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## Formation and observation of a quasi-two-dimensional $d_{xy}$ electron liquid in epitaxially stabilized $Sr_{2-x}La_xTiO_4$ thin films

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We report the formation and observation of an electron liquid in  $Sr_{2-x}La_xTiO_4$ , the quasi-two-dimensional counterpart of  $SrTiO_3$ , through reactive molecular-beam epitaxy and in situ angle-resolved photoemission spectroscopy. The lowest lying states are found to be comprised of Ti  $3d_{xy}$  orbitals, analogous to the  $LaAlO_3/SrTiO_3$  interface and exhibit unusually broad features characterized by quantized energy levels and a reduced Luttinger volume. Using model calculations, we explain these characteristics through an interplay of disorder and electron-phonon coupling acting co-operatively at similar energy scales, which provides a possible mechanism for explaining the low free carrier concentrations observed at various oxide heterostructures such as the  $LaAlO_3/SrTiO_3$  interface.

Strontium titanate (SrTiO<sub>3</sub>) is a key building block in oxide electronics, particularly for the formation of two-dimensional electron liquids (2DELs) at SrTiO<sub>3</sub> interfaces and surfaces. For instance, the interface between LaAlO<sub>3</sub>/SrTiO<sub>3</sub> [1], exhibits exotic properties such as superconductivity and ferromagnetism. There have also been reports of high temperature superconductivity at the monolayer FeSe / SrTiO<sub>3</sub> interface. At the LaAlO<sub>3</sub>/SrTiO<sub>3</sub> interface or SrTiO<sub>3</sub> surface, the degeneracy of the  $t_{2q}$  orbitals is lifted [2-4], and the  $d_{xy}$  states play an important role in the observed ferromagnetism [5] and the superconducting phase diagram [6, 7]. An alternate strategy to break the  $t_{2g}$  degeneracy and realize a 2DEL is to interrupt the three-dimensional network of corner-sharing TiO<sub>6</sub> octahedra with a double SrO layer, resulting in Sr<sub>2</sub>TiO<sub>4</sub>, the quasi-two-dimensional n=1 end member of the Ruddlesden-Popper (RP) series  $Sr_{n+1}Ti_nO_{3n+1}$ , of which  $SrTiO_3$  is the other threedimensional,  $n = \infty$  end member.  $Sr_2TiO_4$  could also provide a natural platform exploring exotic superconductivity, ferroelectricity, and magnetism in the titanates. Bulk single crystals of Sr<sub>2</sub>TiO<sub>4</sub> have never been synthesized [8], hindering the utility and understanding of this compound, and its electronic structure remains unexplored to date.

In this Letter, we report the synthesis and investigation of the electronic structure of lanthanum doped  $Sr_{2-x}La_xTiO_4$  by a combination of oxide MBE and in situ angle-resolved photoemission spectroscopy (ARPES). We observe a single  $d_{xy}$  band resulting in a circular Fermi surface near the Fermi energy, in addi-

tion to a number of unexpected features. The measured Luttinger volume is approximately a factor of 4 smaller than expected, and the spectra exhibit a series of energy levels with  $\Delta=93$  meV separation, reminiscent of the phonon replicas recently reported in monolayer FeSe on SrTiO<sub>3</sub> [9]. We employ model calculations which cooperatively treat the effects of disorder and electron-phonon (el-ph) coupling to successfully these apparent discrepancies

Epitaxial La-doped Sr<sub>2</sub>TiO<sub>4</sub> films with a thickness of 20 formula units were grown on (001) LSAT [(LaAlO<sub>3</sub>)<sub>0.3</sub> (SrAl<sub>1/2</sub>Ta<sub>1/2</sub>O<sub>3</sub>)<sub>0.7</sub>] substrates by MBE at 850° C in  $10^{-7}$  torr of O<sub>2</sub> using a shuttered growth technique [11]. in situ ARPES measurements were taken at 20 K at an energy resolution of  $\Delta E = 12$  meV with a VG Scienta R4000 electron analyzer and He-I $\alpha$  photons ( $h\nu$ = 21.218 eV). Details of the sample growth, DFT calculations, and the theoretical model are provided in the supplementary[url], which includes Refs. [12-15].

