

CHCRUS

This is the accepted manuscript made available via CHORUS. The article has been published as:

Use of B→J/ψ f_{0} Decays to Discern the qq[over ⁻] or Tetraquark Nature of Scalar Mesons

Sheldon Stone and Liming Zhang Phys. Rev. Lett. **111**, 062001 — Published 6 August 2013 DOI: 10.1103/PhysRevLett.111.062001

Use of $B \rightarrow J/\psi f_0$ decays to discern the $q\bar{q}$ or tetraquark nature of scalar mesons

Sheldon Stone and Liming Zhang

Physics Department Syracuse University, Syracuse, NY, USA 13244-1130

Abstract

We consider the relative decay rates of \overline{B}^0 and \overline{B}^0_s mesons into a J/ψ plus a light scalar meson either the $f_0(500)$ (σ) or the $f_0(980)$. We show that it is possible to distinguish between the quark content of the scalars being quark-antiquark or tetraquark by measuring specific ratios of decay rates. Using current data we determine the ratio of form-factors in $\overline{B}^0_s \to J/\psi f_0(980)$ with respect to $\overline{B}^0 \to J/\psi f_0(500)$ decays to be $0.99^{+0.13}_{-0.04}$ at a four-momentum transfer squared equal to the mass of the J/ψ meson squared. In the case where these light mesons are considered to be quark-antiquark states, we give a determination of the mixing angle between strange and light quark states of less than 29° at 90% confidence level. We also discuss the use of a similar ratio to investigate the structure of other isospin singlet states. Scalar mesons in general, and the $f_0(980)$ in particular are not well understood. Their masses do not follow the expectation in the naïve quark model that the state containing two strange quarks is heavier than the state containing only one, in stark contrast to the vector mesons [1]. This has led to theories that the light J^{PC} equal to 0^{++} mesons may be combinations of di-quarks and anti-diquarks, e.g. $[qq][\bar{q}\bar{q}]$, called "tetraquarks" [2].

Recently there have been several studies of the $f_0(980)$ in heavy meson decays, some in the charm system [3]. Based on these data, the existence of the mode $\overline{B}_s^0 \to J/\psi f_0(980)$ was predicted [4], discovered by the LHCb collaboration [5], and confirmed [6]. The LHCb collaboration also found the decay $\overline{B}^0 \to J/\psi f_0(500)$, and set an upper limit on the decay $\overline{B}^0 \to J/\psi f_0(980)$ [7]. From now on the $f_0(500)$ meson will be designated as σ , and the $f_0(980)$ meson will be designed as f_0 . The $\overline{B}_s^0 \to J/\psi f_0(980)$ channel has also been used to measure CP violation [8], but Fleischer *et al.* have claimed that if the f_0 is a tetraquark state the measurement could be influenced by the presence of additional suppressed decay mechanisms [9]. Thus, a resolution of the problem of these states structure would be helpful in several ways.

When the σ and f_0 are considered as $q\bar{q}$ states there is the possibility of their being mixtures of light and strange quarks that is characterized by a 2×2 rotation matrix with a single parameter, the angle ϕ , so that their wave-functions are

$$|f_{0}\rangle = \cos \phi |s\bar{s}\rangle + \sin \phi |n\bar{n}\rangle |\sigma\rangle = -\sin \phi |s\bar{s}\rangle + \cos \phi |n\bar{n}\rangle,$$

where $|n\bar{n}\rangle \equiv \frac{1}{\sqrt{2}} (|u\bar{u}\rangle + |d\bar{d}\rangle).$ (1)

While there have been several attempts to measure the mixing angle ϕ , the model dependent results give a wide range of values. We describe here only a few examples. D^{\pm} and D_s^{\pm} decays into $f_0(980)\pi^{\pm}$ and $f_0(980)K^{\pm}$ give values of $31^{\circ} \pm 5^{\circ}$ or $42^{\circ} \pm 7^{\circ}$ [10]. $D_s^+ \to \pi^+\pi^+\pi^-$ transitions give a range $35^{\circ} < |\phi| < 55^{\circ}$ [11]. In light meson radiative decays two solutions are found either $4^{\circ} \pm 3^{\circ}$ or $136^{\circ} \pm 6^{\circ}$ [12]. Resonance decays from both $\phi \to \gamma \pi^0 \pi^0$ and $J/\psi \to \omega \pi \pi$ give a value of $\simeq 20^{\circ}$. On the basis of SU(3), a value of $19^{\circ} \pm 5^{\circ}$ is provided [13]. Finally, Ochs [14], averaging over several processes, finds $30 \pm 3^{\circ}$

