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Lattice instability during solid-solid structural transformations under general applied stress tensor: example of Si I \rightarrow Si II with metallization

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Density functional theory was employed to study the stress-strain behavior and elastic instabilities during the solid-solid phase transformation (PT) when subjected to a general stress tensor, as exemplified for semiconducting Si I and metallic Si II, where metallization precedes the PT, so stressed Si I can be a metal. The hydrostatic PT occurs at 76 GPa, while under uniaxial loading it is 11 GPa (3.7 GPa mean pressure), 21 times lower. The Si I \rightarrow Si II PT is described by a critical value of phase-field's modified transformation work, and the PT criterion has only two parameters given 6 independent stress elements. Our findings reveal novel, more practical synthesis routes for new or known high-pressure phases under predictable non-hydrostatic loading, where competition of instabilities can serve for phase selection, rather than free energy minima used for equilibrium processing.

Keywords: Phase Transformation; Lattice Instability; General stress tensor; Density functional theory; Phase field

Phase transformations (PTs) in solids are mostly characterized by equilibrium phase diagrams [1], whereas general non-hydrostatic stresses offer novel synthetic routes for new or known high-pressure phases. Here we augment temperature-pressure (T - P) equilibrium diagrams by stress (σ) tensor that affect structural (and electronic) instabilities, providing guidance for creating more accessible processing routes of such phases under predictable non-hydrostatic deformation at significantly lower mean pressures. Indeed, observed PTs occur under significant deviation from equilibrium [2–5], with large hysteresis. For carbon, the graphite-diamond PT at room temperature occurs 2.45 GPa; however, due to hysteresis, the PT is observed at 70 GPa [3]. The actual PT pressure deviates from that of equilibrium due to an enthalpy barrier. When thermal fluctuations can be neglected, the PT criterion is related to disappearance of the enthalpy barrier, i.e., to the lattice instability. Hence, lattice instability conditions are necessarily studied under hydrostatic, uniaxial, and multiaxial loadings [6–12].

In experiments, a significant reduction in PT pressure occurs due to deviatoric (non-hydrostatic) stresses and plastic strains [5, 13–16]. For example, plastic shear reduces the PT from hexagonal to superhard wurtzitic BN from 52.8 to 6.7 GPa [5] – an order of magnitude! This phenomenon is extremely important from fundamental and applied points of view, as it may reduce the PT pressure to a practical level for high-pressure phases that exhibit unique properties.

The suggested physical mechanism responsible for this reduction is related to dislocation pileups associated with a plastic strain [13]. As stresses at the tip of a pileup are proportional to the number of dislocations in a pileup (typically 10 to 100), local stresses exceed the lattice instability limit and cause nucleation of a high-pressure phase even at relatively small external pressure. This was rationalized based on an analytical model [13] and using a phase field approach [17, 18]. However, the phase field inputs for the PT instability criteria

for an ideal crystal under *general stress tensor* was assumed hypothetically, as such criteria are not known for any material [19].

Due to the technological importance of Si and its PTs, a huge literature exists. Relevant are the PTs in Si I under hydrostatic and two-parametric nonhydrostatic loadings, studied with density functional theory (DFT) [20, 21], and the lattice instability under two-parametric loadings (unrelated to a PT) [10, 22–24].

So, we perform a DFT study of the deformation process under applied *general stress*, and determine the lattice instabilities responsible for the cubic-to-tetragonal Si I \rightarrow Si II PT, along with metallization that can occur prior to Si II phase. While finding the instability criteria under all six stress components seems daunting, due to the large number of combinations, an unexpected guidance came from the crystal lattice instability criterion formulated within the phase-field method [11, 12, 25, 26]. The key result is that Si I \rightarrow Si II PT can be described by the critical value of the modified transformation work. With normal stresses ($\sigma_1, \sigma_2, \sigma_3$) acting along $\langle 110 \rangle$, $\langle 1\bar{1}0 \rangle$, and $\langle 001 \rangle$, respectively, the PT criterion is linear in normal stresses, depends on $\sigma_1 + \sigma_2$, is independent of $\sigma_1 - \sigma_2$ and shear stress τ_{21} , acting alone or with one more shear stress, and depends on all shear stresses via theoretically predicted geometric nonlinearity. The PT criterion has only two material parameters for a general applied stress, which can be determined by two DFT simulations under different normal stresses.