Due to the layered crystal structure and an increase in the titanium apical oxygen distance over the in-plane oxygens (2.1%), the degeneracy in Ti  $t_{2g}$  orbitals is removed [Fig. 1(b)]. Similar to the high- $T_c$  cuprates and many other layered compounds, the very weak interlayer hopping leads to quasi-two-dimensional electronic states in  $\rm Sr_2TiO_4$ . Upon electron doping (La substitution for Sr), the  $d_{xy}$  states should first form a two-dimensional cylindrical Fermi surface. X-ray diffaction showed no impurity phases and rocking curves with a narrow full width at half maximum (FWHM) of 12.3 arcseconds and 28.6 arcseconds for the 5% and 15% La-doped  $\rm Sr_2TiO_4$ 

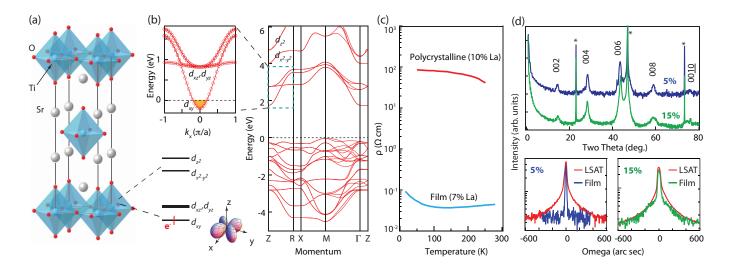


Figure 1: (color online) (a) Diagram of the crystal structure of  $Sr_2TiO_4$ . (b) DFT band calculations of  $Sr_2TiO_4$ , showing the lowest unoccupied band of  $d_{xy}$  character. The left enlarged plot shows a rigid band shift of 5% electron doping. (c) An epitaxial La-doped  $Sr_2TiO_4$  thin film shows orders of magnitude lower resistivity than a bulk polycrystalline sample [10]. (d) X-ray diffraction and rocking curve of the 006 diffraction peak of 5% and 15% La-doped  $Sr_2TiO_4$  films. The X-ray diffraction scans are offset for clarity and the substrate peaks are marked with asterisks (\*).

films, respectively. The resistivity of doped films was found to be comparable with previous thin films grown by MBE [16], but more than 4 orders of magnitude more conducting than previously reported bulk samples [10]. A negative Hall resistivity confirmed the presence of electron-like charge carriers.

ARPES measurements of La doped Sr<sub>2</sub>TiO<sub>4</sub> reveal an electron-like band near  $E_F$  and a Fermi surface comprised of a single circular electron pocket centered at  $\Gamma$ [Fig. 2(a)], in good agreement with DFT calculations. The integrated density of states (DOS) up to higher binding energies indicates a gap of 4 eV between bottom of the  $d_{xy}$  band and the top of the O 2p valence band, consistent with earlier optical measurements [17]. Thus, the doped electrons indeed populate the  $d_{xy}$  band instead of only forming deeply bound impurity states as has been observed in many doped, non-conducting oxides. It should be noted that our ARPES spectra show no clear sign of oxygen vacancies, whose signature is a non-dispersive ingap state 1 eV below the bottom of the conduction band in  $SrTiO_3$  [18–21]. Furthermore, we did not find any illumination dependence of the ARPES spectra, like that observed in  $SrTiO_3$  [19, 21].

A host of additional unusual spectral features are also observed in the ARPES spectra (Fig. 3), which cannot be explained within a simple rigid band shift scenario. In addition to the low-lying electronic states crossing  $E_F$ , we also observe a broad spectral feature extending to higher binding energies. Second, the spectra exhibit a set of characteristic shoulders separated by 93 meV, which is also not present in the DFT calculations. Third, the measured carrier concentrations are substantially lower

than the measured La doping levels.

