Nonlinear Interaction of Edge-Localized Modes and Turbulent Eddies in Toroidal Plasma under $n=1$ Magnetic Perturbation

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The effect of static $n=1$ resonant magnetic perturbation (RMP) on the spatial structure and temporal dynamics of edge-localized modes (ELMs) and edge turbulence in tokamak plasma has been investigated. Two dimensional images measured by a millimeter-wave camera on the KSTAR tokamak revealed that the coherent filamentary modes (i.e., ELMs) are still present in the edge region when the usual large scale collapse of the edge confinement, i.e., the ELM crash, is completely suppressed by $n=1$ RMP. Cross-correlation analyses on the 2-D images show that (1) the RMP enhances turbulent fluctuations in the edge toward the ELM-crash-suppression phase, (2) the induced turbulence has a clear dispersion relation for wide ranges of wavenumber and frequency, and (3) the turbulence involves a net radially outward energy transport. Nonlinear interactions of the turbulent eddies with the coexisting ELMs are clearly observed by bispectral analysis, which implies that the exchange of energy between them may be the key to the prevention of large scale crashes.

High confinement mode (H-mode) plasmas are characterized by an edge region with steep pressure gradient and high current density called the pedestal and the semi-periodic collapse of the pedestal due to the development and crash of filamentary modes called edge localized modes (ELMs) [1, 2]. A reliable control of ELM crashes is an important issue for steady state burning plasma, because the heat and particle losses during the ELM crash are often spatially localized in the first surface causing damages on those hot spots. Perturbing the plasma edge by external magnetic fields is considered a promising solution to the ELM crash control via enhancement of particle transport and thereby reduction of the pressure gradient below the crash threshold [3]. In particular, resonant magnetic perturbation (RMP) has been applied successfully for suppression and/or mitigation of the ELM crashes in several tokamaks [4–7]. The Korea Superconducting Tokamak Advanced Research (KSTAR) is equipped with a set of 12 coils at the outboard wall (4 top coils, 4 middle coils and 4 bottom coils). Each row of coils can produce a radial static magnetic field with toroidal mode number $n=1$ or $n=2$ depending on the coil current configuration [8]. It has been demonstrated experimentally that the RMP can suppress or mitigate the ELM crash without significant change of the energy confinement although neither the exact mechanism nor reliability of the control method is clear yet.

In the KSTAR device, the spatial structure and temporal dynamics of the ELM and edge turbulence have been investigated in 2-D using electron cyclotron emission imaging (ECEI) diagnostics [9, 10]. It should be noted that the electron cyclotron emission (ECE) can be treated as a local measurement in the pedestal region even though the optical depth $\tau$ is marginal ($\tau \lesssim 1$) there. The high contrast and the coherent rotation of ELM filaments (Fig. 1) are good evidences of the localized measurement [11]. The ECE eventually becomes no longer localized close to and outside the separatrix (well known as shine-through problem), where the ECEI system cannot provide imaging.

The experiments for ELM-crash-suppression were con-
figured in a lower single null, high elongation $\kappa > 1.8$ and triangularity $\delta \approx 0.5$. The plasma current $I_p \approx 0.5$ MA, the magnetic field $B_0 \approx 1.9$ T, and the corresponding edge safety factor $\psi_{95} \approx 6$. Figure 1 shows the time history of the $H_\alpha$ signal and ECE images of distinctive ELM filaments at different stages of $n = 1$ RMP. The ELM has toroidal mode number $n \sim 15$ [12] and pattern velocity of $v_{\text{pol}} \approx 1.7$ km/s along the electron diamagnetic direction before application of RMP. Note that the pattern velocity is the lab-frame velocity of the mode taking into account both the poloidal and toroidal plasma flow velocities ($v_{\text{pol}}$ and $v_{\text{tor}}$):

$$v_{\text{pt}} = v_{\text{pol}} - v_{\text{tor}} \times \tan \alpha_\ast + v_{\text{ph}} = v_\perp / \cos \alpha_\ast + v_{\text{ph}}, \quad (1)$$

where $\alpha_\ast$ is the pitch angle near the midplane, $v_\perp$ is the perpendicular plasma flow velocity, and $v_{\text{ph}}$ is the phase velocity of mode in the plasma frame [13]. In the rising phase of the RMP current ($I_{\text{RMP}}$), the amplitude of ELM crash slightly reduced but the mode number ($n \sim 15$) remained the same.