When these states are viewed as $q\bar{q}q\bar{q}$ states the wave functions becomes

$$|f_0\rangle = \frac{1}{\sqrt{2}} \left([su][\bar{s}\bar{u}] + [sd][\bar{s}\bar{d}] \right), \quad |\sigma\rangle = [ud][\bar{u}\bar{d}]. \tag{2}$$

In this Letter we assume the tetraquark states are unmixed, for which there is some justification [2, 10, 15], with a mixing angle estimate of $< 5^{\circ}$ [9].

In general, the decay width for a B meson to decay into a J/ψ and light scalar state f can be expressed as [9, 16, 17]

$$\Gamma\left(B \to J/\psi f\right) = C |F_B^f(m_{J/\psi}^2)|^2 |V_{ci}|^2 \Phi \mathcal{Z}^2,\tag{3}$$

where C is a constant, F_B^f is form-factor evaluated at the four-momentum transfer q^2 equal to the mass of the J/ψ squared, and V_{ci} is the relevant CKM element. The phase

space factor $\Phi = (M_B E(x, y))^3$, where $x = M_{J/\psi}/M_B$, $y = (M_f/M_B)$ and $E(x, y) = \sqrt{[1 - (x + y)^2][1 - (x - y)^2]}$.¹ \mathcal{Z} represents the coupling amplitude that depends on the quark configuration after the *B* meson decay, and the quark content of the light meson in either the $q\bar{q}$ or tetraquark model. The values for \mathcal{Z} are listed in Table 1.

	$\overline{B}{}^0_s$		$\overline{B}{}^{0}$		
Model	f_0	σ	f_0	σ	
qar q	$\cos\phi$	$\sin \phi$	$\sin \phi / \sqrt{2}$	$\cos \phi / \sqrt{2}$	
tetraquark	$\sqrt{2}$	0	$1/\sqrt{2}$	1	

Table 1: Values of the coupling amplitude \mathcal{Z} .

The diagrams for decays of \overline{B}_s^0 mesons into the σ and f_0 are shown in Fig. 1 for both $q\bar{q}$ or tetraquark models. The coupling amplitudes for the f_0 , and σ in the $q\bar{q}$ model are $\cos \phi$ and $\sin \phi$, respectively, while in the tetraquark model the coupling is $\sqrt{2}$ for the f_0 and σ production is not allowed. Thus, a null test of the tetraquark model is evident: if the decay $\overline{B}_s^0 \to J/\psi \sigma$ is observed then the tetraquark model described here is ruled out.



Figure 1: Decays of the \overline{B}_s^0 meson to a J/ψ and (a) f_0 in the $q\bar{q}$ model, (b) σ in the $q\bar{q}$ model, (c) f_0 in the tetraquark model, and (d) σ in the tetraquark model. The factor next to the scalar resonance name indicates the coupling amplitude \mathcal{Z} .

The diagrams for decays of \overline{B}^0 mesons into the σ and f_0 are shown in Fig. 2 for both $q\bar{q}$ or tetraquark models [18].

There are measured branching fractions for some of these decays, that are summarized in Table 2.² The branching fractions into final states with an f_0 have been corrected by their decay rates into $\pi^+\pi^-$ using measurements from BES [19] from which we obtain

¹The phase space is calculated taking into account the mass dependent line shapes.

²In order to minimize systematic uncertainties we use only LHCb measurements even though other measurements of $\mathcal{B}(\overline{B}_s^0 \to J/\psi f_0)$ are available [1].



Figure 2: Decays of the \overline{B}^0 meson to a J/ψ and (a) f_0 in the $q\bar{q}$ model, (b) σ in the $q\bar{q}$ model, (c) f_0 in the tetraquark model, and (d) σ in the tetraquark model. The factor next to the scalar resonance name indicates the coupling amplitude \mathcal{Z} .

