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Pasquale Marra, Krzysztof Wohlfeld, and Jeroen van den Brink Phys. Rev. Lett. **109**, 117401 — Published 14 September 2012 DOI: 10.1103/PhysRevLett.109.117401

## Unraveling Orbital Correlations via Magnetic Resonant Inelastic X-ray Scattering

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(Dated: July 19, 2012)

Although orbital degrees of freedom are a factor of fundamental importance in strongly correlated transition metal compounds, orbital correlations and dynamics remain very difficult to access, in particular by neutron scattering. Via a direct calculation of scattering amplitudes we show that instead *magnetic* resonant inelastic x-ray scattering (RIXS) does reveal *orbital* correlations. In contrast to neutron scattering, the intensity of the magnetic excitations in RIXS depends very sensitively on the symmetry of the orbitals that spins occupy and on photon polarizations. We show in detail how this effect allows magnetic RIXS to distinguish between alternating orbital ordered and ferro-orbital (or orbital liquid) states.

PACS numbers: 75.25.Dk, 75.30.Ds, 78.70.Ck, 74.70.Xa

Introduction Ever since the seminal work of Kugel and Khomskii [1] in the 1980's it has been known that orbital degrees of freedom can play a crucial role in correlated transition metal compounds. Orbital ordering and orbital-orbital interactions are not only closely tied to magnetic ordering and magnetic interactions, but orbital degrees of freedom have also been proposed to be of direct relevance to spectacular phenomena such as colossal magnetoresistance in the manganites or superconductivity in the iron pnictides [2–4]. Yet, the precise nature of correlated orbital states, being either of ordered or liquid type, and their existence in different materials is intensely debated, which for a large part is due to the fact that orbital correlations turn out to be very difficult to detect experimentally. In fact, such experimental access would be of great help in unraveling the puzzling properties of many systems with orbital degrees of freedom, for instance the above mentioned iron-pnictide materials, where the type of the orbital ordering or its lack is heavily debated [5–7] or titanium and vanadium oxides where different theoretical scenarios - a rather exotic orbital liquid phase [8, 9], or a classical alternating orbital-ordered state [10, 11] – have been proposed.

The experimental verification of orbital properties in correlated materials by neutron scattering is difficult because neutrons are almost not sensitive to the orbital symmetries of the ground state, in particular in orbital systems the angular momentum is quenched by the crystal field [12]. Traditional x-ray diffraction, instead, is dominated by scattering from the atomic core electrons while the resonant x-ray diffraction [13, 14], particularly in the soft x-ray regime, which is the modern method of choice to detect orbital ordering, suffers from a very limited scattering phase space making Bragg scattering only possible for special orbital superstructures that have large spatial periodicities [15]. There being few orbitalordering related Bragg spots - if at all - leaves considerable room for controversies on the interpretation of experimental data [16–18].

Recently resonant inelastic x-ray scattering

(RIXS) [19–22] has been proven successful in measuring spin excitations in various cuprates [23–28], nickelates [29], and even iron-based compounds [30]. Here we show in a general setting how the polarization dependent intensity of magnetic RIXS directly provides an insight into the orbital correlations in the ground state of correlated materials. In particular, we verify that RIXS discriminates between different orbital states, e.g., the alternating orbital (AO) order against the ferro-orbital (FO) order or the orbital liquid (OL) state. This method is applicable to any orbital-active material that has distinct dispersive spectral features in its spin structure factor  $S(\mathbf{k}, \omega)$ , for instance due to the presence of magnons arising from long-range magnetic ordering.

