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On the radial acceleration relation of ΛCDM satellite galaxies

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The radial acceleration measured in bright galaxies tightly correlates with that generated by the observed distribution of baryons, a phenomenon known as the radial acceleration relation (RAR). Dwarf spheroidal satellite galaxies have been recently found to depart from the extrapolation of the RAR measured for more massive objects but with a substantially larger scatter. If confirmed by new data, this result provides a powerful test of the theory of gravity at low accelerations that requires robust theoretical predictions. By using high-resolution hydrodynamical simulations, we show that, within the standard model of cosmology (ΛCDM), satellite galaxies are expected to follow the same RAR as brighter systems but with a much larger scatter which does not correlate with the physical properties of the galaxies. In the simulations, the RAR evolves mildly with redshift. Moreover, the acceleration due to the gravitational field of the host has no effect on the RAR. This is in contrast with the External Field Effect in Modified Newtonian Dynamics (MOND) which causes galaxies in strong external fields to deviate from the RAR. This difference between ΛCDM and MOND offers a possible way to discriminate between them.

Introduction.—The standard ΛCDM model of cosmology relies on the theory of general relativity and assumes that the energy budget of the universe is dominated by cold dark matter and a cosmological constant. The cosmic microwave background, gravitational lensing, and galactic dynamics provide abundant evidence for mass discrepancies which are usually interpreted as manifestations of particle dark matter (DM). However, its basic properties of the galaxies. In the simulations, the RAR evolves mildly with redshift. Moreover, the acceleration due to the gravitational field of the host has no effect on the RAR. This is in contrast with the External Field Effect in Modified Newtonian Dynamics (MOND) which causes galaxies in strong external fields to deviate from the RAR. This difference between ΛCDM and MOND offers a possible way to discriminate between them.

The debate was recently revived when [8] and [9] concluded that the (centripetal) radial acceleration \( a_{\text{tot}} \) generated by the visible baryonic matter in galaxies and the actual (centripetal) radial acceleration derived from kinematic measurements \( a_{\text{bar}} \) strongly correlate over the range \( 10^{-12} < a_{\text{bar}} < 10^{-8} \, \text{m s}^{-2} \). In terms of the characteristic acceleration \( g_1 = [1.20 \pm 0.02 \, \text{cmd}, \pm 0.24 \, \text{sys}] \times 10^{-10} \, \text{m s}^{-2} \), the spatially-resolved data for 240 galaxies of different sizes and morphological types scatter around the mean radial acceleration relation (RAR)

\[
\frac{a_{\text{tot}}}{1 - e^{-\sqrt{\frac{a_{\text{bar}}}{g_1}}}},
\]

i.e. \( a_{\text{tot}} \approx a_{\text{bar}} \) for \( a_{\text{bar}} \gg g_1 \) while \( a_{\text{tot}} \approx \sqrt{a_{\text{bar}} g_1} \) for \( a_{\text{bar}} \ll g_1 \). Eq. (1) is inspired by the interpolation function of MOND and the existence of the RAR could be invoked as direct evidence for this alternative theory of gravity (basically, the empirical parameter \( g_1 \) embodies \( a_0 \)). However, numerical simulations of galaxy formation in the ΛCDM framework reproduce the overall shape of the observed correlation [10–13] (see, however, [14] for an exception). Here, the RAR emerges from the dissipative collapse of baryons within DM halos and is less influenced by the feedback of stars and active galactic nuclei. For disc galaxies forming at the centre of their host halos (central galaxies), the RAR reflects: i) the narrow range of the host virial masses; ii) the self-similar acceleration profiles of CDM haloes; iii) the tight correlation between baryonic mass, galaxy size and halo mass [11, 15]. However, simulated RARs tend to overpredict the value of \( g_1 \) regardless of the adopted subgrid feedback model (except possibly [12]). Furthermore, the scatter around the RAR for late-type galaxies \(( \lesssim 0.13 \, \text{dex}) \) is dominated by observational uncertainties, which is difficult to reconcile with simulations which show an intrinsic spread of comparable magnitude [16].

