

# CHCRUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

# Widening the Axion Window via Kinetic and Stückelberg Mixings

Gary Shiu, Wieland Staessens, and Fang Ye Phys. Rev. Lett. **115**, 181601 — Published 27 October 2015 DOI: 10.1103/PhysRevLett.115.181601

## Widening the Axion Window via Kinetic and Stückelberg Mixings

Gary Shiu<sup>1,2,3</sup>, Wieland Staessens<sup>4</sup>, and Fang Ye<sup>1,2</sup>

<sup>1</sup> Department of Physics, 1150 University Avenue,

<sup>2</sup> Center for Fundamental Physics and Institute for Advanced Study,

Hong Kong University of Science and Technology, Hong Kong

<sup>3</sup> University of Chinese Academy of Sciences, Beijing, China

<sup>4</sup> Instituto de Física Teórica UAM-CSIC, Cantoblanco, 28049 Madrid, Spain

We point out that kinetic and Stückelberg mixings that are generically present in the low energy effective action of axions can significantly widen the window of axion decay constants. We show that an effective super-Planckian decay constant can be obtained even when the axion kinetic matrix has only sub-Planckian entries. Our minimal model involves only two axions, a Stückelberg U(1) and a modest rank instanton generating non-Abelian group. Below the mass of the Stückelberg U(1), there is only a single axion with a non-perturbatively generated potential. In contrast to previous approaches, the enhancement of the axion decay constant is not tied to the number of degrees of freedom introduced. We also discuss how kinetic mixings can lower the decay constant to the desired axion dark matter window. String theory embeddings of this scenario and their phenomenological features are briefly discussed.

PACS numbers: 11.25.-w, 98.80.Cq, 95.35.+d

#### INTRODUCTION

Axions or more generally axion-like particles are among the most recurrent extensions of the Standard Model. Their defining shift symmetry, originally proposed to solve the strong CP problem [1], turns out to have far-reaching consequences in many other contexts in particle physics and cosmology. The axionic shift symmetry constrains how they couple to each other and to other matter perturbatively, namely, solely via derivative couplings. These properties of axions also make them an interesting candidate for dark matter and/or the inflaton. Generic arguments in quantum gravity suggest [2] that a continuous global symmetry is at best perturbatively exact. Indeed, the continuous shift symmetry is broken to a discrete one through the coupling of axions to nonperturbative instantons, which in turn induce a potential (in particular, masses) for the axions. Much of the axion physics is dictated by the axion decay constant, which defines the periodicity of the canonically normalized axions. Axionic couplings scale inversely with the axion decay constant, and their masses are determined by the axion decay constant and the non-perturbative scales involved. For example, the QCD axion can make up the cold dark matter of the universe if its decay constant lies within the window  $10^9 \text{ GeV} \leq f_{\text{QCD}} \leq 10^{12} \text{ GeV}$  [3], while the non-perturbative potential for an axion can realize large field inflation [4] if the associated decay constant exceeds the (reduced) Planck mass, i.e.,  $f_{inf} > M_{Pl}$ .

Axions are ubiquitous in string theory, as they arise from dimensional reduction of higher form fields which appear generically in string compactifications. Their shift symmetries originate from gauge symmetries in extra dimensions. Although the origins of various string axions and their shift symmetries differ, careful studies surveying all known formulations of string theory [5, 6] pointed to a universal upper bound for their axion decay constant f:

$$f \lessapprox \frac{g^2}{8\pi^2} M_{Pl},\tag{1}$$

with g the coupling constant of the 4D non-Abelian gauge group to which the axion couples anomalously. This leads to the folklore that the string axion decay constant cannot exceed the Planck scale [6] and at the same time reveals the tension to attain the QCD axion window [5, 7].

In this paper, we propose a new mechanism to widen the range of axion decay constants in theories where the intrinsic axion field range is limited. An implicit assumption behind the aforementioned upper bound is the absence of mixings among axions, i.e., the eigenbasis for the axion kinetic terms matches that of the instanton potential terms. However, it is not uncommon for axions to mix kinetically and in the presence of Stückelberg U(1)gauge fields, there are even further mixing effects. Thus, it is conceivable for the light axion that survives in the low energy theory to have a field range that differs significantly from what the original Lagrangian might suggest.

