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# Observation of a Degenerate Fermi Gas Trapped by a Bose-Einstein Condensate

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We report on the formation of a stable quantum degenerate mixture of fermionic  ${}^6\text{Li}$  and bosonic  ${}^{133}\text{Cs}$  in an optical trap by sympathetic cooling near an interspecies Feshbach resonance. New regimes of quantum degenerate Bose-Fermi mixtures are identified. With moderate attractive interspecies interactions, we show that a degenerate Fermi gas of Li can be fully confined in a Cs Bose-Einstein condensate without external potentials. For stronger attraction where mean-field collapse is expected, no such instability is observed. Potential mechanisms to explain this phenomenon are discussed.

Mixtures of atomic quantum gases are an exciting platform to study a rich variety of physics, such as the observation of heteronuclear molecules [1–7], Bose and Fermi polarons [8–13], and superfluid mixtures [14–16]. Novel quantum phases have been suggested theoretically [17–20] and probed experimentally [21–24]. Intriguing quantum excitations [25–28], mediated long-range interactions [29, 30], and pairing behavior [31–33] are proposed based on degenerate Bose-Fermi mixtures.

An extensive review of previous work and specific mixtures used is found in Ref. [34]. To date, many experiments exploring quantum degenerate Bose-Fermi mixtures exhibit small to moderate mass imbalance [19, 20, 35–37]. For larger mass imbalance, new phenomena are expected to arise [16, 33, 38, 39]. Light fermionic  ${}^6\text{Li}$  and heavy bosonic  ${}^{133}\text{Cs}$  yields the largest mass imbalance among stable alkali atoms. This combination offers rich interaction properties that are well characterized [40–44], and there exist interspecies Feshbach resonances at magnetic fields where both the Cs Bose-Einstein condensate (BEC) and Li Fermi gas are stable. This makes Li-Cs an excellent platform to investigate many-body physics of Bose-Fermi mixtures.

Here, we explore two novel regimes of dual-degenerate Bose-Fermi mixtures accessed by this combination of atomic species by using the tunable interactions afforded by an interspecies Feshbach resonance. First, we find that for small attractive interactions, degenerate fermions are found fully trapped and confined by the Cs BEC. Second, at large attractive scattering lengths, we find the mixture is stable in the mean-field collapse regime [18].

Our experimental procedure to prepare a quantum degenerate Bose-Fermi mixture follows. After initial laser cooling and optical trapping as described in Ref. [46], we obtain samples of  $2 \times 10^6$  Li atoms in a deep translatable optical dipole trap, and  $2 \times 10^6$  Cs atoms in a separate optical trap. At this point, we have a nearly equal spin mixture of Li atoms in the  $F=1/2$  hyperfine manifold, referred to here as  $\text{Li}_a$  and  $\text{Li}_b$ , and Cs atoms spin-polarized into the  $|F, m_F\rangle = |3, 3\rangle$  state, where  $F$  is the total angular momentum quantum number and  $m_F$  is the magnetic quantum number. We then ramp the magnetic field to 894.3 G. This corresponds to a scattering length for Cs of  $a_{BB} = 290 a_0$  and  $a_{\text{Li}_a - \text{Li}_b} = -8\,330 a_0$  for Li, where

