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## Crystal field splitting and correlation effect on the electronic structure of $A_2 Ir O_3$

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The electronic structure of the honeycomb lattice iridates Na<sub>2</sub>IrO<sub>3</sub> and Li<sub>2</sub>IrO<sub>3</sub> has been investigated using resonant inelastic x-ray scattering (RIXS). Crystal-field split d-d excitations are resolved in the high-resolution RIXS spectra. In particular, the splitting due to non-cubic crystal fields, derived from the splitting of  $j_{\rm eff}$ =3/2 states, is much smaller than the typical spin-orbit energy scale in iridates, validating the applicability of  $j_{\rm eff}$  physics in  $A_2$ IrO<sub>3</sub>. We also find excitonic enhancement of the particle-hole excitation gap around 0.4 eV, indicating that the nearest-neighbor Coulomb interaction could be large. These findings suggest that both Na<sub>2</sub>IrO<sub>3</sub> and Li<sub>2</sub>IrO<sub>3</sub> can be described as spin-orbit Mott insulators, similar to the square lattice iridate Sr<sub>2</sub>IrO<sub>4</sub>.

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The intense interest in iridium oxides, or iridates, arises from a number of competing interactions of similar magnitude [1–9]. While the on-site Coulomb interaction is the dominant energy scale in 3d transition metal oxides, the spin-orbit coupling (SOC) is largely ignored. On the other hand, for 5d elements such as Ir, the SOC becomes significant, and in fact plays a dominant role. A good example is  $Sr_2IrO_4$ , whose electronic states are well described by  $j_{\text{eff}}=1/2$  states arising from the spin-orbit split  $t_{2g}$  levels [2, 3, 8].

One of the most intensely scrutinized families of iridates is the honeycomb lattice family  $A_2 \text{IrO}_3$  (A=Na,Li) [5, 7, 10–14]. Originally thought of as Mott [4] or topological insulator [5], these materials are now believed to be Mott insulators [10, 11]. A recent calculation though suggests that uniaxial strain might still drive the system to topological insulating behavior [15]. Furthermore, these materials could be described with the Kitaev-Heisenberg model [7, 11, 12], in which bond-dependent Kitaev interaction are realized and support various types of topological phases. The applicability of such intriguing theoretical possibilities to real system crucially depends on the  $j_{\text{eff}}$  physics arising from strong SOC. However, the experimental situation seems to be far from clear. In particular, structural refinements find a sizable trigonal distortion of the IrO<sub>6</sub> octahedra [16, 17], which will produce crystal field splittings within the  $t_{2q}$  manifold. If the splitting is comparable to the SOC, the  $j_{\text{eff}}=1/2$  states will mix with  $j_{\text{eff}}=3/2$  states [18] and the relevant microscopic model becomes quite different from the ideal  $j_{\text{eff}}$ physics [14, 19], preventing the Kitaev-Heisenberg model from being realized [7, 11, 13]. Recent theoretical studies

have even suggested that the ground state has a large contribution from the  $j_{\text{eff}}=3/2$  state [20].

Therefore, it is of great importance to elucidate the underlying electronic structure of Na<sub>2</sub>IrO<sub>3</sub> experimentally. In particular, the spectroscopic investigation of excitations between spin-orbit split  $j_{\rm eff}$  states can provide us with direct information regarding the size of the crystal field splitting with respect to the typical SOC energy scale in iridates (0.4-0.5 eV) [21, 22]. In the case of Sr<sub>2</sub>IrO<sub>4</sub>, such excitations between  $j_{\rm eff}$ =3/2 to  $j_{\rm eff}$ =1/2 were observed around 0.6-0.8 eV in the resonant inelastic x-ray scattering (RIXS) data [8], which is accounted for in the quantum chemical calculation by Katukuri et al. [23]. The splitting within these "spin-orbit" excitations arises due to non-zero tetragonal crystal fields, and is much smaller ( $\sim$  0.1 eV) than the SOC, justifying the  $j_{\rm eff}$  description of Sr<sub>2</sub>IrO<sub>4</sub>.

In this Letter, we present a comprehensive picture of the low energy electronic structure of  $Na_2IrO_3$  and  $Li_2IrO_3$ , based on Ir  $L_3$ -edge RIXS experiments. Our high-resolution RIXS measurements allow us to resolve the crystal field splitting of the  $j_{\rm eff}=3/2$  states due to the trigonal distortion, which is determined to be about 110 meV in both compounds. This energy scale agrees very well with quantum chemical calculations, and is much smaller than the typical value for SOC, validating the  $j_{\rm eff}$  picture in these compounds. We have also studied momentum dependence of the insulating gap; the observed flat dispersion of the insulating gap is consistent with what is expected from a significant Coulomb interaction in both compounds. Taken together, we argue that just as  $Sr_2IrO_4$ , the honeycomb  $A_2IrO_3$  iridates can

be described as spin-orbit Mott insulators [2, 15, 19, 24].

