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Coherence preservation of a single neutral atom qubit transferred between magic-intensity optical traps

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We demonstrate that the coherence of a single mobile atomic qubit can be well preserved during a transfer process among different optical dipole traps (ODTs). This is a prerequisite step in realizing a large-scale neutral atom quantum information processing platform. A qubit encoded in the hyperfine manifold of ⁸⁷Rb atom is dynamically extracted from the static quantum register by an auxiliary moving ODT and reinserted into the static ODT. Previous experiments were limited by decoherences induced by the differential light shifts of qubit states. Here we apply a magicintensity trapping technique which mitigates the detrimental effects of light shifts and substantially enhances the coherence time to 225 ± 21 ms. The experimentally demonstrated magic trapping technique relies on the previously neglected hyperpolarizability contribution to the light shifts, which makes the light shift dependence on the trapping laser intensity to be parabolic. Because of the parabolic dependence, at a certain "magic" intensity, the first order sensitivity to trapping light intensity variations over ODT volume is eliminated. We experimentally demonstrate the utility of this approach and measure hyperpolarizability for the first time. Our results pave the way for constructing a scalable quantum-computing architectures with single atoms trapped in an array of magic ODTs.

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A quantum computer [1] or a simulator is a scalable physical system with coherently controllable and well characterized qubits. As an important candidate for quantum information processing and quantum simulation, a microscopic array of single atoms confined in optical dipole traps (ODTs) has attracted a great deal of interest in recent years [2, 3]. In such architectures [4] each ODT-stored atom acts as a qubit, and an array of single atoms in static ODTs forms a quantum register. An important requirement is the ability to controllably transport a remote qubit, acting as a mobile qubit, into the interaction range with other register atoms for performing two-qubit gates. This transfer must be carried out without influencing other qubits of the large-scale quantum register. Recently, we experimentally demonstrated such a transfer scheme [5], in which the single mobile qubit was dynamically extracted from a ring optical lattice site by an auxiliary moving ODT and reinserted into the original site. We, however, found that during the transfer process the qubits severely lose coherence. Although an alternative transfer scheme between two ODTs has been also demonstrated [6] and the coherence of the mobile qubit was found not to be affected during the transfer, this scheme is not suitable for scalable quantum systems because the register static ODTs are switched off during the transfer. If the register keeps holding qubits as required for a scalable system, the static ODTs should

remain always on. Then the mobile qubit unavoidably experiences large variations of the trapping potential in the merging process between moving and static ODTs, leading to the coherence losses.

Typically, an atomic qubit is encoded into a superposition of two hyperfine Zeeman levels of the ground states of an alkali-metal atom. Generically different hyperfine states experience mismatched light shifts induced by the trapping laser field, leading to the so-called differential light shift (DLS). The DLS depends on the laser intensity at the qubit position and due to the spatial distribution of laser field intensity in a trap, the qubit suffers from strong inhomogeneous dephasing effect. Thereby the coherence time is limited to scales of several ms in red-detuned ODTs [7–10], or several tens of ms in bluedetuned ODTs [11, 12]. To reduce the DLS-induced dephasing, one could add a weak near-resonant compensating laser beam, but at an expense of a substantially increased scattering rate [13, 14], or employ the dynamical decoupling methods such as the spin echo or the Carr-Purcell-Meiboom-Gill sequence [7, 10]. The dynamical decoupling methods are found to be efficient for qubits in static ODTs but inefficient for mobile qubits. Indeed, the heating of atoms and pointing instabilities of the trap laser beams during the transfer can not be efficiently suppressed by the dynamical decoupling methods, causing the mobile qubits to lose coherence.

Similar to optical lattice clocks [15], a complete control approach over DLS is to construct a "magic" trap, where the two qubit states experience identical trapping potentials and the relative phase accumulation is nearly independent of the atomic center-of-mass motion and trapping field fluctuations. To this end, exploiting the vector light shift, which acts like an effective Zeeman field B_{eff} , to zero out the DLS of $m_F \neq 0$ hyperfine states has been proposed [16, 17] and demonstrated in ⁷Li [18]. Similarly exploiting the vector light shift for cancelling DLS of $m_F=0$ hyperfine states in ⁸⁷Rb atoms has also been demonstrated [19, 20]. While at the cost of increased sensitivity to the magnetic noise due to the requirement of a several Gauss magnetic bias field, this technique has been proven to be efficient in enhancing the lifetime of spinwave qubits in a ⁸⁷Rb ensemble [21, 22]. Furthermore, to reduce the sensitivity to fluctuations of both laser and magnetic fields, doubly magic trapping for $m_F \neq 0$ state was proposed [23] and experimentally demonstrated in 87 Rb atoms confined in optical lattice [24]. To date, the magic trapping techniques have been proved to be efficient in suppressing inhomogeneous DLS of atoms in static ODTs. The open question is whether these technique can be also used to mitigate coherence loss in manipulating the mobile qubits. This question is explicitly answered in this Letter.