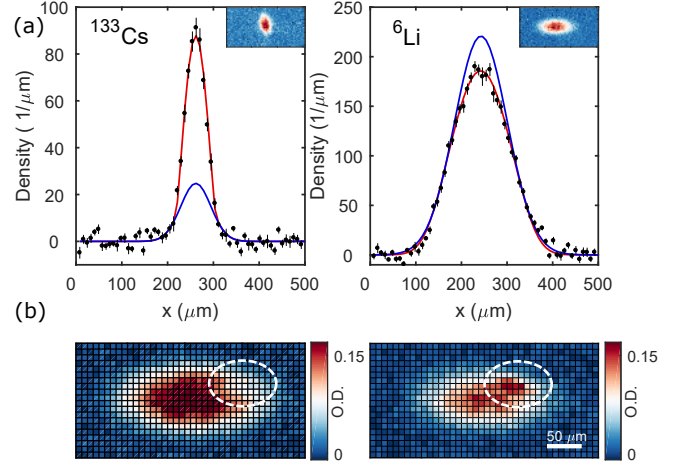


FIG. 1: Simultaneous quantum degeneracy of  ${}^6\text{Li}$  and  ${}^{133}\text{Cs}$ . (a) Left panel: A bimodal distribution of a Cs BEC is visible after a 30 ms TOF expansion. The blue curve indicates the thermal fraction while the red curve shows a fit to the thermal and condensate fraction. Right panel: For Li, a Gaussian fit to the high momentum tail of the atoms after a 1.5 ms TOF overestimates the density at the center (blue curve). The full distribution is fit well using a polylogarithm function (red curve) with  $T/T_F = 0.2(1)$  [45]. For repulsive interactions with  $a_{BF} = 1000 a_0$  (left panel (b)), the Li density is suppressed at the location of the Cs BEC after a 1.5 ms TOF. Conversely, the Li density in the same location is enhanced for attractive interactions with  $a_{BF} = -580 a_0$  (right panel (b)).

$a_0$  is the Bohr radius. This yields efficient evaporative cooling for Cs and the spin mixture of Li. Both species are evaporatively cooled over 10 s to approximately 300 nK. We then remove  $\text{Li}_b$  with a resonant light pulse leaving only the absolute ground state of Li and Cs in the optical dipole trap.

These two species exhibit an interspecies Feshbach resonance at 892.64 G [40, 42, 44] that tunes the interaction between Li and Cs. Across the width of this resonance, the Cs-Cs scattering length varies slowly from  $a_{BB} = 220 \sim 280 a_0$ . In this range, good evaporative cooling efficiency for Cs promises the ability to sympathetically cool  $\text{Li}_a$  atoms for suitable Li-Cs scattering length. To begin sympathetic cooling, we ramp the mag-

netic field to 891 G ( $a_{BF} = 20 a_0$ ) and sequentially load both species into a dual-color optical dipole trap comprised of 785 and 1064 nm light [46]. This trap allows the cancellation of the relative gravitational sag for Li and Cs and ensures good overlap between the species at low temperatures [46]. To prepare a mixture with attractive or repulsive interspecies interactions, once the samples are mixed we ramp the magnetic field over 10 ms to either 891.9 or 893.8 G, yielding an interspecies scattering length  $a_{BF} = 120$  or  $-180 a_0$ , respectively. We then perform evaporative cooling for 1.5 s to obtain degenerate samples.

Detection of quantum degeneracy is performed by analyzing time-of-flight (TOF) absorption images of both species. For Cs, after evaporation we obtain a BEC of  $10^4$  atoms with low thermal fraction at a temperature  $T_{Cs} = 20$  nK, as shown in Fig. 1(a) left panel. For thermometry of Li, we first adiabatically ramp the interspecies scattering length over 25 ms to a small value ( $|a_{BF}| < 30 a_0$ ) so the Cs BEC does not influence the Li cloud. We then release the atoms and image the Li after 1.5 ms expansion, as shown in the right panel of Fig 1(a). We determine the Fermi temperature  $T_F = 480(50)$  nK from the known trapping frequencies of  $\omega_F = 2\pi \times (36, 430, 430)$  Hz, and  $T/T_F = 0.2(1)$  from fitting the absorption images using a polylogarithm function [45]. From these fits, we observe that sympathetic cooling works well for attractive and repulsive interspecies interactions and both species reach deep quantum degeneracy on either side of resonance.

In the presence of strong Li-Cs interaction, the density distribution of Li is distorted. Example images are shown in Fig. 1(b). Here, we shift the position of the Cs BEC to the edge of the Li cloud to gain visual clarity of the effect. For repulsive interactions (Fig 1(b) left panel), Li is repelled from the BEC. Conversely, for attractive interactions (Fig 1(b) right panel), Li atoms are attracted to the Cs BEC.

Per mean field theory, the potential experienced by one atomic species due to interspecies interactions is given by  $2\pi\hbar^2 a_{BF} \left( \frac{1}{m_B} + \frac{1}{m_F} \right) n(\vec{r})$ , where  $m_{F(B)}$  is the mass of the fermion (boson),  $\hbar$  is the reduced Planck's constant, and  $n(\vec{r})$  is the density distribution of the other species. In our case, the density of the Cs BEC is over one order of magnitude larger than the Li degenerate Fermi gas, so the potential experienced by the Li is significantly greater. Given the typical density of a Cs BEC of  $n_B = 5 \times 10^{13} \text{cm}^{-3}$ , for  $a_{BF} = -500 a_0$  the trap depth in temperature units felt by Li is 450 nK. This large depth suggests that Li can be loaded into the Cs BEC even in the absence of another confining potential.

