lines, to suppress the atomic polarizability and hence the change in the external potential, but achieved a tunability of only  $\simeq 0.2 a_{bg}$ . This technique is applicable for well-separated optical transitions, but is not applicable to species such as  ${}^6\text{Li}$ , where the  $D1$  and  $D2$  lines are closely spaced.

Recently, we demonstrated new two-field optical techniques [2, 3], employing EIT [20] in the closed channel to control magnetic Feshbach resonances [21, 22]. Our technique [21] tunes the scattering length near a two-photon resonance, where the loss is at a minimum and tunability of scattering length is at a maximum, in contrast to single-field optical methods [16, 18], where the maximum tunability in the scattering length is associated with maximum loss. Further, our method enables frequency tuning, where changes in one optical frequency by a few MHz (small compared to the detuning  $\approx 1.5$  THz from the atomic resonance), widely tunes the scattering length, with a negligible change in the net external potential experienced by the atoms, making the method broadly applicable.

In this Letter, we report optical frequency tuning of the s-wave scattering length  $a$  near the narrow Feshbach resonance in  ${}^6\text{Li}$ , by up to  $\Delta a \simeq 12 a_{bg}$ , where  $a_{bg} = 62 a_0$  is the background scattering length, with  $a_0$  the bohr radius. We show that our optical method achieves the same tuning range as for magnetic control, which is limited only by the width of the energy distribution, due to the momentum-dependence of the narrow Feshbach resonance [23]. Exploiting this wide tunability, we demonstrate spatial control of interactions by creating an interaction “sandwich”, where the central region of the atomic cloud is resonantly interacting with  $\Delta a > 10 a_{bg}$  and is surrounded by two weakly interacting regions, where  $\Delta a \simeq 1 a_{bg}$ .

Our basic method is shown in Fig 1a. Optical fields  $\nu_1$  (Rabi frequency  $\Omega_1$  and detuning  $\Delta_1$ ) and  $\nu_2$  (Rabi frequency  $\Omega_2$  and detuning  $\Delta_2$ ), couple the ground molecular states of the singlet potential,  $|g_1\rangle$  and  $|g_2\rangle$ , to the