*RIXS cross section* RIXS is particularly apt to probe the properties of strongly correlated electrons, for instance in transition metal (TM) oxides [22]. With an incoming x-ray of energy  $\omega_{in}$  and momentum  $\mathbf{k}_{in}$  an electron is resonantly excited from a core level into the valence shell. At the TM  $L_{2,3}$ -edges this involves a  $2p \rightarrow 3d$ dipole allowed transition. In this intermediate state, the spin of the 2p core-hole is not conserved, as the very large spin-orbit interactions strongly couples the spin and orbital momentum of the core-hole. A spin-flip in the core allows the subsequent recombination of the core-hole with a 3*d*-electron that has a spin opposite to the electron that was originally excited into the 3d-shell. The energy  $\omega_{\rm out}$  and momentum  $\mathbf{k}_{\rm out}$  of the outgoing x-ray resulting from this recombination are then related to a spin excitation with energy  $\omega = \omega_{out} - \omega_{in}$  and momentum  $\mathbf{k} = \mathbf{k}_{\text{out}} - \mathbf{k}_{\text{in}}.$ 

The magnetic RIXS cross section at a TM  $L_{2,3}$  edge is in general [21, 22]

$$I_{\mathbf{e}}(\mathbf{k},\omega) = \lim_{\delta \to 0^+} \operatorname{Im} \langle 0 | \hat{O}_{\mathbf{k},\mathbf{e}}^{\dagger} \frac{1}{\omega + E_0 - H + \imath \delta} \hat{O}_{\mathbf{k},\mathbf{e}} | 0 \rangle, (1)$$

where  $\mathbf{e} = \mathbf{e}^{\text{in}} \cdot (\mathbf{e}^{\text{out}})^{\dagger}$  is the tensor that describes the incoming and outgoing photon polarization, and H is the Hamiltonian describing 3d valence electrons with ground state  $|0\rangle$  and energy  $E_0$ . The Fourier transformed tran-



FIG. 1. (color online) The schematic representation of the RIXS operator  $\hat{O}_{\mathbf{j},\mathbf{e}}$  on a single site at the Cu<sup>2+</sup>  $L_{2,3}$  edge. To calculate the matrix elements of the operator between the same initial and final 3*d* orbital state, one needs to sum over all possible paths connecting them via a three step process, multiplying at every step as indicated in the figure: (i) the incoming polarization  $e_{\alpha}$ , (ii)  $-ic_1$  or the spin operator  $\pm c_2 \hat{S}_{\gamma}$  [positive (negative) sign for steps along (opposite to) the direction of the arrows], and (iii) the complex conjugate of the outgoing polarization  $e_{\beta}^*$  (constants  $c_{1,2}$  depend on the edge).

sition operator  $\hat{O}_{\mathbf{k},\mathbf{e}} = 1/\sqrt{N}\sum_{\mathbf{j}} \hat{O}_{\mathbf{j},\mathbf{e}} \exp(i\mathbf{k}\cdot\mathbf{j})$  can be evaluated from the general expression for  $\hat{O}_{\mathbf{j},\mathbf{e}}$  following the symmetry arguments in Ref. 21 [cf. Eqs. (8)-(10)]

$$\hat{O}_{\mathbf{j},\mathbf{e}} = \sum_{d} \hat{n}_{\mathbf{j}d} \ \hat{\mathbf{S}}_{\mathbf{j}} \cdot \mathbf{W}_{\mathbf{e}}(d_{\mathbf{j}}), \tag{2}$$

where  $\hat{\mathbf{S}}_{\mathbf{j}}$  are spin operators,  $\hat{n}_{\mathbf{j}d}$  are number operators for electrons in the 3*d* orbitals on site  $\mathbf{j}$ , and where the vector amplitudes  $\mathbf{W}_{\mathbf{e}}(d_{\mathbf{j}})$  depend on the orbital symmetry  $d_{\mathbf{j}}$  of the ground state at site  $\mathbf{j}$ . Here each component of the vector  $\mathbf{W}_{\mathbf{e}}(d_{\mathbf{j}})$  is a priori different and thus each spin operator is multiplied by a distinct amplitude, which can be related to the fundamental x-ray absorption cross sectionand therefore *implicitly* depends on the orbital occupancy  $d_{\mathbf{j}}$  at site  $\mathbf{j}$  [21, 31, 32].

