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Detection of a dynamic cone-shaped meniscus on the surface of fluids in electric fields

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A cone-shape meniscus of electrified fluids, often called a Taylor cone, is observed in rain drops and lightning and employed in various physical instruments and experimental techniques, but the way it evolves from a rounded shape to a cone is a longstanding puzzle. Earth gravity and microgravity measurements on the meniscus whose height is just shy of droplet ejection reveal that field-driven cusp evolution exhibits a universal self-similarity insensitive to the forcing field and scaled by the fluid surface tension and density. Our work paves the way for dynamic control of field driven phenomena in fluids.

The conical meniscus of an electrified fluid with spontaneous sparks and fluid ejection has fascinated scientists for centuries [1-3]. This ubiquitous phenomenon is observed in rain drops and lightning and employed in electro-spraying and ink jet printing [2,3], mass spectrometry [4,5], ion beam sources [6], plasma technology [7], fabrication of synthetic fibers [8,9] and nanostructures [10]. Taylor [11-13] showed that surface tension and electric forces form a steady-state conical meniscus with a semi-vertex angle of 49.3°. The initial loss of meniscus stability in a sufficiently strong field can be easily predicted by linear analysis [2,12]. However, field-driven meniscus evolution from a rounded shape to a cone is a longstanding puzzle in this

well-studied phenomenon as it overlaps with spontaneous fluid ejection. In this Letter, we report data on the meniscus whose height is just shy of droplet ejection. Earth gravity and microgravity measurements, spanning more than two orders of magnitude in length and time, reveal that field-driven cusp evolution exhibits a universal self-similarity insensitive to the forcing field while a 50% increase in applied voltage shortens the overall time for the meniscus to rise by more than an order of magnitude.

Until now, two types of apparatus pioneered in 1914-1931 by Zeleny [14-16], Wilson and Taylor [17], Nolan [18] and Macky [19] have been used to electrify fluids. In type [14-17], voltage is applied to two bare electrodes, one immersed in the fluid and the other placed at a certain distance away from the fluid. In type [18,19], a drop falls through or levitates in a field produced between two electrodes. The conditions of meniscus evolution and fluid ejection are similar in the apparatuses of both types. Spontaneous fluid ejection in these apparatuses effectively prevents study of cusp dynamics. The apparatus in Fig. 1 was designed to create and control a cone-shaped meniscus by limiting the buildup of an electric charge on its surface and thus allow a dynamic regime to be investigated without drop ejection. This is achieved by separating a drop from the ground electrode with an electrically insulating film that does not allow electric current to flow between the electrodes (item 4 in Fig. 1). Due to the film presence, the drop serves as a floating electrode capacitively coupled to the electrodes (items 2&5 in Fig. 1). Details of the setup are listed in Supplemental Material [20]. The energized electrode is a metal tube fitted on an insulating nozzle 0.2mm above the nozzle exit. A drop is ejected through the nozzle onto the insulating film. The distance between the drop apex and the nozzle exit is set to 0.6mm. As the electric stress exerted on a fluid is proportional to the square of the field strength, a field is generated by a train of rectangular voltage pulses of oscillating polarity (slew

rate $0.75 \text{kV}/\mu\text{s}$) to keep the electric stress at a constant level similar to classical experiments [11-19] but reduce accumulation of charge on the drop surface due to the voltage reversals.

Experiments were conducted over a wide range of fluid properties [20, Supplemental Table 1]: density $\rho \sim 1 \text{g/cm}^3$, viscosity $\eta \sim 1-76 \text{cP}$, conductivity $\sigma \sim 0.02-10^4 \mu \text{S/cm}$, dielectric constant $\varepsilon \sim 2.7-90$, surface tension $\gamma \sim 30-72 \text{dyn/cm}$, contact angle on the insulating film (item 4 in Fig. 1) $\theta \sim 9-56^0$, charge relaxation time $t_e = \varepsilon \varepsilon_0 / \sigma \sim 1 \text{ns} - 13 \mu \text{s}$ with the vacuum permittivity ε_0 . The fluids as numbered in all figures were: 1) deionized (DI) water; 2) DI-water with 0.1M KCl; 3) polyethylene glycol PEG 200; 4) polymer solution simulating human saliva; 5) low-conducting lubricant with 0.02wt% graphene. The application of high-voltage pulses to a drop of pure lubricant caused the meniscus to oscillate but did not produce a pointed protrusion. As the lubricant conductivity was increased by adding graphene flakes, a drop formed a coneshaped meniscus. Measurements under microgravity (1.5 μ g) on the International Space Station (ISS) allowed length scales to be expanded from the sub-millimeter to the centimeter range.