To explore the theoretically allowed window of axion decay constants, we considered the general multi-axion Lagrangian and found that the bound in eq. (1) can be significantly relaxed when mixing effects are taken into account. We hasten to stress that although our motivation is partly string theoretical, our results apply generally to quantum field theories with multiple axions. More explicitly, for a system of N axions  $a^i$  charged under M U(1) gauge symmetries through Stückelberg couplings and coupling anomalously to P non-Abelian gauge groups, the low energy effective action reads as follows,

University of Wisconsin, Madison, WI 53706, USA

$$\mathcal{S}^{\text{eff}} = -\int \left[ \sum_{\alpha,\beta=1}^{M} f_{\alpha\beta} F^{\alpha} \wedge \star_4 F^{\beta} + \sum_{A=1}^{P} \frac{1}{g_A^2} \text{Tr} \left( G^A \wedge \star_4 G^A \right) + \frac{1}{2} \sum_{i,j=1}^{N} \mathcal{G}_{ij} \left( da^i - \sum_{\alpha=1}^{M} k_{\alpha}^i A^{\alpha} \right) \wedge \star_4 \left( da^j - \sum_{\beta=1}^{M} k_{\beta}^j A^{\beta} \right) \right. \\ \left. - \frac{1}{8\pi^2} \sum_{A=1}^{P} \left( \sum_{i=1}^{N} r_{iA} a^i \right) \text{Tr} \left( G^A \wedge G^A \right) - \frac{1}{8\pi^2} \sum_{\alpha,\beta=1}^{M} \left( \sum_{i=1}^{N} s_{i\alpha\beta} a^i \right) F^{\alpha} \wedge F^{\beta} + \dots \right].$$

$$(2)$$

We choose the convention that the axions  $a^i$  have a periodicity of  $2\pi$  and thus their decay constants are determined by the kinetic terms,  $\mathcal{G}_{ij}$ . The matrix  $f_{\alpha\beta}$  encodes the coupling constants of and possible mixing among the U(1) gauge symmetries with gauge potential  $A^{\alpha}$  and field strength  $F^{\alpha}$ .  $G^{A}$  denotes the field strength of the strongly coupled non-Abelian gauge groups that generate instanton potentials. The axion kinetic terms exhibit two types of mixing effects: mixing due to a non-diagonal metric  $\mathcal{G}_{ij}$  on the axion moduli space and mixing due to Stückelberg couplings for charges  $k^i_{\alpha} \neq 0$ . An additional form of mixing arises as the axionic directions coupling anomalously to the non-Abelian gauge groups do not necessarily correspond to the eigenbasis for the potentials. This is expressed through the integer coefficients  $r_{iA}$  and  $s_{i\alpha\beta}$ , for which at least two different coefficients are simultaneously non-vanishing. The anomalous couplings of the axions to the U(1) gauge groups are included for completeness, but are not expected to contribute to the axion potentials due to the absence of U(1) instantons in four dimensions [8]. The ... denote the possible presence of chiral fermions and/or generalized Chern-Simons terms, required to ensure vanishing gauge anomalies [9]. Moreover, due to the presence of the chiral fermions and/or generalized Chern-Simons terms, the anomalous couplings of the axions to the gauge instantons remain U(1) gauge invariant when the axions carry Stückelberg charges as shown explicitly in section 2.2.1 of [10].

### KINETIC AND STÜCKELBERG MIXINGS

To highlight the mixing effects among axions, it suffices to consider a minimal set-up with two axions (N = 2), one Abelian and one non-Abelian gauge groups (M = P = 1). We can drop the indices  $\alpha$  and A, and neglect the anomalous coupling of the axions to the U(1) field strength. In order to identify the axionic direction eaten by the U(1) gauge boson through the Stückelberg mechanism and to determine the correct axion decay constants, we have to perform a set of transformations  $(SO(2) \text{ rota$  $tions and rescalings})$  diagonalizing the kinetic terms for the two-axion system. A linear combination  $\zeta$  of the axions  $a^1$  and  $a^2$  will form the longitudinal component of the massive U(1) gauge boson with a Stückelberg mass:

$$M_{st} = \sqrt{\lambda_{-}(k^{-})^{2} + \lambda_{+}(k^{+})^{2}},$$
 (3)