Orbital dependence of RIXS operator As stated above the orbital dependence of RIXS amplitudes  $\mathbf{W}_{\mathbf{e}}(d_{\mathbf{j}})$  is generic to any orbital system. Nevertheless, to be explicit, we show how this dependence arises in the simple case of a  $\mathrm{Cu}^{2+}$  ion, i.e., with one hole in the Cu 3d orbital. The amplitudes  $\mathbf{W}_{\mathbf{e}}(d_{\mathbf{j}})$  can be evaluated using Eq. (2) as  $W_{\mathbf{e}}^{\alpha}(d_{\mathbf{j}}) \propto \langle d_{\mathbf{j}}\sigma_{\alpha} | \hat{O}_{\mathbf{j},\mathbf{e}} | d_{\mathbf{j}}\sigma_{\alpha} \rangle$  where  $|d_{\mathbf{j}}\sigma_{\alpha} \rangle$  is the state with a hole in the 3d orbital with spin  $\sigma$  along the  $\alpha$  axis. Since one needs here only to calculate the matrix elements of the operator  $\hat{O}_{\mathbf{j},\mathbf{e}}$  on single site states, this can be done just by applying the dipole and fast collision approximations to the Kramers-Heisenberg formula for RIXS [33, 34], so that  $\hat{O}_{\mathbf{j},\mathbf{e}} = \sum_{\alpha\beta} e_{\alpha\beta} \hat{D}_{\beta,\mathbf{j}}^{\dagger} \hat{G}_{\mathbf{j}} \hat{D}_{\alpha,\mathbf{j}}$ , where  $D_{\alpha \mathbf{j}}$  are the components of the dipole operator [22], and  $\hat{G}_{\mathbf{j}} \propto -ic_1+c_2 \,\hat{\mathbf{S}}_{\mathbf{j}} \cdot \hat{\mathbf{\Pi}}_{\mathbf{j}}$  is the intermediate state propagator  $(c_{1,2} \text{ are constants depending on the resonant edge, see Fig. 1). The intermediate state transitions are expressed here by the operator <math>\hat{\Pi}_{\gamma \mathbf{j}} = \sum_{\alpha \beta} \epsilon_{\alpha \beta \gamma} p^{\dagger}_{\alpha,\mathbf{j}} p_{\beta,\mathbf{j}}$  where  $\epsilon_{\alpha \beta \gamma}$  is the Levi-Civita symbol and  $p^{\dagger}_{\alpha,\mathbf{j}}$  the creation operator of the 2p core hole in the  $p_{\alpha}$  orbital state. This compact expression for the core hole propagator leads to the schematic representation of the operator  $\hat{O}_{\mathbf{j},\mathbf{e}}$  on a single site in Fig. 1.

While the intermediate state propagator  $\hat{G}_{\mathbf{j}}$  brings the spin dependence due to the spin-orbit coupling in the 2p core hole states, the dipole operators  $\hat{D}_{\alpha \mathbf{j}}$  act in a different way depending on the orbital occupancy on site  $\mathbf{j}$ , so that the amplitude  $\mathbf{W}_{\mathbf{e}}(d_{\mathbf{j}})$  strongly depends on the orbital symmetry of the ground state at each site. Since this dependence is merely due to the properties of the dipole transitions and to the spin-orbit coupling, it is indeed generic to any TM  $L_{2,3}$  edge.

Having analyzed the inherent dependence of the scattering amplitudes  $\mathbf{W}_{\mathbf{e}}(d_{\mathbf{j}})$  on the *single site* orbital occupancy, we now investigate how the operator  $\hat{O}_{\mathbf{j},\mathbf{e}}$  in Eq. (2) depends on the orbital ground state of the *bulk*. Hereafter, we consider three different orbital ground states in a 2D bipartite lattice (later we discuss a more general case): ferro-orbital (FO) order with the same *a* orbital occupied on each site, alternating orbital (AO) order with *a* (*b*) orbitals occupied on sublattice A (B), and orbital liquid (OL) ground state with the occupancies of *a* and *b* orbitals fluctuating similarly to the up and down spins in the spin liquid state. Thus we obtain