The Fermi wavevectors  $(k_F s)$  and the total Luttinger volume extracted from the Fermi surface maps [Fig. 2(a)] yield a doping level of  $0.013 \pm 0.004$  electrons per Ti atom (corresponding to a sheet carrier density of 0.9  $\pm$  $0.3 \times 10^{13}$  cm<sup>-2</sup> per TiO<sub>2</sub> layer) and  $0.039 \pm 0.005$  electrons per Ti atom (2.6  $\pm 0.3 \times 10^{13}$  cm<sup>-2</sup> per TiO<sub>2</sub> layer) for the nominal 5 % and 15 % La-doped samples, respectively. The La content was confirmed by x-ray photoelectron spectroscopy to be  $4.0 \pm 0.5\%$  and  $14.4 \pm 0.5\%$ , respectively [Fig. 2(c), 2(d)]. The unexpectedly low carrier activation is reminiscent of the low free carrier activations measured at the LaAlO<sub>3</sub>/SrTiO<sub>3</sub> interface [22, 23]. This could potentially be attributed to electrically inactive lanthanum atoms associated with either dopantinduced disorder or vertically running SrO faults, which have been observed by electron microscopy [24, 25]. The degree of disorder can be estimated from the lineshape of the momentum distribution curve (MDC) taken at  $E_F$ [Fig. 3(g) and 3(h)]. Here, a Gaussian lineshape is found to yield a good fit to the observed MDCs, resulting in momentum width values of  $\Delta k = 0.14 \text{ Å}^{-1}$  and  $0.18 \text{ Å}^{-1}$ (FWHM), which is of the order of 1-2 unit cells. Understanding the nature of the disorder and how to increase the carrier mobility will be essential for future investigations into searching for possible superconductivity in doped or gated  $Sr_2TiO_4$ .

Next, we focus on the 93 meV shoulders observed in our ARPES measurements, where peaks in the spectra show an unusual quantization of the electronic states (Fig. 3). One possible scenario would be the formation of quantum well (QW) states as observed in Si-doped

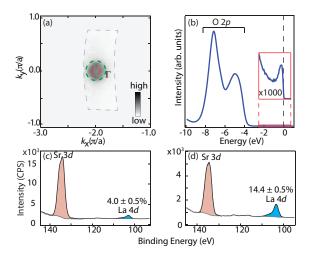


Figure 2: (color online) (a) ARPES isoenergy intensity map with an integration window of  $E_F$  +/- 10 meV of 5% La-doped  $\rm Sr_2TiO_4$  shows a single circular pocket centered at the Brillouin zone center. The red marks indicate the extracted Fermi momenta via fits of momentum distribution curves (MDCs) and the green dashed line is the expected Fermi momenta. (b) Integrated EDC of the valence band indicates a gap of  $\sim 4~\rm eV$ . (c, d) XPS measurements reveal 4.0% and 14.4% lanthanum concentrations in nominal 5% and 15% doped films, respectively.

 $\beta$ -Ga<sub>2</sub>O<sub>3</sub> [26, 27], where the impurity potential strongly confines the electron states in three-dimensions around the dopant La atom, resulting in the formation of quantized levels. In this QW picture the energy separation arising from the dopant ions should be inversely proportional to the impurity-impurity distance, which should decrease with increasing lanthanum concentration. Our ARPES measurements of a much more heavily doped (nominal 15%) La-doped Sr<sub>2</sub>TiO<sub>4</sub> film show a smaller mean free path and larger  $k_F$ , but yield an essentially identical characteristic energy separation (93  $\pm$  7 meV) [Fig. 3(f)]. Furthermore, the states reported in Si-doped  $\beta$  Ga<sub>2</sub>O<sub>3</sub> are essentially dispersionless unlike the bands in Fig. 3(a) and 3(b). Therefore, the QW interpretation cannot fully account for the quantization of the quasilocalized states observed in Sr<sub>2</sub>TiO<sub>4</sub>. In addition, we have considered the possibility of QW states due to the finite thickness of the thin films (Supplemental Information), but due to the very weak interlayer hopping along the c axis for the  $d_{xy}$  orbitals, no appreciable subband formation can be observed for the relevant  $d_{xy}$  bands, only for the unoccupied  $d_{xz}$  and  $d_{yz}$  states.