To investigate this possibility experimentally, we perform a Stern-Gerlach sequence to separate the Li atoms trapped by the Cs BEC from those that are not, as depicted in Fig. 2a. We first prepare a degenerate Bose-Fermi mixture in a single beam trap by performing our usual sequence and slowly ramping the intensity of the 785 nm beam to zero. In this simplified con-

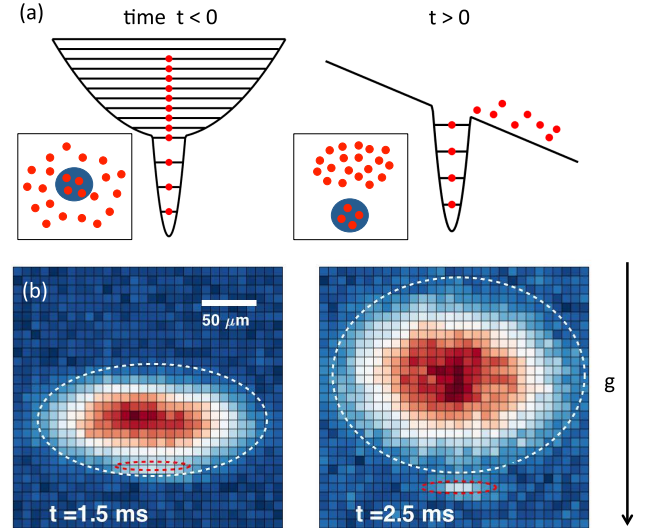


FIG. 2: Stern-Gerlach separation of Li atoms trapped in a Cs BEC. Shown schematically in (a), strong attractive interspecies interactions confine a fraction of Li atoms (red dots) within the Cs BEC (blue circle). At  $t = 0$  we remove the optical trap and apply a magnetic field gradient to separate those trapped from the rest of the sample. Example images of Li after a short TOF are shown in (b). Dashed red circles indicate the position and size of the BEC at the imaging time and the white dashed line indicates the Fermi radius.

figuration, the overlap of the two species is controlled by the magnetic field gradient, and we obtain trap frequencies of  $\omega_B = 2\pi \times (6.5, 130, 160)$  Hz for Cs and  $\omega_F = 2\pi \times (36, 400, 400)$  Hz for Li. Next, we ramp the magnetic field gradient to 4 G/cm providing a force against gravity and simultaneously increase the interaction strength to  $-650 a_0$  over 30 ms. This deepens the potential so a reasonable number of Li are trapped and shifts the Li up such that the Cs BEC sits on the lower edge of the Li cloud. We then extinguish the optical trap while leaving the magnetic field and gradient on. The magnetic field gradient is sufficient to over-levitate Li, but not the Cs atoms. Therefore, Li atoms trapped by Cs BEC fall downwards.

Results of this experiment are shown in the absorption images of Li after a varying TOF, see Fig. 2 (b). In each image, the white dashed curve shows the maximum extent of the cloud from the calculated Fermi radius and the red dashed curve shows the position and spatial extent of the Cs BEC. After a TOF, Li atoms trapped in the Cs BEC spatially separate from the rest of the sample. These Li atoms are contained in the volume of the Cs BEC and follow its trajectory over the entire TOF. Once spatially separated, Li atoms trapped in the Cs BEC can be counted. By following the previously described Stern-Gerlach procedure at different magnetic field values we measure the number of Li atoms trapped by the Cs BEC as a function of  $a_{BF}$  as shown in Fig. 3.

