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Interlayer Couplings Mediated by Antiferromagnetic Magnons

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Collinear antiferromagnets (AFs) support two degenerate magnon excitations carrying opposite spin polarizations, by which magnons can function as electrons in various spin-related phenomena. In an insulating ferromagnet(F)/AF/F trilayer, we explore the magnon-mediated interlayer coupling by calculating the magnon thermal energy in the AF as a function of the orientations of the Fs. The effect manifests as an interlayer exchange interaction and a perpendicular magnetic anisotropy; they both depend on temperature and the AF thickness. In particular, the exchange interaction turns out to be antiferromagnetic at low temperatures and ferromagnetic at high temperatures, whose magnitude can be $10 \sim 100 \mu\text{eV}$ for nanoscale separations, allowing experimental verification.

An emerging thrust in the broad field of magnonics [1] has been the investigation of collinear antiferromagnets (AFs) as promising candidate materials. This is ascribed to an appealing feature unique to collinear AFs: magnon excitations always come up with two degenerate modes as a consequence of symmetry [23]. The two modes carry opposite spin polarizations and form an intrinsic degree of freedom, which enables antiferromagnetic magnons to function as active information carriers in replacement of electrons [3–5]. For example, a longitudinal temperature gradient can drive magnons with opposite spins to opposing transverse edges in layered transition metal trichalcogenides [6–8], realizing a magnonic analogue of the spin Hall effect. Very recently, we have proposed that antiferromagnetic magnons can be utilized to induce magnetic switching in a ferromagnet (F)/AF/F heterostructure [9], paving the way towards all-magnonic memory devices. These studies have demonstrated the exciting possibility of exploiting antiferromagnetic magnons to fulfill tasks that used to be exclusive to electrons.

In spite of tremendous recent progress, the knowledge we have acquired so far refers largely to the transport property, namely, magnon spin currents generated by external stimuli [10, 11]. As for the static property, on the other hand, it remains unexplored whether the analogy between antiferromagnetic magnons and electrons still holds. In particular, when two Fs are separated by an *insulating* thin-film AF, will magnons in the AF mediate non-local interactions between the Fs? Here, magnons are supposed to play the role of conduction electrons in the non-magnetic metal (NM) layer of a F/NM/F sandwich [12–15]. This problem becomes especially important if at least one of the Fs is also insulating so that electron tunneling [16, 17] across the AF is absent.

To address the above issue, we study in this Letter a F/AF/F trilayer structure with exchange-coupled interfaces. We extract the effective interlayer coupling by computing the magnon thermal energy inside the AF as a function of the relative orientation of the two Fs at different AF thicknesses and temperatures. To avoid ambiguity, we only consider insulating magnets so that

conduction electrons are eliminated. We allow the AF to have multi-domains in the lateral dimensions but domain boundaries do not exist in the thickness direction [9], which is true for epitaxially grown films. While the F/AF interface is exchange-coupled, we exclude the exchange bias (EB) effect in this Letter since our predictions can be viewed as additional effects on top of the EB. Moreover, it is experimentally possible to suppress the EB to a negligible level with proper materials choice and careful control of film growth [18].

Let the thickness direction be z and the transverse dimensions be labeled by x and y . Within each domain, translational symmetry is respected along x and y so the in-plane wave vector $\mathbf{k}_{\parallel} = \{k_x, k_y\}$ is a good quantum number. To better associate the phenomenology to the antiferromagnetic character, we only consider a G-type AF with simple cubic lattice and compensated interfaces. One can easily show that an A-type AF or a complicated bipartite lattice can only introduce quantitative differences, leaving the essential physics unaltered.

Model.—We assume that the Curie temperature of the Fs far exceeds the Néel temperature of the AF, which is typically the case for insulating Fs and AFs. As a result, when working below the Néel temperature, we ignore magnon excitations in the Fs and focus only on magnons in the AF, treating the two Fs as boundary conditions practically independent of temperature. For a specified domain with collinear ground state, the AF is characterized by the spin Hamiltonian

$$H_{\text{AF}} = J_{\text{AF}} \sum_{\langle ij \rangle} \mathbf{s}_i \cdot \mathbf{s}_j + K_{\text{AF}} \sum_i (\hat{\mathbf{e}} \cdot \mathbf{s}_i)^2, \quad (1)$$