while the orthogonal linear combination  $\xi$  remains uncharged under this U(1). Here,  $\lambda_{\pm}$  correspond to the eigenvalues of the axion moduli space metric  $\mathcal{G}_{ij}$ :

$$\lambda_{\pm} = \frac{1}{2} \left[ (\mathcal{G}_{11} + \mathcal{G}_{22}) \pm \sqrt{4\mathcal{G}_{12}^2 + (\mathcal{G}_{11} - \mathcal{G}_{22})^2} \right], \quad (4)$$

and the charges  $(k^+, k^-)$  correspond to the U(1) charges in the axion eigenbasis diagonalising the metric  $\mathcal{G}_{ij}$ :

$$k^{+} = \cos\frac{\theta}{2}k^{1} + \sin\frac{\theta}{2}k^{2}, \quad k^{-} = \sin\frac{\theta}{2}k^{1} - \cos\frac{\theta}{2}k^{2}.$$
 (5)

The continuous parameter  $\theta \in [0, 2\pi]$  encodes the amount of axion mixing associated to a non-diagonal metric  $\mathcal{G}_{ij}$ through the parametrisation:

$$\cos \theta = \frac{\mathcal{G}_{11} - \mathcal{G}_{22}}{\lambda_+ - \lambda_-}, \quad \sin \theta = \frac{2\mathcal{G}_{12}}{\lambda_+ - \lambda_-}.$$
 (6)

For a diagonal axion metric  $\mathcal{G}_{ij}$ , i.e.  $\mathcal{G}_{12} = 0$ , the U(1) charges  $(k^+, k^-)$  reduce to the original charges  $(k^1, -k^2)$  as they appear in eq. (2).

In the unitary gauge, the axion  $\zeta$  is part of the massive U(1) gauge boson, and thus only the anomalous coupling between the axion  $\xi$  and the non-Abelian gauge group prevails [10], yielding an effective axion decay constant:

$$f_{\xi} = \frac{\sqrt{\lambda_+ \lambda_- M_{st}}}{\cos \frac{\theta}{2} \left(\lambda_+ k^+ r_2 + \lambda_- k^- r_1\right) + \sin \frac{\theta}{2} \left(\lambda_- k^- r_2 - \lambda_+ k^+ r_1\right)}.$$
(7)

The axion decay constant  $f_{\xi}$  exists purely due to the presence of non-vanishing Stückelberg couplings  $(k^i \neq 0)$ , irrespective of the occurrence of a non-diagonal metric  $\mathcal{G}_{ij}$  on the axion moduli space. Upon integrating out the massive U(1) gauge boson and the non-Abelian degrees of freedom, the gauge instanton background generates an axion-potential for  $\xi$  of the usual cosine-type:

$$V_{\rm eff}(\xi) = \Lambda^4 \left[ 1 - \cos\left(\frac{\xi}{f_{\xi}}\right) \right],\tag{8}$$

where  $\Lambda$  is related to the characteristic energy scale of the condensate. The process of integrating out the massive gauge boson occurs in two steps, as explained in detail in section 2.2.1 of [10]: first, the axion  $\zeta$  is eliminated from the effective action by going to the unitary gauge for the gauge boson. In the unitary gauge, the anomalous coupling of the axion  $\zeta$  to the non-Abelian gauge group vanishes as a consequence of the vanishing anomaly condition. The orthogonal axionic direction  $\xi$  then forms the

remaining axion that couples anomalously to the non-Abelian gauge instantons, explaining why the effective potential in (8) solely depends on  $\xi$ . In a second step, the massive gauge boson is then integrated out by virtue of its equation of motion, giving rise to ( $M_{st}$ -suppressed) four-point interactions among the chiral fermions. In the end, the uncharged axion  $\xi$  is the only field serving as the inflaton, ensuring that the inflationary motion occurs along a gauge-invariant path.

