This is the accepted manuscript made available via CHORUS. The article has been published as:

Measurement of Exclusive $\pi^0$ Electroproduction Structure Functions and their Relationship to Transverse Generalized Parton Distributions

I. Bedlinskiy et al. (CLAS Collaboration)

Phys. Rev. Lett. 109, 112001 — Published 10 September 2012

DOI: 10.1103/PhysRevLett.109.112001
Measurement of Exclusive $\pi^0$ Electroproduction Structure Functions and their Relationship to Transversity GPDs

Exclusive $\pi^0$ electroproduction at a beam energy of 5.75 GeV has been measured with the Jefferson Lab CLAS spectrometer. Differential cross sections were measured at more than 1800 kinematic values in $Q^2$, $x_B$, $t$, and $\phi_q$, in the $Q^2$ range from 1.0 to 4.6 GeV$^2$, $-t$ up to 2 GeV$^2$, and $x_B$ from 0.1 to 0.58. Structure functions $\sigma_T + \epsilon \sigma_L, \sigma_{TT}$ and $\sigma_{LT}$ were extracted as functions of $t$ for each of 17 combinations of $Q^2$ and $x_B$. The data were compared directly with two handbag-based calculations including both longitudinal and transversity GPDs. Inclusion of only longitudinal GPDs very strongly underestimates $\sigma$ and fails to account for $\sigma_{TT}$ and $\sigma_{LT}$, while inclusion of transversity GPDs brings the calculations into substantially better agreement with the data. There is very strong sensitivity to the relative contributions of nucleon helicity flip and helicity non-flip processes. The results confirm that exclusive $\pi^0$ electroproduction offers direct experimental access to the transversity GPDs.

A major goal of hadronic physics is to describe the three dimensional structure of the nucleon in terms of its quark and gluon fields. Deep inelastic scattering experiments have provided a large body of information about quark longitudinal momentum distributions. Exclusive electron scattering experiments, in which all final state particles are measured, have been rather successfully analyzed and interpreted by Regge models which are based on hadronic degrees of freedom - for example most recently in Refs. [1, 2]. However, during the past decade the handbag mechanism has become the leading theoretical approach for extracting nucleon quark and gluon structure from exclusive reactions such as deeply virtual Compton scattering (DVCS) and deeply virtual meson electroproduction (DVMP). In this approach the quark distributions are parameterized in terms of generalized parton distributions (GPDs). The GPDs contain information about the distributions of both the longitudinal momentum and the transverse position of partons in the nucleon. In the handbag mechanism the reaction amplitude factorizes into two parts. One part describes the basic hard electroproduction process with a parton within the nucleon, and the other - the GPD- contains the distribution of partons within the nucleon which are the result of soft processes. While the former is reaction dependent, the latter is a universal property of nucleon structure common to the various exclusive reactions. This is schematically illustrated in Fig. 1. While the handbag mechanism should be most applicable at asymptotically large photon virtuality $Q^2$, DVCS experiments at $Q^2$ as low as 1.5 GeV$^2$ appear to be described rather well at leading twist by the handbag mechanism, while the range of validity of leading order applicability of DVMP is not as clearly determined.

There are eight GPDs. Four correspond to parton helicity conserving (chiral-even) processes, denoted by $H^g$, $H^q$, $E^g$ and $E^q$. Four correspond to parton helicity-flip (chiral-odd) processes $[3, 4]$, $H^q_T$, $H^q_T$, $E^q_T$, and $E^q_T$. The GPDs depend on three kinematic variables: $x$, $\xi$ and $t$, where $x$ is the average parton longitudinal momentum fraction and $\xi$ (skewness) is half of the longitudinal momentum fraction transferred to the struck parton. The skewness can be expressed in terms of the Bjorken variable $x_B$ as $\xi \simeq x_B/(2 - x_B)$, in which $x_B = Q^2/(2p \cdot q)$, $q$ is the four-momentum of the virtual photon and $Q^2 = -q^2$. The momentum transfer to the nucleon is $t = (p - p')^2$, where $p$ and $p'$ are the initial and final four momenta of the nucleon.

In the forward limit where $t \to 0$, $H^q$ and $H^q$ reduce to the parton density distributions $q(x)$ and $h^q(x)$ and parton helicity distributions $\Delta q(x)$ respectively. The first moments in $x$ of the chiral-even GPDs are related to the elastic form factors of the nucleon: the Dirac form factor $F^q_1(t)$, the Pauli form factor $F^q_2(t)$, the axial-vector form factor $g_A^q(t)$ and the pseudoscalar form factor $h_A^q(t)$ [5].