Owing to the Pauli exclusion principle, there is a limited number of Li atoms  $N < N_{max}$  that can be trapped

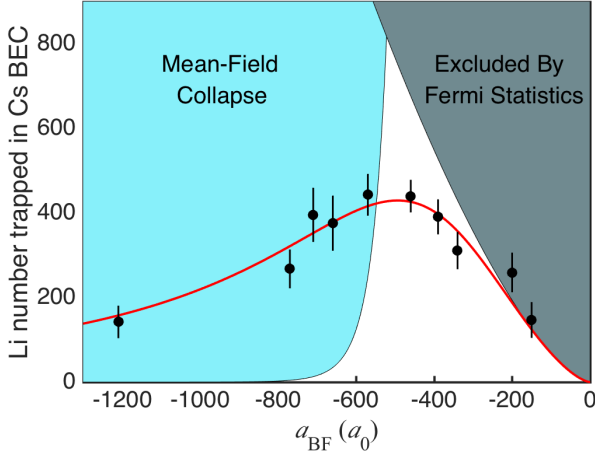


FIG. 3: Number of Li atoms trapped in Cs BEC. As a function of the interspecies scattering length  $a_{BF}$  at the end of the magnetic field ramp, we measure the number of Li atoms trapped in the Cs BEC after a 1.5 ms Stern-Gerlach separation (black dots). Within the approximation described in the text, the grey shaded region represents the region excluded by Fermi statistics and the blue shaded area indicates the region where mean-field collapse is expected. The red curve shows a fit based on a rate equation model describing the steady-state number of atoms trapped by the Cs BEC (see text).

within the Cs BEC. Assuming the density of the BEC is not perturbed by Li atoms, the maximum number  $N_{max}$  can be found analytically. Within the mean-field and Thomas-Fermi approximations, the density distribution of the BEC is an inverted parabola, yielding a harmonic trap for Li with trap depth  $U_0 = \frac{1}{2}(\frac{m_B}{m_F} + 1)\frac{|a_{BF}|}{a_{BB}}\mu$  and trapping frequency  $\omega_{trap} = [\frac{1}{2}\frac{m_B}{m_F}(\frac{m_B}{m_F} + 1)\frac{|a_{BF}|}{a_{BB}}]^{1/2}\omega_B$ , where  $\omega_B$  is the trapping frequency for Cs and  $\mu$  is its chemical potential. Notably the trap frequency for Li  $\omega_F$  is 16 times larger than the trap frequency for Cs due to mass imbalance alone. Therefore, the dynamics of Li in the Cs BEC are much faster than the condensate itself.

By setting the Fermi energy equal to the trap depth, one finds that for  $a_{BF} < 0$  the maximum number of Li trapped by the Cs BEC is

$$N_{max} = \frac{1}{12\sqrt{2}} \left[ \left( 1 + \frac{m_F}{m_B} \right) \frac{|a_{BF}|}{a_{BB}} \right]^{3/2} \left( \frac{\mu}{\hbar\omega_B} \right)^3. \quad (1)$$

This limit is indicated by the grey shaded region in Fig. 3 and is consistent with our measurement for  $|a_{BF}| < 400 a_0$ . For these weak interactions, since the number of Li trapped is close to the maximum, the Li remains deeply quantum degenerate.

For a large negative scattering length, mean-field calculations predict another limit on the number of Li atoms that can be trapped by the Cs BEC. When the Li density exceeds a critical value  $n_{crit}$ , theory predicts a collapse of the mixture due to the loss of mechanical stability. For a homogenous gas, the critical density is [18]

$$n_{crit} = \frac{4\pi}{3} \frac{m_B^3 m_F^3}{(m_B + m_F)^6} \frac{a_{BB}^3}{a_{BF}^6}. \quad (2)$$

The condition for collapse in a trapped gas is found following the numerical procedure described in Ref. [18]. We find that the system collapses when the peak density of the fermions exceeds the critical density given in Eq. 2. This limit sets the lower boundary of the shaded blue region in Fig. 3. Shown in Fig. 3 as well as observed in other experiments including a longer hold time, for large negative scattering lengths  $a_{BF}$  we find significantly more Li atoms trapped in the Cs BEC than permitted by mean-field theory.

One possible explanation for the lack of mean-field collapse is beyond mean-field terms similar to the Lee-Huang-Yang term for bosons [47]. Observed in dipolar quantum gases [48], this effect leads to a short-range repulsion and stabilizes a collapsing BEC with dipolar interactions, and likely a Bose-Bose mixture with strong interspecies attraction [49]. The scenario to stabilize an attractive Bose-Fermi mixture with beyond mean-field effects [50] requires further theoretical investigation.

