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# The nanoscale structure of the oil-water interface

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X-ray reflectivity XR and atomistic molecular dynamics (MD) simulations, carried out to determine the structure of the oil/water interface, provide new insight into the simplest liquid/liquid interface. For several oils (hexane, dodecane, and hexadecane) the XR shows very good agreement with a monotonic interface-normal electron density profile (EDP) broadened only by capillary waves. Similar agreement is also found for an EDP including a sub-Å thick electron depletion layer separating the oil and the water. The XR and MD derived depletions are much smaller than reported for the interface between solid supported hydrophobic monolayers and water.

Interfaces of hydrophobic with hydrophilic matter are ubiquitous in nature and in science. Understanding their structure is, therefore, of fundamental importance in biology, chemistry, materials science, and physics. The archetypical such interface, that of oil with water, attracted most attention [1–3]. Since oil and water do not mix, their laterally averaged, interface-normal electron density profile (EDP) has been considered to vary monotonically between those of the two bulks, over a width dictated by the Capillary Wave (CW) model [4]. This theory assigns the width to roughness created by thermally-excited capillary waves, the amplitudes of which depend on the interfacial tension. However, XR [3, 5, 6] and neutron reflectivity studies [7] probing directly the EDP of interfaces of liquid alkanes with water dispute this simple model. For alkanes they yield broader interfaces than those predicted by CW theory. The excess broadening is attributed for the shorter alkanes to the molecule’s gyration radius and for the longer n-alkanes to the bulk correlation length. Moreover, a long-standing theoretical prediction [8–12] of a low-density (“depletion”) layer intruding at the oil-water interface and thus rendering its EDP non-monotonic, eluded thus far conclusive experimental verification for n-alkanes. While the above-mentioned studies of liquid/liquid interfaces [3] found no evidence for such a layer, XR measurements [13–17] on the closely-related interfaces of water with solid-supported hydrophobic SAMs support the existence of such a depletion layer. The exact nature, and origin, of this layer remains controversial, and assigned either to water depletion [13–15] or to enrichment by the lower-density, hydrogen-rich terminal CH<sub>3</sub> groups of the monolayer [15, 18]. Since both CH<sub>3</sub> and CH<sub>2</sub> groups are expected to be present at the n-alkane/water interface [2, 19] the depletion behavior may differ compared to

the SAMs[20]. To address these issues, we employed XR measurements and MD simulations to probe and model the interface of water with liquid normal-alkanes (CH<sub>3</sub>(CH<sub>2</sub>)<sub>n-2</sub>CH<sub>3</sub>, denoted C<sub>n</sub>, with n = 6, 12, and 16). Our XR measurements, spanning a much-broader angular range than previous ones [6], support a monotonic EDP of a width coinciding with CW theory prediction, and place upper limits on both the depletion magnitude and the non-thermal (intrinsic) contribution to the interfacial width. In particular, the magnitude of the depletion, if it exists, is significantly less than that reported for the SAM-water systems. The simulations support a sub-angstrom depletion layer, and the simulated XR curve lies above the experimental one, especially at large wavevectors. This may originate from a subtle interplay between the effects of intrinsic roughness and the depletion layer on the XR.

XR measures  $R(q_z)$ , the reflected intensity fraction of an x-ray beam of wavelength  $\lambda$  incident on the interface at a grazing angle  $\alpha$ , which yields the surface-normal scattering vector  $q_z = (4\pi/\lambda)\sin\alpha$  [21]. For an ideally flat and abrupt liquid interface, broadened only by CWs [21–23],

$$R(q_z)/R_F(q_z) = \exp[-(\sigma q_z)^2], \quad (1)$$

where  $R_F(q_z)$  is the Fresnel XR of an ideally flat and abrupt interface, and

$$\sigma^2 = \sigma_0^2 + \sigma_{CW}^2 = \sigma_0^2 + k_B T / (2\pi\gamma) \ln(q_{max}/q_{min}), \quad (2)$$

where  $\sigma_{CW}$  is the CW-induced roughness,  $\gamma$  is the interfacial tension,  $\sigma_0$  accounts for any non-thermal intrinsic interfacial roughness [22] and  $q_{min}$  and  $q_{max}$  are the CW lower and upper wavevector cutoffs [6, 21]. In the

experiments  $q_{min} = q_z \Delta\beta/2$  is set by the spectrometer resolution[24] where  $\Delta\beta$  is the angular acceptance of the detector and  $q_{max} = \pi/r_0$  is approximated using the smallest molecular dimension ( $r_0 = 2.5 \text{ \AA}$ )[6]. For the simulations  $q_{min} = 2\pi/L_{box}$  is set by the simulation box size,  $L_{box}$ .