This Letter focuses on the low \( a_{\text{bar}} \) regime which has the potential to distinguish between the two competing scenarios described above. By analyzing a set of satellites of Andromeda and the Milky Way, [9] found that dwarf spheroidal galaxies (dSphs) do not follow Eq. (1) if \( g_1 \) is chosen to fit the data for more massive objects. Instead of dropping as \( g_{\text{tot}} \propto \sqrt{g_{\text{bar}}} \), the total acceleration stays approximately constant, \( g_{\text{tot}} \approx 10^{-11} \, \text{m s}^{-2} \), for \( g_{\text{bar}} \lesssim 9 \times 10^{-12} \, \text{m s}^{-2} \). It is currently impossible to draw conclusions based on this finding. In
fact, the expected signal in ΛCDM has only been computed for central galaxies that probe larger accelerations than faint dSphs. Moreover, as extensively discussed in [0], it is still unclear whether the observed flattening of the RAR is physical or due to observational artifacts. The inferred masses (or, equivalently, the values of $g_{\text{tot}}$) for faint dSphs are based on velocity-dispersion measurements [17] and are plagued by considerably larger uncertainties than measurements of rotation curves for late-type galaxies. Since dSphs have low velocity dispersions and their estimates are often based on a handful of observable stars, current results might be severely affected by unresolved binary systems [18]. Both this effect and out-of-equilibrium dynamics tend to inflate the measured velocity dispersions [19].

This situation provides us with a unique opportunity to predict the expected behavior of the RAR for satellite galaxies in the ΛCDM scenario.

**Numerical simulations.**—We use the ZOMG hydrodynamical simulations that have been comprehensively described in [20–22]. These runs follow the process of galaxy formation zooming in on a set of DM haloes with masses $M_h \approx 3 \times 10^{11} h^{-1} M_{\odot}$, where $h$ denotes the present-day value of the Hubble parameter in units of 100 km s$^{-1}$ Mpc$^{-1}$. The background cosmology and the linear power spectrum of density perturbations match the best-fit Planck+WP+highL+BAO model in [23]. The mass resolution is $m_* = m_{\text{gas}}/2 = m_{\text{DM}}/10.8 = 1.21 \times 10^4 h^{-1} M_{\odot}$ for stars, gas and DM, respectively. The simulations employ a supernova-feedback model and the resulting central galaxies closely match the stellar mass-halo mass and stellar mass-star formation rate relations observed at redshift $z = 0$ [21]. Similarly, the satellite galaxies are consistent with the observed baryonic Tully-Fisher relation, subhalo mass function, stellar fraction and stellar velocity dispersion [22].

**Method.**—DM haloes and their substructures are identified using the AMIGA halo finder code [24, 25]. We associate a ‘main central galaxy’ (MCG) with each of the resimulated central DM haloes by simply considering a spherical region extending for 10% of the halo radius. All substructures with a stellar component that lie within the splashback radius of the main halo (identified with the abrupt steepening of the spherically averaged mass-density profile as in [26]) are labelled as ‘main satellite galaxies’ (MSGs). Finally, we consider the dwarf central galaxies (DCGs) associated with less massive DM clumps lying between one and three splashback radii from the main halos. The centripetal accelerations are evaluated as $g_{\text{c}} = G M(< r)/r^2$, where $G$ is the gravitational constant and $M(< r)$ denotes the galaxy mass (total or baryonic) contained within the radius $r$. For MCGs, we compute the acceleration radial profiles and their correlated bootstrap errors (consistent with Poisson fluctuations) at 7 different positions extending from 1% to 10% of the halo radius equally spaced in log scale.

We find that the resulting $g_{\text{tot}}$ is consistent with measurements based on the gas rotational velocity, as done in observational studies. For MSGs and DCGs, accelerations are only computed at the stellar half-mass radius $R_{1/2}$ (i.e. the radius within which half of the stellar particles are located) to mimic the half-light radius used for observational data. We only consider galaxies containing more than 10 (gravitationally bound) stellar particles within $R_{1/2}$. The covariance matrix for $g_{\text{bar}}$ and $g_{\text{tot}}$ is estimated with the bootstrap method by resampling stellar particles within the individual objects. We find that errors on $\log g_{\text{bar}}$ and $\log g_{\text{tot}}$ approximately follow a bivariate Gaussian distribution. We fit Eq. (1) to our simulated data. Using Bayesian statistics, we jointly constrain $g_1$ and $\sigma_{\text{tot}}$, the intrinsic scatter around the RAR at fixed $g_{\text{bar}}$ (i.e. the rms value of the residuals of $\log g_{\text{tot}}$). For each measured pair ($\log g_{\text{bar}}$, $\log g_{\text{tot}}$), we consider a Gaussian (partial) likelihood function and we marginalize it over the unknown true value of the bayonic acceleration (which does not coincide with $g_{\text{bar}}$ due to measurement errors). We write the variance of $\log g_{\text{tot}}$ at fixed $g_{\text{bar}}$ as the sum in quadrature of the measurement error and
\[ \sigma_{\text{int}} \]

Eventually, we build posterior distributions for the model parameters by uniformly sampling the parameter space and assuming flat priors on \( \sigma_1 \) and \( \sigma_{\text{int}} \).