where \mathbf{s}_i is the local spin vector on site i , $J_{\text{AF}} > 0$ is the Heisenberg exchange interaction, $K_{\text{AF}} < 0$ is the anisotropy constant, $\hat{\mathbf{e}}$ is the local easy-axis (uniform inside a given domain), and $\langle ij \rangle$ denotes nearest neighbor links. On the interfaces, the coupling between F and AF is represented by

$$H_{\text{int}} = J_{\text{int}} \sum_{i;I} \mathbf{s}_i \cdot \mathbf{S}_I, \quad (2)$$

where \mathbf{S}_I ($I = 1, 2$) are the unit magnetization vectors of the Fs and J_{int} is the interfacial exchange coupling connecting the AF to the adjacent F. In the following, we normalize energies and temperature $k_B T$ to J_{AF} , which is the largest energy scale in the system. In particular, we set $K_{\text{AF}}/J_{\text{AF}} = -0.05$ [19] and let $\xi = J_{\text{int}}/J_{\text{AF}}$ be the dimensionless interfacial coupling (ξ is tunable). The sign of ξ does not matter since the magnon-mediated interactions turn out to be scaled as ξ^2 .

Using the Holstein-Primakoff transformation [20], we can recast the total Hamiltonian $H = H_{\text{AF}} + H_{\text{int}}$ in a tight-binding model [6] that parametrically depends on \mathbf{S}_1 and \mathbf{S}_2 . Then magnons are similar to particles confined in a quantum well. For a given configuration of \mathbf{S}_1 and \mathbf{S}_2 , *i.e.*, boundary conditions, the magnon spectrum is solved as $\varepsilon_i(\mathbf{k}_{\parallel})$ with discretized i and continuous \mathbf{k}_{\parallel} . The internal energy of the AF consists of thermal excitations of all magnon bands obeying the Bose-Einstein distribution. Consequently, $U = U(\mathbf{S}_1, \mathbf{S}_2)$ is also a function of \mathbf{S}_1 and \mathbf{S}_2 , which tells the effective interactions between the two Fs. However, bilayer effects associated with each individual F/AF interface also contribute to U . In order to separate the desired interlayer coupling (a trilayer effect) from U , we must compare an F/AF bilayer with an F/AF/F trilayer as illustrated in Fig. 1. The difference between the two cases can be attributed to the effective interlayer coupling after an overall energy shift is disregarded.

Results.—Let us consider a simple circumstance where the AF is single domain with an in-plane Néel vector, and the free F (\mathbf{S}_1) is restricted to rotate in the plane. In the trilayer case, a bottom F (\mathbf{S}_2) is added and fixed parallel to the Néel vector. So in both cases [Fig. 1 (a) and (b)] the internal energy U has a single argument ϕ . Thermodynamically, the amount of change in $U(\phi)$ by varying ϕ is regarded as the work done by the free F on the AF. By symmetry, $U(\phi)$ can be expanded as

$$\text{Bilayer: } U_B(\phi) = U_0 + \sum_{n=1}^{\infty} \mathcal{K}_n \cos 2n\phi, \quad (3)$$

$$\text{Trilayer: } U_T(\phi) = U'_0 - \sum_{n=1}^{\infty} J_n \cos n\phi, \quad (4)$$

where U_0 and U'_0 are two reference energies that do not concern us here. In U_B , we interpret \mathcal{K}_n as a series of magnon-induced anisotropies. The ϕ -dependent part the energy difference $\Delta U = U_T - U_B$ is characterized by J_n ($n \in \text{odd}$) and $\tilde{J}_n = J_n + \mathcal{K}_{n/2}$ ($n \in \text{even}$), which we interpret as the magnon-mediated interlayer couplings. To fit those parameters, we numerically compute $U(\phi)$ by summing over all energy bands $\varepsilon_i(\phi, \mathbf{k}_{\parallel})$ as

$$U(\phi) = \sum_i \int d^2 \mathbf{k}_{\parallel} \frac{\varepsilon_i(\phi, \mathbf{k}_{\parallel})}{\exp[\varepsilon_i(\phi, \mathbf{k}_{\parallel})/k_B T] - 1}, \quad (5)$$