Another possible scenario would be that of a bosonic mode strongly coupled to the electronic states resulting in satellite peaks separated by the characteristic boson energy. An infrared-active  $E_u$  (LO) phonon mode at 727 cm<sup>-1</sup> (90 meV) has been reported in  $\mathrm{Sr_2TiO_4}$  [28, 29], involving the motion of oxygen anions creating an in-plane dipole which can interact with charge carriers. We note

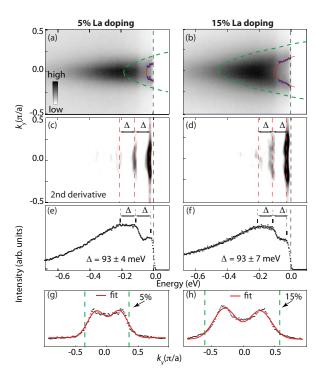


Figure 3: (a, b) ARPES spectra taken along the  $(0,0)-(0,\pi)$  direction of the 5% and 15% La-doped  $\mathrm{Sr_2TiO_4}$  films. The blue symbols mark the peak positions from Gaussian fits to the MDCs. The green and red curves are DFT calculated bands and parabolic fits to the peak positions, respectively. (c, d) The second derivative plots and (e, f) the EDCs show quantized states with a periodic separation of 93 meV for both films. The EDCs are integrated  $\pm 0.01 \text{Å}$  around Fermi momenta and the shifts from  $E_F$  could be due to the experimental resolution. (g, h) The Gaussian fits to the MDCs reveal FWHMs of 0.14 Å<sup>-1</sup> and 0.18 Å<sup>-1</sup> of the 5% and 15% doped samples, respectively.

that similar phonon replicas with comparable energies (100 meV) have also recently been reported in monolayer FeSe thin films grown on  $SrTiO_3$  which have been argued to be relevant to the enhanced superconducting transition temperature [9]. This suggests that  $Sr_2TiO_4$  may also be a potentially interesting substrate for monolayer FeSe, in addition to investigations of doped  $Sr_2TiO_4$  itself. A pure el-ph coupling scenario alone, however, cannot fully explain the broadened spectra and the substantially reduced Luttinger volumes observed in our ARPES measurements.

In order to provide a theoretical understanding of the observed spectra, we consider a model with tightbinding conduction electrons interacting with dispersionless phonon modes and disorder as described by the Hamiltonian [30]

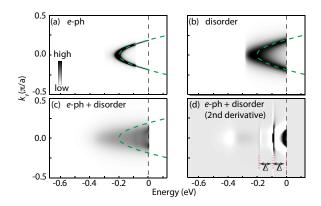


Figure 4: Calculated ARPES spectra considering (a) el-ph coupling for  $\lambda=0.15$  only ( $\lambda$  is defined by equation (4) in Supplementary), (b) disorder only, and (c) both el-ph coupling and disorder, showing the important interplay of el-ph coupling and disorder. (d) The second derivative of (c), demonstrating the quantization of quasi-localized electronic states

$$H = -\sum_{i,j} t_{ij} \left( c_i^{\dagger} c_j + \text{h.c.} \right) - \sum_{i,j} g_{i,j} c_i^{\dagger} c_i (a_j + a_j^{\dagger})$$
$$+ \omega_0 \sum_i a_i^{\dagger} a_i + \sum_i \xi_i c_i^{\dagger} c_i, \tag{1}$$

where  $c_i^{\dagger}(c_i)$  creates (destroys) an electron at site i, and  $a_i^{\dagger}(a_i)$  creates (destroys) a phonon of frequency  $\omega_0$  at site i. The hopping matrix elements  $t_{ij}$ , fitted from DFT calculations, connect neighboring sites up to fifth neighbors. In order to provide the simplest theoretical model to account for experimental evidences, the el-ph polar coupling is described by a non-local coupling  $g_{i,j}$  and the relevant phonon mode is the aforementioned LO infraredactive polar  $E_u$  mode at a frequency  $\omega_0$  of 90 meV in  $Sr_2TiO_4$  [28, 29]. The last term is an Anderson term [30], where  $\xi_i$  are energy levels distributed according to a bimodal probability  $P(\xi) = (1 - x)G_{\sigma}(\xi) + xG_{\sigma}(\xi - \xi_b),$ where  $G(\xi)$  is a Gaussian function of variance  $\sigma$ , with the disorder level  $\xi_b$  extrapolated from supercell DFT calculations and  $\sigma = 60$  meV. To investigate the role of disorder, we performed supercell DFT calculations for five different configurations of lanthanum atoms [see Supplementary Fig. 1(a)-1(f), and weighting the different configurations, we find the growth of an impurity band localized around -0.3 eV which merges into the bottom of the coherent Ti  $d_{xy}$  band.