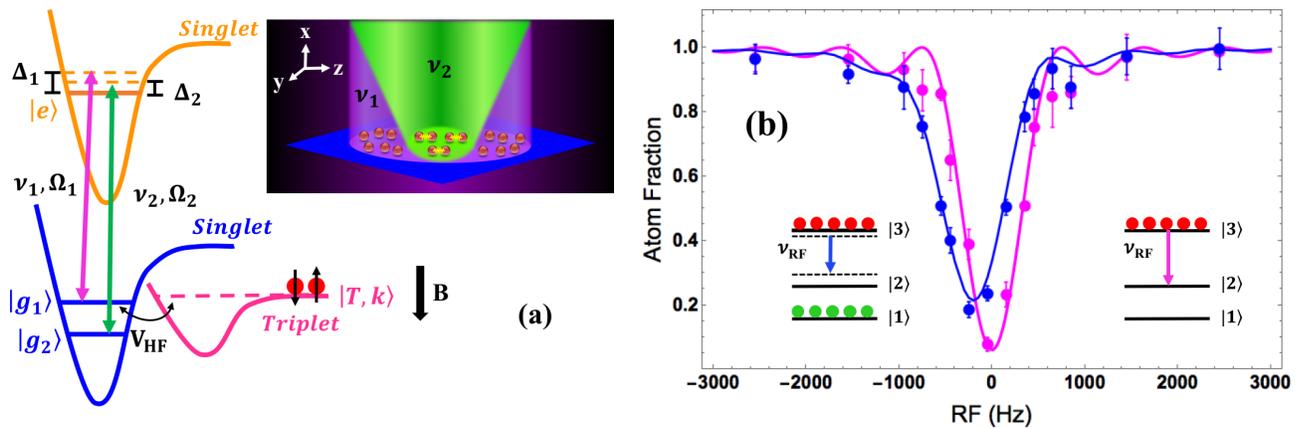


FIG. 1. Basic level scheme to control interactions using electromagnetically induced transparency (EIT). (a) Optical fields  $\nu_1$  (Rabi frequency  $\Omega_1$  and detuning  $\Delta_1$ ) and  $\nu_2$  (Rabi frequency  $\Omega_2$  and detuning  $\Delta_2$ ) couple the ground molecular states  $|g_1\rangle$  and  $|g_2\rangle$  to the excited molecular state  $|e\rangle$  of the singlet potential, allowing precise tuning of the state  $|g_1\rangle$  from below ( $\delta < 0$ ) to above ( $\delta > 0$ ) its unshifted position, where  $\delta = \Delta_2 - \Delta_1$  is the two-photon detuning. Inset shows the optical field arrangement for creating an interaction “sandwich.” The central region of the atomic cloud illuminated by both  $\nu_1$  and  $\nu_2$  beams are resonantly interacting. The outer regions of the atomic cloud illuminated *only* by the  $\nu_1$  beam are weakly interacting. (b) Measuring mean-field interactions using RF spectroscopy. Fraction of atoms remaining in state  $|3\rangle$  by applying an RF  $\pi$  pulse (1.2 ms) to transfer atoms from hyperfine state  $|3\rangle$  to  $|2\rangle$ , obtained with (blue) and without (magenta) atoms present in state  $|1\rangle$ . Solid curves: Predictions (see text).

excited state  $|e\rangle$ , tuning the energy of  $|g_1\rangle$  with suppressed optical scattering [21, 22]. The lowest two hyperfine states in  ${}^6\text{Li}$ ,  $|1\rangle$  and  $|2\rangle$ , have an energy-dependent narrow Feshbach resonance (width  $\Delta B = 0.1$  G) at  $B_{res} = 543.27$  G [23], where the atoms are predominantly in the spin triplet state  $|T, k\rangle$ , which tunes downward with magnetic field  $B$  as  $-2\mu_B B$ , where  $\mu_B$  is the Bohr magneton. The triplet continuum  $|T, k\rangle$  is coupled to state  $|g_1\rangle$  with a second order hyperfine coupling constant  $V_{HF}$ , which causes the narrow Feshbach resonance. For our experiments [24],  $\Omega_1 = 0.5\gamma_e$  and  $\Omega_2 = 2.2\gamma_e$ , where  $\gamma_e = 2\pi \times 11.8$  MHz is the decay rate of the excited molecular state. The detuning  $\Delta_1 = +2\pi \times 19$  MHz. We define the two-photon detuning  $\delta = \Delta_2 - \Delta_1$ , which is varied by changing the frequency of the  $\nu_2$  laser and holding the frequency of  $\nu_1$  laser constant.  $\delta \equiv 0$  is the two-photon resonance corresponding to minimum loss. For  $\delta \equiv 0$ , the state  $|g_1\rangle$  also returns to its original unshifted position. The state  $|g_1\rangle$  is below (above) its unshifted position for  $\delta < 0$  ( $\delta > 0$ ).

We first use radio frequency spectroscopy to demonstrate optical tuning of interactions as a function of the two-photon detuning  $\delta$ . To avoid three body inelastic loss near the narrow  $|1\rangle - |2\rangle$  resonance [23], we initially prepare a  $|1\rangle - |3\rangle$  mixture [24], Fig. 1b, before ramping the magnetic field to  $B = B_{res} + 0.010$  G. Then we apply the  $\nu_2$  beam and wait 50 ms for the atoms to reach equilibrium in the combined potential created by the  $\nu_2$  beam and the  $\text{CO}_2$  laser trap, with a typical Fermi temperature  $T_F = 1.4\mu\text{K}$ . The  $\nu_1$  beam is then applied concurrently with an RF  $\pi$  pulse (1.2 ms) that transfers atoms in state  $|3\rangle$  to the initially empty state  $|2\rangle$ . The

number of atoms remaining in state  $|3\rangle$  is measured by absorption imaging as a function of the radio-frequency. Fig. 1b shows shifted (blue) and unshifted (magenta) RF spectra, obtained with and without atoms in state  $|1\rangle$ , respectively. The unshifted spectrum calibrates the magnetic field. The shifted spectrum is broadened due to the inhomogeneity in the atom density profile and in the intensity of the optical control beams. Fig. 2a (red dots) shows the measured frequency shifts of the RF spectra as a function of two-photon detuning  $\delta$ .