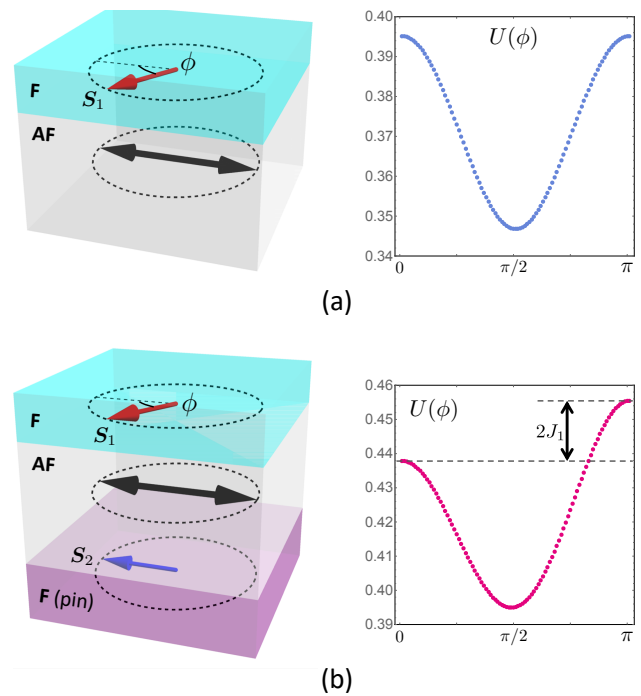


FIG. 1. Dependence of the internal energy U on the free layer orientation in: (a) F/AF bilayer; (b) F/AF/F trilayer with the bottom F pinned parallel to the Néel vector.

where k_B is the Boltzmann constant and T is the system temperature. Figure 1 plots $U(\phi)$ for the simplest possible situation—AF with only two atomic layers ($L = 2$)—at $T = 0.6$ and $\xi = 0.6$. After a straightforward fitting, we see that: (a) in the bilayer case, the $\mathcal{K}_1 \cos 2\phi$ term with $\mathcal{K}_1 \approx 24.17 \times 10^{-3}$ dominates, whereas all \mathcal{K}_n components with $n > 2$ are negligibly small, hence \mathbf{S}_1 prefers to be perpendicular to the Néel vector; (b) in the trilayer case, the leading contributions are $J_1 \cos \phi + J_2 \cos 2\phi$ with $J_1 = 8.82 \times 10^{-3}$ and $\tilde{J}_2 = J_2 + \mathcal{K}_1 = -1.58 \times 10^{-3}$. All J_n with $n > 3$ are negligibly. The negative J_1 is a ferromagnetic exchange interaction between \mathbf{S}_1 and \mathbf{S}_2 , while $|\tilde{J}_2| \approx 6.5\% \mathcal{K}_1 \approx 17.9\% J_1$ is a higher-order interlayer coupling; they both have counterparts in the electron-mediated interactions [12–17].

Next, we allow the AF to have multi-domains where the Néel vector has a random in-plane orientation distributed uniformly from 0 to 2π . As a result, the magnon energy density of a given domain is $u = u(\phi, \gamma)$, where γ specifies the local Néel order direction with respect to the reference [*e.g.*, \mathbf{S}_2 in Fig. 1(b)]. The total magnon energy becomes $U(\phi) = \int_0^{2\pi} d\gamma u(\phi, \gamma)/2\pi$. Repeating the calculation of Eq. (5) for each individual domain and taking the multi-domain average, we find that: (a) in the bilayer case, the free F (\mathbf{S}_2) favors the out-of-plane direction since every domain in the AF prefers to align vertically with \mathbf{S}_2 . The overall effect becomes a magnon-induced perpendicular anisotropy $\mathcal{K}_{\perp} = \mathcal{K}_1$. (b) in the trilayer case, the J_2 component drops out while J_1 survives, as