We begin by studying the DLS of single ⁸⁷Rb qubits (here $|0\rangle \equiv |F = 1, m_F = 0\rangle$ and $|1\rangle \equiv |F = 2, m_F = 0\rangle$) confined in a circularly polarized ODT. We observe and measure previously neglected ground state hyperpolarizability, which makes the DLS dependence on laser intensity to be parabolic. Because of the parabolic dependence, at a certain "magic" intensity, the first order sensitivity to trapping light intensity variations is eliminated [25]. We further demonstrate that the measured coherence time of the mobile qubits is the same as for the static qubits, i.e., the transfer process does not induce extra coherence loss.

The experimental details on trapping single ⁸⁷Rb atoms and individual qubit manipulations have been descried elsewhere [5, 10]. Here, a modified optical layout is illustrated in Fig. 1. The waist of the trap-2 is 1.25 μ m. We load a single ⁸⁷Rb atom from a magneto-optical trap via a collisional blockade mechanism [26]. It is worth noting that in previous experiments on manipulating degenerate ensembles in optical lattice [19], the trap depth $U_a \approx 3.5 \ \mu \text{K}$ and thereby $B_{\text{eff}} = 12 \text{ mG}$ can be neglected to the bias B-field. But here we confine single atoms with temperature of several tens of μK in an ODT with a much larger trap depth up to 0.6 mK. Now the $B_{\rm eff} \approx$ 1.120 G becomes comparable to the externally applied B-field. The corresponding vector light shift is so strong that the usually neglected ground state hyperpolarizability becomes important and must be taken into account. Recent theoretical analysis by Carr and Saffman [25] revealed the importance of hyperpolarizability in reaching



Figure 1. (Color online) Schematic of the optical layout. A movable 830 nm light beam (labeled as trap-1) is deflected in two orthogonal directions by an acoustic-optic deflector (AOD) which is driven by a radio-frequency (RF) signal. The trap-1 is combined with another 830 nm light beam (trap-2) by a beam splitter (BS). Their polarizations are purified by a Glan-Thompson polarizer first, then actively controlled by a liquid crystal retarder (LCR). Both laser beams are finally focused by a microscopic objective to provide a 3D confinement. The same objective also collects fluorescence from the trapped atoms. The fluorescence is then detected by a single photon counting module (SPCM).

magic conditions in trapping of Cs atoms.

The DLS of Zeeman-insensitive clock transition experienced by the 87 Rb atoms in an external magnetic field *B* is expressed as

$$\delta\nu(B, U_a) = \beta_1 U_a + \beta_2 B U_a + \beta_4 U_a^2, \tag{1}$$

where $\delta\nu$ is the total DLS seen by the atoms, U_a (in unit of Hz) is the local trap depth, β_1 is the coefficient of the third order hyperfine-interaction mediated polarizability, β_2 is the coefficient of the third order cross-term and β_4 is the coefficient of the ground state hyperpolarizability.



Figure 2. (Color online) DLS in the presence of hyperpolarizability. DLS of a qubit in the circularly polarized trap-2 is measured as a function of trap depthes at various magnetic field strengthes. The solid curves are fits to the Eq.(1). The inset plots the minima U_M in the DLS curves as a function of magnetic field B. The light intensity of each minimum is chosen as the magic intensity at that B-field value.

 β_2 and β_4 depend on the degree of the circular polarization. For the sake of simplicity, we use fully circular

