Spin-Orbit Coupling Controlled J=3/2 Electronic Ground State in 5d^3 Oxides


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Spin-orbit coupling controlled $J = 3/2$ electronic ground state in 5$d^3$ oxides

A. E. Taylor,¹ S. Calder,¹ R. Morrow,² H. L. Feng,³ M. H. Upton,⁴ M. D. Lumsden,¹ K. Yamaura,³ P. M. Woodward,² and A. D. Christianson¹, ⁵,*

¹Quantum Condensed Matter Division, Oak Ridge National Laboratory, Oak Ridge, Tennessee 37831, USA
²Department of Chemistry, The Ohio State University, Columbus, Ohio 43210-1185, USA
³Research Center for Functional Materials, National Institute for Materials Science, 1-1 Namiki, Tsukuba, Ibaraki 305-0044, Japan
⁴Advanced Photon Source, Argonne National Laboratory, Argonne, Illinois 60439, USA
⁵Department of Physics and Astronomy, The University of Tennessee, Knoxville, TN 37996, USA

Entanglement of spin and orbital degrees of freedom drives the formation of novel quantum and topological physical states. Here we report resonant inelastic x-ray scattering measurements of the transition metal oxides Ca₃LiOsO₆ and Ba₂YOsO₆, which reveals a dramatic splitting of the $t_{2g}$ manifold. We invoke an intermediate coupling approach that incorporates both spin-orbit coupling and electron-electron interactions on an even footing and reveal the ground state of 5$d^3$ based compounds, which has remained elusive in previously applied models, is a novel spin-orbit entangled $J=3/2$ electronic ground state. This work reveals the hidden diversity of spin-orbit controlled ground states in 5$d$ systems and introduces a new arena in the search for spin-orbit controlled phases of matter.

The electronic ground state adopted by an ion is a fundamental determinant of manifested physical properties. Recently, the importance of spin-orbit coupling (SOC) in creating the electronic ground state in 5$d$-based compounds has come to the fore and revealed novel routes to a host of unconventional physical states including quantum spin liquids, Weyl semimetals, and axion insulators [1, 2]. As a result, major experimental and theoretical efforts have been undertaken seeking novel spin-orbit physics in various 5$d$ systems, and the influence of SOC has now been observed in the macroscopic properties of numerous systems. However, beyond the $J_{\text{eff}} = 1/2$ case such as that found in Sr₂IrO₄ [3] — which is a single-hole state that applies only to idealised 5$d^3$ ions in cubic materials — questions abound concerning the nature of the electronic ground states which govern 5$d$ ion interactions.

In this context 5$d^3$ materials present a particularly intriguing puzzle, because octahedral $d^3$ configurations are expected to be orbitally-quenched $S = 3/2$ states — in which case SOC enters only as a 3rd order perturbation [4] — yet there is clear experimental evidence that SOC influences the magnetic properties in 5$d^3$ transition metal oxides (TMOs). This includes the observations of large, SOC-induced spin-gaps in their magnetic excitation spectra [5–7] and x-ray absorption branching ratios which deviate from BR = $I_{13}/I_{12} = 2$ [8, 9]. Despite this, no description beyond the $S = 3/2$ state has been established. The emergent phenomena in 4$d^3$ and 5$d^3$ systems, such as incredibly high magnetic transition temperatures [10–13], Slater insulators [14], and possible Mott-insulators [15] are therefore poorly understood.

We selected 5$d^3$ TMOs Ca₃LiOsO₆ and Ba₂YOsO₆ as model systems in which to investigate the influence of spin-orbit coupling on the electronic ground states via RIXS measurements on polycrystalline samples. Both materials have relatively-high magnetic ordering temperatures, $T_N = 117$ and 67 K, respectively, despite large separation of nearest-neighbour Os ions of 5.4–5.9 Å [5, 10, 16]. The relative isolation of Os-O octahedra allows us to unambiguously access the ground state, because only extended superexchange interactions are present. Stronger, close-range interactions can mask the effective single-ion levels we wish to observe [17]. This is likely the reason that the SOC splitting of levels was not observed in the recent RIXS measurement of 5$d^3$ Cd₂Os₂O₇ [7] and NaOsO₃ [18]. In Ca₃LiOsO₆ the oxygen octahedra surrounding Os$^{5+}$ ions are very close to ideal, despite the overall non-cubic symmetry — hexagonal $R\bar{3}c$ [10] and consequently Ca₃LiOsO₆ serves as a test if considerations beyond the local octahedral environment are important. As previously reported [5], we find that Ba₂YOsO₆ has the ideal cubic double perovskite structure $Fd\bar{3}m$ to within experimental measurement limits, see supplementary material [19] for high-resolution synchrotron x-ray and neutron diffraction.