$$\hat{O}_{\mathbf{j},\mathbf{e}} = \left[ \left( \frac{1}{2} + \hat{T}_{\mathbf{j}}^z \right) \mathbf{W}_{\mathbf{e}}(a) + \left( \frac{1}{2} - \hat{T}_{\mathbf{j}}^z \right) \mathbf{W}_{\mathbf{e}}(b) \right] \cdot \hat{\mathbf{S}}_{\mathbf{j}}, \quad (3)$$

where the orbital pseudospin operator is  $\hat{T}_{\mathbf{j}}^{z} = (\hat{n}_{\mathbf{j}a} - \hat{n}_{\mathbf{j}b})/2$ . Since  $T_{\mathbf{j}}^{z} = 1/2$  for all sites  $\mathbf{j}$  in the FO state while  $T_{\mathbf{j}}^{z} = \pm 1/2$  for every other site in the AO state, the operator  $\hat{O}_{\mathbf{j},\mathbf{e}}$  acts *differently* on different orbital ground states. Below we show how this feature affects spectra, by calculating the cross section using Eq. (1) and Eq. (3) for six ground states with different orbital and magnetic configurations.

FM systems with AO order We consider a 2D FM system with AO order (i.e.,  $|0\rangle = |\text{FM} \otimes \text{AO}\rangle$ ) with the spin interactions described by the *effective* Heisenberg Hamiltonian  $H = J \sum_{\langle \mathbf{i}, \mathbf{j} \rangle} \hat{\mathbf{S}}_{\mathbf{i}} \cdot \hat{\mathbf{S}}_{\mathbf{j}}$  with negative exchange constant J < 0. This spin-only Hamiltonian follows from a Kugel-Khomskii spin-orbital model when the interactions between orbital degrees of freedom generating the AO ground state are integrated out (see Ref. 35).

The spin wave (single magnon) excitation of such an ordered FM follows from the Holstein-Primakoff transformation for spins  $\hat{S}_{\mathbf{j}}^{+} = \alpha_{\mathbf{j}}, \ \hat{S}_{\mathbf{j}}^{-} = \alpha_{\mathbf{j}}^{\dagger}$  and  $\hat{S}_{\mathbf{j}}^{z} = 1/2 - \alpha_{\mathbf{j}}^{\dagger}\alpha_{\mathbf{j}}$  with  $\alpha_{\mathbf{j}}^{\dagger}$  being bosonic creation operators: keeping the quadratic terms in  $\alpha_{\mathbf{j}}$  and Fourier transforming

one obtains the bosonic Hamiltonian  $H = \sum_{\mathbf{k}} \omega_{\mathbf{k}} \alpha_{\mathbf{k}}^{\dagger} \alpha_{\mathbf{k}}$ with spin wave dispersion  $\omega_{\mathbf{k}} = 2|J|(1 - \gamma_{\mathbf{k}})$  where  $\gamma_{\mathbf{k}} = (\cos k_x + \cos k_y)/2$ . Furthermore one has  $\hat{T}_{\mathbf{j}}^z|0\rangle = \exp(i\mathbf{Q}\cdot\mathbf{R}_{\mathbf{j}})/2|0\rangle$  where  $\mathbf{Q} = (\pi,\pi)$  is the AO ordering vector, so that following Eq. (3) one obtains

$$\hat{O}_{\mathbf{k},\mathbf{e}}|\mathrm{FM}\otimes\mathrm{AO}\rangle = \frac{1}{2} \Big\{ \big[ W_{\mathbf{e}}^{-}(a) + W_{\mathbf{e}}^{-}(b) \big] \alpha_{\mathbf{k}}^{\dagger} \\ + \big[ W_{\mathbf{e}}^{-}(a) - W_{\mathbf{e}}^{-}(b) \big] \alpha_{\mathbf{k}+\mathbf{Q}}^{\dagger} \Big\} |\mathrm{FM}\otimes\mathrm{AO}\rangle, \quad (4)$$