A key enabling feature of the present measurements is the use of all-glass sample cells, composed of an inner cup (40-50 mm in diameter) residing concentrically within a taller outer cup (60-70 mm in diameter) and contained in a sealed, temperature controlled environment. The inner cup is first filled to its rim with ultra-clean water. The outer cell is then filled with purified oils (passed through activated basic alumina columns) to a few mm above the water surface. Thus, the liquids contact only glass throughout the experiment. Well-established hot piranha glass cleaning procedures were employed[25]. No equivalent cleaning procedure is possible for the mylar, polycarbonate and stainless steel materials used as cell components in the previous studies[5]. Further it is well established that the x-rays damage plastics through polymer bond breaking and oxidation, yielding soluble contaminants which may segregate to the liquid/liquid interface.

The XR measurements were carried out for  $C_{12}$  and  $C_{16}$  at ID15A (ESRF, France) and for  $C_6$  at 9ID (APS, USA), respectively[24] at  $25 \pm 2 \text{ }^\circ\text{C}$  with beam heights of  $\sim 5 \mu\text{m}$ . The background was measured and subtracted using standard procedures[21] and involved rotating the detector horizontally from the specular position by an angle just greater than the resolution width in both in-plane directions, taking the average of the two values as the background.

In Fig. 1(a) we show the measured  $R(q_z)/R_F(q_z)$  for  $C_{16}$ ,  $C_{12}$ , and  $C_6$  as open symbols where each data set shows a highly linear dependence of  $\ln[R(q_z)/R_F(q_z)]$  on  $q_z^2$ . These results are in very good agreement with the CW model prediction of an ideally flat and abrupt interface, broadened by Gaussian roughness, but otherwise structureless. This calculation uses the instrumental resolution,  $q_{min}$  of  $8.6 \times 10^{-4}$ ,  $1.7 \times 10^{-4}$ , and  $8.4 \times 10^{-5} \text{ \AA}^{-1}$ , for  $C_6$ ,  $C_{12}$ , and  $C_{16}$ , respectively, evaluated at  $q_z = 0.4 \text{ \AA}^{-1}$ [24, 26].

Moreover, Eq. 1 fits yield  $\sigma$  of  $3.38 \pm 0.30$ ,  $3.41 \pm 0.15$ , and  $3.54 \pm 0.20 \text{ \AA}$  for  $C_6$ ,  $C_{12}$ , and  $C_{16}$ , respectively, all close to their corresponding  $\sigma_{CW}$  values of 3.06, 3.31, and 3.41  $\text{\AA}$ . This good agreement suggests that  $\sigma_0 \approx 0 \text{ \AA}$ . Indeed, plots of Eq. 1 with fixed  $\sigma = \sigma_{CW}$  (Fig. 1(a), solid lines) agree well with the measured data, over the full  $0 \leq q_z^2 \leq 0.2 \text{ \AA}^{-2}$  range measured, and without any adjustable parameters. However, a noticeable deviation from experiment is observed already for  $\sigma_0 = \sqrt{2}\sigma_0^{air} = 1.56 \text{ \AA}$  (short-dashed line), a value obtained as an upper limit by adding in quadrature the  $\sigma_0$  of the water and of the alkane interfaces, assuming for both