The RIXS measurements reported here reveal the dramatic splitting of the $t_{2g}$ manifold. Using an intermediate coupling approach, we show that this splitting arises due to strong SOC and that the electronic ground state is a spin-orbit entangled $J=3/2$ state. These results provide a natural explanation of the strong SOC effects observed in 5$d^3$ systems [5–9] and further demonstrate that 5$d^3$ systems are a platform from which the search for new spin-orbit controlled phases of matter can be pursued. Our work also shows that an intermediate coupling approach is useful to extract the values of spin-orbit and Hund’s coupling in cases where the 5$d$ transition metal ions are sufficiently isolated as is the case in many double perovskite and other 5$d$-based TMOs structure types.

The details of sample synthesis and characterization are provided in the supplementary material [19]. RIXS measurements were performed at the Advanced Photon
Source (APS) at Sector 27 using the MERIX instrumentation [20]. A closed-cycle refrigerator was used to control the sample temperature. The Os L$_3$-edge incident energy was accessed with a primary diamond(1 1 1) monochromator and a secondary Si(4 0 0) monochromator. A Si(4 6 6) diced analyzer was used to determine the energy of the beam scattered from the sample, and a MYTHEN strip detector was utilised. All measurements were performed with $2\theta = 90^\circ$ in horizontal geometry. The RIXS energy resolution was 150 meV FWHM. The raw data counts are normalised to the incident beam intensity via an ion chamber monitor. To compare the temperatures, the 6 K data is normalised so that the featureless energy gain side overlaps with the 300 K data – this accounts for deviations of the beam position on the sample.

Figure 1 presents the x-ray energy loss, $E_l$, versus incident energy, $E_i$, RIXS spectra of Ca$_3$LiOsO$_6$ at 300 K. Four lines are present at $E < 2$ eV, which are enhanced at $E_l = 10.874$ keV, whereas the feature at $E \approx 4.5$ eV is enhanced at $E_l = 10.875$ keV. This indicates that the $E < 2$ eV features are intra-$t_{2g}$ excitations, whereas the higher energy feature is from $t_{2g}$ to $e_g$ excited states, as has been observed in many 5$d$ oxides [7, 21–23]. Subsequent measurements were optimised to probe the $t_{2g}$ excitations by fixing $E_i = 10.874$ keV.

Figure 2 presents the detailed RIXS spectra of Ca$_3$LiOsO$_6$ and Ba$_2$YOsO$_6$ at temperatures of 300 K and 6 K. In each spectrum there are 5 peaks in addition to the elastic line: four peaks with $E < 2$ eV, labeled a, b, c and d (Fig. 2c and d) which we associated with intra-$t_{2g}$ excitations, and a broad peak, e, centered at $E \sim 4.5$ eV (Fig. 2a and b) associated with $t_{2g}$ to $e_g$ excited states. The size of the splitting is significant and is larger than the splitting between the $J_{eff}=3/2$ and $J_{eff}=1/2$ in Sr$_2$IrO$_4$ [24]. The qualitative similarity of the spectra of Ca$_3$LiOsO$_6$ and Ba$_2$YOsO$_6$ indicates that these features are not controlled by non-cubic structural distortions, as splittings would be heightened in Ca$_3$LiOsO$_6$.

The four $t_{2g}$-character peaks we observe, are incompatible with the multiplets expected in standard crystal field theory developed for 3$d$ ions which leads to the $S=3/2$ ground state [4]. Here, we identify that a method first proposed by Kamimura et al. [25, 26] for transition metal halides is relevant in this case, in which the assumption that inter-electron interaction energies (including intra- and inter-orbital Coulomb and exchange interactions) are much larger than SOC is dropped. This approach can be utilised to model our TMO RIXS data, with the primary assumption that the hybridisation with the surrounding oxygen ligands leaves the transformation properties of the free ion wavefunctions unaltered. This therefore promotes the breaking of the $S = 3/2$ singlet and strong entry of SOC. The wavefunctions are therefore described in terms of irreducible representations in the $O$ double group determined by the octahedral symmetry [4, 27, 28], Fig. 3. This formulation does not necessitate approximations that the cubic crystal field is infinite or that Coulomb or SOC must be neglected, and is not restricted to use for 5$d^3$ configurations [25].