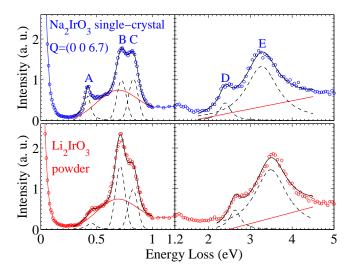


FIG. 1: (Color online) Top: Wide energy range RIXS spectrum for a single-crystal sample of Na<sub>2</sub>IrO<sub>3</sub> at  $\mathbf{Q} = (0~0~6.7)$  obtained with  $E_i = 11.217$  keV. Note the different scale used for left and right panel. Bottom: RIXS spectrum for Li<sub>2</sub>IrO<sub>3</sub> powder sample at  $|\mathbf{Q}| \approx 8~\text{Å}^{-1}$ , obtained with the same  $E_i$ . All spectra were measured at room temperature. The black dashed curves are the result of a fit (see text) and the red solid lines represent the background.

The RIXS experiment was carried out at the Advanced Photon Source using the 30ID MERIX and 9ID RIXS spectrometer. A spherical (1 m radius) diced Si(844) analyzer and Si(844) secondary monochromator were used to obtain overall energy resolution (FWHM) of  $\sim 35$  meV [25]. To minimize the elastic background, most of the measurements were carried out in a horizontal scattering geometry near  $\mathbf{Q}=(0~0~6.7)$ , for which the scattering angle  $2\theta$  was close to 90°. We use the C2/m notation for the lattice [16, 17]. A single crystal of Na<sub>2</sub>IrO<sub>3</sub> and a polycrystalline samples of Li<sub>2</sub>IrO<sub>3</sub>were grown by the solid state synthesis method, previously described in detail [10, 11]. The Na<sub>2</sub>IrO<sub>3</sub> crystal was plate-like with a flat shiny surface, the surface normal was in the (001) direction.

The RIXS process at the  $L_3$ -edge of Ir (or any other d electron system) is a second order process consisting of two dipole transitions  $(2p \to 5d \text{ followed by } 5d \to 2p)$ . Therefore, it is especially valuable for detecting excitations between the d-levels and has been extensively utilized in the study of 3d transition metal compounds [26–32]. Recent instrumental advances have made it possible to measure collective magnetic excitations [8, 33]. In  $A_2$ IrO<sub>3</sub>, Ir<sup>4+</sup> ions are in the  $5d^5$  configuration in a slightly distorted octahedral environment of oxygen ions, with the edge-sharing IrO<sub>6</sub> octahedra forming a honeycomb net. Due to the octahedral crystal field, there exists a fairly large splitting (10Dq) between the  $t_{2q}$  and  $e_q$ 

TABLE I: RIXS and MRCI+SOC excitation energies (C2/m) structure for 213 iridates (eV).

	Na213	Na213	Li213	Li213
	RIXS	MRCI	RIXS	MRCI
Peak A	0.42(1)	_	0.45(2)	-
Peak B	0.72(2)	0.82	0.72(2)	0.80
Peak C	0.83(2)	0.89	0.83(2)	0.97
Peak D	2.4(1)	2.8 – 3.4	2.6(1)	3.1 – 3.7
Peak E	3.3(1)	3.8 – 4.1	3.5(1)	4.1 – 5.0

states. Since the 5d orbitals are spatially more extended than the 3d orbitals, the 10Dq value is expected to be much larger. Indeed, in our RIXS investigations of various iridium compounds, well separated  $t_{2g}$  and  $e_g$  states have been observed, with the 10Dq value typically about 3 eV [34].

In Fig. 1, a representative high-resolution RIXS spectrum of Na<sub>2</sub>IrO<sub>3</sub> is plotted on a wide energy scale. This scan was obtained at room temperature and plotted as a function of energy loss ( $\hbar\omega = E_i - E_f$ ). The incident energy,  $E_i = 11.217 \text{ keV}$ , was chosen to maximize the resonant enhancement of the spectral features of interest below 1 eV. A broad and strong feature is observed at 2-4 eV and other sharper features are observed below 1 eV, corresponding to d-d transitions from occupied  $t_{2q}$  states into the empty  $e_q$  and  $t_{2q}$  levels, respectively. Also plotted in the figure is the room temperature data of polycrystalline Li<sub>2</sub>IrO<sub>3</sub>. Lack of significant momentum dependence of these d-d excitations (shown later in Fig. 3) allows one to directly compare the peak positions between the single crystal and powder samples. The spectra were fit to 5 peaks (labeled A-E), as shown by the black dashed lines. The low energy excitations can be fit to three peaks, two Gaussians (B and C) of the same width and one Lorentzian peak (A) on top of a broad background (Gaussian). Two Lorentzian functions with sloping background were used to fit the higher energy excitations (D and E). The resulting peak positions are listed in Table I.