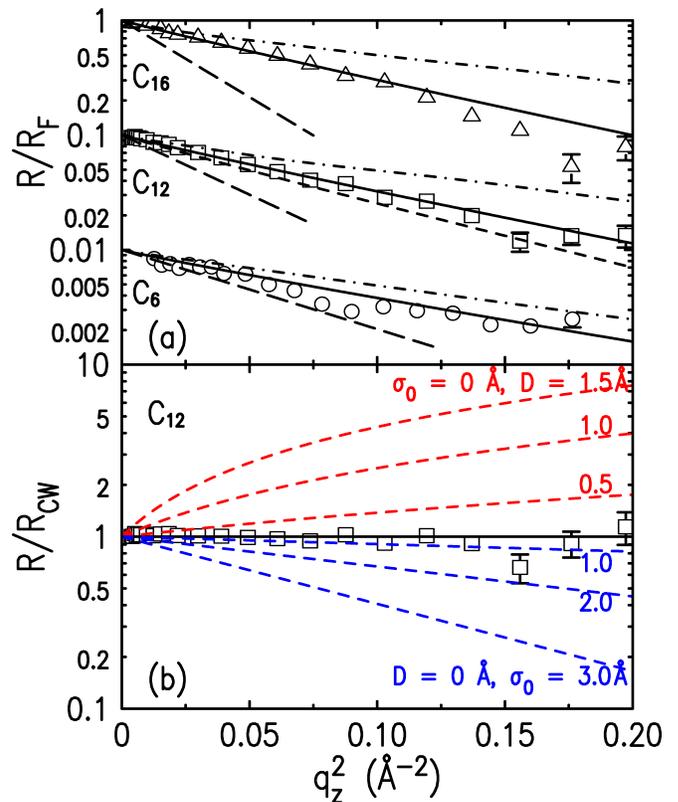


FIG. 1. (a) Fresnel-normalized reflectivity  $R/R_F$  for alkane( $C_n$ )-water interfaces: measured (symbols), calculated (no-fit) CW theory prediction ( $R_{CW}/R_F$ ), for  $\sigma_0 = 0$  and  $D = 0$  (solid lines), showing good agreement, and the same with  $\sigma_0 = \sqrt{2}(1.1 \text{ \AA}) = 1.56 \text{ \AA}$  (short-dashed line for  $C_{12}$ ). The best fits of previous measurements [6] (long-dashed lines) show reduced  $q_z^2$ -range and systematic deviations from CW theory. MD simulations along with CW corrections are shown for  $D^{MD} = 0.5 \text{ \AA}$  (dot-dashed lines). (b)  $C_{12}$ -water  $R/R_{CW}$ : measured (symbols), and calculated (lines) for combinations of  $\sigma_0$  and  $D$ . See text for discussion.

the same  $\sigma_0^{air} = 1.1 \text{ \AA}$ , measured for long-chain alkane-melt/air interfaces [22]. Thus, for a CW-broadened monotonic interfacial EDP, experiment clearly limits the non-thermal contribution to  $\sigma_0 \lesssim 1.5 \text{ \AA}$ . The discrepancy with the previous comprehensive XR study of  $C_n$ -water interfaces [6] is clear even for their smaller  $q$ -range ( $q_z^2 \leq 0.07 - 0.12 \text{ \AA}^{-2}$ ). Their analysis yields  $\sigma_0$  increasing with  $n$ , reaching 4.43  $\text{\AA}$  for  $n = 16$  and they attribute the  $\sigma_0$  to the molecules' radius of gyration.

Whereas the analysis above is consistent with a CW-determined monotonic-EDP interface, it neglects the possibility of an interfacial electron depletion layer. For a thin layer of thickness  $D$  and density  $\rho_D$ , XR is insensitive to the specific values of  $D$  and  $\rho_D$ , and only sensitive to the  $z$ -integrated electron depletion,  $\Gamma = D \times \Delta\rho$ , where  $\Delta\rho$  is the density difference between  $\rho_D$  and the average of water ( $\rho_w$ ) and alkane ( $\rho_a$ ) [17, 18]. Including a depletion layer in the model and choosing a limiting

$\rho_D = 0 \text{ e}/\text{\AA}^3$  modifies Eq. 1 to:

$$R_D/R_F = \exp[-(\sigma q_z)^2] [1 + 4\varepsilon \sin^2(Dq_z/2)], \quad (3)$$

where  $\varepsilon = \rho_w \rho_a / (\rho_w - \rho_a)^2$ . At 25°C,  $\varepsilon = 6.9, 15.6$  and 19.2 for the water interface with C<sub>6</sub>, C<sub>12</sub>, and C<sub>16</sub>, respectively. Accordingly, the impact of a depletion layer on the measured reflectivity is expected to increase with the chain length.  $R_D/R_F$  is well approximated by Eq. 1 with

$$\sigma^2 = \sigma_{CW}^2 + \sigma_0^2 - \varepsilon D^2, \quad (4)$$

demonstrating that increasing  $\sigma_0$  reduces  $R_D/R_F$  while increasing  $D$  increases  $R_D/R_F$ ; see Fig 1(b). This mutual cancellation makes it difficult to distinguish EDPs having a thin ( $D > 0$ ) and rough ( $\sigma_0 > 0$ ) depletion layer from EDPs having a sharp ( $\sigma_0 = 0$ ) water/oil interface and no depletion layer ( $D = 0$ ), corresponding to the CW model with only a single, sharp interface at the oil/water interface.

