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Phys. Rev. Lett. 121, 227003 — Published 29 November 2018
DOI: 10.1103/PhysRevLett.121.227003
Orbital selectivity enhanced by nematic order in FeSe

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Motivated by the recent low-temperature experiments on bulk FeSe, we study the electron correlation effects in a multiorbital model for this compound in the nematic phase using the U(1) slave-spin theory. We find that a finite nematic order helps to stabilize an orbital selective Mott phase. Moreover, we propose that when the d- and s-wave bond nematic orders are combined with the ferro-orbital order, there exists a surprisingly large orbital selectivity between the xz and yz orbitals even though the associated band splitting is relatively small. Our results explain the seemingly unusual observation of strong orbital selectivity in the nematic phase of FeSe, uncover new clues on the nature of the nematic order, and set the stage to elucidate the interplay between superconductivity and nematicity in iron-based superconductors.

Introduction. The iron-based superconductors (FeSCs) present a topic of extensive current research in condensed matter physics [1–6]. One characteristic feature of these materials is that multiple electronic 3d orbitals are important for their electronic structure. With the electron-electron interactions in these multiorbital systems, the entwined degrees of freedom generate a very rich phase diagram with a variety of correlation-induced electronic orders [2–6].

Besides the overall effect of electron correlations [7–11], the multiple orbitals in the FeSCs may possess different degrees of correlation effects. Such an orbital selectivity has been found in multiorbital models for FeSCs [12–15]. Due to the kinetic hybridization between the different orbitals in these models, this effect is surprising and to be contrasted [16, 17] with what happens when the orbitals do not mix with each other [18–22]. It has been shown that the Hund’s coupling helps to stabilize an orbital-selective Mott phase (OSMP) inside which the Fe 3d_{xy} orbital is Mott localized while the other orbitals are still itinerant [13]. Many iron chalcogenides and pnictides appear to be close to the OSMP in the phase diagram, and can be driven into this phase by doping, applying pressure, or varying temperature [23–31].

Another important aspect of the multiorbital effect in FeSCs is associated with the nematic order. In most of the undoped iron pnictides, there is a structural transition from a tetragonal phase to an orthorhombic one with lowering the temperature. Right at or slightly below the structural transition temperature, the system develops a long-range (π, 0) antiferromagnetic (AFM) order. The superconductivity usually appears near this antiferromagnetic phase. In between the structural and the magnetic transitions the C4 lattice rotational symmetry is broken, and the system is in a nematic phase. The origin of this nematic phase is still under debate. In the spin-driven-nematicity scenario, the nematicity is associated with an Ising order characterizing the anisotropic antiferromagnetic fluctuations [32–35] or the antiferroquadrupolar ones [36]. The corresponding bond nematicity may have different forms, such as d- or s-wave nearest neighbor bond nematic orders [37]. On symmetry grounds, this bond nematicity is linearly coupled to a ferroorbital order that lifts the degeneracy of the Fe d_{xz} and d_{yz} orbitals. Thus, a ferroorbital order is also expected to be present. Interestingly, recent angle-resolved photoemission spectroscopy (ARPES) measurements on a variety of FeSCs observed a momentum dependent splitting between the xz and yz orbital dominant bands, which suggests the coexistence of several different nematic orders [38–40].

Among the FeSCs, FeSe is one of the most fascinating compounds. The single-layer FeSe on the SrTiO3 substrate holds the record of the highest superconducting transition temperature of the FeSCs [41]. On the other hand, the bulk FeSe has a structural transition at T_s = 90 K without showing an AFM long-range order down to the lowest accessible temperature under ambient pressure, suggesting an unusual magnetism in the ground state [36]. In the nematic phase, ARPES measurements find a momentum dependent splitting between the xz and yz-orbital dominant bands with small splittings at both Γ and M points of the Brilluion zone (BZ) [38, 42]. Recent scanning tunneling microscopy (STM) experiments have revealed a strong orbital selectivity [43, 44]. Especially, the estimated ratio of the quasiparticle weights between the yz and xz orbitals is very large: Z_{yz}/Z_{xz} ∼ 4. Because the band splittings are relatively small [38, 42], such a strong orbital selectivity is surprising [45]. It is important to resolve this puzzle, given that both the nematic correlations and orbital selectivity may be of broad interest to unconventional superconductivity in the iron-based materials and beyond.

In this Letter, we examine the electron correlation effects in a multiorbital Hubbard model for the nematic phase of FeSe using previously developed U(1) slave-spin
theory [46]. We consider three types of nematic orders, a ferro-orbital order, a $d$-wave nearest-neighbor bond order, and an $s$-wave nearest-neighbor bond order, and analyze their effects on the orbital selectivity. We solve the saddle-point equations and show that the OSMP is promoted by any of these nematic orders. This effect is delicate, because we also find that the full Mott localization of the system depends on the type and strength of the nematic order. Remarkably, we find that, by taking a proper combination of the three types of nematic order, the system can exhibit a strong orbital selectivity with comparable strength implies that the nematicity in FeSe [43, 44], thereby setting the stage to understand the superconducting state in this compound. More generally, the necessity of coexisting nematic orders with comparable strength implies that the nematicity in the FeSCs can not be entirely driven by the orbital order, thereby providing new clues to the origin of the nematicity in FeSCs.