To explore the physical field range of the axion  $\xi$ , it suffices to determine how its axion decay constant scales with the continuous parameters in a specific region of the moduli space. For illustrative purposes, let us consider three regions of the parameter space where the axion decay constant takes super-Planckian values:

**Region 1:** for small kinetic mixing in the metric, i.e.  $\theta \approx 0$ , the decay constant (7) takes the form:

$$f_{\xi} = \frac{\sqrt{\mathcal{G}_{11}\mathcal{G}_{22}}M_{st}}{k^{1}r_{2}\mathcal{G}_{11} - k^{2}r_{1}\mathcal{G}_{22}} = \frac{\sqrt{\mathcal{G}_{22}}\sqrt{(k^{1})^{2} + \varepsilon^{2}(k^{2})^{2}}}{k^{1}r_{2} - \varepsilon^{2}k^{2}r_{1}}, \quad (9)$$

where the continuous parameter  $\varepsilon^2 \equiv \mathcal{G}_{22}/\mathcal{G}_{11}$  indicates the amount of isotropy between the metric eigenvalues. The decay constant takes trans-Planckian values in the region of the moduli space where the continuous parameter  $\varepsilon$  asymptotes to

$$\varepsilon^2 \to \frac{k^1 r_2}{k^2 r_1}.\tag{10}$$

**Region 2:** for perfect isotropy between the diagonal entries of the metric, i.e.  $\varepsilon^2 = 1$ , and a non-negligible amount of kinetic mixing, i.e.  $\theta \approx \frac{\pi}{2}$ , the U(1) charges  $(k^+, k^-)$  reduce to  $(\frac{k^1+k^2}{\sqrt{2}}, \frac{k^1-k^2}{\sqrt{2}})$ . If we assume  $r_1 = r_2$ for simplicity, the decay constant can be simplified to:

$$f_{\xi} = \frac{\sqrt{\mathcal{G}_{11}}\sqrt{1+\varrho^2}\sqrt{(k^1)^2+(k^2)^2+2k^1k^2\varrho^2}}{|(k^1-k^2)r_1|\sqrt{1-\varrho^2}},$$
 (11)

where the continuous parameter  $\rho^2 \equiv \mathcal{G}_{12}/\mathcal{G}_{11}$  measures the amount of kinetic mixing. In this moduli space region the decay constant reaches trans-Planckian values whenever the non-diagonal entries in the metric are of the same order as the diagonal ones, namely for:

$$\varrho^2 \to 1.$$
(12)

**Region 3:** for intermediary kinetic mixing the range of the decay constant (7) can be represented through contour plots as functions of the continuous parameters  $\varepsilon$ and  $\theta (\in [0, \frac{\pi}{2}])$  as in fig. 1 upon fixing the U(1) charges  $k^i$  and the parameters  $r_i$ . Regions in the moduli space with  $f_{\xi} > 10^2 \sqrt{\mathcal{G}_{11}}$  are highlighted in white.

While we exploit multiple axions to obtain an effective super-Planckian decay constant, our mechanism differs fundamentally from earlier approaches. Unlike N-flation [11] and aligned natural inflation [12], the enhancement



FIG. 1. Contour plots of decay constant  $f_{\xi}(\theta, \varepsilon)$  for  $2r_1 = 2r_2 = 2k^1 = k^2$  (left) and  $r_1 = 2r_2 = k^1 = 2k^2$  (right). The  $f_{\xi}$ -values range from small (purple) to large (red) following the rainbow contour colors. Unphysical regions with complex  $f_{\xi}$  are located in the black band.

in the physical axion field range we found here is not tied to the number of degrees of freedom introduced (including axions, gauge fields, and any additional fields needed to ensure consistency of the theory). This can be seen already in the minimal setup above as an enhancement in neither (9) nor (11) requires adjusting the discrete parameters (e.g. axion charges, axion-instanton couplings, and the rank of the non-Abelian gauge group) of the model but rather *continuous* parameters (i.e. mixing angle  $\theta$  and ratios  $\varepsilon$  or  $\rho$  of metric entries) in the axion moduli space which leave the low energy spectrum intact. This decoupling of the axion field range enhancement from the low energy spectrum holds generally for the multi-axion system described by eq. (2) and not just the minimal setup considered here. In contrast, the enhancement in the axion field range scales as  $\sim \sqrt{N}$  in N-flation, and as  $\sim \sqrt{N!} n^N$  [13] in aligned natural inflation, with N the number of axions and  $n \in \mathbb{Z}$  the coefficients for the axion-instanton couplings. The presence of these light fields generically renormalize the Planck mass and we expect on general grounds [14] that  $\delta M_{Pl}^2 \sim N$ . Thus our scenario is minimal in that parametrically fewer degrees of freedom are needed to achieve the same enhancement and so their associated quantum corrections to the Planck mass are less severe.