Typical  $\chi^2$  maps for C<sub>12</sub> (Fig. 2(a)), for a mesh of  $\sigma$  (or  $\sigma_0$ , with calculated  $\sigma_{CW}$ ) and  $D$  [15, 17, 18], demonstrate the severe limits imposed by the data on the maximal  $D$  and  $\sigma_0$ . Statistical analysis [27, 28] yields the best-fit  $D^{bf} = 0.46 \pm 0.46 \text{ \AA}$  and  $\sigma_0^{bf} = 1.9^{+1.3}_{-1.9} \text{ \AA}$ , and the 68% confidence level contour (Fig. 2(a)), corresponding to the conventional one-variable 1-standard-deviation. Whereas  $D^{bf}$  is in good agreement with our simulations (see below),  $\sigma_0^{bf}$  much exceeds  $\sigma_0^{\text{air}} = 1.1 \text{ \AA}$  found for the alkane-air interface [22]. We note that for  $D = 0$  we obtain  $0 < \sigma_0 = 0.9 \text{ \AA} < \sigma_0^{\text{air}}$ . Importantly, the  $D^{bf} = 0.46 \text{ \AA}$  and the corresponding best-fit  $\Gamma^{bf} = 0.136 \text{ e}/\text{\AA}^2$  are much lower than those of SAM-water interfaces [18, 29]:  $1.8 \text{ \AA} \leq D \leq 3.8 \text{ \AA}$  and  $0.30 \text{ e}/\text{\AA}^2 \leq \Gamma \leq 0.67 \text{ e}/\text{\AA}^2$ .

Fig. 2(b) shows several different model EDP profiles after including the effects of CW induced broadening. Note that the CW EDP with no depletion (red-dashed line) overlaps almost everywhere the EDPs with a depletion of  $\Gamma = 0.136 \text{ e}/\text{\AA}^2$  ( $D = 0.46 \text{ \AA}$  for  $\rho_D = 0$ ) and  $\sigma_0 = 1.9 \text{ \AA}$  (black and blue-dashed lines). Thus, not only is the quality of the fits similar for EDPs with  $D = 0$  and  $0.46 \text{ \AA}$  as demonstrated by Figs. 2(a), but their EDPs are identical after inclusion of  $\sigma_0$  for the latter case. We also note that the near-overlap between the two curves (blue and black) with the same value of  $\Gamma$  and different values of  $D$  provides further justification for Eq. 3.

Our MD simulations (GROMACS), done in the NPT ensemble at 300 K, employ SPC/E [30] and OPLS-AA [31] force fields for the water and C<sub>n</sub>, respectively. We obtain bulk mass densities  $m_i^{\text{BULK}} = 645 \pm 1, 741 \pm 2, 764 \pm 2$  and  $1000 \pm 1 \text{ kg}/\text{m}^3$  for C<sub>6</sub>, C<sub>12</sub>, C<sub>16</sub> and H<sub>2</sub>O, and oil-water interfacial tensions, calculated from the anisotropy of the pressure tensors,  $\gamma_i = 51 \pm 2, 54 \pm 2$  and  $54 \pm 2 \text{ mN}/\text{m}$ , for C<sub>6</sub>, C<sub>12</sub> and C<sub>16</sub>. These values are within 1.5% ( $m_i^{\text{BULK}}$ ) and 1% ( $\gamma_i$ ) of their respective experimental values[6],