Model and Method. We study a five-orbital Hubbard model for FeSe. The Hamiltonian reads as

$$H = H_{TB} + H_{nem} + H_{int}.$$ 

(1)

$H_{TB}$ is a five-orbital tight-binding Hamiltonian with tetragonal lattice symmetry,

$$H_{TB} = \frac{1}{2} \sum_{ij,\alpha\beta} t_{ij}^{\alpha\beta} d_{i\alpha\sigma}^\dagger d_{j\beta\sigma} + \sum_{i\alpha\sigma} (\epsilon_\alpha - \mu) d_{i\alpha\sigma}^\dagger d_{i\alpha\sigma},$$

(2)

where $d_{i\alpha\sigma}^\dagger$ creates an electron in orbital $\alpha$ ($\alpha = 1, ..., 5$ denoting $xz$, $yz$, $x^2 - y^2$, $xy$, and $3z^2 - r^2$ orbitals, respectively) with spin $\sigma$ at site $i$, $\epsilon_\alpha$ refers to the energy level associated with the crystal field splitting (which is diagonal in the orbital basis), and $\mu$ is the chemical potential. The tight-binding parameters $t_{ij}^{\alpha\beta}$ and $\epsilon_\alpha$, which are presented in the Supplemental Material (SM) [47], are determined by fitting to DFT bandstructure for FeSe, and we specify $\mu$ to fix the total electron density to 6 per Fe. The onsite interaction $H_{int}$ reads

$$H_{int} = \frac{U}{2} \sum_{i,\alpha,\sigma} n_{i\alpha\sigma} n_{i\alpha\bar{\sigma}} + \sum_{i,\alpha<\beta,\sigma} \{U' n_{i\alpha\sigma} n_{i\beta\bar{\sigma}} + (U' - J_H) n_{i\alpha\sigma} n_{i\beta\sigma}

- J_H (d_{i\alpha\sigma}^\dagger d_{i\alpha\bar{\sigma}} d_{i\beta\bar{\sigma}} d_{i\beta\sigma} + d_{i\alpha\sigma}^\dagger d_{i\alpha\bar{\sigma}} d_{i\beta\sigma} d_{i\beta\bar{\sigma}})\}.$$ 

(3)

where $n_{i\alpha\sigma} = d_{i\alpha\sigma}^\dagger d_{i\alpha\sigma}$. Here, $U$, $U'$, and $J_H$ respectively denote the intraoorbital repulsion, the interorbital repulsion, and the Hund’s rule coupling, and we take $U' = U - 2J_H$ [55]. To study the model in the nematic phase, we introduce bare nematic orders in the $xz$ and $yz$ orbital subspace into $H_{nem}$. In the momentum space

$$H_{nem} = \sum_{k} (-2\delta_d (\cos k_x - \cos k_y)(n_{k1} + n_{k2}) - 2\delta_s (\cos k_x + \cos k_y)(n_{k1} - n_{k2}) + \delta_f (n_{k1} - n_{k2}))$$

(4)

Here, besides the ferro-orbital order ($\delta_d$) we have also taken into account a $d$- and an $s$-wave bond nematic order ($\delta_s$ and $\delta_f$), which corresponds to nearest-neighbor hopping anisotropy. [37]

We investigate the electron correlation effects by using a $U(1)$ slave-spin theory [46]. In this approach, we rewrite $d_{i\alpha\sigma}^\dagger = S_{i\alpha\sigma}^+ f_{i\alpha\sigma}^\dagger$, where $S_{i\alpha\sigma}^+$ ($f_{i\alpha\sigma}^\dagger$) is the introduced quantum $S = 1/2$ spin (fermionic spinon) operator to carry the charge (spin) degree of freedom of the electron at each site. For a general multiorbital model three saddle-point solutions can be stabilized: a metallic state with the quasiparticle spectral weight $Z_\alpha > 0$ in all orbitals, a Mott insulator with $Z_\alpha = 0$ in all orbitals, and an OSMP with $Z_\alpha = 0$ in some orbitals but $Z_\alpha > 0$ in other orbitals. In the metallic state, a significant effect of the electron correlations is that the electron bandstructure is renormalized by $Z_\alpha$ and the effective onsite potential $\mu_\alpha$ [47]. We are particularly interested in how the band splittings between the $xz$- and $yz$-dominant bands at $\Gamma$ and $M$ points of the BZ ($\Delta E_\Gamma$ and $\Delta E_M$) evolves with interaction $U$ and nematic order $\delta_\alpha$ ($\alpha = f, d, s$). Keeping in mind the aim of understanding the effect of nematicity on the orbital selectivity, we simplify our analysis by focusing on the diagonal part of $J_H$ (SM, end of the 2nd section [47]).