In our system, another possible explanation for the lack of mean-field collapse is a dynamical process including three-body loss and Fermi statistics. The association of higher particle number with collisional loss seems counterintuitive, but the strong density dependence of three-body collisions is key to removing atoms preferentially from the high-density region and preventing mean-field collapse.

To explore this possibility, we suggest the following model. Since the dynamical timescale for Li is much shorter than for Cs, we describe the density of Li atoms trapped in the Cs BEC as

$$\frac{dn}{dt} = Aa_{BF}^2 n_F n_B f - Ba_{BF}^4 n_B^2 n, \quad (3)$$

where  $A$  and  $B$  are constants,  $n_B$  is the density of the Cs BEC,  $n$  is the density of Li confined in the BEC, and  $n_F$  is the density of unconfined Li. The first term accounts for elastic collisions that populate available states in the BEC potential with probability  $f \approx 1 - N/N_{max}$  given by Fermi statistics. The second term represents three-body loss due to Li-Cs-Cs collisions [51].

Due to the small number of Li atoms trapped in the Cs BEC and the large separation in dynamical timescales between the two species, we assume that the BEC density profile and Cs number are not disturbed in the time the Li density profile reaches steady-state. Averaging Eq. (3) over the extent of the Cs BEC, we obtain  $d\bar{n}/dt = A'a_{BF}^2 \bar{n}_B \bar{n}_F f - B'a_{BF}^4 \bar{n}_B^2 \bar{n}$ , where  $\bar{x}$  is the averaged value of  $x$ , and  $A'$  and  $B'$  are constants incorporating geometric factors from averaging.

In steady-state  $d\bar{n}/dt = 0$ , we obtain  $N = N_{max}/(1 + Ca_{BF}^2 N_{max})$ , where  $C$  is a constant. Combining this expression with Eq. (1), we fit our data in Fig. 3 with  $C$  as



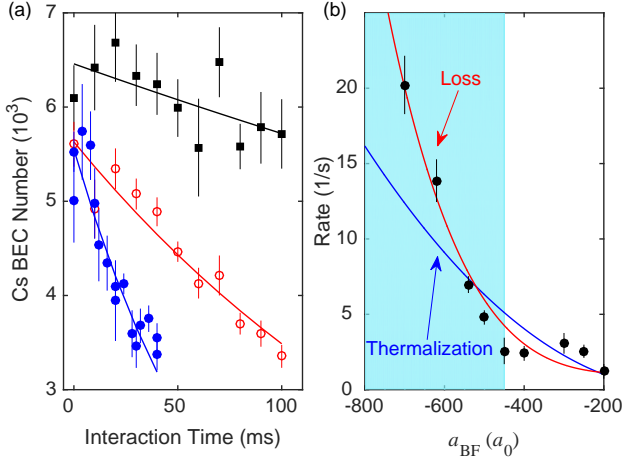


FIG. 4: Loss dynamics of Cs BEC immersed in Li degenerate Fermi gas. (a) Atom number in Cs BEC for  $a_{BF} = -200$  (black),  $-500$  (red), and  $-620$   $a_0$  (blue). The data is well described by smooth exponential loss (solid lines). The  $1/e$  loss rates extracted from these fits shown in panel (b) are well fit by the expected  $a_{BF}^4$  scaling including a constant offset in the loss rate to account for measured Cs-Cs-Cs recombination (red line). An estimation of the thermalization rate (see text) is indicated by the solid blue curve. The loss rate exceeds the thermalization rate at  $a_{BF} = -520a_0$ , above which the system no longer reaches thermal equilibrium.

the only fitting parameter. The result yields good agreement. In the case of no collisional loss  $B' = 0$ , the fit function reproduces the limit where a deeply degenerate Fermi gas of  $N_{max}$  Li atoms is supported by the BEC.

In this picture, for large negative scattering length, Li atoms are quickly lost through recombination. Since this process is the highest at the center of the BEC, the loss of Li atoms prevents the runaway density build up at the trap center. Similar loss of Cs atoms occurs predominately at the trap center. However, the loss of Cs is slowed by the limited rate at which its volume is replenished with fermions from the surrounding Fermi gas.

