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Negative Coulomb Drag in Double Bilayer Graphene

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We report experimental measurement of Coulomb drag in a double quantum well structure consisting of bilayer-bilayer graphene, separated by few layer hexagonal boron-nitride. At low temperatures and intermediate densities a novel negative drag response with inverse sign is observed, distinct from the momentum and energy drag mechanisms previously reported in double monolayer graphene. By varying the device aspect ratio the negative drag component is suppressed and a response consistent with pure momentum drag is recovered. In the momentum drag dominated regime, excellent quantitative agreement with the density and temperature dependence predicted for double bilayer graphene is found.

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Coulomb drag \textsuperscript{1} between parallel quantum wells provides a uniquely sensitive measurement of electron correlations since the drag response depends on interactions only \textsuperscript{2–5}. Recently it has been demonstrated that a new regime of strong interactions can be accessed for devices consisting of two monolayer graphene (MLG) crystals, separated by few layer hexagonal boron-nitride \textsuperscript{6–20}. In addition to the unique dispersion of the graphene bandstructure, advancements in the mechanical assembly of 2D materials make it possible to reduce the interlayer well distance to only a few atomic lengths, while preserving high mobility\textsuperscript{21}. Moreover, the ambipolar nature of graphene allows independent control over the carrier type and density in each layer with simple electrostatic gating. In this regime of strong interactions and low disorder, new phases of matter, such as the superfluid exciton condensate, are expected to emerge\textsuperscript{22–26}.

Drag experiments in double MLG \textsuperscript{6–9} have indeed revealed a rich complexity of new behaviors, including a low density response at both zero and finite field driven by energy coupling mechanisms \textsuperscript{18–20}, and a high density scaling not captured by existing theories \textsuperscript{6}. The precise relationship of these observations to the MLG bandstructure is the subject of ongoing studies. In a parallel vein, owing to the different single particle energy spectrum and density of states in bilayer graphene (BLG), significant variation in the drag coefficient is expected for double quantum wells consisting of two BLG layers\textsuperscript{10,11}. Moreover, further enhancement of the interaction strength compared with MLG is anticipated, allowing good electrical contact to each layer (in double BLG, leads defined by etching, such as in previous studies of double MLG structures \textsuperscript{6–9} develop a band gap under transverse magnetic field and become highly resistive). Further details of the device fabrication including the effect of introducing graphite leads can be found in the supplementary information (SI).

In a typical drag measurement current, \(I_{\text{drive}}\), is applied through two corner leads of the drive BLG layer, and the resulting voltage, \(V_{\text{drag}}\), is measured from corner leads of the drag BLG layer (Fig. 1a). Fig. 1b shows an example of the drag resistance, defined by the relation \(R_{\text{drag}} = V_{\text{drag}}/I_{\text{drive}}\), plotted as a function of the top and bottom layer densities, \(n_T\) and, \(n_B\), respectively, acquired at \(T = 300\) K. The carrier density of each BLG layer is related to the applied gate voltages by independent measurement of the layer Hall resistivities under applied magnetic field (see SI). The density dependence exhibits a 4 quadrant symmetry, with \(R_{\text{drag}}\) being negative (positive) when the carriers in the two BLG layers have the same (opposite) sign. This is the expected sign relation in a momentum coupling drag picture \textsuperscript{18,19}, and we adopt the convention of referring to this as positive drag in all four quadrants. We note that all drag responses reported are similar under switching the drive and drag layers, satisfying the expected Onsager relation.

At \(T = 300\) K, the isolevels of \(R_{\text{drag}}\) suggests a functional dependence of \(R_{\text{drag}} = f(n_T + n_B)\), as opposed to
FIG. 1. Coulomb drag. (a) Schematic of a double-bilayer graphene device and local Coulomb drag measurement. Left inset, optical image of a double-bilayer graphene device. Right inset, cross section of the bilayer graphene-hBN heterostructure. (b) $R_{\text{drag}}$ as a function of $n_T$ and $n_B$ at 300K from the local drag measurement. The solid curves are isolevels. Inset, The behavior of $R_{\text{drag}}$ at 300K along matched density lines, $n_T = n_B$ (e-e) and $n_T = -n_B$ (e-h).