Phase diagram in the tetragonal phase. We first examine the correlation effects in the tetragonal phase. The ground-state phase diagram in the $J_H-U'$ plane is shown in Fig. 1(a). It contains three phases: a metal, a MI, and a strongly correlated metal (SCM). Here, besides the ferro-orbital order ($\delta_d$) we have also taken into account a $d$- and an $s$-wave bond nematic order ($\delta_s$ and $\delta_f$), which corresponds to nearest-neighbor hopping anisotropy. [37]

The threshold for FeSe is only stabilized above the structural transition. As shown in Fig. S3 of the SM [47], the threshold $U$ value for the orbital-selective Mott transition (OSMT) decreases with increasing temperature. Thus, for $T \gtrsim 90$ K in the tetragonal phase, the system may already be close to the boundary of the OSMP.

Enhanced orbital selectivity in the nematic phase. We turn next to how the nematicity influences electron cor-
relations. Fig. 2(a) shows how the phase diagram varies with the bare ferro-orbital order $\delta_f$ at $J_H/U = 0.25$. The phase boundaries change very little for $\delta_f \lesssim 0.2$ eV (see also Fig. 2(b)). Further increasing $\delta_f$, $U^*$ slightly increases. This is because $U^*$ corresponds to an energy scale for the overall correlation effect, where a high-spin $S \sim 2$ state is approximately formed.\cite{footnote13} By increasing $\delta_f$, the $d_{xz}$ and $d_{yz}$ orbitals are driven away from half-filling. Therefore, a larger $U$ value is needed to push these orbitals back to being close to half-filling to form the high-spin state. On the other hand, the critical $U$ for the OSMT significantly decreases, indicating an enhancement of orbital selectivity by the nematic order. This can be understood as follow: For a small $\delta_f$, the electron densities at $U = 0$ in all three $t_{2g}$ orbitals are close to half-filling (Fig.S4). But for a large $\delta_f$, since it lifts the $xz/yz$ orbital degeneracy, the electron densities $n_{xz}$ and $n_{yz}$ are highly different and away from half-filling, but $n_{xy}$ still is close to half-filling at $U = 0$ (Fig.S5). This makes the Mott localization of the $xy$ orbital much easier for large $\delta_f$. However, the critical $U$ for the full Mott localization first increases with $\delta_f$ then decreases for $\delta_f \gtrsim 0.5$ eV. For small $\delta_f$, the $xz/yz$ orbitals are nearly degenerate, and a splitting between them effectively increases the total bare bandwidth, making the Mott localization of all orbitals harder. But further increases $\delta_f$, the center of the $yz$ band is shifted much lower than the other four. With a moderate $U$, it can be driven to a band insulator. Once this takes place, the other bands would be at half-filling, which is known to be the easiest to be Mott localized than at any other commensurate filling.

We also analyze the effects of the two bond nematic orders on the Mott localization, and find that the enhancement of orbital selectivity is a general feature (Fig.S6), but a MI is disfavored. In the tight-binding model for FeSe \cite{footnote47}, the nearest-neighbor hoppings along the $\hat{x}$ and $\hat{y}$ directions within the $xz$ orbitals (also within the $yz$ orbitals), $t_{11}^{xz(\hat{x})}$ and $t_{22}^{yz(\hat{y})}$ are highly anisotropic. In particular, $t_{11}^{xz} = t_{22}^{yz} \approx 0$. Hence either a $d$- or an $s$-wave bond nematic order will enhance the kinetic energy associated with the $xz$ and $yz$ orbitals. This increases the orbital selectivity, promoting an OSMP. But the overall bandwidth is also increased, and therefore destabilizes a MI.

**Orbital selectivity and band splitting.** The nematic order not only helps stabilizing an OSMP by Mott localizing the $xy$ orbital, but also enhances the orbital selectivity between the $xz$ and $yz$ orbitals. As shown in Fig. 2(b), the $xz$ orbital is more correlated than in the tetragonal
phase, while the $yz$ orbital is less so. The ratio $Z_{yz}/Z_{xz}$ increases with $\delta_f$ monotonically. As mentioned earlier, recent STM experiments have observed $Z_{yz}/Z_{xz} \sim 4$ in the nematic phase of FeSe [43, 44].