To determine the spectral function from the Hamiltonian in Eq. (1), we use a combined Coherent Potential Approximation (CPA) [31] and phonon-phonon Non-Crossing Approximation (PPNCA) [32, 33] to treat both the local disorder and non-local el-ph coupling. The details of the formalism are reported in the supplementary and in a theoretical paper [34]. As output of our calcu-

lations, we obtain the self-energy  $\sum (k, \omega)$ , and thus the spectral function  $A(k,\omega) = (-1/\pi)\Im G(k,\omega)$ . It is clear that considering only the el-ph coupling [Fig. 4(a)] or disorder alone [Fig. 4(b)] cannot qualitatively describe the experimental ARPES spectra. The former is missing the broad structure below - 0.1 eV and the latter is missing the observed quantized phonon signatures. In contrast, including both el-ph coupling and disorder [Fig. 4(c)], the spectral function shows the quantized levels (shown clearly in the second derivative in Fig. 4(d), as well as the broad and intense spectral weight at higher binding energy, even when the value of the el-ph coupling strength is not large (see Supplementary for additional details). Inclusion of the impurities' spatial correlations, neglected in this simple approach, could lead to a larger shift of the broad spectral weight to higher binding energy [35]. The apparent discrepancy between the nominal lanthanum concentration and the small Luttinger volume can be attributed to the presence of strong disorder in the system, consistent with earlier calculations which also considered the effect of strong disorder on the low energy electronic structure [36–38]. On the other hand, in our case, impurity induced disorder alone is not enough to explain such a large deviation of the nominal doping from the Luttinger volume as is seen from the comparison of Fig. 4 b) and c). The reason for such a dramatic effect of the e-ph interaction in conjunction with a strongly disordered energy landscape originates from an increase in the binding energy of the states, which is caused by the e-ph interaction. By pushing the electronic states to higher energies and reducing the density of states near  $E_F$ , we find a strongly non-linear and non-perturbative decrease in the Luttinger volume and hence, a drop in the carrier density, particularly at the impurity sites [34] (see also Supplemental Information).

In summary, our investigation of an epitaxially stabilized 2DEL in La-doped Sr<sub>2</sub>TiO<sub>4</sub> reveals a single electronic band of  $d_{xy}$  character crossing the Fermi These electronic states, however, are strongly modified due to the interplay between dopant-induced disorder and el-ph coupling, resulting in quantized semi-localized electronic states, as recently observed in monolayer FeSe on SrTiO<sub>3</sub> [39], and a striking reduction of the expected Luttinger volume. Understanding the nature of the disorder and the interplay with the electron-phonon coupling will be essential for increasing the carrier mobility and realizing superconductivity in doped Sr<sub>2</sub>TiO<sub>4</sub>. Since Sr<sub>2</sub>TiO<sub>4</sub> is less prone to forming oxygen vacancies [10], it should provide an intriguing new platform for controllable investigations of exotic superconductivity and electron-phonon interactions in oxide heterostructures and interfaces. We have directly examined, for the first time, the interplay between disorder and el-ph coupling in a complex oxide, which we expect to be important in understanding the phenomenology of correlated transition metal oxides, where

electron-phonon coupling and disorder are known to play important roles in the underlying physics, such as the 2DEL at the LaAlO<sub>3</sub>/SrTiO<sub>3</sub> interface [22, 40–46], where the observed carrier density is much less than the expected 0.5 electrons per Ti. Our work suggests that the interplay between disorder and el-ph coupling is one natural mechanism that could explain the unusually low carrier densities at complex oxide interfaces.

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