 $\frac{\mathcal{B}(f_0(980) \to K^+K^-)}{\mathcal{B}(f_0(980) \to \pi^+\pi^-)} = 0.25^{+0.17}_{-0.11} \ [3], \text{ and from BaBar of } \frac{\mathcal{B}(f_0(980) \to K^+K^-)}{\mathcal{B}(f_0(980) \to \pi^+\pi^-)} = 0.69 \pm 0.32 \ [20].$ Averaging the two measurements gives

$$\frac{\mathcal{B}(f_0(980) \to K^+K^-)}{\mathcal{B}(f_0(980) \to \pi^+\pi^-)} = 0.35^{+0.15}_{-0.14}.$$
(4)

To determine the $\pi^+\pi^-$ branching fraction it is assumed that the $\pi\pi$ and KK decays are dominant, and that the ratios of $\pi^0\pi^0$ to $\pi^+\pi^-$, and $K^0\overline{K}^0$ to K^+K^- are given by isospin conservation as 1/2 and 1, respectively, leading to [7]

$$\mathcal{B}(f_0(980) \to \pi^+\pi^-) = (46 \pm 6)\%.$$
 (5)

For σ decay we use $\mathcal{B}(\sigma \to \pi^+\pi^-) = \frac{2}{3}$, which again results from isospin conservation and the assumption that the only decays are into two pions. The uncertainties in these rates are not included in Table 2, but are introduced when comparisons between σ and f_0 are made.

Table 2: Experimental branching fractions from LHCb for $B \to J/\psi f$ meson final states. The uncertainties on $\mathcal{B}(f \to \pi^+\pi^-)$ are not included.

Final state	$\overline{B}{}^0_s$	$\overline{B}{}^{0}$
σ	—	$9.60^{+3.79}_{-1.70} \times 10^{-6}$
f_0	$3.40^{+0.63}_{-0.16} \times 10^{-4}$	$<1.7\times10^{-6}$

In this Letter we present information obtainable from ratios of the \overline{B}_s^0 and \overline{B}^0 decay rates into σ and f_0 mesons. Using the ratios allows cancellation of many of the experimental and theoretical uncertainties. The ratios we will consider are listed in Table 3 for both $q\bar{q}$ and tetraquark models.

Table 3: Ratios of decay widths. The rate ratio is multiplied by the value for \mathcal{Z}^2 in either the $q\bar{q}$ model, or the tetraquark model. The form-factors are notated as F_j^i , and the phase space factor Φ_j^i , where *i* indicates either σ or f_0 and *j* indicates either \overline{B}^0 or \overline{B}_s^0 .

Label	Mode ratio	Rate ratio	$\mathcal{Z}^2 \; q ar{q}$	\mathcal{Z}^2 tetraquark
$r^{0f_0}_{sf_0}$	$\frac{\Gamma(\bar{B}^0 \to J/\psi f_0)}{\Gamma(\bar{B}^0_s \to J/\psi f_0)} =$	$\frac{ F_{B0}^{f_0}(m_{J/\psi}^2) ^2}{ F_{B0}^{f_0}(m_{J/\psi}^2) ^2}\frac{ V_{cd} ^2\Phi_{B0}^{f_0}}{ V_{cs} ^2\Phi_{B0}^{f_0}}$	$\frac{1}{2}\tan^2\phi$	$\frac{1}{4}$
$r^{0f_0}_{s\sigma}$	$\frac{\Gamma(\bar{B}^0 \to J/\psi f_0)}{\Gamma(\bar{B}^0 \to J/\psi \sigma)} =$	$\frac{ F_{B0}^{f_0}(m_{J/\psi}^2) ^2}{ F_{B0}^{\sigma}(m_{J/\psi}^2) ^2} \frac{\Phi_{B0}^{f_0}}{\Phi_{B0}^{\sigma}}$	$\tan^2\phi$	$\frac{1}{2}$
$r^{s\sigma}_{sf_0}$	$\frac{\Gamma(\bar{B}^0_s \rightarrow J/\psi \sigma)}{\Gamma(\bar{B}^0_s \rightarrow J/\psi f_0)} =$	$\frac{ F^{\sigma}_{B_{s}^{0}}(m^{2}_{J/\psi}) ^{2}}{ F^{f_{0}}_{B_{s}^{0}}(m^{2}_{J/\psi}) ^{2}}\frac{\Phi^{\sigma}_{B_{s}^{0}}}{\Phi^{f_{0}}_{B_{s}^{0}}}$	$\tan^2\phi$	0
$r^{sf_0}_{0\sigma}$	$\frac{\Gamma(\bar{B}^0_s \rightarrow J/\psi f_0)}{\Gamma(\bar{B}^0 \rightarrow J/\psi \sigma)} =$	$\frac{ F^{f_0}_{B_s^0}(m_{J/\psi}^2) ^2}{ F^{\sigma}_{B^0}(m_{J/\psi}^2) ^2}\frac{ V_{cs} ^2\Phi^{f_0}_{B_s^0}}{ V_{cd} ^2\Phi^{\sigma}_{B^0}}$	2	2