In Fig. 4, we show the evolution dynamics of a Cs BEC immersed in the Li degenerate Fermi gas. Here, we first create a degenerate mixture in the single beam dipole trap. After quickly ramping the magnetic field to a desired value, we measure the number of Cs atoms in the condensate after a TOF. The atom number in the BEC smoothly decays with a loss rate proportional to  $a_{BF}^4$  as expected [52]. No dramatic drop in atom number associated with collapse is observed.

Mean-field calculations assume that the system thermalizes quickly enough to reach equilibrium. However, thermalization is known to be slow for systems with large mass imbalance. Unlike atoms must undergo  $\xi = 3(m_B + m_F)^2 / (4m_B m_F)$  collisions to thermalize [53]. An estimation of the collision rate between degenerate Bose and Fermi gases is in general complicated, and we employ

a model for thermal gases that offers an upper bound on the collision rate given by  $\gamma = 4\pi a_{BF}^2 \bar{v} \int d^3r n'_F(\vec{r}) n_B(\vec{r})$ , where  $n'_F(\vec{r})$  is the density of fermions available for collisions and the averaged relative velocity of Li and Cs atoms is given by  $\bar{v} \approx \sqrt{2E_F/m_F}$  in our experiment. Combining the above results with the fermion density's slow variation across the BEC, we obtain the thermalization rate  $\Gamma = \frac{N'_F + N_B}{N'_F N_B} \frac{\gamma}{\xi}$  [54] as

$$\Gamma \approx 3.74 \frac{m_B m_F^2}{(m_B + m_F)^2} \frac{(N_B + N'_F)}{N_F^{1/3}} \frac{a_{BF}^2 \bar{\omega}_F^2}{\hbar}, \quad (4)$$

where  $\bar{\omega}_F$  is the geometric mean of the trap frequencies of the fermions,  $N_B$  is the number of bosons and  $N'_F$  is the number of fermions participating in collisions. Using  $N'_F \approx g(E_F) k_B T = 3N_F (T/T_F)$  where  $g(\epsilon)$  is the single particle density of states we obtain the thermalization rate, shown in Fig 4(b).

At large scattering lengths  $|a_{BF}| > 520a_0$ , the loss rate exceeds the thermalization rate, suggesting the mixture will deviate from thermal equilibrium. Notably, the dominance of inelastic loss is more likely to occur in a Li-Cs system due to its strong mass imbalance. In comparison to the  $^{40}\text{K}$ - $^{87}\text{Rb}$  mixture in Refs. [19, 20] where mean-field collapse was reported, our thermalization rate is two times lower (from Eq. (4)), while the three-body collision rate increases by a factor of two [52] for the same trap frequency and atom numbers. Consequently, our system with large attractive Li-Cs interactions likely reaches a dynamical equilibrium where fast loss allows the mixture to survive for much longer than the mean-field expectation.

In conclusion, we report the first quantum degenerate mixture of Li and Cs and use this system to probe novel regimes of Bose-Fermi mixtures. For weak attractive interactions, a degenerate Fermi gas with few hundred Li atoms is confined within the BEC. This represents an intriguing quantum object well-suited for future study. For strong attractive interactions, we observe that the system is stable against mean-field collapse. We present one possible model to explain this observation based on the relative timescales of loss and thermalization. Other possible explanations involving beyond mean-field effects are under investigation. The lack of the mean-field collapse in our system allows us to explore a region of the Bose-Fermi mixture that was previously thought inaccessible.