Depending on the pulse voltage V_p and length T_p (Fig. 1), three modes of meniscus evolution were observed under earth gravity [Fig. 2(a) for DI-water and similar for other fluids]. <u>Mode 1</u> occurs when the electric force is weak compared with the capillary and gravity forces. The fluid level rises to form a stationary bell-shape hump in the high field region under the nozzle. When V_p exceeds the instability threshold, the portion of the fluid meniscus under the nozzle rises, oscillatory or monotonically for larger voltage and fluid viscosity, and produces a pointed protrusion. The threshold field ~2kV/mm is similar to the value observed in conventional apparatuses [12,21].

Mode 2, the subject of this work and referred to as dynamic Taylor cone, is attributed to voltages forming a cone-shaped meniscus that rises to a certain height, recedes, and then repeats itself again and again. Remarkably, meniscus evolution of low volatile PEG 200 drop, Fig.3(a), does not change throughout eight-hour testing $(1.8 \cdot 10^5 \text{ oscillations})$. The overall time for the meniscus to rise is governed by the pulse voltage. The increase of V_p from 2kV to 3kV shortens it by more than an order of magnitude [Fig.2(b,c) for DI-water and similar for other fluids]. As frequency in varying the pulse polarity increases, meniscus oscillations gradually become more irregular since a change in the voltage polarity disturbs the drop by reversing the sign of charge induced on the fluid surface. To graphically display the effects of disturbances, we plot a series of consecutive time instances, t_m, in which the drop apex rises to maximum height, h_m, against the amount of time, t_p , that passed in each such instance after the last change in the pulse polarity [Fig.2(d-f) for DI-water and similar for other fluids]. Meniscus oscillations at a fixed pulse polarity, $0 \le t_p \le T_p$, are represented on this diagram with a set of neighboring points in the direction of increasing tp. Patterns of well-ordered points demonstrate periodicity of cone-shaped tips formed at long pulses, whereas randomly scattered points show irregular cone formation at short pulses. However, a cone is remarkably insensitive to disturbances and, once formed, evolves in the same way, Fig. 3(b).

<u>Mode 3</u> occurs for larger voltages. The meniscus develops a cone-shaped tip, ejects droplets and then recedes. The process repeats itself several times and rapidly comes to an end when the drop volume becomes depleted. As the air dielectric strength \sim 3kV/mm, it begins to break down over a rising pointed protrusion in modes 2 and 3 and becomes partially conducting. In <u>mode 2</u>, a conducting channel bridges the air gap earlier than the meniscus ejects fluid. Once it forms, buildup of charge on the insulating film under the drop (item 4 in Fig. 1) reduces the field strength in the gap and chokes the electric current flow similar to that in dielectric-barrier discharge in air [22,23]. The charge transferred through the air gap produces a low current (estimated \sim nA), thus no light emissions or sparks were observed. Self-arresting of fluid ejection in <u>mode 2</u> is achieved by designing the electrical capacitance between the drop and the ground electrode to be much larger than the capacitance between the drop and the energized electrode. The voltage across the air gap therefore prevails when a pointed protrusion rises but reduces drastically as a discharge occurs.

Microgravity experiments on DI-water drops of several centimeters in size were carried out aboard ISS in Expedition 30/31. Voltage was produced with a belts-and-rollers type Van de Graaff generator assembled from LEGOs (details in Supplemental Material [20]). Water placed on the 9.8-cm diameter collector sphere formed a cone-shaped meniscus when another drop situated on an electrically insulating support was brought nearby to serve as a floating electrode for increasing the local field (photos in Figs.4,5). Three modes of meniscus evolution that appeared in earth gravity experiments were observed on ISS. Similar to the apparatus in Fig. 1, buildup of charge on the insulating support choked the electric current between the drops when a discharge occurred. A cone-shaped tip formed by a drop either emitted some fluid or receded if charge leakage weakened the electric force. Observations of microgravity dynamic Taylor cones in mode 2 are presented here.