To calculate the width ratios from the branching fractions when both $\overline{B}{}^0$ and $\overline{B}{}^0_s$ initial states are present, we use values of the lifetimes of 1.530 ± 0.007 ps and 1.622 ± 0.0023 ps [21], respectively. (Since the $\overline{B}{}^0_s$ modes are all negative *CP* eigenstates, we use the value provided for $\tau_{\text{long.}}$) Input on the form-factor ratios is needed to reach quantitative conclusions. For $r_{0\sigma}^{sf_0}$ both the $q\bar{q}$ and tetraquark models predict identical ratios, and this ratio is independent of ϕ . Using the data in Table 2 we find

$$\frac{|F_{B_s^0}^{f_0}(m_{J/\psi}^2)|}{|F_{B^0}^{\sigma}(m_{J/\psi}^2)|} = 0.99_{-0.04}^{+0.13}.$$
(6)

The ratio $r_{sf_0}^{s\sigma}$ was suggested as a way of measuring $\tan \phi$ by Li *et al.* [17]. The formfactor ratio calculated by Li *et al.* is very close to unity, $|F_{B_s}^{\sigma}(m_{J/\psi}^2)|^2/|F_{B_s}^{f_0}(m_{J/\psi}^2)|^2 = 1$. Assuming that the similar form-factor ratio $|F_{B^0}^{f_0}(m_{J/\psi}^2)/|F_{B^0}^{\sigma}(m_{J/\psi}^2)|$ is unity, LHCb used their data to set an upper limit on $\phi < 31^{\circ}$ at 90% confidence level [7].

Measurement of the branching fraction of $\overline{B}^0 \to J/\psi f_0$ was suggested by Fleischer *et al.* [9] as a way of investigating the tetraquark structure of the f_0 . In the $q\bar{q}$ model they use the form-factor ratio, $|F_{B^0}^{f_0}(m_{J/\psi}^2)|/|F_{B_s^0}^{f_0}(m_{J/\psi}^2)|$ that was computed by El-Bennich *et al.* [16] of 0.69 using dispersion relations.³ They find results that are mixing angle dependent. In the tetraquark model they use a unit form-factor ratio, and predict $\mathcal{B}(\overline{B}^0 \to J/\psi f_0, f_0 \to \pi^+\pi^-) \sim (1-3) \times 10^{-6}$. The measured upper limit from LHCb is 1.1×10^{-6} at 90% c.l., which is barely consistent. It is also interesting that using the upper limit on the measured ratio $r_{sf_0}^{0f_0}$ and a unit form-factor ratio, we find an upper limit $\phi < 29^{\circ}$ in

³In the covariant light front dynamics model El-Bennich *et al.* compute 0.58.

the $q\bar{q}$ model, slightly more restrictive than the LHCb determined limit of $\phi < 31^{\circ}$ using $r_{sf_0}^{s\sigma}$; this evaluation does not depend on any properties of the σ , nor on $\mathcal{B}(f_0 \to \pi^+\pi^-)$. The ratio $r_{sf_0}^{0f_0}$ was also suggested by Ochs [14] as a way of investigating the properties of the $f_0(980)$ and the $f_(1500)$; he also takes a unit form-factor ratio.

A further elucidation of the null prediction of $r_{sf_0}^{s\sigma}$ in the tetraquark model is in order. Besides the caveat that there could be a small amount of mixing, $< 5^{\circ}$, between the σ and f_0 tetraquark states, there also could be higher order diagrams that couple to the σ in the \overline{B}_s^0 decay. In terms of the topological diagrams illustrated in ref. [9], both the tree and leading penguin diagrams don't couple to the σ , as well as three other higher order diagrams. On the other hand three diagrams involving penguin annihilation and W exchange would couple to the σ . As these are expected to have a very small in rate compared to the tree diagram, we do not expect that they could induce a rate corresponding to a mixing angle of more than a few degrees.