where  $W_{\mathbf{e}}^{-} = W_{\mathbf{e}}^{x} - iW_{\mathbf{e}}^{y}$  are the amplitudes for the spin flip transition, which can be calculated for the simple case of a Cu<sup>2+</sup> ion (cf. Fig. 1) or for any other TM ion (cf. Refs. [21, 31]). Using Eq. (4) and the spin Hamiltonian defined above, RIXS cross section can be directly calculated from Eq. (1) (cf. Fig. 2 and Ref. 36). Due to the physical inequivalence of the two sublattices, the magnetic and the orbital Brillouin zones are no longer the same, so that the backfolded branch of the magnon dispersion (pseudo optical branch in Fig. 2) gains a finite intensity  $\propto |W_{\mathbf{e}}^{-}(a) - W_{\mathbf{e}}^{-}(b)|^{2}$  [cf. Ref. 36 and Eq. (4)], as the spin flip amplitudes are different for orbitals *a* and *b*.

FM systems with FO order or OL state The above result stays in contrast with the 2D FM case with FO order ( $|0\rangle = |\text{FM} \otimes \text{FO}\rangle$ ), for which one has  $\hat{T}_{\mathbf{i}}^{z}|0\rangle =$  $1/2|0\rangle$  for all sites **j**. Again using Eq. (3) one obtains an equation for the operator  $O_{\mathbf{k},\mathbf{e}}$  and for the cross section in Eq. (1). In this case the orbital and magnetic Brillouin zones coincide since  $W_{\mathbf{e}}^{-}(b) = W_{\mathbf{e}}^{-}(a)$  and there is no pseudo-optical magnon branch in the RIXS cross section (see Ref. 36 and Fig. 2). Finally for the 2D FM case with an OL state  $(|0\rangle = |FM \otimes OL\rangle)$  with two fluctuating orbital states a and b the off-diagonal terms in  $\hat{T}_{\mathbf{i}}^{z}|0\rangle$  lead to orbital excitations and therefore can be omitted from Eq. (3), as we are interested only in pure spin excitations and not in coupled spin-orbital ones. Again the orbital and magnetic Brillouin zones are identical and only the acoustic branch is detectable [36].

AF systems with AO order We consider a 2D AF with AO order (i.e.,  $|0\rangle = |AF \otimes AO\rangle$ ) with the effective Heisenberg interaction between spins as in the FM case but with J > 0. Similarly to the previous case, the single magnon excitations are obtained by applying sequentially Holstein-Primakoff, Fourier, and Bogoliubov transformations and keeping only harmonic terms in bosonic operators  $\alpha_{\mathbf{k}}^{\dagger}$  and  $\alpha_{\mathbf{k}}$ , cf. Ref. [5], so that

$$\hat{O}_{\mathbf{k},\mathbf{e}}|AF \otimes AO\rangle = \frac{1}{2} \Big\{ \Big[ W_{\mathbf{e}}^{+}(a) + W_{\mathbf{e}}^{-}(b) \Big] u_{\mathbf{k}} \alpha_{\mathbf{k}}^{\dagger} \\ - \Big[ W_{\mathbf{e}}^{+}(b) + W_{\mathbf{e}}^{-}(a) \Big] v_{\mathbf{k}} \alpha_{\mathbf{k}}^{\dagger} \\ + \Big[ W_{\mathbf{e}}^{+}(a) - W_{\mathbf{e}}^{-}(b) \Big] u_{\mathbf{k}+\mathbf{Q}} \alpha_{\mathbf{k}+\mathbf{Q}}^{\dagger} \\ + \Big[ W_{\mathbf{e}}^{+}(b) - W_{\mathbf{e}}^{-}(a) \Big] v_{\mathbf{k}+\mathbf{Q}} \alpha_{\mathbf{k}+\mathbf{Q}}^{\dagger} \Big\} |AF \otimes AO\rangle, \quad (5)$$

with  $W_{\mathbf{e}}^+ = W_{\mathbf{e}}^x + \imath W_{\mathbf{e}}^y$  and where the Bogoliubov factors are defined as  $u_{\mathbf{k}} = \sqrt{J/2\Omega_{\mathbf{k}} + 1/2}$  and  $v_{\mathbf{k}} =$ 