The expected form of $f(n_T \times n_B)^{10,11}$. This is consistent with the drag response reported for double MLG suggesting a similar origin for the unconventional, but so far unknown, density dependence. Inset of Fig. 1b shows the drag response along the matched density condition, $n_T \pm n_B$. $R_{\text{drag}}$ initially diverges with decreasing density, but then diminishes to zero near the charge neutrality point (CNP). When the Fermi energy in both BLG layers is tuned to their respective CNP [referred to as the double neutrality point (DNP)] the drag response drops to zero within our measurement resolution.

Fig. 2a shows a plot of the drag resistance for the same measurement configuration, but acquired at $T = 120$ K. At this temperature the drag unexpectedly inverts sign in all four quadrants. The inversion regime remains symmetric with $R_{\text{drag}}$ positive (negative) when both layers contain carriers with the same (opposite) sign. Examining the response along the matched density lines at low temperature (Fig. 2b and 2c) reveals three distinct drag regimes. Along $n_T = -n_B$ the sign of the drag is expected to be positive at all densities. Instead, the drag begins positive at high density, crosses over to negative at intermediate density, and then becomes posi-
The fit coefficient $\alpha$ is plotted in the inset against geometric factor $w/L$. The finite drag response at $V = 0$ meV, corresponding to an energy gap smaller than 10meV, $27$. The finite drag response at the DNP (green curve, Fig. 2c inset) shows similar magnitude and temperature dependence to that observed for the DNP response in double MLG $^6$, suggests the same energy drag mechanism as the origin of this zero density feature.

Figs. 3b shows the result of varying the measurement configuration. We characterize the geometry by the ratio $w/L$ where $w$ is the lateral distance separating the current and voltage leads, and $L$ is the distance between the source and drain. A schematic cartoon of a “local” geometry (defined by $w = 0$) and a “nonlocal” geometry are shown in Fig. 3a (we note that in all measurements the voltage leads remain parallel to the current leads). In the nonlocal geometry the negative drag component is suppressed (Fig. 3b), and a picture qualitatively similar to the high temperature response is fully recovered. Since interaction is mediated through long-range Coulomb scattering in the momentum transfer picture, we argue that the negative drag originates from a more local interaction between charge carriers.

In the Fermi liquid regime with drag mediated by a momentum-relaxation mechanism, the drag coefficient for double BLG, in the matched density configuration, is expected theoretically to vary with temperature, $T$, and density, $n = \|n_{T,B}\|$, according to the scaling formula

$$ R_{\text{drag}}(T) \propto \alpha T^\beta $$

where $\beta = 2$ (Figs. 3c and 3d).
negative drag components, with the relative contribution of the competing mechanisms of the positive and significant deviation. We interpret this to be a consequence of the hydrodynamic response plays an important role. At present the origin of the negative drag is not known. Because of its appearance in all four density quadrants we do not consider this to be related to formation of indirect excitons between the layers. We find that both the local and non-local drag response appear to be independent of the contact metal and configuration in our devices. The suppression in non-local geometry suggests the negative drag results from a shorter relaxation mechanism than can be attributed to a momentum coupling picture. One possibility is that in the density and temperature range of negative drag, electron liquid is collision dominated, as recent measurement in graphene suggests that at such temperature hydrodynamic response plays an important role. Negative drag was also reported for 1D-1D systems, but there is no obvious reason to believe there is a relation to the mechanism of negative drag reported here. Similar negative drag behavior at zero field, the power law coefficient $\beta$ is plotted against the geometric factor $w/L$. The contribution from the negative component is increasingly suppressed as the measurement geometry is made more nonlocal, and the power converges to the expected value of $\beta = 2$ within the measurement uncertainty [the same result is observed for $n_T = n_B$ (see SI)]. Fig. 3d shows the density dependence of $R_{\text{drag}}$ in the equal density regime at $T = 150$ K, for different measurement geometries. With increasing nonlocal geometry, the density dependence of $R_{\text{drag}}$ converges to the expected $1/n^\alpha$ dependence, with $\alpha = 3$ (inset in Fig. 3d). Both the temperature and density response suggests that by measuring in the nonlocal geometry we are able to isolate the momentum coupling component of the drag response, and moreover we find good quantitative agreement with the theoretically calculated temperature and density dependence for double BLG $^{10,11}$.