Shortly after the ramp-up phase of $I_{\text{RMP}}$, ELM crashes were fully suppressed (i.e., no spikes in the $H_\alpha$ signal) but the filamentary ELMs still persisted at the edge with higher mode number ($n \sim 20$) and more complex behavior compared to the ordinary ELMs with the usual quasi-periodic crashes (prior to the application of RMP): The filamentary mode appears and disappears repeatedly and sometimes bursts with small amplitude. The small burst events are easily identified by large spikes in the RF signal of a filter-bank RF spectrometer similar to the case of the usual ELM crashes [14]. At the same time, absence of $H_\alpha$ spikes at those burst events indicates that the bursts are localized in the plasma edge region, which is distinguished from the usual ELM crashes involving the collapse of the pedestal with large particle transport. The pattern velocity of the ELMs in the crash-suppression phase is typically small on the order of $\sim 1$ km/s and sometimes they appear to halt, similar to the reduction of perpendicular electron flow in the ELM-crash-suppression phase observed in DIII-D [15]. On the other hand, the pattern velocity of ordinary ELMs in the KSTAR is observed in wide range (up to several 10s km/s) in both electron and ion diamagnetic directions. As an important comparison, ELMs without bursts were also observed in some cases of ELM-crash-suppression under RMP (Fig. 2b). The absence of ELM bursts is supported by the quiescent RF signal. The mode grows and decays repeatedly in a random way. Assuming that the ELM filaments are formed along the magnetic field line, the lifetime of the non-bursting ELMs was estimated as $\sim 500\mu s$, which is much shorter than the typical lifetime of ordinary ELMs $\sim 10$ ms. These observations suggest that the RMP did not completely suppress the growth of ELMs but instead provided a damping to balance against the instability drive and thereby kept the perturbation amplitude below the threshold of a large ELM crash.

In an effort to understand the different dynamics among the three cases (ordinary ELMs, ELMs with small-scale bursts without pedestal collapse, and non-bursting ELM), cross-correlation analyses including correlation coefficients, coherence, and cross-phase among ECEI channels were performed to measure the wave dispersion of the turbulent fluctuations [16]. The cross-correlation analysis has been performed for a steady-state ELM-crash-suppressed H-mode plasma under the $n = 1$ RMP (time $t = 15.7 - 15.85$ s, line-average density $n_{e,f} \sim 2.5 \times 10^{19}$ m$^{-3}$, and toroidal velocity in the pedestal $v_{\text{tor,ped}} \sim 70$ km/s). Figure 3 is an example of coherence and cross-phase for 4 (radial) $\times$ 3 (poloidal) ECEI channels covering approximately $8 \times 5$ cm$^2$ near $\psi \sim 0.95$, where $\psi$ is the poloidal flux coordinate. The cross correlation parameters are obtained at every 150 ms by averaging over 10 data segments of 15 ms duration (each segment contains 7, 500 data points for 500 kHz sampling rate). This example clearly shows the existence of broadband and low frequency coherent modes ($f < 70$ kHz) along the poloidal direction in a narrow radial zone ($0.97 < \psi < 0.99$). Note that the random background noise cannot make substantial correlation among
the channels well separated in space. The fact that the finite correlations were observed in the narrow radial zone along the specific poloidal direction suggests that the observations are real. Similar broadband fluctuations were also observed in magnetic signals by Mirnov coil array [8].