The observed frequency shifts are density dependent and arise from mean-field interactions [23, 25, 26] of atoms in states  $|3\rangle$  and  $|2\rangle$  with atoms in state  $|1\rangle$ , where  $n_1(\mathbf{r})$  is the density. To understand the data, we calculate the local transition probability [24], which depends on the local mean field shift  $\Delta\nu_{MF}$ . For two-body scattering, neglecting atom-atom correlations [27, 28],

$$\Delta\nu_{MF}(\text{Hz}) = \frac{2\hbar}{m} n_1(\mathbf{r}) [a_{13} - \langle a_{12}^{opt}(\nu_2, \Omega_2(z)) \rangle], \quad (1)$$

where  $m$  is the atom mass and  $a_{13} \approx -267a_0$  is the  $|1\rangle - |3\rangle$  s-wave scattering length near 543 G, far from the  $|1\rangle - |3\rangle$  broad Feshbach resonance (width  $\Delta B \approx 122$  G) at 690 G [23, 29].  $\langle a_{12}^{opt} \rangle$  is the real part of the momentum-averaged, optically controlled, two-body scattering amplitude calculated from the continuum-dressed state model [21, 24] for the  $|1\rangle - |2\rangle$  narrow Feshbach resonance. Note that  $\langle a_{12}^{opt} \rangle$  depends on the optical frequencies  $\nu_1, \nu_2$ , the magnetic field  $B$ , and on the Rabi frequencies  $\Omega_1, \Omega_2$ , which are generally position dependent (along  $z$ -in our experiments), enabling spatial control as demonstrated below.

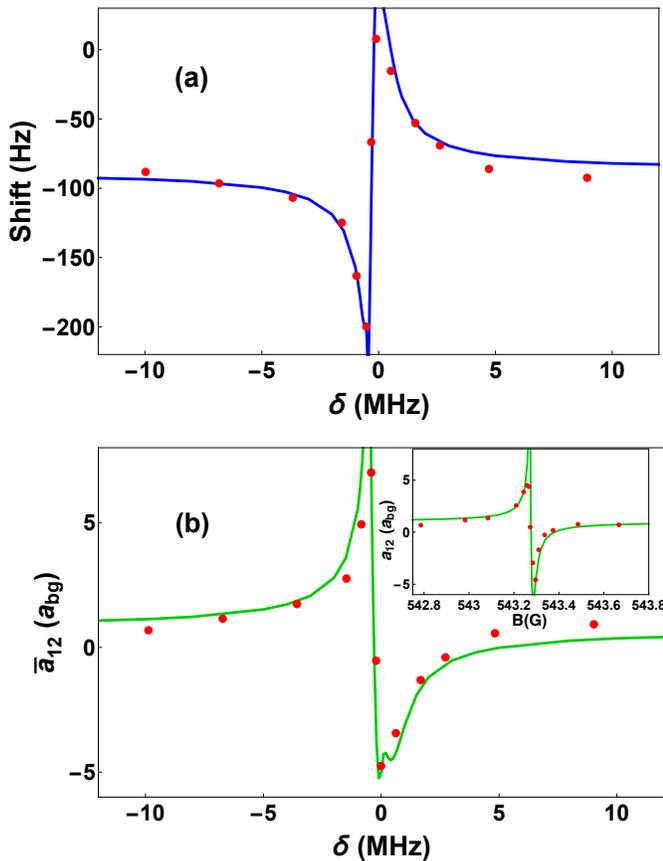


FIG. 2. Optical control of the two-body scattering length near the energy dependent narrow Feshbach resonance of  ${}^6\text{Li}$  at 543.27 G (a) Measured frequency shifts in the rf spectra (red dots) and prediction (blue curve) as a function of two-photon detuning  $\delta$ , by changing  $\nu_2$  and holding  $\nu_1$  constant.  $\delta \equiv 0$  denotes the two-photon resonance. (b) Momentum-averaged scattering length  $\bar{a}_{12}$  (red dots) determined from the measured frequency shifts versus  $\delta$  and prediction (green solid curve). Inset: Magnetically tuned  $a_{12}$ . Note that optical tuning achieves the same range as magnetic tuning.  $a_{bg} = 62 a_0$ .