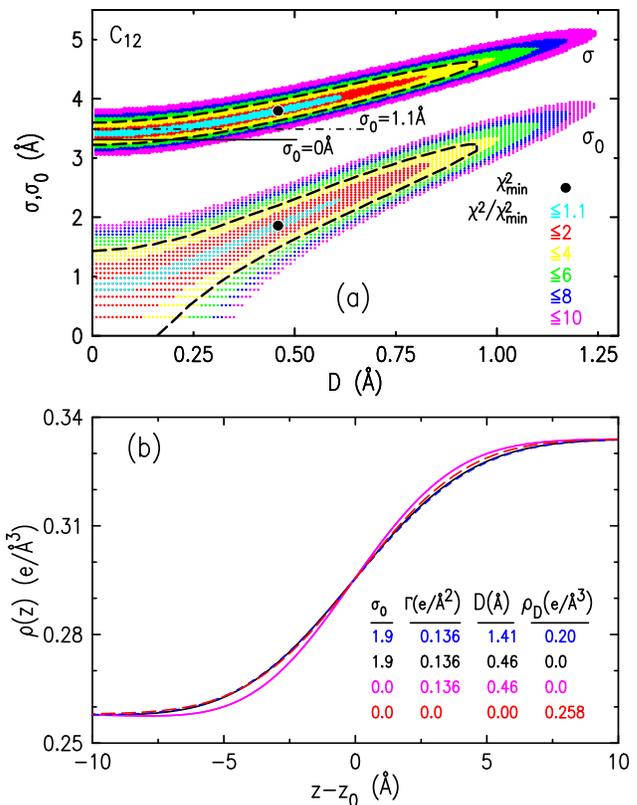


FIG. 2. (a)  $\chi^2/\chi_{min}^2$  maps for two-parameter models ( $\sigma, D$ ) and ( $\sigma_0, D$ ) for C<sub>12</sub> that includes a depletion layer, where the  $\chi_{min}^2$  position is shown by the black dot;  $\sigma$  for  $\sigma_{CW} = 3.31 \text{ \AA}$  and  $\sigma_0 = 0, 1.1 \text{ \AA}$  (horizontal lines), and 68% confidence level contour (dashed lines). (b) C<sub>12</sub>-water interface EDPs for ( $D, \rho_D$ ) with various parameter combinations. The density profile is insensitive to the depth of the depletion for the same  $\Gamma$  (black and blue-dashed). The same depletion, with  $\sigma_0 = 0$ , provides a noticeably narrower profile (purple). The CW prediction with  $\sigma_0 = 0$  (red-dashed) yields a profile similar to those for  $\Gamma = 0.136 \text{ e}/\text{\AA}^2$  and  $\sigma_0 = 1.9 \text{ \AA}$ .

demonstrating the simulations' quality. The simulations box size,  $L_{box}$  was either 40  $\text{\AA}$  (C<sub>12</sub>) or 35  $\text{\AA}$  (C<sub>6</sub> and C<sub>16</sub>).

The simulated mass density profiles  $m(z)$  (Fig. 3(a)) were used to calculate the positions of the Gibbs dividing surfaces as  $z_i^{\text{GDS}} = z_j + \int_{z_j}^{z_i} (1 - m_i(z))/m_i^{\text{BULK}} dz$ , where  $i, j = w$  (water) or  $a$  (alkane), and  $z_{i,j}$  - positions in the bulk of the respective liquids. From these, we obtain a depletion layer width as  $D^{MD} = z_a^{\text{GDS}} - z_w^{\text{GDS}} = 0.5 \pm 0.04 \text{ \AA}$  for all C<sub>n</sub>, yielding  $\Gamma^{MD} = 0.148 \text{ e}/\text{\AA}^2$ . These results are in good agreement with previous simulations using polarizable force fields [19], and with the experiment-derived  $D^{bf}$  and  $\Gamma^{bf}$  presented above.

The electron density profiles (Fig. 3(b)) are calculated as  $\rho(z) = \sum_i \alpha_i n_i(z)$  where  $n_i(z)$  and  $\alpha_i$  are the number-density and atomic number of atom  $i$ . For all C<sub>n</sub>,  $\rho(z)$  exhibits a dip at the interface, and clear oscillations on the alkane side with a C<sub>n</sub>-independent period of