Two distinct features of the ELM-crash-suppressed phase identified by the correlation analysis are summarized in Fig. 4: (1) ELM component around $\sim 20$ kHz and (2) broadband turbulent eddies. Note that the broadband turbulence structure has been observed in all cases of ELM-crash-suppression regardless of the existence of the small localized bursts. The spectral power of the turbulence ($30 - 70$ kHz) increases with $I_{\text{RMP}}$ while the spectral power of the ELM component ($5 - 30$ kHz) decreases (Fig. 4a). This may suggest that the RMP induces the edge turbulence [17, 18] and ELM crashes are suppressed when the edge turbulence level exceeds a certain threshold. The spectral power distribution $S_L(k_\rho, \omega)$ [19] in Fig. 4b shows the dispersion relation obtained from 2-D ECEI signals in the ELM-crash-suppression phase. A clear dispersion relation is observed over a wide range of wavenumber ($k_\rho < 1$ cm$^{-1}$) and frequency ($f < 70$ kHz) with the average group velocity $\sim 3$ km/s along the electron diamagnetic direction in the laboratory frame. Note that the dispersion curves in both Fig. 4b and 4c change the slope slightly around the ELM frequency. The measured wavenumber allows one to deduce the characteristic size of the turbulence, usually compared with the hybrid Larmor radius $\rho_s = \sqrt{2m_iT_e}/eB$ where $m_i$ is the ion mass and $e$ is the electric charge. In this example case, $k_\rho \rho_s < 0.1$ using $\rho_s \sim 1$ mm at the edge. Kinetic ballooning modes (KBMs) [20], microtearing modes (MTMs) [21], resistive ballooning modes (RBMs) [22] and ion temperature gradient (ITG) modes [23] are of similar size ($k_\rho \rho_s \sim 0.1$ in a tokamak). These instability modes can be distinguished by the propagation direction: KBM and ITG propagate in the ion diamagnetic direction, the MTM propagates in the electron diamagnetic direction, and the RBM does not have any preferential direction. The observed group velocity of the turbulence suggests the plasma frame phase velocity of the turbulence ($v_{\text{ph}}$) is in the electron diamagnetic drift direction since the expected poloidal flows can-

FIG. 3. The cross-phase and cross-coherence measurement using 4 (radial) ×3 (poloidal) ECEI channels. Each channel position is marked by coordinates [R,z]. The red line is the separatrix position and the blue box indicates the reference channel for cross-correlation. The red horizontal line in the cross-coherence plot is the statistical error limit.

FIG. 4. (a) The time traces of integrated spectral powers of ELM (blue; 5 – 30 kHz) and turbulence (red; 30 – 70 kHz) along with the RMP coil current. (b) The spectral power distribution $S_L(k_\rho, \omega)$ in the ELM-crash-suppression phase. (c) Parallel wavenumber measurement using two toroidally separated ECE imaging systems.
not exceed sum of other factors in the KSTAR plasma, i.e., $|v_{pol}| < |v_{pt} + v_{tor} \times \tan \alpha_s| \approx 12$ km/s. Figure 4c is the dispersion of the parallel wavenumber $k_\parallel$ during the ELM-crash-suppression phase measured by the two independent ECEI systems [10] separated by 1/16th of the torus circumference on the KSTAR device. A broad dispersion is found for $f < 70$ kHz and $10/qR < k_\parallel < 20/qR$, where $q \approx 6$ is the safety factor at the mode position $R \approx 2.25$ m. $k_\parallel$ is determined by measuring the phase delay $\Delta \Phi_{12}$ between the two systems according to the relation, $k_\parallel = \Delta \Phi_{12}/\Delta l$, where $\Delta l$ is the distance between the two toroidally-separated view positions.