Let us end this section by briefly discussing the possibility to lower the effective axion decay constant to within the dark matter window. If we consider the same configuration as in region 2, but assume that  $r_1 = -r_2$  and  $k^1 = k^2$ , the axion decay constant instead reads:

$$f_{\xi} = \frac{\sqrt{\mathcal{G}_{11}^2 - \mathcal{G}_{12}^2}}{\sqrt{2}|r_2|\sqrt{\mathcal{G}_{11} + \mathcal{G}_{12}}} = \frac{\sqrt{\mathcal{G}_{11}}\sqrt{1 - \varrho^2}}{\sqrt{2}|r_2|}, \qquad (13)$$

where the numerator decreases significantly in the limit (12). Considering moderate values for  $r_2 \sim \mathcal{O}(1 - 10)$  and  $\sqrt{\mathcal{G}_{11}} \sim \mathcal{O}(10^{15} - 10^{17})$  GeV, a desired decay constant within the axion dark matter window can be obtained for moduli space regions with large kinetic mixing effects, i.e.  $1 - \rho^2 \sim \mathcal{O}(10^{-4} - 10^{-8})$ . More generically, eigenvalue repulsion can be used to lower the decay constant, similar to the Z' masses considered in [15–17].

In summary, by scanning the continuous moduli dependent parameter space for the axion moduli space metric  $\mathcal{G}_{ij}$ , we can find regions where the axion decay constant  $f_{\xi}$  in eq. (7) takes trans-Planckian field ranges  $f_{\xi} > M_{Pl}$ and regions where the decay constant falls within the classical axion decay window  $10^9 \text{ GeV} \leq f_{\xi} \leq 10^{12} \text{ GeV}$ . These regions are mostly uncovered through the proposed kinetic mixing mechanisms in settings with a high amount of isotropy between the entries in the metric  $\mathcal{G}_{ij}$ . Nonetheless, the inclusion of kinetic mixing effects among axions allows for effective axion decay constants with a much broader energy window than the one of a single axion, alleviating the tension between current experimental bounds and the typical decay constants for string axions.

#### STRING THEORY IMPLEMENTATION

It is natural to ask if our scenario can be realized in string theory where axion candidates are abundant. Axion models with a super-Planckian field range are sensitive to Planck scale physics. Thus, in such cases, a string theory implementation is not only natural but a necessity. Here we lay out the criteria that a string compactification needs to satisfy in order to implement the mechanisms we proposed above. Closed string axions emerge naturally from the dimensional reduction of ten dimensional p-forms as summarised in table I, where for concreteness we restricted to four-dimensional (4D) Calabi-Yau  $(\mathcal{CY}_3)$  orientifold compactifications of Type II superstring theory [21]. The background-dependence is reflected by the Hodge-numbers  $h_{\pm}^{(1,1)}$ ,  $h^{(2,1)}$  and  $h_{+}^{(2,2)}$  expressing the number of orientifold-even/odd 2-forms, 3-forms and 4forms respectively, and thereby setting the number  $N_a$ of axions. De Rahm-duality then associates to every axion an orientifold-even/odd closed p-cycle  $\gamma_i$  on the  $\mathcal{CY}_3$ orientifold such that an axion  $a^i$  can be defined as:

$$a^{i} \equiv \frac{1}{2\pi} \int_{\gamma_{i}} \mathcal{C}_{p}.$$
 (14)

Overview of Type II closed string axions						
	Type IIA		Type IIB			
<i>p</i> -form $\mathcal{C}_p$	$B_2$	$C_3$	$C_0$	$B_2$	$C_2$	$C_4$
axion $a^i$	$b^a$	$\xi^k$	$c_0$	$b^a$	$c^a$	$\rho^{lpha}$
Na	$h_{-}^{(1,1)}$	$h^{2,1} + 1$	1	$h_{-}^{(1,1)}$	$h_{-}^{(1,1)}$	$h_{+}^{(2,2)}$
U(1)		D6 on 3-cycle			D7 on	4-cycle

TABLE I. Summary of model-dependent axions in Type II superstring theory on  $\mathcal{CY}_3$  orientifolds [22]. The D-brane configuration in the last row indicates which axions acquire Stückelberg U(1) charges and the origin of such U(1)'s.