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- [1] T. Takekoshi, L. Reichsöllner, A. Schindewolf, J. M. Hutson, C. R. Le Sueur, O. Dulieu, F. Ferlaino, R. Grimm, and H. C. Nägerl, *Phys. Rev. Lett.* **113**, 205301 (2014).
- [2] K. K. Ni, S. Ospelkaus, M. H. G. de Miranda, A. Pe'er, B. Neyenhuis, J. J. Zirbel, S. Kotochigova, P. S. Julienne, D. S. Jin, and J. Ye, *Science* **322**, 231 (2008).
- [3] M. S. Heo, T. T. Wang, C. A. Christensen, T. M. Rvachov, D. A. Cotta, J. H. Choi, Y. R. Lee, and W. Ketterle, *Phys. Rev. A* **86**, 021602(R) (2012).
- [4] S. D. Kraft, P. Staunum, J. Lange, L. Vogel, R. Wester, and M. Weidemüller, *J. Phys. B* **39**, S993 (2006).
- [5] R. Roy, R. Shrestha, A. Green, S. Gupta, M. Li, S. Kotochigova, A. Petrov, and C. H. Yuen, *Phys. Rev. A* **94**, 033413 (2016).
- [6] J. W. Park, S. A. Will, and M. W. Zwierlein, *Phys. Rev. Lett.* **114**, 205302 (2015).
- [7] A.-C. Voigt, M. Taglieber, L. Costa, T. Aoki, W. Wieser, T. W. Hänsch, and K. Dieckmann, *Phys. Rev. Lett.* **102**, 020405 (2009).
- [8] M. G. Hu, M. J. Van De Graaff, D. Kedar, J. P. Corson, E. A. Cornell, and D. S. Jin, *Phys. Rev. Lett.* **117**, 055301 (2016).
- [9] N. B. Jørgensen, L. Wacker, K. T. Skalmstang, M. M. Parish, J. Levinsen, R. S. Christensen, G. M. Bruun, and J. J. Arlt, *Phys. Rev. Lett.* **117**, 055302 (2016).
- [10] C. Kohstall, M. Zaccanti, M. Jag, A. Trenkwalder, P. Massignan, G. M. Bruun, F. Schreck, and R. Grimm, *Nature* **485**, 615 (2012).
- [11] A. Schirotzek, C. H. Wu, A. Sommer, and M. W. Zwierlein, *Phys. Rev. Lett.* **102**, 230402 (2009).
- [12] F. Scazza, G. Valtolina, P. Massignan, A. Recati, A. Amico, A. Burchianti, C. Fort, M. Inguscio, M. Zaccanti, and G. Roati, *Phys. Rev. Lett.* **118**, 083602 (2017).
- [13] M. Cetina, M. Jag, R. S. Lous, J. T. M. Walraven, R. Grimm, R. S. Christensen, and G. M. Bruun, *Phys. Rev. Lett.* **115**, 135302 (2015).
- [14] R. Roy, A. Green, R. Bowler, and S. Gupta, *Phys. Rev. Lett.* **118**, 055301 (2017).
- [15] I. Ferrier-Barbut, M. Delehay, S. Laurent, A. Griem, B. Rem, F. Chevy, and C. Salomon, *Science* **345**, 1035 (2014).
- [16] X. C. Yao, H. Z. Chen, Y. P. Wu, X. P. Liu, X. Q. Wang, X. Jiang, Y. Deng, Y. A. Chen, and J. W. Pan, *Phys. Rev. Lett.* **117**, 145301 (2016).
- [17] F. M. Marchetti, C. J. M. Mathy, D. A. Huse, and M. M. Parish, *Phys. Rev. B* **78**, 134517 (2008).
- [18] K. Mølmer, *Phys. Rev. Lett.* **80**, 1804 (1998).
- [19] M. Zaccanti, C. D'Errico, F. Ferlaino, G. Roati, M. Inguscio, and G. Modugno, *Phys. Rev. A* **74**, 041605(R) (2006).
- [20] S. Ospelkaus, C. Ospelkaus, L. Humbert, K. Sengstock, and K. Bongs, *Phys. Rev. Lett.* **97**, 120403 (2006).
- [21] K. Sengupta, N. Dupuis, and P. Majumdar, *Phys. Rev. A* **75**, 063625 (2007).
- [22] M. Lewenstein, L. Santos, M. A. Baranov, and H. Fehrmann, *Phys. Rev. Lett.* **92**, 050401 (2004).
- [23] T. Best, S. Will, U. Schneider, L. Hackermüller, D. van Oosten, I. Bloch, and D. S. Lühmann, *Phys. Rev. Lett.* **102**, 030408 (2009).