 σ^+ light. Varying the trap depths and B-fields we can deduce the values of β_2 and β_4 in Eq. (1) from our DLS measurements. In case of linearly polarized light field, β_2 and β_4 terms vanish and DLS is linearly dependent on the trap depth. Thereby we calibrate the trap depth by comparing the measured DLS in the linearly polarized trap with the calculated value of $\beta_1 \approx 3.67 \times 10^{-4}$ from the atomic structure data [27, 28]. Then we measure the DLS curves in the circularly polarized trap-2 for several values of magnetic fields. As shown in Fig. 2, all of the measured curves exhibit nonlinear (parabolic) dependence of the DLS on the trap depths unlike the linear dependence in previous measurements [19]. Given our calculated value of $\beta_1 \approx 3.47 \times 10^{-4}$ for circular polarization, all the curves are fitted to Eq.(1) yielding the values of β_2 and β_4 . Averaging over all of the fitted results, the β_2 and β_4 are found to be $-0.99(3) \times 10^{-4} \,\mathrm{G}^{-1}$ and $4.6(2) \times 10^{-12} \,\mathrm{Hz}^{-1}$ respectively. The theoretical results [29], $\beta_2 = -1.03 \times 10^{-4} \text{ G}^{-1}$ and $\beta_4 = 4.64 \times 10^{-12} \text{ Hz}^{-1}$, are in a good agreement with the experimental values. Further, from Eq. (1), the minimum trap depths are given by $U_M =$ $-(\beta_1 + \beta_2 B)(2\beta_4)^{-1}$, i.e., they scale linearly with B-field. Further, from Eq. (1), the minimum trap depths are given by $U_M = -(\beta_1 + \beta_2 B)(2\beta_4)^{-1}$, i.e., they scale linearly with B-field. Fig. 2 inset shows the linear dependence of the measured DLS minima on the external B-field. When $B \rightarrow -\beta_1/\beta_2 \approx 3.51 \,\mathrm{G}, U_M$ approaches 0 and the trap is too weak to trap atoms. In contrast, smaller B-fields require deeper trapping depths. It means that the atoms scatter more spontaneous Raman photons from the trapping laser, leading to faster spin relaxation rate. So the working B-field is set to 3.115 G to make a reliable trapping and low spin relaxation rate.

Next we measure the dependence of qubit coherence times on the ratios of trap depth to the measured magic trap depth which is the fitted minimum (with 10% uncertainty) in the DLS curves for 3.115 G in trap-2. The coherence time is measured by recording the decay of the visibility of Ramsey signal, as shown in the inset of Fig. 3. By varying the trap depths, we find the longest coherence time at around U_M , which is consistent with the magic operating condition $\partial \delta \nu(B_0, U_a)/\partial U_a = 0$. At $U_a = U_M, \tau = 225 \pm 21$ ms.

We remind the reader that the decay time τ of the Ramsey signal can be decomposed into two main parts, $1/\tau = 1/T_1 + 1/T_2$, where T_1 is longitudinal relaxation time and T_2 is transverse decay time. In our experiment, the measured T_1 is over 4 s and $1/T_1$ can be neglected. In addition, T_2 can be decomposed as $1/T_2 = 1/T'_2 + 1/T'_2$, where T'_2 is the homogeneous dephasing time and T'_2 is the inhomogeneous reversible dephasing time [7, 10].

Given the measured U_a and temperature T_a , we can obtain the values of T_2^* , which is the 1/e decay time of the amplitude of Ramsey fringes [29]. At the magic light intensity $(U_a/U_M = 1)$ and a temperature of 17 μ K, we obtain $T_2^* \approx 1.5$ s. For different U_a/U_M we thus



Figure 3. (Color online) Coherence time τ and its dependence on normalized ratios U_a/U_M . At $U_a = U_M, \tau = 225 \pm 21$ ms. The error bars of ratios are from the measured error of U_M (10%). A coherence time is extracted from a decay time of the envelope of Ramsey visibility, as shown in the inset, which is the measured visibility of Ramsey signals as a function of the duration between two $\pi/2$ pulses at U_M . All the accompanying error bars of coherence times and visibility are fitting errors. The theoretical curve is obtained by combining the calculated T_2^* with Eq.(2), an estimated $T_2' \approx 300$ ms and the measured value of $T_1 \approx 4$ s.

have different T_2^* . Together with an estimated $T_2' \approx 300$ ms [5], and an independently measured value of $T_1 \approx 4$ s, the coherence time τ is deduced for each ratio of trap depths, and is plotted as a curve in Fig.3.

Notice that the predictions of described model deviate from the measurements when the trap depth is away from the magic point. This is likely caused by the neglected anharmonicity of the motion of the atoms in the Gaussian ODT at high temperatures. In this experiment, the decay time of the Ramsey signal is dominated by the magnetic noise. We monitor the drift of the magnetic field as time by monitoring the change of the resonance frequency of a single atom in the magic dipole trap. The typical result is 0.6 mG per 2 hours. It is worth noting that the homogeneous dephasing time due to relative intensity fluctuations (0.15%) and heating rate $(2 \,\mu \text{K/s})$ are estimated to be 300 s and 34 s respectively [5, 7], thereby both of them can be neglected for magic trapping. Meanwhile, because of working magnetic bias field is relatively large, 3.115 G, compared to our previous work [5], the sensitivity to the B-field noise is enhanced; this is presently the dominant source of decoherence.