To clarify the nature of the excitations revealed by RIXS, we have carried out multiconfiguration self-consistent-field and multireference configuration-interaction (MRCI) calculations [35] on clusters consisting of one central IrO<sub>6</sub> octahedron, all adjacent Na or Li ions, and the three nearest-neighbor (NN) IrO<sub>6</sub> octahedra (see Ref. 23 and Supplemental Material for details). Local d-d transitions are computed only for the central IrO<sub>6</sub> octahedron while the NN octahedra are explicitly included in the cluster for providing an accurate description of the nearby charge distribution. Two different lattice configurations are considered, i.e., the C2/c structure [10, 37] and also the C2/m arrangement proposed more recently [16, 17, 36].

Results of spin-orbit MRCI (MRCI+SOC) calculations using the C2/m configuration [16] are listed for Na<sub>2</sub>IrO<sub>3</sub> in the third column of Table I. The MRCI+SOC data fit the experiment reasonably well, with peaks B and C corresponding to  $j_{\text{eff}}=3/2$  to  $j_{\text{eff}}=1/2$  electronic transitions. Above 2.5 eV, the MRCI+SOC results indicate multiple  $t_{2q}$  to  $e_q$  excitations displaying a two-peak structure reminiscent of the D and E features in the RIXS spectra. Although direct comparison is difficult due to the broad spectral widths of D and E arising from multiple excitations, MRCI+SOC seems to overestimate somewhat the relative energies of those latter features. Interestingly, for the alternative C2/c structure of Na<sub>2</sub>IrO<sub>3</sub> [10], the splitting between the two doublets originating from the  $j_{\text{eff}}=3/2$  quartet in an ideal octahedral environment is much larger and the position of the C peak is overestimated by 0.25 eV in the MRCI+SOC treatment. Since the deviations from the experimental data are in this case larger, the MRCI+SOC results for C2/c symmetry are not listed in Table I. The  $t_{2q}$  splittings in calculations with no SOC are in fact as large as 0.6 eV for the C2/cstructure of Na<sub>2</sub>IrO<sub>3</sub>, which gives rise to a highly uneven admixture of  $t_{2g}$  components in the spin-orbit calculations. In contrast, for the C2/m configuration, the  $t_{2q}$ splittings are about 0.1 eV and the three different  $t_{2q}$ hole configurations contribute with similar weight to the spin-orbit ground-state wave function (see Table II).

For Li<sub>2</sub>IrO<sub>3</sub>, the calculations correctly reproduce the shift to higher energies of the  $t_{2g}$  to  $e_g$  transitions relative to those in  $Na_2IrO_3$ . The discrepancy between the experimental values and the MRCI+SOC results (e.g., peak C) could be caused by the uncertainty in the structural model used for this calculation (C2/m from Ref. [36]). Since local structural disorder is not easily captured in the regular diffraction data, local structure probes such as pair-distribution function (PDF) measurements can sometimes be useful for clarifying the structural details. We have carried out X-ray PDF studies on Li<sub>2</sub>IrO<sub>3</sub> and Na<sub>2</sub>IrO<sub>3</sub> powder samples. Details of these measurements and the comparison of the two structures are reported in the Supplemental Material. Except for the overall lattice contraction, the Li<sub>2</sub>IrO<sub>3</sub> PDF seems to be well described by the C2/m symmetry, eliminating the local structural disorder as a possible explanation. Most likely cause of the structural uncertainty is the oxygen position, since x-ray structural probes are not particularly sensitive to light elements like oxygen [36, 37]. We note that the latest refinements using both powder neutron and single crystal x-ray data on Na<sub>2</sub>IrO<sub>3</sub> do show important differences compared to earlier x-ray powder diffraction data and the MRCI+SOC results are very different for the two structures. Better structural refinements using neutron diffraction would reduce the oxygen position uncertainty in Li<sub>2</sub>IrO<sub>3</sub> and could improve the agreement between our MRCI+SOC calculation and the experiment.