- [24] K. Gunter, T. Stoferle, H. Moritz, M. Kohl, and T. Esslinger, *Phys. Rev. Lett.* **96**, 180402 (2006).
- [25] J. Santhanam, V. M. Kenkre, and V. V. Konotop, *Phys. Rev. A* **73**, 013612 (2006).
- [26] S. K. Adhikari, *Phys. Rev. A* **72**, 053608 (2005).
- [27] T. Karpiuk, M. Brewczyk, S. Ospelkaus-Schwarzer, K. Bongs, M. Gajda, and K. Rzążewski, *Phys. Rev. Lett.* **93**, 100401 (2004).
- [28] T. Karpiuk, M. Brewczyk, and K. Rzążewski, *Phys. Rev. A* **73**, 053602 (2006).
- [29] M. J. Bijlsma, B. A. Heringa, and H. T. C. Stoof, *Phys. Rev. A* **61**, 053601 (2000).
- [30] S. De and I. B. Spielman, *Applied Physics B* **114**, 527 (2014).
- [31] D. V. Efremov and L. Viverit, *Phys. Rev. B* **65**, 134519 (2002).
- [32] E. Fratini and P. Pieri, *Phys. Rev. A* **81**, 051605(R) (2010).
- [33] S. Gopalakrishnan, C. V. Parker, and E. Demler, *Phys. Rev. Lett.* **114**, 045301 (2015).
- [34] R. Onofrio, *Physics-Uspekhi* **59**, 1129 (2017).
- [35] M. Taglieber, A.-C. Voigt, T. Aoki, T. W. Hänsch, and K. Dieckmann, *Phys. Rev. Lett.* **100**, 010401 (2008).
- [36] J. W. Park, C.-H. Wu, I. Santiago, T. G. Tiecke, S. Will, P. Ahmadi, and M. W. Zwierlein, *Phys. Rev. A* **85**, 051602(R) (2012).
- [37] V. D. Vaidya, J. Tiamsuphat, S. L. Rolston, and J. V. Porto, *Phys. Rev. A* **92**, 043604 (2015).
- [38] E. Fratini and P. Pieri, *Phys. Rev. A* **85**, 063618 (2012).
- [39] A. Banerjee, *Journal of Physics B: Atomic, Molecular and Optical Physics* **42**, 235301 (2009).
- [40] S. K. Tung, C. Parker, J. Johansen, C. Chin, Y. Wang, and P. S. Julienne, *Phys. Rev. A* **87**, 010702(R) (2013).
- [41] S. K. Tung, K. Jimenez-Garcia, J. Johansen, C. V. Parker, and C. Chin, *Phys. Rev. Lett.* **113**, 240402 (2014).
- [42] J. Johansen, B. J. DeSalvo, K. Patel, and C. Chin, *Nat. Phys.* **13**, 731-735 (2017).
- [43] J. Ulmanis, S. Häfner, R. Pires, E. D. Kuhnle, M. Weidemüller, and E. Tiemann, *New J. Phys.* **17**, 055009 (2015).
- [44] M. Repp, R. Pires, J. Ulmanis, R. Heck, E. D. Kuhnle, M. Weidemüller, and E. Tiemann, *Phys. Rev. A* **87**, 010701 (2013).
- [45] W. Ketterle and M. W. Zwierlein, in *Ultracold Fermi Gases, Proceedings of the International School of Physics Enrico Fermi, Course CLXIV* (2006).
- [46] J. Johansen, Ph.D. thesis, University of Chicago (2017).
- [47] T. D. Lee, K. Huang, and C. N. Yang, *Phys. Rev.* **106**, 1135 (1957).
- [48] I. Ferrier-Barbut, H. Kadau, M. Schmitt, M. Wenzel, and T. Pfau, *Phys. Rev. Lett.* **116**, 215301 (2016).
- [49] D. S. Petrov, *Phys. Rev. Lett.* **115**, 155302 (2015).
- [50] A. P. Albus, S. A. Gardiner, F. Illuminati, and M. Wilkens, *Phys. Rev. A* **65**, 053607 (2002).
- [51] E. Braaten and H. W. Hammer, *Physics Reports* **428**, 259 (2006).
- [52] J. P. D'Incao and B. D. Esry, *Phys. Rev. A* **73**, 030702(R) (2006).
- [53] G. Delannoy, S. G. Murdoch, V. Boyer, V. Josse, P. Bouyer, and A. Aspect, *Phys. Rev. A* **63**, 051602(R) (2001).
- [54] A. Mosk, S. Kraft, M. Mudrich, K. Singer, W. Wohlleben,

R. Grimm, and M. Weidemüller, Applied Physics B **73**, 791 (2001).