The dimensional reduction of the kinetic terms for the *p*-forms yields the kinetic terms for the respective axions whose continuous shift symmetries are remnants of the

ten-dimensional gauge-invariance. Furthermore, the kinetic terms for the axions are characterised by a nondiagonal metric  $\mathcal{G}_{ij}$  on the axion moduli space, as in eq. (2), except for the axion  $c_0$ . The metric  $\mathcal{G}_{ij}$  depends on the moduli fields appearing in the same fourdimensional  $\mathcal{N} = 1$  supermultiplet as the respective axions. These moduli have to be stabilised at higher energy scales for the effective action in eq. (2) to be applicable.

The axions  $\xi^k$ ,  $c^a$  and  $\rho^\alpha$  can be charged under the U(1) gauge group [23, 24] supported by the appropriate Dp-brane as listed in table I. The Stückelberg couplings for the charged axions in eq. (2) are required for anomaly cancelation by virtue of the generalised Green-Schwarz mechanism though they can also appear for anomaly free U(1)'s. The axions  $\xi^k$  and  $c^a$  are charged under the U(1) gauge symmetry when the corresponding D-brane wraps the (6 - p)-cycle Poincaré dual to the *p*-cycle associated with the axion. For the  $\rho^\alpha$  axions to be charged under the Abelian gauge group, the D7-brane has to wrap the 4-cycle Poincaré dual to the 2-cycle supporting an internal magnetic 2-form flux. The Stückelberg charges  $k^i$  are thus directly related to the integer wrapping numbers of the U(1) D-brane along the internal dimensions.

The anomalous couplings to gauge instantons in eq. (2) follow naturally from the reduction of the Chern-Simons action for the D-brane stack supporting the non-Abelian gauge group [23, 24]. For the axions  $\xi^k$  and  $\rho^{\alpha}$  to couple anomalously to the non-Abelian gauge symmetry, it suffices that the corresponding D-brane stack wraps their associated *p*-cycles. For the  $c^a$  axions the D-brane stack has to wrap the 4-cycle Poincaré dual to the 2-cycle supporting an internal magnetic 2-form flux.

Apart from gauge instantons, string theory also allows for the presence of D-brane instantons where Euclidean D-branes wrap *p*-cycles  $\gamma_i$  on  $\mathcal{CY}_3$  while being pointlike spacetime objects. The instanton amplitude is set by the action  $\mathcal{S}_{E_{p-1}}$  for the Euclidean D-brane, which scales with the volume  $\operatorname{Vol}(\gamma_i)$  of the wrapped *p*-cycle:

$$e^{-\mathcal{S}_{E_{p-1}}} = e^{-\frac{2\pi}{g_s} \operatorname{Vol}(\gamma_i) - i \, a^i}.$$
(15)

The axion dependence in the phase then breaks the axion symmetry to the discrete shift symmetry  $a^i \rightarrow a^i + 2\pi$ , implying that the moduli space for stringy axions is a torus  $T^{N_a}$  equipped with metric  $\mathcal{G}_{ij}$ . Instanton corrections only contribute to the effective action when their fermionic zero modes can be saturated upon integration over the instanton moduli space, e.g. for orientifoldinvariant rigid cycles  $\gamma_i$ . For Stückelberg charged axions the D-brane instanton amplitude violates the U(1) symmetry and effective contributions to the superpotential require the presence of U(1) charged fermions whose collective charge cancels the U(1) charge violation by the instanton to ensure gauge invariance [25]. Such chiral fermions arise at the intersections of two D-branes in the bi-fundamental representation under the gauge groups supported by the respective D-branes. Which instanton type is the leading non-perturbative contribution and thereby sets the axion potential, is a model-dependent consideration. Explicit stringy realisations of set-up (2) are constructed in [10] using Type IIA with intersecting D6-branes [26] on the toroidal orientifold  $T^6/\Omega \mathcal{R}$ . A large axion decay constant is realised through certain isotropy relations among the complex structure moduli, analogous to the discussion for region 1 in eq. (9).