Finally, we examine the drag response in the presence of a magnetic field. Near the DNP, $R_{\text{drag}}$ is shown to be negative in a small magnetic field, and grows in amplitude with increasing $B$ field. This behavior is consistent with previous result from MLG, originating from an energy driven Nernst effect. At $B = 1$ T, the density dependence of $R_{\text{drag}}$ measured at $T = 200$ K and $70$ K are shown in the lower left and lower right corner of Fig. 4a. At $T = 200$ K, $R_{\text{drag}}$ displays the four quadrant symmetry consistent with momentum drag. At $70$ K, $R_{\text{drag}}$ changes sign away from the DNP. The sign inversion is particularly clear in the $n_T = n_B$ (e-e and h-h) quadrants, contrasted by the strong negative peak at the DNP. Simultaneous Hall drag measured at $200$ K and $70$ K, is shown in Fig. 4b. Hall drag is expected to be zero in a pure momentum transfer picture and a nonzero Hall drag response has been explained by the field induced coupling between the momentum and energy transfer modes. In the same temperature regime where we observe negative drag at zero field, we find that the Hall drag response under finite field also changes sign (Fig. 4b). This behaviour is unlike the monotonic response of the Hall drag observed in double monolayer graphene.

$R_{\text{drag}} \propto T^{\beta}/n^\alpha$ (1)

with temperature and density power exponents dependent on a particular transport regime defined by the Fermi energy $E_F$, Fermi momentum $k_F$, interlayer separation $d$, and inverse Thomas-Fermi screening radius $k_{TF}$, respectively. We estimate our samples to be in a strong coupling regime with $k_{TF}d \sim 0.6$ and always at temperatures satisfying $T \ll E_F/(k_Fd)$ (see SI), and therefore expect $R_{\text{drag}} \propto T^2/n^3$.

In Fig. 3c we compare the temperature dependence of $R_{\text{drag}}$ in the equal density regime $n_T = n_B$, from the local and nonlocal geometry. In the nonlocal geometry, the response appears to well fit a power law over large temperature range whereas the local drag response displays significant deviation. We interpret this to be a consequence of the competing mechanisms of the positive and negative drag components, with the relative contributions apparently varying with temperature. In the inset,

FIG. 4. Magnetodrag. a) $R_{\text{drag}}$ measured at $T = 200$ K and $70$ K, $B = 1$ T as a function of match density, $n_T = n_B$. The insets show the density dependence of $R_{\text{drag}}$ at 200K (lower left) and 70K (lower right). b) Hall drag $R_{xy}$ measured at $T = 200$ K and $70$ K, $B = 1$ T as a function of match density, $n_T = n_B$. Inset shows the density dependence of $R_{xy}$ measured at $T = 200$ K (lower left) and 70 K (lower right).

$^{10,11}$.
magnetodrag and Hall drag responses are observed in all BLG devices studied (with interlayer distances spanning 5 nm-12 nm). We note that negative drag has not been reported for MLG, suggesting a possible relation to the dispersion relation which is quadratic in BLG compared to linear for MLG.

In summary, Coulomb drag measurement is reported for the first time in a double well consisting of two graphene bilayers. At low temperature and intermediate density, a negative drag is observed with sign opposite to that expected in a simple momentum coupling regime. We find that the negative drag response can be suppressed using a nonlocal measurement geometry, and that the temperature and density dependence of $R_{\text{drag}}$ from nonlocal measurement matches well with theory for the momentum drag. In a non-zero magnetic field, Hall drag and magnetodrag observed at high temperature are consistent with the energy driven mechanism observed in double MLG, whereas in the negative drag regime, Hall drag changes sign. Finally we note that the negative drag response is fully symmetric and for both matched e-e (h-h) and mismatched, e-h (h-e) carrier types. The capability to achieve good electrical contact to a double BLG structure, and to isolate the momentum driven drag component in a nonlocal geometry, over wide density range, makes it feasible to look for the excitonic condensate phase, possibly with smaller interlayer separation, and at lower temperature.

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**COMPETING FINANCIAL INTERESTS**

The authors declare no competing financial interests.