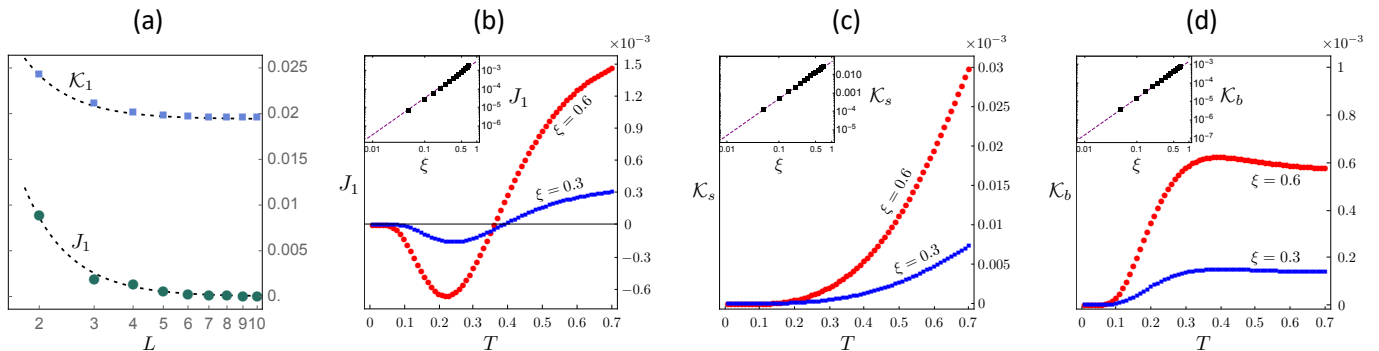


FIG. 2. Properties of J_1 and \mathcal{K}_1 . (a) The decay of J_1 fits into $1/L^3$; \mathcal{K}_1 fits into $\mathcal{K}_s + \mathcal{K}_b(L)$ with $\mathcal{K}_b \sim 1/L^3$ and \mathcal{K}_s being the interfacial contribution independent of L (for $T = 0.6$ and $\xi = 0.6$). (b), (c), and (d) plot the temperature dependences of J_1 , \mathcal{K}_s and \mathcal{K}_b , respectively (for $L = 4$ and different ξ 's). The insets show the logarithmic plots of the ξ dependences of J_1 , \mathcal{K}_s and \mathcal{K}_b at $T = 0.6$, which fits into ξ^2 (dashed lines).

the averaging operation introduces the azimuthal symmetry. Correspondingly, the interlayer coupling $J_1 \cos \phi$ can be written as $J_1 \mathbf{S}_1 \cdot \mathbf{S}_2$. The above analysis indicates that J_1 and \mathcal{K}_1 are the most relevant quantities in our geometry. In the following, we will focus on the physical properties of the two parameters.

When the AF becomes thicker, both J_1 and \mathcal{K}_1 should get smaller since the fraction of spins under direct influence of boundaries reduces. Figure 2(a) plots J_1 and \mathcal{K}_1 versus the number of layers L from 2 to 10. The decay patterns of J_1 and \mathcal{K}_1 fit well into

$$J_1 \sim \frac{1}{L^3}; \quad (6)$$

$$\mathcal{K}_1 = \mathcal{K}_s + \mathcal{K}_b(L) \quad \text{with} \quad \mathcal{K}_b(L) \sim \frac{1}{L^3}. \quad (7)$$

We interpret the L -independent term \mathcal{K}_s as an interfacial anisotropy arising from surface magnons, which do not connect the two Fs together. By contrast, the term $\mathcal{K}_b(L)$ decays similarly as J_1 ; it originates from bulk magnons with (quantized) wave vectors in the thickness direction. We will discuss the physics underlying this $1/L^3$ decay pattern of J_1 and \mathcal{K}_b later.

Here we estimate the magnitudes of J_1 and \mathcal{K}_1 . As shown earlier, J_1 is nearly 1% of J_{AF} at $L = 2$ assuming an interfacial coupling of $\xi = 0.6$. With the $1/L^3$ decay, J_1 is roughly 0.1% of J_{AF} at $L = 4$. In insulating AFs such as Cr_2O_3 [21], J_{AF} is typically few tens of meV, and the lattice constant in the in-plane geometry is 5\AA . We then deduce that J_1 is $10 \sim 100 \mu\text{eV}$ and \mathcal{K}_1 is $0.1 \sim 1$ meV at nanometer separations. Comparing with other interlayer couplings such as the electron-mediated RKKY interaction [12–15] and the dipole-dipole interaction [22] at similar separations, the magnon-mediated mechanism appears comparably strong.

Since magnons are bosons without particle number conservation (chemical potential is zero), they become more populated when we raise the temperature. As such, we would naively expect that the magnon-mediated in-

terlayer coupling increases monotonically with temperature. In Fig. 2(b), (c), and (d), we plot J_1 , \mathcal{K}_s , and \mathcal{K}_b as functions of temperature at separation $L = 4$ for $\xi = 0.6$, where we see that only \mathcal{K}_s bears a monotonic temperature dependence. Counterintuitively, J_1 flips sign at a finite turning temperature: it is antiferromagnetic at low temperatures and ferromagnetic at high temperatures. We find that the turning temperature is smaller for larger ξ and thicker films (not shown), but this remarkable sign change persists. We will discuss the underlying physics of the sign change in the next section.