Before preceding to a more quantitative analysis of the four $t_{2g}$-character peaks, we briefly discuss the temperature dependence of the RIXS spectrum. At 300 K the peaks a–d are resolution limited, as determined from least-squares fitting of Gaussian peaks on a flat background to the data, Fig. 2c and d. The peak energies for Ca$_3$LiOsO$_6$ are $a_{Ca} = 0.760(7)$ eV, $b_{Ca} = 0.992(5)$ eV, $c_{Ca} = 1.470(5)$ eV and $d_{Ca} = 1.72(1)$ eV, and for Ba$_2$YOsO$_6$ are $a_{Ba} = 0.745(7)$ eV, $b_{Ba} = 0.971(7)$ eV, $c_{Ba} = 1.447(9)$ eV and $d_{Ba} = 1.68(1)$ eV. At 6 K, well below $T_N$ in both materials, the peaks appear broadened, although maintain the SOC-induced four peak character, indicating that magnetic order is not responsible for splitting of the $t_{2g}$ manifold. The low temperature broadening is most pronounced in peak e — this peak is due to 20 different excited levels in the Coulomb plus SOC regime, so no discrete levels can be resolved with current RIXS capabilities. The broadening could be due to splittings from non-cubic structural distortions occurring below the magnetic ordering temperatures - some distortion should be expected from magnetoelastic coupling. However, if a purely structural distortion were the origin we would expect to see broadening in Ca$_3$IrOsO$_6$ which leads to the $S=3/2$ ground state.

To determine the wavefunctions for the 5$d^3$ case, as in crystal field theory we use initial basis states that de-
FIG. 2. RIXS excitation spectra measured in Ca$_3$LiOsO$_6$ and Ba$_2$YOsO$_6$. Panels (a) and (b) show the data for Ca$_3$LiOsO$_6$ and Ba$_2$YOsO$_6$, respectively. Black lines indicate the full-width half maximum of the elastic line. Panels (c) and (d) show the energy range 0.4–2 eV, i.e. the $t_{2g}$ manifold, with the results of Gaussian peak fitting to the data shown as solid lines.

scribe the ways in which three electrons can occupy the pure $t_{2g}$ and $e_g$ levels (i.e. terms such as $^4A_{2g}$ - which is one electron in each of $d_{xy}$, $d_{yz}$, $d_{zx}$ with total spin $3/2$), and then apply inter-electron interaction and SOC between these states. The inter-electron interactions are expressed in terms of the Racah parameters $B$ and $C$. Due to hybridisation, the radial form of the $d$ levels are unknown, i.e. $B$ and $C$ deviate from pure ionic values, but the Racah parameters are formulated such that they can be easily extracted from experiment [4, 28, 29]. The same interactions can be expressed in terms of intra- and inter-orbital Coulomb interactions, $U$ and $U'$, and the effective Hund’s coupling $J_h$, which have the relationships to the Racah parameters $J_h = 3B + C$, $U = A + 4B + 3C$ and $U' = A - 2B + C$ [29]. The Racah parameter $A$, however, only appears in the diagonal matrix elements of the interactions matrices and causes a constant shift in all eigenvalues, including the ground state, [27, 30] so cannot be determined by the energies of the excited states probed by RIXS. The full interaction matrices are given in Ref. [27]. By numerically diagonalising the matrices we determine the eigenstates illustrated in Fig. 3, and are able to fit the resulting eigenvalues to the determined energies $a_{Ba} - d_{Ba}$ and $a_{Ca} - d_{Ca}$. Fig. 2, see supplementary material for further details. We fix the value of the crystal field to the peak value of peak e, 10$D_q$ = 4.5 eV for Ca$_3$LiOsO$_6$ and 10$D_q$ = 4.3 eV for Ba$_2$YOsO$_6$, because the positions of levels $a$–$d$ are insensitive to small changes in this term, and the resulting levels include negligible mixing of $e_g$ states, as expected for a strong cubic crystal field splitting. We note that quantitative comparisons between the measured intensity and calculation are difficult due to the complexity of the RIXS cross section and, consequently, will be left as the subject of future work.