In conclusion, we discuss the importance of branching fraction ratios in $(\overline{B}_s^0 \text{ or } \overline{B}^0) \rightarrow J/\psi(\sigma \text{ or } f_0)$ decays. These measurements can discern whether or not the σ and f_0 are $q\bar{q}$ or tetraquarks. To aid in these tests we have determined the form-factor ratio $\frac{|F_{B_0}^0(m_{J/\psi}^2)|}{|F_{B_0}^\sigma(m_{J/\psi}^2)|} = 0.99_{-0.04}^{+0.13}$, based on LHCb data. If the σ is a tetraquark state, we do not expect to see it \overline{B}_s^0 decays at a level of more than a percent of the $f_0(980)$ rate. For the σ and f_0 being $q\bar{q}$ states we provide a limit on the mixing angle of < 29° at 90% confidence level. Furthermore, we note that these tests could be extended to other systems. For example, if an isospin equal zero meson, $f_{I=0}$ was found in both $\overline{B}^0 \to J/\psi f_{I=0}$ and $\overline{B}_s^0 \to J/\psi f_{I=0}$ decays its mixing angle with another meson could be determined using a ratio similar to $r_{sf_0}^{0f_0}$ (See also ref. [14]). It is interesting that the square of the coupling amplitude would be 1/4 in the tetraquark model, and in the $q\bar{q}$ model its mixing angle with some other, possibly unknown, meson could be determined.

We gratefully acknowledge support from the National Science Foundation, and thank Jack Laiho, and Joe Schechter for useful discussions.

References

- Particle Data Group, J. Beringer et al., Review of Particle Physics, Phys. Rev. D86 (2012) 010001.
- [2] G. 't Hooft et al., A Theory of Scalar Mesons, Phys. Lett. B662 (2008) 424, arXiv:0801.2288; S. Weinberg, Tetraquark Mesons in Large N Quantum Chromo-dynamics, arXiv:1303.0342; A. H. Fariborz, R. Jora, and J. Schechter, Global aspects of the scalar meson puzzle, Phys. Rev. D79 (2009) 074014, arXiv:0902.2825; G. Mennessier, S. Narison, and X.-G. Wang, σ and f₀(980) substructures from γγ → ππ, J/ψ, φ radiative and D_s semi-leptonic decays, Phys. Lett. B696 (2011) 40, arXiv:1009.2773; R. L. Jaffe, Multi-Quark Hadrons I. The Phenomenology of Q²Q̄² Mesons, Phys. Rev. D15 (1977) 267; N. Achasov and A. Kiselev, Light scalars in semi-leptonic decays of heavy quarkonia, Phys. Rev. D86 (2012) 114010, arXiv:1206.5500; N. Achasov and A. Kiselev, The analytical ππ scattering amplitude and the light scalars, Phys. Rev. D83 (2011) 054008, arXiv:1011.4446.
- [3] CLEO Collaboration, K. Ecklund et al., Study of the semileptonic decay D⁺_s → f₀(980)e⁺ν and implications for B⁰_s → J/ψ f₀, Phys. Rev. **D80** (2009) 052009, arXiv:0907.3201; BaBar Collaboration, P. del Amo Sanchez et al., Dalitz plot analysis of D⁺_s → K⁺K⁻π⁺, Phys. Rev. **D83** (2011) 052001, arXiv:1011.4190.
- [4] S. Stone and L. Zhang, S-waves and the Measurement of CP Violating Phases in B_s Decays, Phys. Rev. D79 (2009) 074024, arXiv:0812.2832.
- [5] LHCb Collaboration, R. Aaij *et al.*, First observation of $B_s^0 \rightarrow J/\psi f_0(980)$ decays, Phys. Lett. **B698** (2011) 115, arXiv:1102.0206.
- [6] Belle Collaboration, J. Li et al., Observation of B⁰_s → J/ψf₀(980) and Evidence for B⁰_s → J/ψf₀(1370), Phys. Rev. Lett. **106** (2011) 121802, arXiv:1102.2759; CDF Collaboration, T. Aaltonen et al., Measurement of branching ratio and B⁰_s lifetime in the decay B⁰_s → J/ψf₀(980) at CDF, Phys. Rev. **D84** (2011) 052012, arXiv:1106.3682; D0 Collaboration, V. M. Abazov et al., Measurement of the relative branching ratio of B⁰_stoJ/ψf₀(980) → B⁰_s → J/ψφ, Phys. Rev. **D85** (2012) 011103, arXiv:1110.4272.
- [7] LHCb collaboration, R. Aaij *et al.*, Analysis of the resonant components in $\overline{B}^0 \rightarrow J/\psi \pi^+\pi^-$, R. Aaij et. **al**, (LHCb Collaboration), Phys. Rev. D87 (2013) 052001, **arXiv:1301.5347**.
- [8] LHCb collaboration, R. Aaij et al., Measurement of CP violation and the B_s^0 meson decay width difference with $B_s^0 \rightarrow J/\psi K^+ K^-$ and $B_s^0 \rightarrow J/\psi \pi^+ \pi^-$ decays, arXiv:1304.2600.
- [9] R. Fleischer, R. Knegjens, and G. Ricciardi, Anatomy of $B_{s,d}^0 \to J/\psi f_0(980)$, Eur. Phys. J. C71 (2011) 1832, arXiv:1109.1112.