The RAR at redshift zero.— Fig. 2 compares real and simulated galaxies in the \( \log g_{\text{bar}}-\log g_{\text{tot}} \) plane at \( z = 0 \). Our MCGs and DCGs follow a tight RAR which is in excellent agreement with observations. For \( g_{\text{bar}} < 10^{-12} \text{ m s}^{-2} \), DCGs depart from Eq. (1) and tend to have higher \( g_{\text{tot}} \) (see also [12, 13]). The dSph satellite galaxies analyzed in Ref. [10] sprinkle around \( g_{\text{tot}} \lesssim 10^{-11} \text{ m s}^{-2} \) independently of \( g_{\text{bar}} \). Conversely, the simulated MSGs form a well defined sequence to a great extent aligned with the observed RAR (but with a larger scatter) and do not show any transition to a constant \( g_{\text{tot}} \) for the least massive satellites. For \( g_{\text{bar}} < 10^{-13} \text{ m s}^{-2} \), their mean \( g_{\text{tot}} \) at fixed \( g_{\text{bar}} \) lies slightly above the observed RAR of the central galaxies (in fact \( g_{\text{tot}} \propto g_{\text{bar}}^{0.5} \) in this regime) but slightly below that of DCGs. The observed dSph seem to be composed of two subsets: a sizeable fraction of them behave as the simulated satellites while the remainder align at \( g_{\text{tot}} \simeq 3 \times 10^{-11} \text{ m s}^{-2} \).

A quantitative analysis is presented in Fig. 2 where we compare the best-fit RARs for our MCGs and MSGs. The posterior probability densities of the model parameters show that centrals and satellites follow a RAR characterized by the same \( g_1 \) but with very different values for the intrinsic scatter. In fact, for the MCGs, we find \( g_1 = (1.40 \pm 0.07) \times 10^{-10} \text{ m s}^{-2} \) and \( \sigma_{\text{int}} = 0.048 \pm 0.005 \text{ dex} \) while, for the satellites, \( g_1 = (1.48 \pm 0.08) \times 10^{-10} \text{ m s}^{-2} \) and \( \sigma_{\text{int}} = 0.192 \pm 0.008 \text{ dex} \). The characteristic acceleration we measure is larger than, but compatible with, the observed value for MCGs which is plagued with a relatively large systematic error. We note that the model-fitting method influences the result. For instance, adopting the (frequentist) orthogonal-distance regression algorithm to fit only the characteristic acceleration (as in [8, 9]) yields \( g_1 = (1.19 \pm 0.02) \times 10^{-10} \text{ m s}^{-2} \) for MCGs, in very good agreement with the observational results.

Following [9], we define a ‘high-quality’ sample of satellites that contain a large number of stellar particles, have small ellipticities and are barely affected by the tidal field of the host galaxy. This does not significantly change the best-fit intervals for \( g_1 \) and \( \sigma_{\text{int}} \).

Independency of the RAR on the satellite properties.— Given the large scatter characterizing the RAR for MSGs, we investigate whether sub-classes of satellites with different physical properties follow distinct RARs at \( z = 0 \). We first sort the satellites based on some physical property. Then we separately fit Eq. (1) to the subsets containing the upper and lower 20 per cent of the sorted data. Specifically, we examine the following variables: (a) the tidal acceleration at \( R_{1/2} \) due to the gravitational field of the host galaxy, \( g_{\text{tidal}} = 2 G M_{\text{host}} R_{1/2}/D^2_{\text{host}} \), as defined in [9]; (b) The distance of the satellite from the main galaxy; (c) The triaxiality parameter of the stellar distribution; (d) The minor-to-major and medium-to-major axis ratios; (e) The cosine of the angle between the satellite velocity and the radial direction with respect to the central host; (f) The stellar concentration defined as the ratio between the radius enclosing 80% of the stellar mass and that enclosing 20% of it; (g) The accretion time of the satellite on to its host; (h) The mass loss experienced between accretion time and redshift zero. The only significant discrepancy we find is between the credibility intervals of \( \sigma_{\text{int}} \) for the sub-
samples of case (h): the scatter is three times larger for satellites that experienced a large mass loss.