The resulting parameters provide direct insight into the dominant interactions in the materials. For Ca$_3$LiOsO$_6$ we find $\zeta_{SO} = 0.35(7)$ eV, $B = 0.00(5)$, $C = 0.3(2)$ and $J_h = 3B + C = 0.3(2)$ eV, and for Ba$_2$YOsO$_6$ we find $\zeta_{SO} = 0.32(6)$ eV, $B = 0.00(5)$ eV, $C = 0.3(2)$ eV and $J_h = 0.3(2)$ eV. The energy levels calculated for these parameters are given in the supplementary information [19]. The fact that $\zeta_{SO}$ is of similar
size to C (and \( J_h \)) clearly demonstrates that perturbative approaches are not appropriate for the treatment of SOC in 5d³ systems. The ratio of \( C/B \) is commonly used to indicate the scale of deviation from pure ionic wavefunctions (the nephelauxetic effect) by comparison to the same ratio in 3d materials where SOC is weak, with \( C/B = 4 \) for Cr³⁺ (3d³) ions [4, 28]. We find \( B \) to be zero within the error, indicative of a large nephelauxetic effect; improved resolution of RIXS measurements would be advantageous for this comparison. We can, however, look at the eigenvector we determined for the \( \Gamma_8 \) ground state - which is a linear combination of the 21 initial basis states which describe 3 electrons occupying the \( t_{2g} \) levels, or two occupying the \( t_{2g} \) levels and one in the \( e_g \) levels (the latter ultimately form a negligible contribution, see supplementary material). The largest component is, as expected, from the \( S = 3/2 \) \( L = 0 \) state, but the next major contribution is from the \( S = 1/2 \) \( T_{2g} \) state. For \( \text{Ca}_3\text{LiOsO}_6 \) (\( \text{Ba}_2\text{YO}_6 \)), these \( |A_2⟩ \) and \( |T_{2g}⟩ \) terms appear in the normalised eigenvector with weights of 0.95 (0.95) and 0.27 (0.25), respectively — the complete eigenfunctions are given in the supplementary material. This latter component (plus smaller terms) directly explains the entry of SOC physics and the observations of small orbital moments for 5d³ ions [5, 6, 8, 9, 31].

We finally explore how the framework presented provides insight about the physical manifestation of SOC. An x-ray absorption near-edge spectroscopy plus x-ray circular dichroism study of 5d³ \( \text{Ir}^{5+} \) double perovskites found strong coupling between orbital and spin moments despite small orbital moments, and suggested this should be due to some deviation from the pure \( t_{2g}^3 \) levels [8], with similar results reported in Os⁵⁺ materials [9]. The wavefunction we determine explains these results, with a \( J = 3/2 \) state which has only a small orbital moment. The observation of a large spin gap in the magnetic excitation spectra of \( \text{Ba}_2\text{YO}_6 \) and related double perovskites is also explained by the intermediate coupling framework, as the spin gap results from strong SOC-induced anisotropy which is unexplained in a \( S = 3/2 \) picture. In these double perovskites and the pyrochlore \( \text{Cd}_2\text{Os}_2\text{O}_7 \) anisotropy is held responsible for stabilization of the observed magnetic ground states [6, 7, 32]. Furthermore, recent observations of a large spin gap in \( \text{NaOsO}_3 \) [18] and recent theoretical calculations [33] indicate the importance of strong SOC. Finally, the energy scale of the overall spitting of the \( t_{2g} \) manifold observed here and the broad intra \( t_{2g} \) feature observed in the RIXS spectra of \( \text{NaOsO}_3 \) [18] and \( \text{Cd}_2\text{Os}_2\text{O}_7 \) [7] is similar suggesting SOC of a comparable magnitude (see Fig. S4 in [19]). Our results therefore show that intermediate coupling electronic ground states are influential in dictating the macroscopic physical properties of a broad class of materials. Along these lines, similar studies of 4d³ \( \text{Ba}_2\text{YRuO}_6 \) will likely yield deeper insight in the prominence of spin-orbit coupling physics in d³ systems. We further speculate that a similar approach should be utilised for 5d² and 5d⁴ materials, as they are expected to show larger SOC effects [34], alongside increased hybridisation in the \( d^2 \) case. The \( d^4 \) materials have attracted interest for hosting correlated magnetic moments [35, 36] despite the \( d^4 \) configuration leading to non-magnetic singlets in either LS or Jj limits [34].

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* christiansad@ornl.gov

[19] See Supplemental Material at [URL will be inserted by publisher] where we discuss details regarding the sample preparation and characterization, the RIXS measurements, and the fitting procedure and model and also includes Refs. [37–43].