Considering that the electron-mediated RKKY interaction scales quadratically with the interfacial exchange coupling, we expect a similar behavior for the magnon-mediated interlayer coupling. The insets of Fig. 2 show the ξ^2 fittings of J_1 and \mathcal{K}_1 in the range $\xi \in (0.05, 0.65)$ with 0.05 increment. Above $\xi = 0.7$, the collinear ground state becomes energetically unstable such that the Néel vector undergoes a spin-flop transition and bends perpendicular to the F, which invalidates our model. A stronger anisotropy K_{AF} can increase the spin-flop threshold, but it also enlarges the magnon gap of the AF. Since magnons are bosons that preferably occupy low-energy states, an enlarged gap will diminish the magnitude of our results (although the essential pattern in Fig. 2 will be kept). It is numerically feasible to find a good balance between K_{AF} and the maximum possible ξ without incurring spin-flop breakdown. Nevertheless, this is a matter of materials choice, and we leave it for future studies.

Discussions.—The unique physical behavior of the magnon-mediated interlayer coupling is closely related to the Bose-Einstein statistics, where the most prominent contribution stems from a few low-energy states. Those states are long wavelength magnons ($\mathbf{k}_{\parallel} \rightarrow 0$) with small band index i . Because of uniaxial symmetry, a magnon eigenstate is always circularly-polarized and appears in pair with its partner of the opposite chirality [21, 23], as schematically depicted in Fig. 3(a). At the bottom of the lowest band, all spins precess uniformly with nearly the

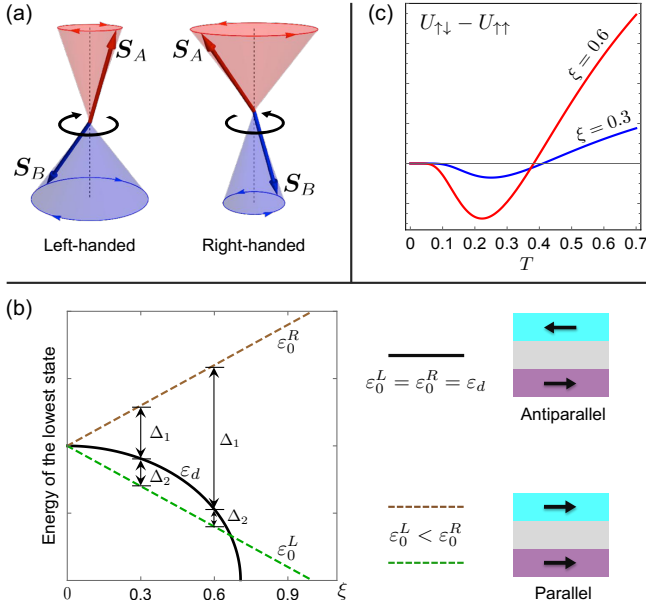


FIG. 3. (a) Schematics of the two circularly-polarized modes in the AF, where the two sublattice spins, \mathbf{S}_A and \mathbf{S}_B , precess with the same chirality but different cone angles [23]. (b) Energy of the lowest magnon band as a function of the interfacial coupling ξ , where ε_0^R (ε_0^L) stands for the right-handed (left-handed) subband. For parallel (antiparallel) alignment of the Fs, the degeneracy between ε_0^R and ε_0^L is lifted (maintained). For any ξ below the spin-flop transition, $\Delta_1 > \Delta_2$. (c) $\Delta U = U_{\uparrow\downarrow} - U_{\uparrow\uparrow}$ as a function of T for $\xi = 0.3$ and $\xi = 0.6$, which qualitatively reproduces J_1 in Fig. 2(b).

same phase, and its left-handed (right-handed) component has energy ε_0^L (ε_0^R). As shown in Fig. 3(b), when the Fs are parallel and polarized along the easy-axis of the AF, the degeneracy of the lowest band splits *linearly* with ξ (dashed lines). By contrast, when the Fs are antiparallel, the degeneracy is preserved so that $\varepsilon_0^L = \varepsilon_0^R = \varepsilon_d$ (solid black curve). As ξ increases, ε_d bends downwards until reaching the spin-flop transition at around $\xi = 0.7$. The energy relation between the parallel and antiparallel configurations is $\varepsilon_0^R = \varepsilon_d + \Delta_1$ and $\varepsilon_0^L = \varepsilon_d - \Delta_2$ with $\Delta_1 > \Delta_2$. Accordingly, the difference of thermal energy between the two configurations reads

$$\begin{aligned} \Delta U &= U_{\uparrow\downarrow} - U_{\uparrow\uparrow} \\ &= \frac{2\varepsilon_d}{\exp(\varepsilon_d/k_B T) - 1} - \frac{\varepsilon_d + \Delta_1}{\exp[(\varepsilon_d + \Delta_1)/k_B T] - 1} \\ &\quad - \frac{\varepsilon_d - \Delta_2}{\exp[(\varepsilon_d - \Delta_2)/k_B T] - 1}. \end{aligned} \quad (8)$$