One of our main findings is that the splitting of the

TABLE II: Percentage contributions of the different Ir  $5d^5$  configurations to the lowest on-site d-d excited states in Na<sub>2</sub>IrO<sub>3</sub>, as obtained from MRCI+SOC calculations.

Energy (eV)	0	0.82	0.89
$d_{xy}^2 d_{yz}^2 d_{zx}^1$	38.7	24.3	32.2
$d_{xy}^2 d_{yz}^1 d_{zx}^2$	34.7	60.3	24.7
$d_{xy}^1 d_{yz}^2 d_{zx}^2$	26.6	15.4	43.1

strong RIXS peak located at 0.7-0.8 eV is due to the trigonal distortion which is well corroborated with our MRCI+SOC calculations. The fact that this splitting (110 meV) is much smaller than a SOC of 0.4-0.5 eV [21, 22] strongly supports that these excitations are transitions from crystal-field-split  $j_{\text{eff}}=3/2$  levels to the  $j_{\text{eff}}=1/2$  state (labeled spin-orbit exciton in Ref. [8]). Given that the optical gap in this material is about 350 meV [24] and that there is no such excitation in the MRCI+SOC calculations which only look at on-site dd excitations, it is reasonable to associate feature A at low energy as arising from the excitation of a particle and hole pair across the charge gap. Additional periodic density functional theory (DFT) calculations shows that a moderate size U and SOC can indeed open a (Mott) gap of 300-400 meV, in accordance with the experimental observation (see Supplemental Material).

The nature of the charge excitation gap can be further revealed by its momentum dependence. In Fig. 2, we plot the momentum dependence of the low energy peaks (A-C) in Na<sub>2</sub>IrO<sub>3</sub>. In the honeycomb plane, the magnetic ordering doubles the unit cell [38], and correspondingly the first Brillouin zone (BZ) becomes smaller. Two different BZ schemes are illustrated in the inset of Fig. 2 (a) to aid the comparison. We will use the rectangular BZ notation. Note that the two high symmetry directions of interest, the  $\mathbf{q}=(h\ 0)$  and  $\mathbf{q}=(0\ k)$  in rectangular notation, correspond to the  $\Gamma - K$  and  $\Gamma - M$  directions in the honeycomb plane, respectively. One can see that the overall momentum dependence of the excitation spectrum is very small, except for peak A. To investigate the behavior of peak A in detail, the low energy portion of the spectra was fit to a Lorentzian peak. Since the peak seems to disappear at  $q=(1\ 0)$ , we have used the spectrum at this q as an empirical background. The fitting results for peak positions, widths, and intensities are shown in Fig. 2(b)-(c). The width and peak position remains almost unchanged ( $\approx 10 \text{ meV dispersion}$ ), but the intensity is strongly peaked around the BZ center. This can be clearly seen in the pseudocolor plot of the spectra shown in Fig. 2(d), in which a strong peak around  $\mathbf{q}=(0)$ 0) and 0.42 eV is contrasted with the q-independent features B+C. In addition, one can see that the spectral weight changes abruptly around 0.4 eV, confirming that this is the particle-hole continuum boundary. Based on

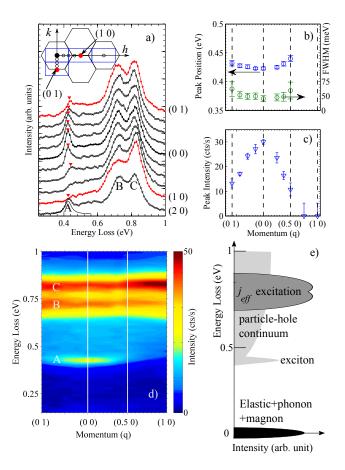


FIG. 2: (Color online) (a) Momentum dependence of the low energy RIXS spectra of  $Na_2IrO_3$  obtained at T=9 K. The inset shows a schematic diagram of the  $(h\ k\ 0)$  reciprocal space plane. The Brillouin zones (BZ) corresponding to the monoclinic unit cell are blue rectangles. For comparison, we also plot the BZ of the honeycomb net in black. The circles are the points where RIXS spectra are taken. The low energy peaks denoted with red triangles are fit to a Lorentzian, and the momentum dependence of (b) the peak position and width, and (c) the peak intensity are shown. (d) Same data are plotted in false color scale. (e) Schematics of electronic excitations in  $A_2IrO_3$  determined from our RIXS measurements.

our RIXS results, the electronic excitations in  $A_2 \text{IrO}_3$  can be summarized as shown in Fig. 2(e).