Most of the reactions studied, such as DVCS or vector meson production, are at leading order primarily sensitive to the chiral-even GPDs. Very little is known about the chiral-odd GPDs. $H^q_T$ becomes the transversity function $h^q_T(x)$ in the forward limit. The chiral-odd GPDs are difficult to access since subprocesses with a quark helicity-flip are suppressed. However, a complete description of nucleon structure requires the knowledge of the transversity GPDs as well as chiral even GPDs.

Pseudoscalar meson electroproduction, and in particular $\pi^0$ production in the reaction $e p \to e' p' \pi^0$, was identified [6, 7] as especially sensitive to the helicity-flip subprocesses. Evidence of their possible contribution to $\pi^+\pi^-$ electroproduction in target spin asymmetry data [8] was noted in Ref. [7]. A disadvantage of $\pi^+\pi^-$ production is that the interpretation is complicated by the dominance of the longitudinal $\pi^\pm$-pole term, which is absent in $\pi^0$ production. In addition, for $\pi^0$ production the structure of the amplitudes further suppresses the quark helicity conserving amplitudes relative to the helicity-flip amplitudes [7]. On the other hand, $\pi^0$ cross sections over a large kinematic range are much more difficult to obtain than for $\pi^+\pi^-$ for two reasons: First, the cross sections are much smaller than for $\pi^+\pi^-$, and second,
the clean detection of $\pi^0$s requires the measurement of their two decay photons.

This letter presents the results of a measurement of $\pi^0$ electroproduction cross sections. The primary focus here is in its interpretation within the framework of the handbag model and on its sensitivity, within this framework, of accessing the quark helicity flip GPDs.

The handbag mechanism is schematically illustrated in Fig. 1. The reaction can be written as a linear sum of amplitudes, each of which factorizes in the framework of the handbag mechanism. The helicities of the initial and final nucleons are denoted by $\nu$ and $\nu'$, the incident photon and produced meson by $\mu$ and $\mu'$ and the active initial and final quark by $\lambda$ and $\lambda'$. The arrows in the figure represent the corresponding helicities.

The primary contributing GPDs in meson production for transverse photons are $H_T$, which characterizes the quark distributions involved in nucleon helicity-flip, and $E_T(=2H_T+E_T)$ which characterizes the quark distributions involved in nucleon non-helicity-flip processes [9], [10]. This GPD describes the density of transversely polarized quarks in an unpolarized nucleon [9], [10].

The relative contributions of the nucleon helicity-flip and nucleon helicity non-flip processes determine the $t$ dependence of the differential cross sections.
tent with the data. The ratio of the number of re-
constructed Monte-Carlo events to the data events
was typically a factor of about 12. Thus the statis-
tical error introduced by the acceptance calculation
was much smaller than for the data.

The data were binned in $Q^2$, $x_B$, $t$, and $\phi_\pi$, and dif-
ferential cross sections $d^4\sigma/dQ^2dx_Bdtd\phi_\pi$ were ob-
tained for more than 1800 bins.

Radiative corrections were calculated using the
software package EXCLURAD [12], which had been
previously developed and used for analyzing earlier
CLAS $\pi^0$ experiments. Radiative corrections de-
pend on $Q^2$, $t$, $x_B$ and $\phi_\pi$. They vary from 5 to 10%,
depending on the kinematics.

An overall normalization factor of 1.12 was ob-
tained for more than 1800 bins.

The results of two GPD-based models [14, 15] are
superimposed in Fig. 2. The contributions from
transversely polarized photons are primarily from
$H_T$ and $E_T$. Reference [14] obtains the following
relations:

$$\sigma_T = \frac{4\pi\alpha_e}{2\kappa} \frac{\mu^2}{Q^2} \left[ (1 - \xi^2) \langle H_T \rangle^2 - \frac{t'}{8m^2} \langle E_T \rangle^2 \right]$$

(2)

and

$$\sigma_{TT} = \frac{4\pi\alpha_e}{2\kappa} \frac{\mu^2}{Q^4} \frac{t'}{8m^2} \langle |E_T| \rangle^2.$$  

(3)

Here $\kappa(Q^2, x_B)$ is a phase space factor, $t' = t - t_{\text{min}}$, and the brackets $\langle H_T \rangle$ and $\langle |E_T| \rangle$ denote the con-
volution of the elementary process with the GPDs $H_T$
and $E_T$.

The contribution $\sigma_L$ accounts for only a small frac-
tion in both calculations (typically less than a few percent) of the unseparated $\sigma_{T+L}$ in the kinematic regime under investigation. This is because $H$ and $E$, the GPDs which are responsible for the leading-twist structure function $\sigma_L$, are very small.