Energy landscape. The DFT potential energy (vs. lattice constants $a_i = b_i$ and c_i) is given in Fig. 1; the data is in supplemental material [27]. We find two local energy minima, corresponding to the fully relaxed (stress-free) Si I and Si II, and a saddle point (SP) – the unstable state corresponding to the enthalpy barrier (Fig. 1). The tetragonal cell of Si I is bounded by (110) , $(1\bar{1}0)$, and (001) planes. The DFT energies and lattice constants relative to the stress-free Si

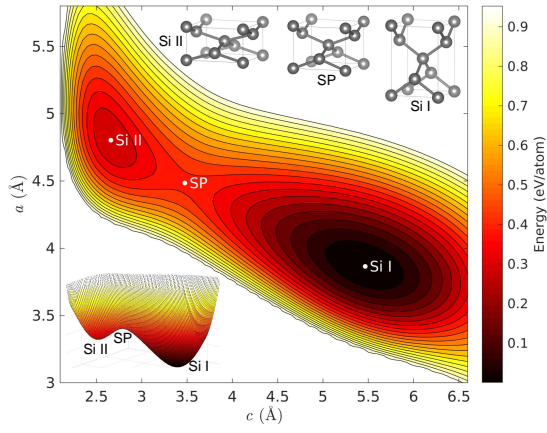


FIG. 1. (Color online) DFT energy of Si versus lattice parameters c and a . Insets: Tetragonal ($a = b, c$) unit cells for stress-free Si II (left), unstable SP (middle), and Si I (right).

I ($a_1 = 3.8653 \text{ \AA}$, $c_1 = \sqrt{2}a_1 = 5.4665 \text{ \AA}$) are 0.2949 eV/atom for Si II ($a_2 = 4.8030 \text{ \AA}$, $c_2 = 2.6592 \text{ \AA}$), and 0.4192 eV/atom for the SP state ($a = 4.4847 \text{ \AA}$, $c = 3.4763 \text{ \AA}$). The calculated c_1 is $+0.7\%$ of experiment (5.43 \AA) [28].

We designate tensors with boldface, e.g., \mathbf{I} is the unit tensor. Contractions of tensors $\mathbf{A} = \{A_{ij}\}$ and $\mathbf{B} = \{B_{jk}\}$ over one and two indices in Einstein notations are $\mathbf{A} \cdot \mathbf{B} = \{A_{ij} B_{jk}\}$ and $\mathbf{A} : \mathbf{B} = A_{ij} B_{ji}$, respectively. The inverse and transpose of \mathbf{A} are \mathbf{A}^{-1} and \mathbf{A}^T , respectively.

Deformation gradient $\mathbf{F} = \mathbf{F}_e \cdot \mathbf{U}_t$, mapping undeformed state of a crystal into a deformed state, is decomposed into elastic \mathbf{F}_e and transformational \mathbf{U}_t parts. Deformation gradient \mathbf{U}_t changes the Si I stress-free cell to the Si II stress-free cell; its diagonal components are $U_{t1} = U_{t2} = a_2/a_1 = 1.243$ and $U_{t3} = c_2/c_1 = 0.486$. For a Tersoff potential [11, 12], it is quite different: $U_{t1} = U_{t2} = 1.175$ and $U_{t3} = 0.553$. We label tetragonal directions $a = b$ and c by indices 1, 2, and 3. We use true Cauchy stress $\boldsymbol{\sigma}$ (force per unit deformed area) and Lagrangian strain $\mathbf{E} = \frac{1}{2}(\mathbf{F}^T \cdot \mathbf{F} - \mathbf{I})$.

Stress-strain $\sigma_3 - E_3$ curves for fixed lateral stresses $\sigma_1 = \sigma_2$ are in Fig. 2, along with corresponding transformation paths in $(F_1 = F_2, F_3)$ plane. The elastic instability occurs when determinant of the elastic moduli tensor, modified by some geometrically nonlinear terms, reduces to zero [6–10]. This results in a condition that some elastic moduli (or combination thereof) reduce to zero. We will use an alternative (more strict) condition: Elastic lattice instability at true stress $\boldsymbol{\sigma}$ occurs at stresses above (or below for the reverse PT) which the crystal cannot be at equilibrium. Instability points correspond to the stress maximum for forward PT (and minimum for reverse PT) on the stress-strain curves (Fig. 2). Our condition is more general and universal, because it is applicable even to the cases with discontinuous or undefined derivatives of stress with respect to strain.