We predict the spectra from the local probability for a transition from  $|3\rangle$  to  $|2\rangle$ , integrated with the phase space distribution of atoms in the initial state  $|3\rangle$  [24]. The predictions employ the measured Rabi frequencies, atom density, and RF pulse duration, with the temperature, which controls the momentum distribution, as the only adjustable parameter. For  $T = 1.0 \mu\text{K}$ , the predicted frequency shifts, shown as the solid blue curve for in Fig. 2a, are in excellent agreement with the measurements. The error bars on the data points, estimated from the fluctuations in the magnetic field and optical frequencies, are negligible compared to the statistical error, which is smaller than the point size.

The predicted two-body scattering length at  $z = 0$ , Fig. 2b green curve, is evaluated from  $\langle a_{12}^{opt}(\nu_2, \Omega_2(z)) \rangle$  in Eq. 1, which was used to generate the predicted mean-

field frequency shifts in Fig. 2a. For comparison, we use a simple approximation to extract the scattering length  $\bar{a}_{12}$  at  $z = 0$ , from each of the measured frequency shifts in Fig. 2a. The  $\bar{a}_{12}$ , displayed as red dots in Fig. 2b, are obtained by assuming  $\Delta\nu_{meas} = \frac{2\hbar}{m} \bar{n}_1 (a_{13} - \bar{a}_{12})$ , where  $\bar{n}_1$  is a fitting parameter. We determine  $\bar{n}_1$  by comparing the measured mean-field shifts with the predictions at large detunings, where the tunability of the scattering length is small. We find  $\bar{n}_1 = 1.5 \times 10^{11} \text{ cm}^{-3}$  [24]. As expected,  $\bar{n}_1$  is smaller than the typical mean density in the experiments,  $\bar{n} = 2.0 \times 10^{11} \text{ cm}^{-3}$ , since the predicted scattering length is largest at  $z = 0$ .

Fig. 2b shows that changing the frequency  $\delta$  by just a few MHz tunes the two-body scattering length between  $+7 a_{bg}$  (BEC side of resonance) and  $-5 a_{bg}$  (BCS side), the same range as obtained by magnetic tuning without optical fields, Fig. 2b (Inset). As noted previously [23], for a narrow resonance, the effective range is large, i.e., the maximum scattering length is limited by small width  $\simeq 0.1\text{G}$  and the energy spread, i.e.,  $|a_{\text{max}}/a_{bg}| \simeq 2\mu_B \Delta B / \Delta E \simeq 10$  for the conditions of our experiment.

We demonstrate spatial control of two-body interactions by using the scheme of Fig. 1(Inset), where the spot sizes of the control fields are made large enough [24] to enable in-situ images of the spatially controlled interaction profiles, as shown in Fig. 3. The two-photon detuning  $\delta$  is employed as a control parameter to change the interaction spatial profiles. After illuminating the atoms with the  $\nu_1$  and  $\nu_2$  beams, we apply an RF  $\pi$  pulse (1.2 ms) that transfers atoms from the initial state  $|3\rangle$  to state  $|2\rangle$ , in the presence of atoms in state  $|1\rangle$ . The frequency of the RF pulse is chosen to be resonant for  $\delta = \pm 10$  MHz, where the entire cloud is weakly interacting.

Measured 2D absorption images of the atoms that arrive in state  $|2\rangle$  are shown in Fig. 3a as a function of  $\delta$ , where  $\nu_2$  is varied and  $\nu_1$  is held constant. The corresponding 1D axial profiles are shown in Fig. 3c (blue). The transferred fraction of atoms in state  $|2\rangle$  depends on the spatially varying, optically controlled  $|1\rangle - |2\rangle$  scattering amplitude. Fig. 3d shows the two-body scattering length  $a_{12}^{opt}(z)$  used to generate the predicted 1D spatial profiles (red curves in Fig. 3c) and the predicted 2D absorption images in Fig. 3b [24].