FIG. 2. (color online) Magnetic RIXS cross section  $I_{\mathbf{e}}(\mathbf{k},\omega)$ for different magnetic (FM and AF) and orbital orders (FO and AO) along a high symmetry path in the Brillouin zone [where  $\Gamma = (0,0)$ ,  $\mathbf{X} = (\pi, 0)$ , and  $\mathbf{M} = (\pi, \pi)$ ], averaged over incoming and outgoing polarizations. The FO (AO) order is formed by the  $x^2 - y^2$  orbital  $(x^2 - z^2 \text{ and } y^2 - z^2)$  while the spin quantization axis is in the xy plane. The color scale is nonlinear, since intensities of the AF spectra diverge at M, and at  $\Gamma$  in the AF-AO case. Spectra for the OL case (not shown) differ only quantitatively from the FO one.

 $\operatorname{sgn}(\gamma_{\mathbf{k}})\sqrt{J/2\Omega_{\mathbf{k}}-1/2}$ , and the AF spin wave dispersion is  $\Omega_{\mathbf{k}} = 2J\sqrt{1-\gamma_{\mathbf{k}}^2}$ . This form of the operator in general leads to a nonvanishing intensity when  $\mathbf{k} \to \Gamma$  as a result of the AO ordering, see Ref. 36 and Fig. 2. In the case of ideal AF  $\Omega_{\mathbf{k}+\mathbf{Q}} = \Omega_{\mathbf{k}}$  so that in contrast to the  $|\mathrm{FM} \otimes \mathrm{AO}\rangle$  case one can observe only one branch in the RIXS spectrum (although any corrections to the Heisenberg model for which  $\Omega_{\mathbf{k}+\mathbf{Q}} \neq \Omega_{\mathbf{k}}$  will give rise to a pseudo optical branch in the spectrum, somewhat similar to the  $|\mathrm{FM} \otimes \mathrm{AO}\rangle$  case).

AF systems with FO order or OL state Again the above result stays in contrast with the 2D AF case with FO order ( $|0\rangle = |AF \otimes FO\rangle$ ) for which the RIXS operator has a simpler expression than Eq. (5) since  $W_{\mathbf{e}}^{\pm}(b) =$  $W_{\mathbf{e}}^{\pm}(a)$ . In a similar way intensities for the 2D AF case with OL state ( $|0\rangle = |AF \otimes OL\rangle$ ) are obtained [36]. The intensity vanishes in both cases when  $\mathbf{k} \to \Gamma$  in agreement with Ref. 20, cf. Fig. 2 and Ref. 36.

Discriminating different orbital states As shown above for FM and AF systems, RIXS spectra can discriminate an AO against FO order or OL ground states (cf. Fig. 2). While in the FM case the pseudo-optical magnon branch signals the onset of the AO order, in the AF case the intensity of magnons with momenta  $\mathbf{k} \rightarrow \Gamma$  does not vanish in the AO case, contrarily to the FO and OL case. This dependence is not due to distinct magnon dispersions for different orbital or electronic ground states [37– 39], but to the orbital dependency of magnetic RIXS amplitudes.

Furthermore, circular dichroism of *magnetic* RIXS intensities allows one to distinguish between different orbital ground states, see Fig. 3. While for FM systems whether a circular dichroism is present depends on the symmetry of the orbital occupied, in the AF ones its presence only depends on the system translational symmetry. Specifically, for  $|AF \otimes FO\rangle$  (or  $|AF \otimes OL\rangle$ ) systems, circular dichroism vanishes, while in the case of  $|AF \otimes AO\rangle$  order (for which the RIXS spin flip amplitude is finite for both orbitals forming the AO ground state, cf. Ref. [20]) the circular dichroism is nonzero (Fig. 3).