A tetragonal stressed lattice of Si I transforms into a tetragonal stressed lattice of Si II (Figs. 1 and 2), and the lattice instability does not change this tetragonal symmetry. The slope

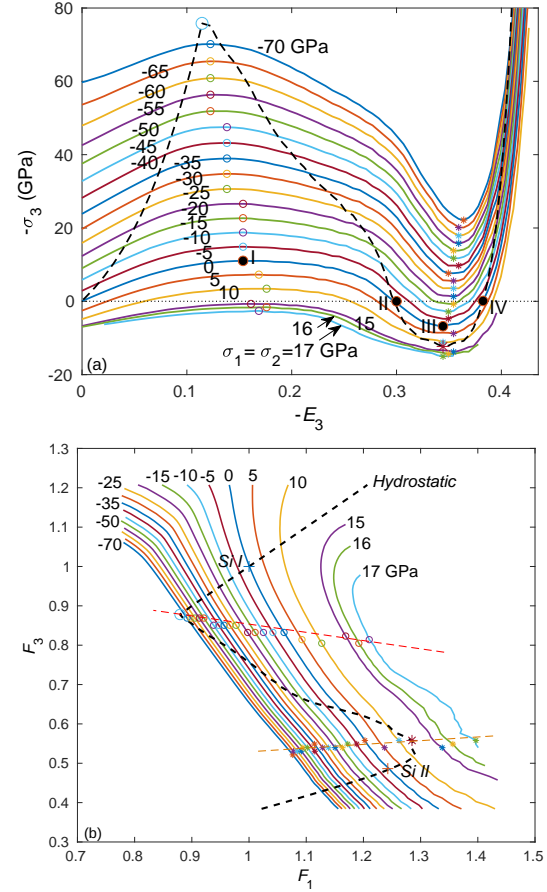


FIG. 2. (Color online) (a) True (Cauchy) stress σ_3 vs. Lagrangian strain E_3 for compression/tension along c for lateral stresses $\sigma_1 = \sigma_2$ for Si I \leftrightarrow Si II PTs; (b) corresponding transformation paths in $(F_1 = F_2, F_3)$ plane. Hollow (solid) symbols mark instability points for forward (reverse) PT. Dashed line shows hydrostatic loading.

of the stress-strain curve is continuous and is zero at instability points. Under hydrostatic loading (dashed line in Fig. 2), a cubic lattice loses its stability under tetragonal perturbations, i.e., there is a bifurcation from a primary isotropic deformation to a secondary tetragonal deformation; hence, the derivative at the hydrostatic instability point is discontinuous. Both under hydrostatic ($\sigma_1 = \sigma_2 = \sigma_3$) and uniaxial ($\sigma_1 = \sigma_2 = 0$) compression there are three stress-free states (Fig. 1): Si I, Si II (stable or metastable enthalpy minima) and an intermediate unstable state at the SP (enthalpy barrier). Interestingly, a stress-free Si II is metastable with stable phonons [29–31]. Thus, one could search for a pressure-plastic shear path for arresting the metastable Si II, as suggested in [13] for any metastable phase. In experiments, a stress-free Si II was not observed.

Elastic lattice instability conditions under two-parametric loading at $\sigma_1 = \sigma_2$ for forward (direct) (σ_{3d}) and reverse (σ_{3r}) PTs are approximated by linear relationships in Fig. 3. Tersoff-potential (TP) results from [11, 12] for Si I \rightarrow Si II PT are generally in good agreement with the present DFT results,

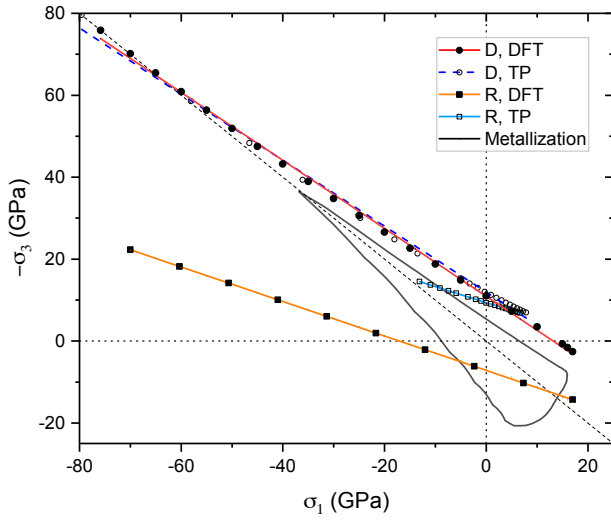


FIG. 3. (Color online) Elastic instability vs. σ_3 and $\sigma_1 = \sigma_2$ for direct (D) Si I \rightarrow Si II and reverse (R) Si II \rightarrow Si I PTs from DFT and TP-based results [11, 12], and metallization curve from DFT. Hydrostatic condition ($\sigma_1 = \sigma_2 = \sigma_3$) is a diagonal (dashed black) line.

however there is a difference for tensile and small compressive σ_1 , where TP results are slightly higher and nonlinear. Under hydrostatic loading, PT pressure from DFT and TP is 75.81 GPa and 79.58 GPa, respectively.