#### CONCLUSIONS

In this paper, we propose and demonstrate that kinetic and Stückelberg mixing effects can widen the axion window. Our scenario applies generally to field and string theories with multiple axions so long as the effective action in eq. (2) is applicable. In the context of string theory, our mechanism to lower the axion decay constant does not invoke large compact cycles, thereby alleviating the requirement for an intermediate string mass scale [27] or the utility of field theory axions [28]. Our results thus open up new possibilities of detecting string axions through astrophysical, cosmological and laboratory means. It also allows to reconcile with a high fundamental string scale, should a detection of primordial tensor mode points us to high scale inflation. On the other hand, an enhancement of the axion decay constant to super-Planckian values through mixings enables us to realize "natural-like inflation" in string theory. Generically, one expects the leading cosine potential (assumed to be exact in natural inflation [4]) to receive model-dependent modifications from higher (or other subleading) instanton effects when the effective axion decay constant becomes large [29]. This expectation is in line with the weak gravity conjecture [18, 19] whose formulation for multi-axion systems is currently under investigation [20]. Nonetheless, the extended periodicity of the axion is not expected to be altered by these subleading corrections. While such corrections are model-dependent and hard to compute, their presence is suggestive of quantum gravity at work in order to couple the multiple axion system to gravity. The deviation from a cosine potential could leave a measurable effect on the inflationary perturbation spectrum. Quantifying such deviation requires a detailed understanding of the ultraviolet completion of inflation and the moduli stabilization mechanism involved. Turning this around, precise cosmological measurements may point us closer to the structure of our string vacuum.

#### Acknowledgments

We thank Kiwoon Choi, Fernando Marchesano, Pablo Soler, and Angel Uranga for useful discussions. The work of G.S. and F.Y. is supported in part by the DOE grant DE-FG-02-95ER40896 and the HKRGC grants HKUST4/CRF/13G, 604231 and 16304414. W.S. is supported by the ERC Advanced Grant SPLE under contract ERC-2012-ADG-20120216-320421, by the grant FPA2012-32828 from the MINECO, and the grant SEV-2012-0249 of the "Centro de Excelencia Severo Ochoa" Programme. W.S. would also like to thank the European COST action MP1210 "The String Theory Universe" for a Short Term Scientific Mission Grant.

- R. D. Peccei and H. R. Quinn, Phys. Rev. Lett. 38, 1440 (1977); Phys. Rev. D 16, 1791 (1977).
- [2] L. F. Abbott and M. B. Wise, Nucl. Phys. B **325** (1989)
  687; S. R. Coleman and K. M. Lee, Nucl. Phys. B **329** (1990) 387; R. Kallosh, A. D. Linde, D. A. Linde and L. Susskind, Phys. Rev. D **52** (1995) 912 T. Banks and N. Seiberg, Phys. Rev. D **83** (2011) 084019.
- [3] M. S. Turner, Phys. Rept. **197** (1990) 67.
- [4] K. Freese, J. A. Frieman and A. V. Olinto, Phys. Rev. Lett. 65, 3233 (1990).
- [5] P. Svrcek and E. Witten, JHEP 0606, 051 (2006)
- [6] T. Banks, M. Dine, P. J. Fox and E. Gorbatov, JCAP 0306, 001 (2003)
- [7] K. Choi and J. E. Kim, Phys. Lett. B 154, 393 (1985)
   [Erratum-ibid. 156B, 452 (1985)].
- [8] Note however that string theory allows for the existence of U(1)-type D-brane instantons. Such instantons can contribute to the effective superpotential when a Euclidean D-brane wraps the same internal cycle as the Dbrane, even if the D-brane supports a U(1) gauge group.
- [9] G. Aldazabal, L. E. Ibanez and A. M. Uranga, JHEP 0403 (2004) 065; P. Anastasopoulos, M. Bianchi, E. Dudas and E. Kiritsis, JHEP 0611 (2006) 057; J. De Rydt, J. Rosseel, T. T. Schmidt, A. Van Proeyen and M. Zagermann, Class. Quant. Grav. 24 (2007) 5201.
- [10] G. Shiu, W. Staessens and F. Ye, arXiv:1503.02965 [hepth].
- [11] S. Dimopoulos, S. Kachru, J. McGreevy and J. G. Wacker, JCAP 0808, 003 (2008)
- [12] J. E. Kim, H. P. Nilles and M. Peloso, JCAP 0501, 005 (2005)
- [13] K. Choi, H. Kim and S. Yun, Phys. Rev. D 90, no. 2, 023545 (2014)
- [14] G. Dvali, Fortsch. Phys. 58 (2010) 528
- [15] G. Shiu, P. Soler and F. Ye, Phys. Rev. Lett. **110**, 241304 (2013)
- [16] W. Z. Feng, G. Shiu, P. Soler and F. Ye, Phys. Rev. Lett. 113, 061802 (2014)
- [17] W. Z. Feng, G. Shiu, P. Soler and F. Ye, JHEP 1405, 065 (2014)
- [18] N. Arkani-Hamed, L. Motl, A. Nicolis and C. Vafa, JHEP 0706, 060 (2007)
- [19] H. Ooguri and C. Vafa, Nucl. Phys. B 766, 21 (2007)
- [20] J. Brown, W. Cottrell, G. Shiu and P. Soler, to appear; D. Junghans, private communication.
- [21] T. W. Grimm and J. Louis, Nucl. Phys. B 699 (2004) 387; T. W. Grimm and J. Louis, Nucl. Phys. B 718 (2005) 153.