In the case of a single bare ferro-orbital order, $\delta_f$ must be larger than 0.4 eV to arrive at such a large ratio within a reasonable range of $U$ (See Fig. S7). This leads to the band splittings $\Delta E_F$ and $\Delta E_M$ higher than 100 meV, which is much larger than the observed values ($\lesssim 50$ meV). [38–40, 56] Similar issue applies to the bond nematic orders alone (Fig. S7). Thus, it is seemingly impossible to reconcile the contrasting properties as observed in STM and ARPES, respectively.

To make progress, we consider a combination of the three nematic orders. An observation of Eq. (4) is that the bare band splittings at both $\Gamma$ and M points will be exactly canceled when taking $\delta_f/4 = \delta_d = \delta_s$ (see SM [47]). For definiteness, we simply take this combined nematic order. As shown in Fig. 3, for $U \sim 3.5$–4 eV, such a combined nematic order gives $Z_{yz} \approx 0.5$, $Z_{xz} \approx 0.15$, and $Z_{xy} \approx 0.05$, close to the experimentally determined values. Moreover, though the electron correlations renormalize the band splittings, the cancelation effect is still prominent: The band splittings $\Delta E_F$ and $\Delta E_M$ are less than 50 meV; this result is fully consistent with the ARPES results.

We further show how the orbital selectivity and band splitting evolve with this combined nematic order in Fig. 4. We find it quite remarkable that a large orbital selectivity ($Z_{yz}/Z_{xz}$) while, at the same time, a small band splitting is stabilized by a moderate (bare) combined nematic order.

**Discussions.** With a single nematic order alone, to keep the band splittings $\Delta E_F$ and $\Delta E_M$ to be compatible to the observed values ($< 50$ meV), we find that the bare nematic order must be small, leading to a weak orbital selectivity in the $xz$ and $yz$ sector with $Z_{yz}/Z_{xz}$ close to 1. This is consistent with a previous study [45]. Our calculations, however, have demonstrated a new effect: with a proper combination of the bond nematic orders and the ferro-orbital order, the band splittings at $\Gamma$ (and M) point caused by the different nematic orders compensate. In this way, moderate bare nematic orders can give rise to a strong orbital selectivity with $Z_{yz}/Z_{xz} \sim 4$, while keeping the band splittings near the Fermi level small at both $\Gamma$ and M points of the BZ. This result is robust against nematic quantum fluctuations, given that the system is not close to a nematic quantum critical point even though the band splittings are small. The large orbital selectivity manifests the effect of electron correlations. The latter is also implicated by the fact that the anisotropy in the optical conductivity induced by the nematic order extends to a large energy range, all the way to about 0.5 eV (i.e., about 50 times of $k_B T_s$) [57].

The necessity that all the three types of nematic orders coexist implies that the nematic order observed in FeSCs has an unconventional origin and can not be entirely driven by orbital order. In the spin driven nematicity, the nematic order is just an Ising order associated with short-range antiferromagnetic or antifer-
roquadrupolar orders within an effective frustrated spin model including short-range Heisenberg and quadratic ice interactions. Within this scenario, it is expected that the nearest-neighbor bond nematic order, together with the linearly-coupled ferro-orbital order, contribute significantly in the nematic phase [58], leading to a combined nematic order. Our results thus suggest that the nematicity in FeSCs likely has a magnetic origin.

Conclusions. We have studied the effects of electron correlation with a nematic order in a multiorbital Hubbard model for FeSe by using the slave-spin method. We show that the orbital selectivity is generally enhanced by the nematic order. A large combined nematic order can give rise to a large orbital selectivity in the \(xz/yz\) orbital subspace with a small band splitting. Our results resolve an outstanding puzzle in the recent experimental observations on the orbital selectivity and nematicity in FeSe, elucidate the nature and origin of the nematic order in FeSCs, and pave the way for understanding the interplay between nematicity and high temperature superconductivity.

We thank E. Abrahams, E. Bascones, P. C. Dai, H. Hu, D. H. Lu, M. Yi, and X.-J. Zhou for useful discussions. This work has in part been supported by the National Science Foundation of China Grant numbers 11674392 and Ministry of Science and Technology of China, National Program on Key Research Project Grant number 2016YFA0300504 (R.Y.), and by the U.S. Department of Energy, Office of Science, Basic Energy Sciences, under Award No. DE-SC0018197, the Robert A. Welch Foundation Grant No. C-1411 and a QuantEmX grant from ICAM and the Gordon and Betty Moore Foundation through Grant No. GBMF5305 (Q.S.), and by the U.S. DOE Office of Basic Energy Sciences E3B7 (J.-X.Z.). The work was supported in part by the Center for Integrated Nanotechnologies, a U.S. DOE BES user facility. Q.S. acknowledges the hospitality of University of California at Berkeley and of the Aspen Center for Physics (NSF grant No. PHY-1607611).

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[47] See Supplemental Material [http://link...] for details on the tight-binding parameters of the model, the U(1) slave spin theory, and analysis on the band splittings and orbital selectivity, which include Refs. [48–54].