Excellent quantitative agreement is obtained between the measured (blue) and the calculated (red) 1D axial profiles, Fig. 3c. For the predictions, we again use the measured density and optical field parameters, and adjust the temperature, which determines the momentum distribution to be  $T = 1.0 \mu\text{K}$ , the same as for Fig. 2. The asymmetry in the 1D profiles for  $\delta = -0.64$  MHz and  $\delta = -0.54$  MHz is due to the off-center position of the  $\nu_2$  beam, which is taken into account in generating the calculated 1D profiles.

At  $\delta = -0.64$  MHz, we create an interaction “sandwich,” where the central region of the atomic cloud is res-

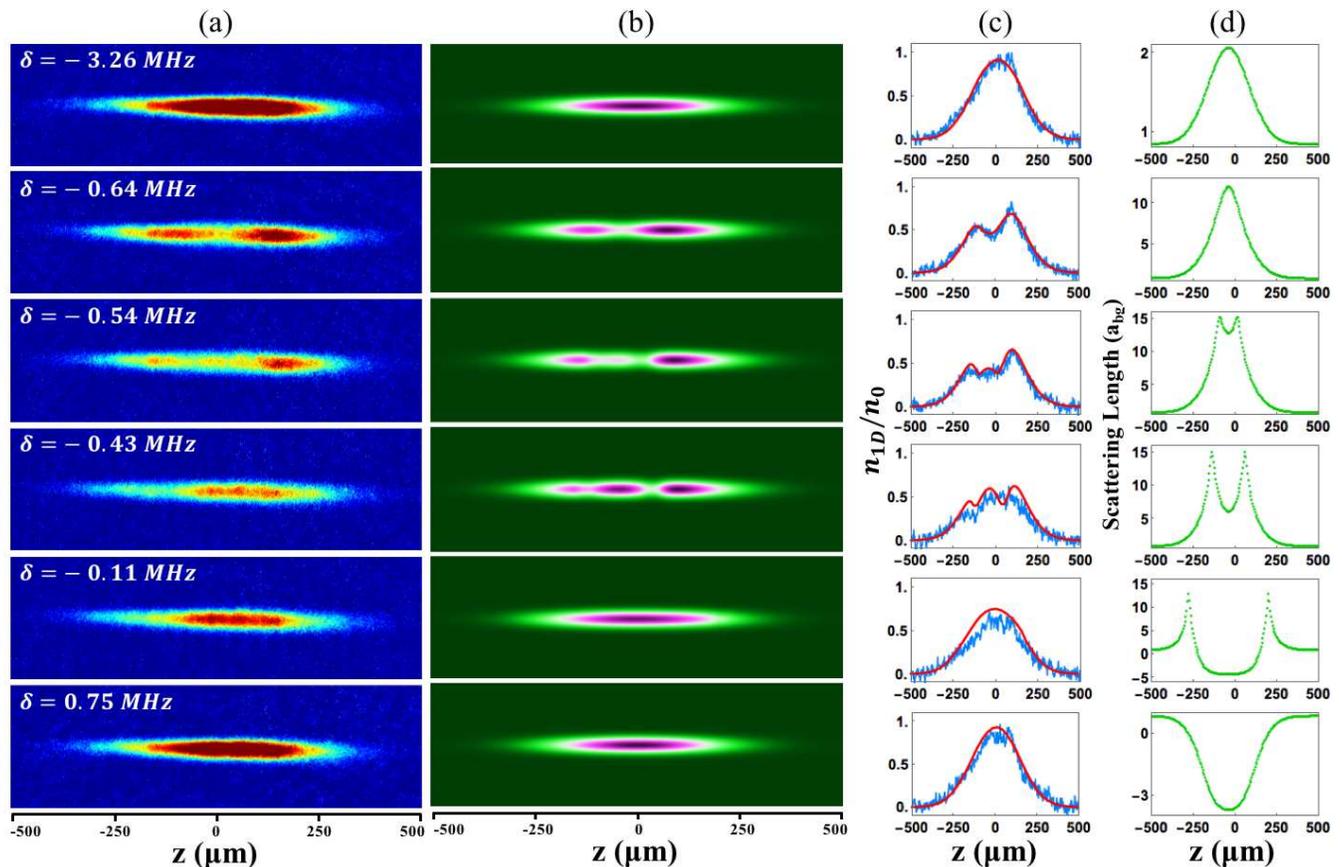


FIG. 3. Designer interaction patterns in an ultracold gas of  ${}^6\text{Li}$  atoms versus two-photon detuning  $\delta$ , with  $\delta \equiv 0$  at the two-photon resonance. (a) Measured false color 2D absorption images of atoms arriving into  $|2\rangle$  after transfer from state  $|3\rangle$  by a 1.2 ms RF  $\pi$  pulse, in the presence of atoms in state  $|1\rangle$ . (b) Predicted 2D images using measured parameters [24]; (c) Normalized 1D axial profiles  $n_{1D}/n_0$ , where  $n_0$  is the peak density with no atoms in state  $|1\rangle$ . Measured (blue) and calculated (red); (d) Momentum averaged two-body scattering length  $a_{12}^{opt}$  used to generate the predicted 2D and 1D spatial profiles.

onantly interacting with  $a_{12} \approx 12 a_{bg}$  and is enclosed by two weakly interacting regions with  $a_{12} \approx 1 a_{bg}$  (Fig. 3d). This is evident from the measured 2D profile in (Fig. 3a), where the fraction of atoms transferred to state  $|2\rangle$  in the central region of the cloud is heavily suppressed, due to the large frequency shift arising from resonant interactions. The measured suppression is not due to atom loss, as we observe that atoms remain in the initial state  $|3\rangle$ , when they are not transferred to state  $|2\rangle$ .

We see that a small frequency change from  $\delta = -0.64$  MHz to  $\delta = -0.43$  MHz, inverts the interaction “sandwich” by making the central region more weakly interacting than the wings of the atomic cloud, resulting in increased transfer near the center, Fig. 3a. Although the sign of the interaction is not directly evident in the 2D profiles, the predicted scattering amplitude, Fig. 3d, shows that we can invert the sign of the 1-2 scattering length between the central and the outer regions of the cloud. For  $\delta = -0.11$  MHz, the interactions in the central region become attractive with  $a_{12} \approx -5 a_{bg}$