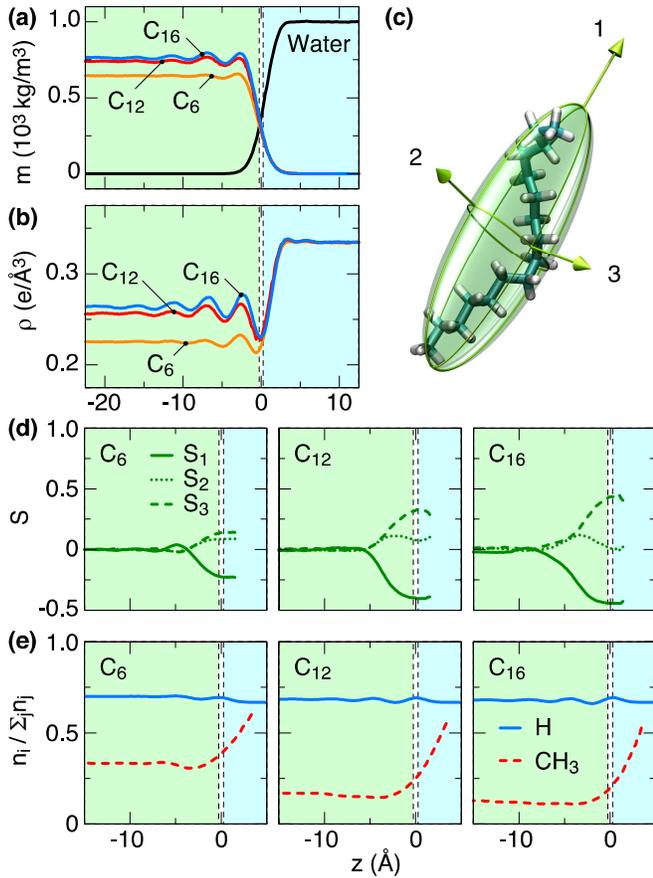


FIG. 3. (a) The mass density with the Gibbs dividing surfaces (black dashed lines). (b) The electron density  $\rho(z)$ . (c) A snapshot of a  $\text{C}_{16}$  molecule together with its three principal axes. (d) The order parameter  $S_k$ . (e) The relative densities of  $\text{CH}_3$  and H.

$\sim 4.5 \text{ \AA}$ . This period corresponds well to the bulk correlation lengths  $\xi = 4.9 \text{ \AA}$  ( $\text{C}_6$ ),  $4.5 \text{ \AA}$  ( $\text{C}_{12}$ ) and  $4.5 \text{ \AA}$  ( $\text{C}_{16}$ ), calculated as  $\xi = (l \times n_{\text{C}}^{\text{BULK}})^{-\frac{1}{2}}$ , where  $l = 1.529 \text{ \AA}$  is the C-C bond length and  $n_{\text{C}}^{\text{BULK}}$  is the C monomer bulk density [6].

The molecular orientation (Fig. 3(c-d)) is calculated from the gyration tensor for each molecule,  $G = \sum_{i,j} (\mathbf{r}_i - \mathbf{r}_j)(\mathbf{r}_i - \mathbf{r}_j)^T / (2N^2)$ .  $i, j$  runs over all  $N$  atoms of the molecule, with  $\mathbf{r}_i$  denoting atom  $i$ 's position. Diagonalizing  $G$  is equivalent to fitting an ellipsoid to the molecule's shape.  $G$ 's eigenvectors, labeled  $k = 1, 2, 3$  for the largest, medium and smallest eigenvalues, are the directions of molecule's principal axes (Fig. 3(c)). The order parameter is calculated as  $S_k(z) = \langle 3 \cos^2 \theta_k - 1 \rangle / 2$ , where  $\theta_k$  is the angle between the  $k$ th eigenvector and the vector  $(x, y, z) = (0, 0, 1)$ , and  $\langle \dots \rangle$  indicates an average over all molecules at position  $z$ .  $S_k = 1$  corresponds to an orientation perpendicular to the interface whereas  $S_k = -0.5$  corresponds to orientation parallel. Fig. 3(d) shows that for all  $\text{C}_n$  the interface-adjacent molecules have their longest axis interface-parallel and their short-

est axis - mostly interface-normal. The alignment is more pronounced for longer alkanes. The interface-adjacent density oscillations discussed above are likely caused by this strong interface-parallel molecular layering which also explains their periods' chain length independence. The short length scale of the oscillations resulting from the parallel orientation also explains that no molecular structure is visible in the XR profiles, and that the interfacial width is independent of the chain length, contrary to previous reports [6]. A chain-length-dependent  $\sigma$  would be expected for other alkane orientation.

Despite the interface-parallel alignment, the relative  $\text{CH}_3$  density at the interface is enhanced (Fig. 3(e)). The relative density of species  $i$  is  $n_i(z) / \sum_j n_j(z)$ , with  $n_{i,j}(z)$  being the number density of  $\text{CH}_3$  groups or H atoms, and the sum running over all carbon groups (for  $\text{CH}_3$ ), or over all atoms (for H). The  $\text{CH}_3$  densities (dashed red lines in Fig. 3e) exhibit a roughly two-fold increase in the interfacial region. This, in turn, increases the relative hydrogen content in the density-depleted interfacial layer (solid blue lines in Fig. 3(e)). However, this effect is small, indicating that the  $\rho(z=0)$  dip in Fig. 3(b) is due to heavier-atom depletion rather than hydrogen enrichment.