Figure 3(c) plots ΔU as a function of T for $\xi = 0.3$ and 0.6 , which qualitatively reproduces the numerical result in Fig. 2(b), suggesting that the non-monotonic behavior of J_1 is largely attributed to the lowest magnon band. Figure 3(b) also reveals a fine structure: there is a very narrow window of ξ just below the spin-flop transition within which $\varepsilon_d < \varepsilon_0^L < \varepsilon_0^R$ thus Δ_2 is negative. In this

special region, the antiparallel configuration always has a lower energy thus the interlayer exchange coupling is antiferromagnetic for any temperature.

Now we turn to the crucial question why J_1 scale as $1/L^3$ when it is ferromagnetic (at high temperatures). The magnon band structure along the thickness direction is analogous to that of a quantum well, where the gaps between neighboring energy levels scale as $1/L^2$. In addition, the percentage of boundary atoms that are exchange-coupled to the Fs scales as $1/L$, *i.e.*, the relative strength of exchange-fields on the boundaries scales as $1/L$. Therefore, the overall magnon energy splitting scales as $1/L^3$. Up to the leading order in $\varepsilon/k_B T$, Equation (8) expands into $\Delta U = (\Delta_1 - \Delta_2)/2 + h.o.$, which respects the $1/L^3$ law. A similar argument applies to \mathcal{K}_d as well, but in that case, we should compare $U_{\uparrow\uparrow}$ with the thermal energy for the perpendicular F/AF configuration in which $\varepsilon_0^L = \varepsilon_0^R$ (no splitting). This provides a qualitative but not rigorous physical explanation of the decay pattern obtained numerically.

The conceived in-plane Néel vector shown in Fig. 1 has been successfully fabricated in a recent experiment using Cr_2O_3 [24]. But it remains a challenge to achieve the collinear exchange-coupled F/AF interface based on this device geometry. Since our predicted effects are proportional to ξ^2 , good interfacial quality is crucial to the observation. Therefore, to fully verify our predictions, it calls for a serious materials search that goes beyond the scope of this Letter.

To close the discussion, we finally comment on the crucial distinction between magnon-mediated interlayer couplings and their well-established electronic counterparts. Electrons obey Fermi-Dirac statistics, and most physical properties are directly linked to the existence of Fermi surface. Because of geometrical confinement in the thin film, electrons on the Fermi surface exhibits oscillatory interference pattern as a function of the spacer thickness, giving rise to an oscillatory exchange coupling [14, 15]. If the non-magnetic spacer is electronically insulating while the two Fs are metallic, electron tunneling becomes the dominant mechanism for the interlayer coupling [15–17]. In this case, the interlayer coupling does not oscillate but simply decays exponentially with the spacer thickness. In contrast to electrons, magnons are bosonic excitations that do not have a Fermi surface, which is responsible for the absence of an oscillatory decay with thickness. The most defining feature lies in the nontrivial sign change of J_1 with temperature, which can be directly measured from the hysteresis loop. Last but not least, we notice that the magnon-mediated interlayer coupling proposed in this Letter is the magnonic counterpart of the thermal Casimir effect [25].

In summary, we have demonstrated that two ferromagnetic layers separated by a thin-film AF can couple each other via magnon excitations inside the AF, which is especially important when all layers are insulating and con-

duction electrons are absent. The central result involves a magnon-mediated exchange interaction (a trilayer effect) and a magnon-induced anisotropy (a bilayer effect). While the former decays with the AF thickness as $1/L^3$, the latter can be decomposed into a constant surface contribution independent of L plus a term decaying as $1/L^3$. The interlayer exchange interaction turns out to be antiferromagnetic at low temperatures and ferromagnetic at high temperatures. This sign change can be qualitatively explained in terms of the lowest magnon excitation quantized in the thickness direction. Although antiferromagnetic magnons with opposite spins bear an apparent resemblance to electrons, the difference in their statistical properties leads to drastically different behaviors.

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