The PT stress for uniaxial compression is -11.03 GPa (σ_{3d}) at $E_3 = -0.154$. Then the pressure for uniaxial loading is $-\sigma_{3d}/3 = 3.68$ GPa, which is $75.81/3.68 = 20.6$ times lower than hydrostatic case. This characterizes very strong effect of non-hydrostatic stresses on PT, which can partially explain a scatter in experimental data under quasi-hydrostatic conditions and a significantly lower experimental PT pressure than the predicted hydrostatic instability pressure. The instability lines are described by $\sigma_{3d} = -10.9 + 1.20\sigma_1$ for $\sigma_1 \in [-75.81; 17]$ and $\sigma_{3r} = 7.175 + 0.4209\sigma_1$ for $\sigma_1 \in [-70; 17]$. Theoretical strength is approximately $\sigma_{3d} = -10.6 + 0.77\sigma_1$ for $\sigma_1 \in [-15; 12]$. As it is close to our result, instability in [23] is related to Si I \rightarrow Si II PT.

While instability line for forward PT, calculated in [11, 12] using TP, is quite close to our DFT results, for reverse PT the TP results are completely different from DFT. Thus, none of the classical potentials in [11, 12] (Tersoff, modified Tersoff, and Stillinger-Weber) are able to describe the reverse PT.

Metallization. This electronic transition from semiconducting to metallic phase (band gap \rightarrow zero) is caused by deformation of Si I under combinations of σ_3 and fixed $\sigma_1 = \sigma_2$ (Fig. 3). The band gap vs. compressive/tensile strain is given in Fig. S2 [27]. The electronic transition is found to precede the structural PT for all combinations of stresses, i.e., a sufficiently deformed Si I under stress is metallic (Fig. 3). This transition does not change the continuity of the stress-strain curves and their first derivatives (Fig. 2); this differs from the stress discontinuity in magneto-structural phase transitions [32]. The metallization curve is closed in the (σ_3, σ_1)

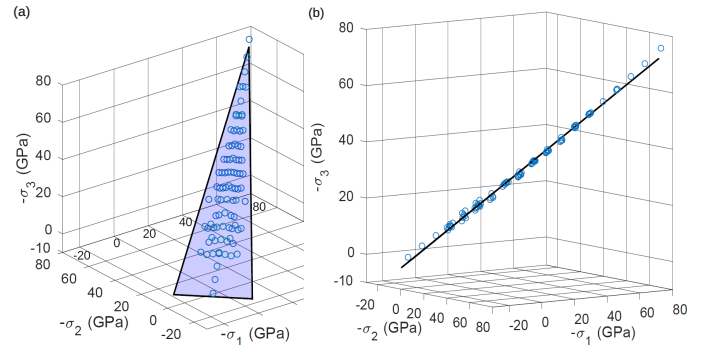


FIG. 4. (Color online) Criterion for Si I \rightarrow Si II PT for triaxial stresses. (a) DFT results (points) lie very close to a plane described by a constant value of modified transformation work in Eq. 3. (b) Result in (a) rotated to visualize an approximate plane.

plane and surrounds the stress-free Si I; it can be approximated by two straight lines $\sigma_{3m} = -5.605 + 0.8417\sigma_1$ and $\sigma_{3m} = 13.04 + 1.396\sigma_1$, and a parabolic section $\sigma_{3m} = 11.95 + 2.378\sigma_1 + 0.16\sigma_1^2$. While one of the metallization lines is relatively close and approximately parallel to the Si I \rightarrow Si II PT line, two other lines are deeply in the region of stability of Si I (Fig. 3). Metallization occurs at compressive -36.82 GPa and tensile $+13.91$ GPa under hydrostatic pressure; -5.4 GPa and $+12.78$ GPa under uniaxial loading at $\sigma_1 = \sigma_2 = 0$; and -6.69 GPa and $+8.79$ GPa under biaxial loading at $\sigma_3 = 0$. Hence, the effect of non-hydrostatic stresses is extremely strong.