The exceptional robustness of <u>mode 2</u> made it possible to study the cusp evolution over a broad range of length and time scales. As a protrusion develops, its round top shrinks approaching the cone shape. The limiting value of its semi-vertex angle averaged over all data under earth gravity is $48.3^{\circ}\pm1.7^{\circ}$ and $46.8^{\circ}\pm2.4^{\circ}$ under microgravity that is close to the Taylor angle 49.3° [11]. Displacement of the drop apex h is plotted in Fig.4 over the time period of the

constant vertex angle. This log-log plot demonstrates the power-law scaling over two orders of magnitude in length and time with the slope 0.64 ± 0.04 remarkably close to 2/3 recently observed in computer simulations [24,25] of the cone rise. The slope changes to 0.42 in mode 3 regime when a cone-shaped tip ejects droplets [26]. Starting with the 2/3 power law, we can form a dimensionless parameter

$$\boldsymbol{\xi} = (\mathbf{h}_{\mathrm{m}} - \mathbf{h}) / \left[\gamma (\mathbf{t}_{\mathrm{m}} - \mathbf{t})^{2} / \rho \right]^{1/3}$$
(1)

that measures the cusp self-similarity before the singularity. All earth and microgravity measurements in Fig. 4 collapse on a value of $\xi = 0.30\pm0.05$. The meniscus semi-vertex angle θ and ξ converge gradually to their limiting values as h approaches h_m regardless of the drop volume, voltage and gravity, even though ξ monotonically increases for small drops and decreases for large drops (Fig. 5). Scaling of the instantaneous meniscus shape, relative height H(r,t) vs. radius r, with the instantaneous distance of the tip from its maximum $h_m - h = H(0,t)$ demonstrates the universal self-similarity of cusp evolution (Fig.5). The selfsimilarity of field-induced cusp evolution appears to be independent of the forcing field and surprisingly resembles self-similarity observed in breakup of liquid drops, sheets and eruption of jets in the absence of a field [3,27-30] when the surface tension and inertial forces dominate.

Now we present a scaling analysis of meniscus evolution. Relative contributions of the gravity, viscous, electric, and surface tension forces in its initial stage are represented [2,3] by the gravity Bond number $Bo_g = \rho g R_D^2 / \gamma$, the Ohnesorge number $Oh = \eta / \sqrt{\rho R_D \gamma}$, and the pulse electric Bond number $Bo_e = \epsilon_0 E_{ext}^2 R_D / 2\gamma$ with the gravitational acceleration g, the drop diameter $2R_D$, and the external field strength estimated as $E_{ext} = V_p / S$, where S is the separation

between the energized electrode and the drop apex (Fig. 1). Mode 2 was observed at Bog~0.04-0.08, *Oh*~0.005-0.48, *Bo_e*~0.2-1 in earth gravity and *Bo_g*<~10⁻⁴, *Oh*~10⁻³, *Bo_e*~2.7-6.5 in microgravity [20] when the electric, inertial and surface tension forces dominated. The selfsimilar cusp evolution described by Eq. (1) with $\xi \approx 0.3$ is not affected by the fluid viscosity as it occurs at h_m-h and t_m-t (Figs. 4,5) much greater than the viscous length $L_{\eta} = \eta^2 / \gamma \rho$ and time $t_{\eta} = \eta^3 / \gamma^2 \rho$ scales where viscous forces are important [3]; $L_{\eta} \sim 0.014 - 119 \mu m$, $t_{\eta} \sim 0.0002 - 206 \mu s$ for tested fluids [20, Supplemental Table 1]. Relative contributions of inertia and surface tension to unsteady flow are represented by the Weber number $We=\rho v^2 L/\gamma$ measuring the ratio of the fluid kinetic energy to its surface energy [3] and the ratio of the fluid acceleration force to the surface tension force $A = \rho L^2 dv/dt/\gamma$, where L and v are the characteristic length and velocity. Taking h_m-h and dh/dt from Eq. (1) with $\xi \approx 0.3$ for L and v in the cusp region whose radial and longitudinal scales are of the same order (Fig.5), we obtain $We=2A\sim0.012$. Since the viscous and inertial forces are relatively small, the capillary and electric pressures are nearly balanced in the cusp region. Therefore, the field in air at the cusp surface can be approximated by Taylor's solution for a cone in equilibrium $E_a \sim \sqrt{2\gamma/\epsilon_0 R}$ [11] with the radius of cusp curvature R scaled with h_mh (Fig.5). The cusp charge increases with decreasing h_m -h. To estimate the field E_f in fluid, we use the balance equation for charge transport to the cusp surface by conduction $\varepsilon_0 d(E_a - \varepsilon E_f)/dt = \sigma E_f$ that yields $E_f/E_a \sim t_e/(t_m - t) <<1$ as the charge relaxation time t_e is shorter by several orders of magnitude than the period of cusp motion (Fig. 4). Since E_f is negligible, the field around the cusp is well approximated by Taylor's solution for an equipotential cone in equilibrium [11] that yields the limiting value of the semi-vertex cusp angle close to 49.3° (Fig. 5). As $E_a >> E_{ext}$ in the range of h_m-h where $\xi \approx 0.3$ (Figs.4,5), cusp motion is not affected by applied voltage. In fact, scaling of the instantaneous cusp shape given by Fig.5 and Eq. (1) represents the self-similar solution of electro-hydrodynamic equations for an inviscid conducting fluid with the electric pressure scaled by the capillary pressure.