**Time evolution of the RAR.**—Finally, we study the RAR at $z > 0$. At all epochs, we identify a well defined relation for both MCGs and MSGs which we fit using Eq. (1). Our findings, summarized in Fig. 3, show that both $g_l$ and $\sigma_{\text{int}}$ evolve little with time. To good approximation, the best-fit parameters for the RAR scale linearly with the scale factor $a$ of the universe. In the range $0.33 \leq a \leq 1$, $g_l \simeq (-0.84 a + 2.23) \times 10^{-10} \text{m s}^{-2}$ for MCGs and $g_l \simeq (-0.72 a + 2.11) \times 10^{-10} \text{m s}^{-2}$ for MSGs (the uncertainty on the parameters is $\sim 10\%$). On the other hand, the intrinsic scatter around the RAR stays approximately constant for MCGs, $\sigma_{\text{int}} \simeq -0.01 a + 0.06$ dex, and grows as $\sigma_{\text{int}} \simeq 0.1 a + 0.1$ dex for the satellites.

The evolution of the RAR for central galaxies is promoted by stellar feedback which drives important outflows at high redshift [12].

In order to characterize the time evolution of the satellites, in the top panel of Fig. 4, we partition them based on their $g_{\text{bar}}$ at the present time and plot the median trajectory of each subset in the $g_{\text{bar}}$-$g_{\text{tot}}$ plane as a function of redshift (indicated by the color). The trend is to move from the top right to the bottom left nearly parallel to the RAR. The other panels of Fig. 4 reveal the reason for this tendency. Essentially, while $R_{1/2}$ and the DM mass within it tend to grow with time, the stellar mass of the satellites decreases. This is the net result of tidal stripping that makes satellites more DM dominated with time. Since the DM and the stars in a satellite follow distinct spatial distributions at the accretion time, they react differently to tidal forces. The (physical) extension of the stellar distribution increases during the evolution [27, 28] while the DM density profile becomes more concentrated [29, 30]. Of course, individual objects follow complex trajectories in the $g_{\text{bar}}$-$g_{\text{tot}}$ plane which produce some scatter around the median trend (see also [31]).

**Conclusions.**—The RAR is an empirical law describing a tight relation between the radial acceleration generated by the visible matter in galaxies and the actual acceleration derived from kinematic measurements. For bright central galaxies, the correlation is such that both $g_{\text{bar}}$ and $g_{\text{tot}}$ decrease in the outer regions. This result could hint towards a scenario in which there is no DM and the law of gravity needs to be modified along the lines of MOND. Galaxy-formation models within the ΛCDM scenario are able to reproduce the observed relation, although with too large a scatter. Ref. [9] provides evidence that nearby dSph satellite galaxies depart from the RAR and show a constant $g_{\text{tot}}$ for $g_{\text{bar}} \lesssim 10^{-12} \text{m s}^{-2}$. However, the authors caution that unresolved binary stars and out-of-equilibrium dynamics could bias the measurements of $g_{\text{tot}}$ high in these low-mass structures. It is yet unclear what are the implications for the theory of gravity. The missing pieces of the puzzle are (a) more precise measurements and (b) accurate theoretical predictions for the behaviour of satellite galaxies in ΛCDM. This work supplies the latter by making use of a suite of zoom hydrodynamical simulations. Our main results are: (i) At $z = 0$, the simulated satellites scatter around a well defined sequence in the $g_{\text{bar}}$-$g_{\text{tot}}$ plane which is approximately aligned with the observed RAR for central galaxies and does not show any transition to a constant $g_{\text{tot}}$ at low accelerations. (ii) For the least massive objects, the satellite sequence is shallower than the RAR for central galaxies and does not show any transition to a constant $g_{\text{tot}}$ as $g_{\text{tot}}$ increases with increasing $z$.

![FIG. 4](image-url)
distribution gets more concentrated. (vii) Since satellites follow the RAR of the central galaxies before accreting on to their hosts and evolve along the main sequence afterwards, their $g_t$ shows the same time evolution as for the central galaxies. Given the wide variety of the evolutionary paths, the scatter around the relation between the accelerations for the satellites increases with time and with decreasing $g_{\text{bar}}$. (viii) In our simulations, residuals from the RAR for the satellites do not correlate with $g_{\text{hid}}$. Conversely, in the MOND framework, satellites in a strong external gravitational field show different internal accelerations than if they were isolated. Detecting the absence or presence of the correlations from observations would therefore provide a powerful test of the theory of gravity.

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