Elastic lattice instability under triaxial loading. Evidently, DFT results for $\sigma_1 \neq \sigma_2$ case (Fig. 4) suggest that the criterion for forward Si I \rightarrow Si II PT is described accurately in 3D space of normal stresses by a plane

$$\sigma_3 = -9.911 + 0.4145(\sigma_1 + \sigma_2). \quad (1)$$

It is very surprising that the elastic instability for a material with strong physical and geometric nonlinearities can be approximated by a linear criterion.

Lattice instability under general stress tensor – the phase-field approach. As shown in [11, 12, 25, 26], a PT condition linear in normal stress can be derived by the phase-field approach to martensitic PTs. Using several assumptions, the instability Si I \rightarrow Si II PT criterion is:

$$2W = \boldsymbol{\sigma} : \mathbf{F}_e^{T-1} \cdot \left. \frac{d^2 \bar{\mathbf{U}}_t}{d\eta^2} \right|_{\eta=0} \cdot \mathbf{F}_e^T \geq 2A, \quad (2)$$

where deformation gradient $\bar{\mathbf{U}}_t(\eta) \equiv \mathbf{I} + \bar{\boldsymbol{\varepsilon}}_t(\eta)$, and other material parameters (e.g., elastic moduli, and transformation strain $\bar{\boldsymbol{\varepsilon}}_t(\eta)$) depend on the order parameter η , which changes during the transformation process from $\eta = 0$ for Si I [$\bar{\boldsymbol{\varepsilon}}_t(0) = \mathbf{0}$] to $\eta = 1$ for Si II [$\bar{\boldsymbol{\varepsilon}}_t(1) = \boldsymbol{\varepsilon}_t = \text{diag}(\varepsilon_{t1}, \varepsilon_{t1}, \varepsilon_{t3})$]. W is called the modified transformation work [11], and A is the magnitude of the double-well barrier. For cubic-to-tetragonal transformation, $\left. \frac{d^2 \bar{\mathbf{U}}_t}{d\eta^2} \right|_{\eta=0} = 2 \text{diag}(b_1 \varepsilon_{t1}, b_1 \varepsilon_{t1}, b_3 \varepsilon_{t3})$, where b_i are the coefficients in the

interpolation of $\bar{\varepsilon}_t(\eta)$. For the loading by three stresses normal to the chosen above faces, all tensors in Eq. 2 are coaxial, tensors \mathbf{F}_e^{T-1} and \mathbf{F}_e^T eliminate each other, and Eq. 2 reduces to the linear modified transformation work criterion:

$$W = b_3\sigma_3\varepsilon_{t3} + b_1(\sigma_1 + \sigma_2)\varepsilon_{t1} = A. \quad (3)$$

The equality is used to describe combination of stresses at the limit of stability and calibrate material parameters. W reduces to the transformation work for $b_1 = b_3 = 1$. The consequence of Eq. 3 for cubic-to-tetragonal PT is that, with $\varepsilon_{t1} = \varepsilon_{t2}$, the stresses σ_1 and σ_2 contribute to the instability criterion via $\sigma_1 + \sigma_2$, as in Eq. 1. Comparing Eqs. 3 and 1 with $\varepsilon_{t1} = U_{t1} - 1 = 0.243$ and $\varepsilon_{t3} = U_{t3} - 1 = -0.514$ leads to $A(\theta)/b_3 = 5.094$ GPa and $b_3/b_1 = 1.141$.

When shear stresses τ_{ij} are applied, causing nonzero deformation gradients F_{21}, F_{31}, F_{32} , with rigid-body rotations excluded by imposing a constraint $F_{12} = F_{13} = F_{23} = 0$, Eq. 2 reduces to

$$W = b_3\sigma_3\varepsilon_{t3} + b_1(\sigma_1 + \sigma_2)\varepsilon_{t1} + \frac{b_1\varepsilon_{t1} - b_3\varepsilon_{t3}}{F_{11}^e F_{22}^e} [\tau_{32}F_{32}^e F_{11}^e + \tau_{31}(F_{31}^e F_{22}^e - F_{32}^e F_{21}^e)] = A, \quad (4)$$

where $(b_1\varepsilon_{t1} - b_3\varepsilon_{t3})/A = 0.143$ and the terms proportional to $\varepsilon_{t2} - \varepsilon_{t1}$ are eliminated. With transformation shears absent in a cubic-to-tetragonal PT, the shear transformation work is absent. The terms proportional to the shear stresses are due to geometric nonlinearity (finite strains); they do not contain any additional material parameters. Shear stresses change geometry of the crystal, and this affects transformation work along the normal components of transformation strain.