- [10] D. Black, A. H. Fariborz, F. Sannino, and J. Schechter, *Putative light scalar nonet*, Phys. Rev. D59 (1999) 074026, arXiv:hep-ph/9808415.
- [11] V. Anisovich, L. Dakhno, and V. Nikonov, $D_s^+ \rightarrow \pi^+\pi^- decay$: The 1^3P_0 ss component in scalar isoscalar mesons, Phys. Atom. Nucl. **67** (2004) 1571, arXiv:hep-ph/0302137.
- [12] A. Anisovich, V. Anisovich, and V. Nikonov, Radiative decays of basic scalar, vector and tensor mesons and the determination of the P wave q anti-q multiplet, Eur. Phys. J. A12 (2001) 103, arXiv:hep-ph/0108186.
- [13] J. A. Oller, The Mixing angle of the lightest scalar nonet, Nucl. Phys. A727 (2003) 353, arXiv:hep-ph/0306031.
- [14] W. Ochs, The Status of Glueballs, J. Phys. G 40 (2013) 043001, arXiv:1301.5183.
- [15] L. Maiani, F. Piccinini, A. Polosa, and V. Riquer, A New look at scalar mesons, Phys. Rev. Lett. 93 (2004) 212002, arXiv:hep-ph/0407017.
- [16] B. El-Bennich, O. Leitner, J.-P. Dedonder, and B. Loiseau, *The Scalar Meson* $f_0(980)$ in *Heavy-Meson Decays*, Phys. Rev. **D79** (2009) 076004, arXiv:0810.5771.
- [17] J.-W. Li, D.-S. Du, and C.-D. Lu, Determination of $f_0 \sigma$ mixing angle through $B_s^0 \rightarrow J/\Psi f_0(980)(\sigma)$ decays, Eur. Phys. J. C72 (2012) 2229, arXiv:1212.5987.
- [18] W. Wang and C.-D. Lu, Distinguishing two kinds of scalar mesons from heavy meson decays, Phys. Rev. D82 (2010) 034016, arXiv:0910.0613.
- [19] BES collaboration, M. Ablikim et al., Evidence for f₀(980) f₀(980) production in χ_{c0} decays, Phys. Rev. D70 (2004) 092002, arXiv:hep-ex/0406079; BES collaboration, M. Ablikim et al., Partial wave analysis of χ_{c0} → π⁺π⁻K⁺K⁻, Phys. Rev. D72 (2005) 092002, arXiv:hep-ex/0508050.
- [20] BaBar collaboration, B. Aubert *et al.*, Dalitz plot analysis of the decay $B^{\pm} \rightarrow K^{\pm}K^{\pm}K^{\mp}$, Phys. Rev. **D74** (2006) 032003, arXiv:hep-ex/0605003.
- [21] Heavy Flavor Averaging Group, *Results for the PDG 2013 web update*, results and plots are available at: http://www.slac.stanford.edu/xorg/hfag/osc/PDG_2013.