- [22] For Type IIB string theory, we considered the orientifold projection inverting the sign of the Calabi-Yau threeform. For an orientifold projection leaving the Calabi-Yau three-form completely invariant, the Hodge-numbers for the axions  $c^a$  and  $\rho^{\alpha}$  have to be swapped.
- [23] T. W. Grimm and D. V. Lopes, Nucl. Phys. B 855 (2012)
   639; M. Kerstan and T. Weigand, JHEP 1106 (2011)
   105; P. G. Camara, L. E. Ibanez and F. Marchesano, JHEP 1109 (2011) 110.
- H. Jockers and J. Louis, Nucl. Phys. B **705** (2005) 167;
   M. Haack, D. Krefl, D. Lust, A. Van Proeyen and M. Zagermann, JHEP **0701** (2007) 078;
   M. Cicoli, M. Goodsell, J. Jaeckel and A. Ringwald, JHEP **1107** (2011) 114.
- [25] R. Blumenhagen, M. Cvetic and T. Weigand, Nucl. Phys. B **771** (2007) 113; L. E. Ibanez and A. M. Uranga, JHEP **0703** (2007) 052; R. Blumenhagen, M. Cvetic, S. Kachru and T. Weigand, Ann. Rev. Nucl. Part. Sci. **59** (2009) 269; L. E. Ibanez and A. M. Uranga, Cambridge, UK: Univ. Pr. (2012) 673 p.
- [26] See, e.g., R. Blumenhagen, M. Cvetic, P. Langacker and G. Shiu, Ann. Rev. Nucl. Part. Sci. 55, 71 (2005); R. Blu-

menhagen, B. Kors, D. Lust and S. Stieberger, Phys. Rept. 445, 1 (2007); F. Marchesano, Fortsch. Phys. 55, 491 (2007) for a review.

- [27] M. Cicoli, M. Goodsell and A. Ringwald, JHEP **1210** (2012) 146
- [28] G. Honecker and W. Staessens, Fortsch. Phys. 62 (2014) 115
- [29] This comment applies also to aligned natural inflation [12]. In axion monodromy inflation [30], the axion decay constant controlling the non-perturbative potential remains sub-Planckian; see [31] (also [32]) for its implementations in supersymmetric compactifications.
- [30] E. Silverstein and A. Westphal, Phys. Rev. D 78 (2008) 106003; L. McAllister, E. Silverstein and A. Westphal, Phys. Rev. D 82 (2010) 046003
- [31] F. Marchesano, G. Shiu and A. M. Uranga, JHEP 1409 (2014) 184
- [32] R. Blumenhagen and E. Plauschinn, Phys. Lett. B
   **736** (2014) 482; A. Hebecker, S. C. Kraus and L. T. Witkowski, Phys. Lett. B **737** (2014) 16.