It is clear from this observation that the insulating gap is direct (minimum gap at  $\Gamma$ ). The relatively flat dispersion observed in our data is also consistent with the DFT calculation which suggests that the bandwidth is about 50 % (40 %) for the GGA+SOC (GGA+SOC+U) result compared to the GGA-only case, leading to an almost dispersionless charge gap. Both the sharpness in energy and the momentum dependence of peak A is quite reminiscent of the excitonic behavior of the BZ center particle-hole excitation across the charge-transfer gap in the insulating cuprate La<sub>2</sub>CuO<sub>4</sub> [39]. This suggests that an extra nearest-neighbor Coulomb interaction V (in addition to the on-site interaction U) might be important

for modelling this material [40, 41]. Sizable V could promote the tendency towards exciton binding and also further narrow the bandwidths. The smaller intensity of the charge gap feature in  $\text{Li}_2\text{IrO}_3$  compared to  $\text{Na}_2\text{IrO}_3$  could be due to the fact that the  $\text{Li}_2\text{IrO}_3$  data are powder averaged. However, one cannot rule out the possibility of weaker V in  $\text{Li}_2\text{IrO}_3$  as compared to  $\text{Na}_2\text{IrO}_3$ .

Another interesting aspect of our data is that the dispersion of the gap appears to follow the underlying honeycomb lattice rather than the crystallographic/magnetic unit cell. This is clearly observed by the spectrum obtained at  $\mathbf{q}=(2\ 0)$ . While  $(2\ 0)$  is the next BZ center along the  $\Gamma-K$  (in honeycomb notation),  $(1\ 0)$  is on the zone boundary; peak A disappears at  $(1\ 0)$  but recovers its intensity at the  $\mathbf{q}=(2\ 0)$  position. Additional momentum dependence data, reported in the Supplemental Material, shows the lack of momentum dependence along the L-direction (perpendicular to the honeycomb plane). Therefore, the electronic structure of Na<sub>2</sub>IrO<sub>3</sub> seems to be quite well described as that of a 2D honeycomb lattice.

It is worth comparing the observed low energy RIXS spectrum with that of Sr<sub>2</sub>IrO<sub>4</sub>. In Sr<sub>2</sub>IrO<sub>4</sub>, a low energy magnon was observed below 200 meV, while highly dispersive excitations were observed between 0.4 eV and 0.8 eV. This latter band of excitations is composed of particle-hole excitation across the Mott gap and spinorbit excitations from  $j_{\text{eff}}=3/2$  states to the  $j_{\text{eff}}=1/2$ states. Because of the smaller single-particle band width in  $A_2$ IrO<sub>3</sub> (see DFT calculations in Ref. 15), the " $j_{\text{eff}}$ excitation" in Na<sub>2</sub>IrO<sub>3</sub> is almost dispersionless, unlike the highly dispersive counterpart in Sr<sub>2</sub>IrO<sub>4</sub>. Perhaps an even more significant difference is the well separated energy scale of the  $j_{\text{eff}}$  excitation and the particle-hole continuum in Na<sub>2</sub>IrO<sub>3</sub>. These two energy scales are very similar in Sr<sub>2</sub>IrO<sub>4</sub>, but the large separation in Na<sub>2</sub>IrO<sub>3</sub> allows one to investigate these two types of excitations separately.

To summarize, we have carried out a resonant inelastic x-ray scattering investigations of electronic excitations in Na<sub>2</sub>IrO<sub>3</sub> and Li<sub>2</sub>IrO<sub>3</sub>. We observe three well-defined features below 1 eV and a broad two peak feature at 2-5 eV. By comparing our observation with quantum chemical and density functional theory calculations, we associate these features with d-d transitions. Specifically, the high energy excitations are from  $t_{2g}$  to  $e_g$  excitations, while the low energy excitations around 0.7-0.8 eV are excitations from  $j_{\text{eff}}=3/2$  to  $j_{\text{eff}}=1/2$  states. The splitting of the latter feature arising from the trigonal crystal field is about 110 meV, much smaller than the spin-orbit coupling energy scale of Ir compounds, which validates the applicability of  $j_{\text{eff}}$  physics in  $A_2 \text{IrO}_3$ . In addition, we observe a lower energy excitation around 0.4 eV, which shows very little momentum dependence and is associated with the particle-hole excitation across the Mott gap; the "excitonic" behavior of this peak suggests the nearest-neighbor Coulomb interaction V is sizable. We

conclude that the electronic structures of both  $\rm Na_2IrO_3$  and  $\rm Li_2IrO_3$  are similar and these systems can be described as spin-orbit Mott insulators.

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