The cusp evolution generates a vortex flow that can affect mixing and separation processes in the drop (Supplemental Fig. 1 [20]). Examples are shown in Supplemental Figs. 2(a) [20], where polystyrene spheres are concentrated under the conical apex or dispersed, and Supplemental Fig. 2(b) [20], where gypsum rapidly precipitates from a supersaturated aqueous solution.

In summary, we have revealed the universal self-similarity of the field-induced meniscus evolution from a rounded shape to a cone that is scaled by the fluid surface tension and density. The proposed non-contact technique paves the way for dynamic control of field driven phenomena in widespread applications [2-10,31].

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FIGURES



FIG 1 (color online). Concept of experimental apparatus. 1, electrically insulating nozzle; 2, energized electrode; 3, drop; 4, insulating film; 5, ground electrode; 6, insulating cover of 3D movable stage; V_p , pulse voltage; T_p , time of reversing voltage polarity.



FIG 2 (color online). Deionized water. Earth gravity experiments on 10-µL drop. (a) V_p - T_p diagram for modes 1, 2, 3 of drop evolution. Photos illustrate drop behavior. (b,c) Displacement h of drop apex as a function of time t in mode 2 at T_p =0.5s and V_p =(b) 2kV, (c) 3kV. Cones appear in rising at h= (b) 0.32±0.03mm; (c) 0.22±0.02mm. Larger h at 3kV caused by drop spreading. (d,e,f) Mode 2. Time instance t_m when drop apex reaches its maximum displacement h_m vs. time t_p passed after the last voltage polarity reversal, circles and triangles refer to rounded and pointed ends. V_p/T_p =(d) 2kV/0.5s, (e) 2kV/2.5ms, (f) 3kV/0.5s.



FIG 3 (color online). Earth gravity experiments. Displacement h of 10-µL drop apex as a function of time t-t_m, t_m is the instance of rising to maximum h_m. (a) Meniscus evolution of low volatile PEG 200 drop throughout eight-hour testing at $V_p/T_p=2kV/0.5s$. Cones appear at 0>t-t_m>-3.0±0.21ms, h>0.31±0.02mm. Symbols refer to testing time. Photo at 8 hrs. (b) Polymer solution simulating human saliva forms cones at 0>t-t_m>-1.67±0.15ms, h>0.32±0.02mm for $V_p=2kV$. Symbols refer to time of changing voltage polarity T_p . Cones form sporadically at $T_p=5ms$ and 2.5ms and periodically at longer T_p . Photo at $T_p=2.5ms$.



FIG 4 (color online). Dynamic Taylor cone. Displacement h of drop apex as a function of time t_m -t, t_m is the instance of rising to maximum h_m . Filled symbols refer to experiments under earth gravity on 10-µL drops at V_p =2kV and 3kV with T_p =0.5s. Data and error bars from 20 randomly chosen videos of three drops for each fluid. Open symbols refer to data under microgravity on three 0.5-mL DI-water drops. Photos show DI-water drops.



FIG 5 (color online). Meniscus rising in mode 2. Semi-vertex angle θ and parameter ξ as a function of h_m-h, and the instantaneous meniscus shape scaled with the instantaneous distance of the tip from its maximum h_m-h. (a) Experiments under earth gravity on 10-µL drops at V_p=2kV and 3kV with T_p=0.5s. Data and error bars for θ , ξ from 10 randomly chosen videos of three drops for each fluid; six instantaneous shapes of a drop at 2kV used to construct the scaled meniscus shape. (b) Experiments under microgravity on DI-water drops. Filled and open symbols refer to ten 10-mL drops (top photo) and three 0.5-mL drops (bottom photo); five instantaneous shapes of a 0.5-mL drop used to construct the scaled meniscus shape.

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