For the obtained parameters, and because $F_{ii}^e > 0$ and $\tau_{ij}F_{ij}^e > 0$, when τ_{32} and F_{32}^e or τ_{31} and F_{31}^e are applied alone, contribution of shear stresses to W is positive, i.e., they promote tetragonal instabilities. Shear stress τ_{21} (more exactly, elastic shear strain F_{21}^e) alone or with τ_{32} does not contribute to the instability condition; but τ_{21} contributes when two other stresses, τ_{31} and τ_{32} , are applied simultaneously, and depending on signs of all shear stresses, τ_{21} may promote or suppress tetragonal instability.

Shear stress-strain curves and shear lattice instability. In typical shear stress–deformation gradient (τ_{31} – F_{31}) curves (Fig. S3 [27]) shear instability starts at the maximum shear stress. This instability does not lead to Si II but rather to possible amorphization or hexagonal diamond Si IV (which is beyond our present focus).

Under an initial (before shear) hydrostatic compression, the shear instability at an infinitesimal shear starts at 72 GPa, i.e., below the tetragonal mode of lattice instability. This may explain amorphization in nanocrystalline Si I under increasing pressure when Si II PT is kinetically suppressed [33]. Amorphization may be caused by virtual melting [34] after crossing metastable continuation of the melting line, as melting temperature for Si reduces with pressure.

Effect of shear stresses on tetragonal instability. $\sigma_3 - E_3$ curves were obtained for different fixed shears, along the path

in the $(F_1 = F_2, F_3)$ plane corresponding to $\sigma_1 = \sigma_2$ before shear. The instability stress (Fig. S4) is determined as the local maximum of $|\sigma_3|$ (Fig. 2). While during shear $\sigma_1 \neq \sigma_2$ but their sum $\sigma_1 + \sigma_2$ practically does not change. That is why curves in Fig. S4 are given for the fixed values of $(\sigma_1 + \sigma_2)/2$.

Absolute and relative deviations between the actual instability stress σ_3 and σ_3^{an} based on the analytical prediction (4) are small (Figs. S5 and S6) and can be neglected. Thus, the tetragonal lattice instability under action of all six components of the stress tensor is described by the critical value of the modified transformation work (Eq. (4)), which is (a) linear in normal stresses, depends on $\sigma_1 + \sigma_2$, and has only two adjustable coefficients (b_1 and b_3); (b) independent of $\sigma_1 - \sigma_2$ and shear stress τ_{21} acting alone or with one more shear stress, and (c) contains a geometric nonlinear term describing contribution of all shear stresses without any additional adjustable parameters.

In summary, we augmented standard T - P diagrams with criteria for structural and electronic instabilities (PTs) under a general applied stress tensor, providing guidance for more accessible processing routes for new or known high-pressure phases with novel properties. Our comprehensive DFT study of the PT between semiconducting Si I and metallic Si II under general applied stresses investigated stress-strain curves, elastic lattice instabilities, and regions of metallization. Metallization occurs deeply in the region of stability of Si I and is not caused by Si I→Si II PT. Deformed Si I becomes metallic, and the effect of non-hydrostatic stresses is very strong. The hydrostatic PT pressure is ~ 21 times larger than for uniaxial loading. Such a strong non-hydrostatic stress effect at least partially explains the significant difference between the observed PT pressure (9–12 GPa) and the instability pressure of 75.81 GPa, and scatter in measured data under quasi-hydrostatic conditions.

Our key result is that Si I → Si II PT is given by a critical value of the modified transformation work (Eq. 4). For a general stress tensor (6 independent variables), the PT criterion has just two parameters. Hence, PT criterion can be determined by just two DFT calculations versus applied stress.

These results are significant for creating new, more practical and economical processing routes for discovery and stabilizing materials with novel properties. While comparison of the Gibbs free energy minima defines thermodynamic equilibrium (possibly unachievable in practice), we suggest competition of instabilities to serve for phase selection. Critically, this approach enables ways to reduce PT pressure due to non-hydrostatic stresses by an order of magnitude or more [5, 13–15]. They can also be used for quantitative studies of the influence of crystal defects on phase transitions [17, 18], and quantitatively rationalize connections between PT conditions for ideal and real (defective) crystals.

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