This is not the case for $E_T$ and $H_T$ which contribute to $\sigma_T$ and $\sigma_{TT}$. In addition, the transverse cross sec-
tions are strongly enhanced by the chiral condensate
through the parameter $\mu_\pi = \frac{m^2}{(m_u + m_d)}$, where $m_u$ and $m_d$ are current quark masses [7].

With the inclusion of the quark helicity non-
conserving chiral-odd GPDs, which contribute pri-
marily to $\sigma_T$ and $\sigma_{TT}$ and, to a lesser extent $\sigma_{LT}$,
the model agrees moderately well with the data. De-
viation in shape become greater at smaller $t'$ for
the unseparated cross section $\sigma_U$. The behavior of
the cross section near the threshold $t'$ is determined
by the interplay between $H_T$ and $E_T$. If $E_T$ dom-
inates, the cross section becomes small as $t' \rightarrow 0$.

For the GPDs of Ref. [14] the parameterization was
guided by the lattice calculation results of Ref. [10],
while Ref. [15] used a GPD Reggeized diquark-quark
model to obtain the GPDs. The results in Fig. 2 for
the model of Ref. [14] (solid curves), in which $E_T$
is dominant, agree rather well with the data. In par-
cular, the structure function $\sigma_U$ begins to decrease
as $-t$ becomes small, showing the effect of $E_T$. In
the model of Ref. [15] (dashed curves) $H_T$ is dom-
inant, which leads to a large rise in cross section as
$t'$ becomes small. Thus, in their parameterization,
the relative contribution of $E_T$ to $H_T$ appears to be
underestimated. One can make a similar conclusion
from the comparison between data and model pre-
dictions for $\sigma_{TT}$. This shows the sensitivity of the
measured $\pi^0$ structure functions for constraining the
transversity GPDs.

From Eq. (2) for $\sigma_T$ and Eq. (3) for $\sigma_{TT}$ one can
conclude that $|\sigma_{TT}| < \sigma_T < \sigma_U$. One sees from
Fig. 2 that $-\sigma_{TT}$ is a sizable fraction of the unsepa-
rated cross section while $\sigma_{LT}$ is very small, which
implies that contributions from transversely polar-
ized photons play a dominant role in the $\pi^0$ elec-
tronic production process.

In conclusion, differential cross sections of exclu-
sive pion electroproduction have been obtained in
the few GeV region over a wide range of $Q^2$, $x_B$ and
$t$. While the general features of $\pi^0$ electroproduction
have been described by recent Regge models [1, 2],
the focus of this letter is on the handbag mecha-
nism in terms of quark and gluon degrees of freedom.
Within the handbag interpretation, the data appear
to confirm the expectation that pseudoscalar, and
in particular $\pi^0$, electroproduction appears to be a uniquely sensitive process to access the transversity GPDs $\tilde{E}_T$ and $H_T$. The measured unseparated cross section is much larger than expected from leading-twist handbag calculations. This means that the contribution of the longitudinal cross section $\sigma_L$ is small in comparison with $\sigma_T$. The same conclusion can be made in an almost model independent way from comparison of the cross section $\sigma_U$, $\sigma_{TT}$ and $\sigma_{LT}$ [17].

Detailed interpretations are model dependent and quite dynamic in that they are strongly influenced by new data as they become available. In particular, calculations are in progress to compare the theoretical models with the single beam spin asymmetries obtained earlier with CLAS [18] and longitudinal target spin asymmetries which are currently under analysis.

In the near future new data on $\eta$ production and ratios of $\eta$ to $\pi^0$ cross sections are expected to further constrain GPD models. Extracting $\sigma_L$ and $\sigma_T$ with improved statistical accuracy and performing new measurements with transversely and longitudinally polarized targets would also be very useful.

We thank the staff of the Accelerator and Physics Divisions at Jefferson Lab for making the experiment possible. We also thank G. Goldstein, S. Goloskokov, P. Kroll, J. M. Laget and S. Liuti for many informative discussions and clarifications of their work, and making available the results of their calculations. This work was supported in part by the U.S. Department of Energy and National Science Foundation, the French Centre National de la Recherche Scientifique and Commissariat à l’Energie Atomique, the French-American Cultural Exchange (FACE), the Italian Istituto Nazionale di Fisica Nucleare, the Chilean Comisión Nacional de Investigación Científica y Tecnológica (CONICYT), the National Research Foundation of Korea, and the UK Science and Technology Facilities Council (STFC). The Jefferson Science Associates (JSA) operates the Thomas Jefferson National Accelerator Facility for
the United States Department of Energy under contract DE-AC05-06OR23177.