The effect of the turbulent eddies on the radial transport can be studied by measuring the phase relationship between the radial velocity fluctuations ($\tilde{v}_r$) and the ECE intensity fluctuations ($\tilde{T}_{ECE}$). Because $T_{ECE}/\tilde{T}_{ECE} = (1 + A_2)\tilde{T}_e/T_e + A_2\tilde{n}_e/n_e$ in the edge region where $0 < A_2 < 1$ is a numerical function of the optical depth and wall reflection [24, 25], the radial flux $\Gamma_{ECE} = \frac{1}{2}(\tilde{v}_r \tilde{T}_{ECE})$ may be considered as a combination of particle and heat flux. The cross-correlation velocimetry technique with time-delay estimation [26] is applied to the ECE images to track the high speed motion of the turbulent eddies which are moving and deforming in the presence of the turbulent flow field and then obtain $\tilde{v}_r$. The measured cross-phase between $\tilde{v}_r$ and $\tilde{T}_{ECE}$ during the ELM-crash suppression period is approximately zero in the range of 30 – 50 kHz, suggesting that the turbulent eddies cause a net outward energy flux $\Gamma_{ECE} \propto |\tilde{T}_{ECE}|^2 > 0$. This is consistent with the observed reduction of the stored energy (by about 10-30%) [8] and may have prevented the buildup of free energy for the ELM growth. Note that the velocimetry analysis also provides the information on the potential fluctuations $\phi$ (Fig. 5) assuming the relation $\tilde{v}_r = \tilde{E}_\theta/B = -\nabla_\theta \tilde{\phi}/B = -ik_\theta \tilde{\phi}/B$ (here, $\tilde{E}_\theta$ is the poloidal electric field component) [27]. If independent simultaneous measurement of $\tilde{n}_e$ is available, the cross-phase between $\tilde{\phi}$ and $\tilde{n}_e$ can be used to distinguish among different instability drives (e.g. $\pi/2$ for interchange mode and 0 for drift mode [28]).

In addition to the particle flux enhancement by the turbulent eddies in the ELM-crash-suppression phase, nonlinear interactions are expected between ELMs and turbulent eddies as they coexist in the $S_L(k_\theta, \omega)$ plot (Fig. 4b). The simplest nonlinear interactions are the three-wave coupling represented by the bispectrum $B(f_1, f_2) = F(f_1)F(f_2)F^*(f_1 + f_2)$ where $F$ denotes the Fourier transform and $f$’s denote the wave frequencies [29]. As expected from nonlinear interactions between a narrow-band coherent wave (i.e., ELM with frequency $f_{ELM}$) and broad-band waves (i.e., turbulent eddies), the auto-bispectrum plot obtained from ECEI signals (Fig. 6) shows line features (vertical, horizontal, and $-45^\circ$ lines with intercepts at $\pm f_{ELM}$). Note that these lines are essentially identical by the symmetries of bispectrum $B(f_{ELM}, f) = B(f, f_{ELM}) = B^*(f_{ELM} + f, -f)$ where $B$ is the bispectrum of ECEI signals before the suppression of ELM crashes. The nonlinear interaction revealed by the bispectrum (Fig. 6) and the opposite trends in the spectral power between ELM and turbulent eddies (Fig. 4a) suggest that the turbulent fluctuations induced by RMP dissipates the free energy for the ELM growth.

In summary, the ELM-crash-suppression phase under $n = 1$ RMP is characterized by the coexistence of the filamentary ELMs and smaller scale turbulent eddies in the edge. It is found that the filamentary structure of ELMs is maintained with substantial fluctuations in amplitude without large scale collapse, which is distinguished from the ordinary ELMs with quasi-periodic collapse of pedestal. Cross-correlation technique on the 2-D ECEI signals revealed that the turbulence at the edge has a wide range of poloidal wavenumber $k_\theta < 1$ cm$^{-1}$ and rotates in the electron diamagnetic direction with parallel wavenumber in the range of $10/qR < k_\parallel < 20/qR$. The
radial velocity and ECE intensity fluctuations of these turbulent eddies are approximately in phase and thus the turbulence involves a net radial energy transport. The bispectrum analysis clearly shows that the coexisting ELMs and turbulent eddies nonlinearly interact with each other. However, it is not clear whether the nonlinear interaction suppresses the ELM growth and/or facilitates triggering of small-scale burst, which remains as a future study. Both the enhancement of radially outward transport and the nonlinear interaction with ELMs are the main effects of the edge turbulence and may be the key to the physics mechanism of ELM-crash-suppression by low-n RMP.

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