Finally, we study the coherence loss of a mobile qubit during a transfer process. The key issue is to see whether the described magic trapping technique can mitigate the coherence loss of the mobile qubit. The experimental time sequence is illustrated in Fig.4. The trap-1 (mobile ODT) and trap-2 (static ODT) serve as the "moving head" and the "register" respectively. The trap-2 is operated at the magic-intensity condition, i.e., trap depth



Figure 4. (Color online) Schematic illustration of the transfer process of a mobile qubit. An atom in a superposition state (the qubit) is initially confined in the static ODT (trap-2). It is then overlapped with the mobile ODT (trap-1). The qubit is extracted out by the mobile ODT and becomes a mobile qubit. The mobile qubit travels for time interval t, and then it is returned to the static ODT.

of 0.17(2) mK and magnetic field of 3.115 G. In this trap, the measured temperature is about 8 μ K, translating into $T_2^* \approx 6.6$ s. Once the atom in the $|1\rangle$ state is confined in trap-2, a $\pi/2$ pulse is applied. At 1.9 ms, the trap-1 is overlapped with trap-2, switched on, and ramped up to 0.2 mK within 0.1 ms. Then the trap-1 is moved away a distance of $5\mu m$ (4 times as much as the trap beam waist radius) from trap-2 by linearly sweeping the AOD driving frequency. Since the moving trap-1 is deeper than trap-2, the atom follows trap-1 [5] and is extracted out by the mobile ODT. The extracted atom becomes a mobile qubit. The mobile qubit travels for a duration time t. Then it is sent back to the static ODT, and the trap-1 is ramped down within 0.1 ms. The qubit returns to the original register site again. The atom is detected in trap-1 with efficiency of > 98%, no measurable particle loss has been detected after the transfer process. To measure the coherence loss, the second $\pi/2$ pulse is applied at time T to complete the Ramsey interferometry sequence.

The measured Ramsey signal as a function of time Tis shown in Fig.5, together with the Ramsey signal for static qubits. The fitted decay time of the Ramsey signal of single mobile qubits is the same as for the static qubits. At the beginning and the end of the transfer, the atoms are confined in an overlap of the two traps. The total trap depth is up to 0.37 mK and is far away form the magic operation condition. The dephasing time of the qubits trapped in this overlap trap is measured to be about 25 ms. But the actual trap overlap duration (< 0.2ms) is too short to cause significant dephasing. Besides, for the measured temperature of 14 μ K, the estimated dephasing time in the "moving head" trap is long, $T_2^* \approx 3$ s. The entire transport takes only 2 ms and the accompanying dephasing is negligible. After returning to trap-2, the temperature of the atoms is increased to 16 μ K. The DLS

difference caused by the temperature change is about 1 Hz. Using Eq. (2), the calculated T_2^* in magic trap-2 drops to about 1.9 s because of the increase in the temperature. This causes mobile qubits to lose 10% of their coherence time, which is undetectable in the experiment, as verified by the data in Fig. 5. This is because with the magic trap method, fluctuations of other sources like heating of atoms and pointing instabilities of the trap laser beams have been greatly suppressed. The remaining dominant noise source is the magnetic noise which is not changed during the transfer process. The data in Fig. 5 shows that mobile qubits do not experience additional coherence loss in the transfer process, and the magic ODTs is indeed robust for coherently transfer of mobile qubits. But the frequencies of two curves (for static and mobile qubits) in Fig. 5 are different (25.3 Hz and 28.8 Hz, respectively). This discrepancy is again attributed to the uncontrolled magnetic field drift, which can reach 5.4 mG (corresponding to 3.8 Hz shift of the Ramsey fringe) in the 2 day experiment.



Figure 5. (Color online) Measured Ramsey signals for single static qubits (black square) and single mobile qubits (red dots) at B=3.115 G. Every point is an average over 100 experimental runs. The solid curves are fits to the damped sinusoidal function. The fitted values of coherence times τ of static qubits and mobile qubits are 206 ± 69 ms and 205 ± 74 ms respectively.

In summary, we demonstrated a coherent transfer of a mobile qubit, a prerequisite step in realizing a largescale neutral atom quantum information processing platform. This transfer was crucially aided by magic trapping technique that mitigated the leading source of decoherence, the DLS for two qubit states. To this end, we experimentally demonstrated the novel technique of magic intensity trapping. This technique relies on the importance of the previously neglected ground state hyperpolarizability which makes the dependence of DLS on laser intensity parabolic; at the extrema of that dependence, the DLS is insensitive to spatial variations and fluctuations of the trapping laser intensity. The measured coherence time is limited by the residual magnetic noise. The coherence preservation of single mobile qubits has been demonstrated. Extending the operation to a large scale register is straightforward. Our results pave the way for constructing a scalable quantum-computing architectures with single atoms trapped in an array of ODTs. The quantum gate operation [30] and quantum speed limit exploration [31] may also be improved by using the magic trapping technique. Although this work has focused on quantum information processing applications, the demostrated magic trapping technique is anticipated to benefit other studies with optically trapped atoms, e.g., controlled coherent collisions between ⁸⁵Rb and ⁸⁷Rb atoms [32].

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