In fact, if there is an AO order in a magnetic system, translational symmetry is broken into two physically inequivalent sublattices. Consequently a pseudooptical branch in the magnon dispersion appears in the  $|FM \otimes AO\rangle$  case. On the other hand, while a simple  $|AF \otimes FO\rangle$  (or  $|AF \otimes OL\rangle$ ) system is symmetric under the combination of time reversal and a discrete translation [40], in the  $|AF \otimes AO\rangle$  case the latter is broken. Macroscopically [41], that means that the system is no longer symmetric under the combination of time reversal and translation. As a consequence, a finite circular dichroism appears, i.e., RIXS intensities (at fixed **k** and  $\omega$ ) for left and right circular polarization of the incoming photon are no longer equivalent.

Although the actual values of the  $\mathbf{W}_{\mathbf{e}}(d_{\mathbf{j}})$  transition amplitudes depend on the orbital symmetry at each site, differences in the RIXS spectra between the AO and the FO/OL ground states show up (cf. Fig. 2 and Fig. 3), as long as  $\mathbf{W}_{\mathbf{e}}(a) \neq \mathbf{W}_{\mathbf{e}}(b)$ . For this reason, the discrimination between different orbital states does not rely on the particular orbital occupancy on the *single site*, but on the breaking of the translational symmetry caused by the onset of the AO orbital order.

While other inelastic scattering methods have been theoretically proposed to detect orbital ordering [42, 43], it should be stressed that, due to the onset of characteristic dispersion, the magnetic peaks in RIXS can, unlike, e.g., orbitons, be easily identified. Besides, as typically magnons interact weakly, quasiparticle peaks in RIXS spectra have sharp and well-defined line shapes which would rather not be obliterated by other low energy excitations (cf. Ref. [22]) so that their dependence on the orbital ground state is very pronounced.

Conclusions We have shown in detail how ground state orbital correlations directly reflect themselves in magnetic Resonant Inelastic X-ray Scattering (RIXS) intensities. It follows that measuring the RIXS spectra at transition metal  $L_{2,3}$  edges in correlated materials with orbital degrees of freedom and magnetic order, allows one to distinguish between different orbital ground states [44]. This is possible because in magnetic RIXS the spin flip mechanism involves a strong spin-orbit coupling deep in the electronic core so that, unlike in inelastic neutron scattering, the magnetic scattering spectra strongly depend on the symmetry of the orbitals where the spins are in.

The method proposed here is of direct relevance to



FIG. 3. (color online) Circular dichroism  $D = (I_{\mathbf{e}_L} - I_{\mathbf{e}_R})/(I_{\mathbf{e}_L} + I_{\mathbf{e}_R})$  for RIXS spectra intensities at  $\omega = \Omega_{\mathbf{k}}$  as a function of transferred momentum  $\mathbf{k}$  for the AF state, where  $\mathbf{e}_L$  ( $\mathbf{e}_R$ ) is left (right) incoming circular polarization, for AO (FO and OL) state plotted with solid (dashed) line.

2D orbital systems, e.g,  $K_2CuF_4$  or  $Cs_2AgF_4$  with FM layers and predicted (but not yet explicitly verified) AO ordering [45–47], as well as to 3D transition metal oxides with orbital degrees of freedom such as LaMnO<sub>3</sub>, KCuF<sub>3</sub>, LaTiO<sub>3</sub> or LaVO<sub>3</sub> [48]. In particular, in Ref. 49 we predict magnetic RIXS spectra for two different polytypes of KCuF<sub>3</sub> with distinct orbitally ordered ground states.

We thank V. Bisogni, M. Daghofer, M. W. Haverkort, C. Ortix and M. van Veenendaal for fruitful discussions. K. W. acknowledges support from the Alexander von Humboldt Foundation. This research benefited from the RIXS collaboration supported by the Computational Materials Science Network (CMSN) program of the Division of Materials Science and Engineering, U.S. Department of Energy, Grant No. DE-FG02-08ER46540.

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