and the interactions in the wings become repulsive with  $a_{12} \approx 10 a_{bg}$ . As  $\delta$  is tuned from below the two-photon resonance,  $\delta = -3.26$  MHz, to above the two-photon resonance,  $\delta = +0.75$  MHz, the interactions in the central region of the cloud changes sign from repulsive to attractive [24]. We see that a  $\delta$  tuning range of just 4 MHz imprints widely different interaction “designs” on the atomic cloud.

Previous experiments demonstrating spatial control of interactions either suffered from extremely short (10  $\mu\text{s}$ ) lifetimes [15] or limited optical tunability,  $0.15 a_{bg}$  [18]. Further, all-optical manipulation of spatial interaction profiles has not been previously demonstrated. The two-field EIT method demonstrated here provides a robust, frequency tunable method for spatio-temporal control of interactions with negligible change the net confining potential. For the time scale (1.2 ms) and densities used in our optical control experiments, the atom loss due to spontaneous scattering is negligible [24], making this method ideal for studies of local non-equilibrium dynam-

ics on time scales fast compared to the Fermi time [6, 17],  $\tau_F \simeq \hbar/E_F \simeq 10 \mu\text{s}$  for  $E_F = 5 \mu\text{K}$  and for studies of resonantly interacting Bose gases, which exhibit hydrodynamic flow and achieve local equilibrium on ms time scales [30].

Our method has broad applications, creating new fields of study in ultracold gases. For example, one can imprint an interaction superlattice, where interactions between atoms at different lattice sites are independently controlled and manipulated with minimum scattering loss, permitting studies of “collisionally inhomogenous” systems [31]. Further, a momentum selective extension of our method has been suggested as a means for realizing synthetic Fulde-Ferrell superfluids, where resonant interactions and atom pairing occur at finite momentum, with suppressed optical loss [4, 5].

This research is supported by the Physics Divisions of the Air Force Office of Scientific Research and the National Science Foundation. Additional support is provided by the Army Research Office and the Division of Materials Science and Engineering, the Office of Basic Energy Sciences, Office of Science, U.S. Department of Energy.

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