The width,  $\sigma_{\text{water}}$ , of the simulated water electron density profiles is a measure of the CW roughness over the simulation's box size. Excellent fits (not shown) are obtained for  $\text{C}_6$ ,  $\text{C}_{12}$ , and  $\text{C}_{16}$  with  $\sigma_{\text{water}} = 1.32 \pm 0.04 \text{ \AA}$  which is considerably smoother than the calculated CW value  $\sigma_{\text{CW}} = 1.8 \text{ \AA}$  calculated using the molecular size of water,  $r_0 = 2.5 \text{ \AA}$ , and  $L_{\text{box}}$ . Agreement between CW model and simulations is obtained with  $r_0 = 10 \text{ \AA}$ , suggesting that the shortest wavelength capillary mode may be influenced by the bending rigidity of the elongated alkane chains lying parallel to the interface.

To compare the simulated XR,  $R_s(q_z)$ , with experiment, we first correct the simulated  $\rho(z)$  for the CW spectrum cutoff by the simulation box size.  $\rho(z)$  is thus convoluted with a Gaussian of width  $\sigma_{\text{CW}}$  calculated from Eq. 2 with  $r_0 = L_{\text{box}}$ . This accounts for the CW modes between  $2\pi/L_{\text{box}}$  and the resolution-determined  $q_{\text{min}}$  since these CW modes are not accounted for by the simulation.  $R_s(q_z)$  is calculated from this corrected  $\rho(z)$  using the Born approximation [21],  $R_s(q_z)/R_F(q_z) = |(\rho_w - \rho_a)^{-1} \int [d\rho(z)/dz] \exp(-iq_z z) dz|^2$ .

For all three chain lengths, using the simulated  $\rho(z)$  with its depletion layer width of  $D^{\text{MD}} = 0.5 \text{ \AA}$ ,  $R_s(q_z)/R_F(q_z)$  is higher (see dot-dashed lines in Fig. 1(a)) than both the measured reflectivity and the CW prediction. We note that excellent agreement of the simulations with the measured reflectivity can be obtained by either artificially reducing  $D$  found in the simulations,  $D^{\text{MD}} = 0.5 \text{ \AA}$  to zero for all alkanes, or by incorporating ad-hoc an additional non-thermal roughness  $\sigma_0$ , not exhibited by the simulations. For ex-

ample, for C12, to reach a good simulation-experiment agreement in Fig. 1 (a) requires increasing  $\sigma$  to 3.9 Å from the CW value of 3.3 Å. This, in turn, requires  $\sigma_0 = \sqrt{(\sigma^2 - \sigma_{CW}^2)} = 2.1$  Å, greater than the upper limit of  $\sqrt{2}(1.1 \text{ Å}) = 1.56$  Å discussed above. There is no apparent justification for this increased broadening within the MD simulation since the capillary correction should account for the smearing of the atomic positions, except for a small form factor contribution which is negligible over the measured  $q_z$  range. Deviations from CW behavior have been detected by diffuse scattering [32] and reflectivity measurements on alcohol/water mixtures [33] at free liquid surfaces. These studies suggest that the CW model may need modifications for complex interfaces.

The major result of the present XR measurements is the mending of a long-standing apparent discrepancy of previous, shorter-range, XR measurements[6] with the CW theory. However, due to the shallow minimum in the  $\chi^2$ , resulting from the mutually canceling effects of  $\sigma_0$  and  $D$ , it is not possible to unambiguously distinguish between the CW-broadened monotonic interface model with a zero or small  $\sigma_0$  and a model including a thin depletion layer with a larger  $\sigma_0$ . The simulations and experiments together suggest a gap in the range,  $0 \leq D \leq 0.5$  Å where the upper bound for  $D$  is 3-8 times smaller than those obtained for SAM-water interfaces [18, 29]. Our results weakens the case for the existence of a significant depletion layer, thus illuminating the dichotomy between interfaces of water with solid-supported SAMs and with liquid alkanes. Although the simulations overestimate the measured  $R/R_F$ , they provide valuable information on the interface-adjacent orientation of the alkane molecules and on hydrogen enrichment at the interface. A better separation of the interfacial roughness into a thermal and non-thermal contribution, and a better understanding of the simulation-experiment discrepancy, would require extensive temperature-dependent XR measurements and simulations, preferably over a larger range of alkane length.

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